Package 'BGGM'

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Type Package

```
Title Bayesian Gaussian Graphical Models
Version 2.0.4
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Description Fit Bayesian Gaussian graphical models. The methods are separated into
      two Bayesian approaches for inference: hypothesis testing and estimation. There are
      extensions for confirmatory hypothesis testing, comparing Gaussian graphical models,
      and node wise predictability. These methods were recently introduced in the Gaussian
      graphical model literature, including
      Williams (2019) <doi:10.31234/osf.io/x8dpr>,
      Williams and Mulder (2019) <doi:10.31234/osf.io/ypxd8>,
      Williams, Rast, Pericchi, and Mulder (2019) <doi:10.31234/osf.io/yt386>.
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License GPL-2
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BGGM-package

BGGM: Bayesian Gaussian Graphical Models

Description

The R package **BGGM** provides tools for making Bayesian inference in Gaussian graphical models (GGM). The methods are organized around two general approaches for Bayesian inference: (1) estimation (Williams 2018) and (2) hypothesis testing (Williams and Mulder 2019). The key distinction is that the former focuses on either the posterior or posterior predictive distribution, whereas the latter focuses on model comparison with the Bayes factor.

The methods in **BGGM** build upon existing algorithms that are well-known in the literature. The central contribution of **BGGM** is to extend those approaches:

- 1. Bayesian estimation with the novel matrix-F prior distribution (Mulder and Pericchi 2018).
 - Estimation estimate.
- 2. Bayesian hypothesis testing with the novel matrix-F prior distribution (Mulder and Pericchi 2018).
 - Exploratory hypothesis testing explore.
 - Confirmatory hypothesis testing confirm.
- 3. Comparing GGMs (Williams et al. 2020)
 - Partial correlation differences ggm_compare_estimate.
 - Posterior predictive check ggm_compare_ppc.
 - Exploratory hypothesis testing ggm_compare_explore.
 - Confirmatory hypothesis testing ggm_compare_confirm.
- 4. Extending inference beyond the conditional (in)dependence structure
 - Predictability with Bayesian variance explained (Gelman et al. 2019) predictability.
 - Posterior uncertainty in the partial correlations estimate.
 - Custom Network Statistics roll_your_own.

Furthermore, the computationally intensive tasks are written in c++ via the R package **Rcpp** (Eddel-buettel et al. 2011) and the c++ library **Armadillo** (Sanderson and Curtin 2016), there are plotting functions for each method, control variables can be included in the model, and there is support for missing values bggm_missing.

Supported Data Types:

- Continuous: The continuous method was described in Williams and Mulder (2019).
- Binary: The binary method builds directly upon in Talhouk et al. (2012), that, in turn, built upon the approaches of Lawrence et al. (2008) and Webb and Forster (2008) (to name a few).
- Ordinal: Ordinal data requires sampling thresholds. There are two approach included in **BGGM**: (1) the customary approach described in Albert and Chib (1993) (the default) and the 'Cowles' algorithm described in Cowles (1996).

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• Mixed: The mixed data (a combination of discrete and continuous) method was introduced in Hoff (2007). This is a semi-parametric copula model (i.e., a copula GGM) based on the ranked likelihood. Note that this can be used for data consisting entirely of ordinal data.

Additional Features:

The primary focus of BGGM is Gaussian graphical modeling (the inverse covariance matrix). The residue is a suite of useful methods not explicitly for GGMs:

- 1. Bivariate correlations for binary (tetrachoric), ordinal (polychoric), mixed (rank based), and continuous (Pearson's) data zero_order_cors.
- 2. Multivariate regression for binary (probit), ordinal (probit), mixed (rank likelihood), and continous data (estimate).
- 3. Multiple regression for binary (probit), ordinal (probit), mixed (rank likelihood), and continous data (e.g., coef.estimate).

Note on Conditional (In)dependence Models for Latent Data:

All of the data types (besides continuous) model latent data. That is, unoboserved data that is assumed to be Gaussian distributed. For example, a tetrachoric correlation (binary data) is a special case of a polychoric correlation (ordinal data). Both relations are between "theorized normally distributed continuous **latent** variables" (Wikipedia). In both instances, the correpsonding partial correlation between observed variables is conditioned on the remaining variables in the *latent* space. This implies that interpration is similar to continuous data, but with respect to latent variables. We refer interested users to page 2364, section 2.2, in Webb and Forster (2008).

High Dimensional Data?

BGGM was built specificially for social-behvarioal scientists. Of course, the methods can be used by all researchers. However, there is *not* support for high-dimensonal data (i.e., more variables than observations) that are common place in the genetics literature. These data are rare in the social-behavioral sciences. In the future, support for high-dimensional data may be added to **BGGM**.

References

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Gelman A, Goodrich B, Gabry J, Vehtari A (2019). "R-squared for Bayesian Regression Models." *American Statistician*, **73**(3), 307–309. ISSN 15372731, doi: 10.1080/00031305.2018.1549100.

Hoff PD (2007). "Extending the rank likelihood for semiparametric copula estimation." *The Annals of Applied Statistics*, **1**(1), 265–283. doi: 10.1214/07AOAS107.

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Mulder J, Pericchi L (2018). "The Matrix-F Prior for Estimating and Testing Covariance Matrices." *Bayesian Analysis*, 1–22. ISSN 19316690, doi: 10.1214/17BA1092.

Sanderson C, Curtin R (2016). "Armadillo: a template-based C++ library for linear algebra." *Journal of Open Source Software*, **1**(2), 26. doi: 10.21105/joss.00026.

Talhouk A, Doucet A, Murphy K (2012). "Efficient Bayesian inference for multivariate probit models with sparse inverse correlation matrices." *Journal of Computational and Graphical Statistics*, **21**(3), 739–757. doi: 10.1080/10618600.2012.679239.

Webb EL, Forster JJ (2008). "Bayesian model determination for multivariate ordinal and binary data." *Computational statistics* & *data analysis*, **52**(5), 2632–2649. doi: 10.1016/j.csda.2007.09.008.

Williams DR (2018). "Bayesian Estimation for Gaussian Graphical Models: Structure Learning, Predictability, and Network Comparisons." *arXiv*. doi: 10.31234/OSF.IO/X8DPR.

Williams DR, Mulder J (2019). "Bayesian Hypothesis Testing for Gaussian Graphical Models: Conditional Independence and Order Constraints." *PsyArXiv*. doi: 10.31234/osf.io/ypxd8.

Williams DR, Rast P, Pericchi LR, Mulder J (2020). "Comparing Gaussian graphical models with the posterior predictive distribution and Bayesian model selection." *Psychological Methods*. doi: 10.1037/met0000254.

asd_ocd

Data: Autism and Obssesive Compulsive Disorder

Description

A correlation matrix with 17 variables in total (autsim: 9; OCD: 8). The sample size was 213.

Usage

```
data("asd_ocd")
```

Format

A correlation matrix including 17 variables. These data were measured on a 4 level likert scale.

Details

Autism:

- CI Circumscribed interests
- UP Unusual preoccupations
- RO Repetitive use of objects or interests in parts of objects

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- CR Compulsions and/or rituals
- CI Unusual sensory interests
- SM Complex mannerisms or stereotyped body movements
- SU Stereotyped utterances/delayed echolalia
- NIL Neologisms and/or idiosyncratic language
- · VR Verbal rituals

OCD

- CD Concern with things touched due to dirt/bacteria
- TB Thoughts of doing something bad around others
- · CT Continual thoughts that do not go away
- HP Belief that someone/higher power put reoccurring thoughts in their head
- CW Continual washing
- CCh Continual checking CntCheck
- CC Continual counting/repeating
- RD Repeatedly do things until it feels good or just right

References

Jones, P. J., Ma, R., & McNally, R. J. (2019). Bridge centrality: A network approach to understanding comorbidity. Multivariate behavioral research, 1-15.

Ruzzano, L., Borsboom, D., & Geurts, H. M. (2015). Repetitive behaviors in autism and obsessive-compulsive disorder: New perspectives from a network analysis. Journal of Autism and Developmental Disorders, 45(1), 192-202. doi:10.1007/s10803-014-2204-9

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bfi

Data: 25 Personality items representing 5 factors

Description

This dataset and the corresponding documentation was taken from the **psych** package. We refer users to that package for further details (Revelle 2019).

Usage

```
data("bfi")
```

Format

A data frame with 25 variables and 2800 observations (including missing values)

Details

- A1 Am indifferent to the feelings of others. (q_146)
- A2 Inquire about others' well-being. (q_1162)
- A3 Know how to comfort others. (q_1206)
- A4 Love children. (q_1364)
- A5 Make people feel at ease. (q_1419)
- C1 Am exacting in my work. (q_124)
- C2 Continue until everything is perfect. (q_530)
- C3 Do things according to a plan. (q_619)
- C4 Do things in a half-way manner. (q_626)
- C5 Waste my time. (q_1949)
- E1 Don't talk a lot. (q_712)
- E2 Find it difficult to approach others. (q_901)
- E3 Know how to captivate people. (q_1205)
- E4 Make friends easily. (q_1410)
- E5 Take charge. (q_1768)
- N1 Get angry easily. (q_952)
- N2 Get irritated easily. (q_974)
- N3 Have frequent mood swings. (q_1099)
- N4 Often feel blue. (q_1479)
- N5 Panic easily. (q_1505)
- o1 Am full of ideas. (q_128)
- o2 Avoid difficult reading material.(q_316)

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- o3 Carry the conversation to a higher level. (q_492)
- o4 Spend time reflecting on things. (q_1738)
- o5 Will not probe deeply into a subject. (q_1964)
- gender Males = 1, Females =2
- education 1 = HS, 2 = finished HS, 3 = some college, 4 = college graduate 5 = graduate degree

References

Revelle W (2019). *psych: Procedures for Psychological, Psychometric, and Personality Research.* Northwestern University, Evanston, Illinois. R package version 1.9.12, https://CRAN.R-project.org/package=psych.

bggm_missing

GGM: Missing Data

Description

Estimation and exploratory hypothesis testing with missing data.

Usage

```
bggm_missing(x, iter = 2000, method = "estimate", ...)
```

Arguments

x An object of class mid mice.

iter Number of iterations for each imputed dataset (posterior samples; defaults to

2000).

method Character string. Which method should be used (default set to estimate)? The

current options are "estimate" and "explore".

... Additional arguments passed to either estimate or explore.

Value

An object of class estimate or explore.

Note

Currently, **BGGM** is compatible with the package mice for handling the missing data. This is accomplished by fitting a model for each imputed dataset (i.e., more than one to account for uncertainty in the imputation step) and then pooling the estimates.

In a future version, an additional option will be added that allows for imputing the missing values during model fitting. This option will be incorporated directly into the estimate or explore functions, such that bggm_missing will always support missing data with mice.

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Support:

There is limited support for missing data. As of version 2.0.0, it is possible to determine the graphical structure with either estimate or explore, in addition to plotting the graph with plot.select. All data types *are* currently supported.

Memory Warning: A model is fitted for each imputed dataset. This results in a potentially large object.

```
# note: iter = 250 for demonstrative purposes
# need this package
library(mice, warn.conflicts = FALSE)
# data
Y <- ptsd[,1:5]
# matrix for indices
mat \leftarrow matrix(0, nrow = 221, ncol = 5)
# indices
indices <- which(mat == 0, arr.ind = TRUE)</pre>
Y[indices[sample(1:nrow(indices), 50),]] <- NA
x <- mice(Y, m = 5, print = FALSE)
#############################
###### copula
                  #####
# rank based parital correlations
# estimate the model
fit_est <- bggm_missing(x,</pre>
                         method = "estimate",
                         type = "mixed",
                         iter = 250,
                         progress = FALSE)
# select edge set
E <- select(fit_est)</pre>
# plot E
plt_E <- plot(E)$plt</pre>
plt_E
```

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coef.estimate	Compute Regression Parameters for estimate Objects
COET.ESTINATE	Compute Regression I arameters for estimate Objects

Description

There is a direct correspondence between the inverse covariance matrix and multiple regression (Kwan 2014; Stephens 1998). This readily allows for converting the GGM paramters to regression coefficients. All data types are supported.

Usage

```
## S3 method for class 'estimate'
coef(object, iter = NULL, progress = TRUE, ...)
```

Arguments

object An Object of class estimate

iter Number of iterations (posterior samples; defaults to the number in the object).

progress Logical. Should a progress bar be included (defaults to TRUE)?

Currently ignored.

Value

An object of class coef, containing two lists.

- betas A list of length p, each containing a p 1 by iter matrix of posterior samples
- object An object of class estimate (the fitted model).

References

Kwan CC (2014). "A regression-based interpretation of the inverse of the sample covariance matrix." *Spreadsheets in Education*, **7**(1), 4613.

Stephens G (1998). "On the Inverse of the Covariance Matrix in Portfolio Analysis." *The Journal of Finance*, **53**(5), 1821–1827.

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coef.explore

Compute Regression Parameters for explore Objects

Description

There is a direct correspondence between the inverse covariance matrix and multiple regression (Kwan 2014; Stephens 1998). This readily allows for converting the GGM paramters to regression coefficients. All data types are supported.

Usage

```
## S3 method for class 'explore'
coef(object, iter = NULL, progress = TRUE, ...)
```

Arguments

object An Object of class explore.

iter Number of iterations (posterior samples; defaults to the number in the object).

progress Logical. Should a progress bar be included (defaults to TRUE)?

... Currently ignored.

Value

An object of class coef, containing two lists.

- betas A list of length p, each containing a p 1 by iter matrix of posterior samples
- object An object of class explore (the fitted model).

References

Kwan CC (2014). "A regression-based interpretation of the inverse of the sample covariance matrix." *Spreadsheets in Education*, **7**(1), 4613.

Stephens G (1998). "On the Inverse of the Covariance Matrix in Portfolio Analysis." *The Journal of Finance*, **53**(5), 1821–1827.

Examples

```
# note: iter = 250 for demonstrative purposes
# data
Y <- ptsd[,1:4]
### example 1: ordinal ###
######################################
# fit model (note + 1, due to zeros)
fit <- explore(Y + 1,</pre>
               type = "ordinal",
               iter = 250,
               progress = FALSE)
# summarize the partial correlations
reg <- coef(fit, progress = FALSE)</pre>
# summary
summ <- summary(reg)</pre>
summ
```

confirm

GGM: Confirmatory Hypothesis Testing

Description

Confirmatory hypothesis testing in GGMs. Hypotheses are expressed as equality and/or inequality contraints on the partial correlations of interest. Here the focus is *not* on determining the graph (see explore) but testing specific hypotheses related to the conditional (in)dependence structure. These methods were introduced in Williams and Mulder (2019).

Usage

```
confirm(
   Y,
   hypothesis,
   prior_sd = 0.25,
   formula = NULL,
   type = "continuous",
   mixed_type = NULL,
   iter = 25000,
   progress = TRUE,
   impute = TRUE,
```

```
seed = 1,
...
```

Arguments

Υ	Matrix (or data frame) of dimensions n (observations) by p (variables).
hypothesis	Character string. The hypothesis (or hypotheses) to be tested. See details.
prior_sd	Numeric. Scale of the prior distribution, approximately the standard deviation of a beta distribution (defaults to 0.25).
formula	An object of class formula. This allows for including control variables in the model (e.g.,, \sim gender * education).
type	Character string. Which type of data for \mathbf{Y} ? The options include continuous, binary, ordinal, or mixed. See the note for further details.
mixed_type	Numeric vector of length p . An indicator for which varibles should be treated as ranks. (1 for rank and 0 to assume normality). The default is currently (dev version) to treat all integer variables as ranks when type = "mixed" and NULL otherwise. See note for further details.
iter	Number of iterations (posterior samples; defaults to 25,000).
progress	Logical. Should a progress bar be included (defaults to TRUE)?
impute	Logicial. Should the missing values (NA) be imputed during model fitting (defaults to TRUE) $?$
seed	An integer for the random seed.
	Currently ignored.

Details

The hypotheses can be written either with the respective column names or numbers. For example, 1–2 denotes the relation between the variables in column 1 and 2. Note that these must correspond to the upper triangular elements of the correlation matrix. This is accomplished by ensuring that the first number is smaller than the second number. This also applies when using column names (i.e., in reference to the column number).

One Hypothesis:

To test whether some relations are larger than others, while others are expected to be equal, this can be writting as

```
• hyp <-c(1--2 > 1--3 = 1--4 > 0),
```

where there is an addition additional contraint that all effects are expected to be positive. This is then compared to the complement.

More Than One Hypothesis:

The above hypothesis can also be compared to, say, a null model by using ";" to seperate the hypotheses, for example,

```
• hyp < c(1--2 > 1--3 = 1--4 > 0; 1--2 = 1--3 = 1--4 = 0).
```

Any number of hypotheses can be compared this way.

Using "&"

It is also possible to include &. This allows for testing one constraint **and** another contraint as one hypothesis.

• hyp
$$<$$
 c("A1--A2 $>$ A1--A3 $=$ A1--A3")

Of course, it is then possible to include additional hypotheses by separating them with ";". Note also that the column names were used in this example (e.g., A1--A2 is the relation between those nodes).

Testing Sums

It might also be interesting to test the sum of partial correlations. For example, that the sum of specific relations is larger than the sum of other relations. This can be written as

• hyp
$$<$$
 c("A1--A2 + A1--A3 > A1--A4 + A1--A5; A1--A2 + A1--A3 = A1--A4 + A1--A5")

Potential Delays:

There is a chance for a potentially long delay from the time the progress bar finishes to when the function is done running. This occurs when the hypotheses require further sampling to be tested, for example, when grouping relations c("(A1--A2, A1--A3) > (A1--A4, A1--A5)". This is not an error.

Controlling for Variables:

When controlling for variables, it is assumed that Y includes *only* the nodes in the GGM and the control variables. Internally, only the predictors that are included in formula are removed from Y. This is not behavior of, say, lm, but was adopted to ensure users do not have to write out each variable that should be included in the GGM. An example is provided below.

Mixed Type:

The term "mixed" is somewhat of a misnomer, because the method can be used for data including *only* continuous or *only* discrete variables (Hoff 2007). This is based on the ranked likelihood which requires sampling the ranks for each variable (i.e., the data is not merely transformed to ranks). This is computationally expensive when there are many levels. For example, with continuous data, there are as many ranks as data points!

The option mixed_type allows the user to determine which variable should be treated as ranks and the "emprical" distribution is used otherwise. This is accomplished by specifying an indicator vector of length *p*. A one indicates to use the ranks, whereas a zero indicates to "ignore" that variable. By default all integer variables are handled as ranks.

Dealing with Errors:

An error is most likely to arise when type = "ordinal". The are two common errors (although still rare):

• The first is due to sampling the thresholds, especially when the data is heavily skewed. This can result in an ill-defined matrix. If this occurs, we recommend to first try decreasing prior_sd (i.e., a more informative prior). If that does not work, then change the data type to type = mixed which then estimates a copula GGM (this method can be used for data containing **only** ordinal variable). This should work without a problem.

• The second is due to how the ordinal data are categorized. For example, if the error states that the index is out of bounds, this indicates that the first category is a zero. This is not allowed, as the first category must be one. This is addressed by adding one (e.g., Y + 1) to the data matrix.

Value

The returned object of class confirm contains a lot of information that is used for printing and plotting the results. For users of **BGGM**, the following are the useful objects:

- out_hyp_prob Posterior hypothesis probabilities.
- info An object of class BF from the R package BFpack.

Note

"Default" Prior:

In Bayesian statistics, a default Bayes factor needs to have several properties. I refer interested users to section 2.2 in Dablander et al. (2020). In Williams and Mulder (2019), some of these propteries were investigated (e.g., model selection consistency). That said, we would not consider this a "default" or "automatic" Bayes factor and thus we encourage users to perform sensitivity analyses by varying the scale of the prior distribution.

Furthermore, it is important to note there is no "correct" prior and, also, there is no need to entertain the possibility of a "true" model. Rather, the Bayes factor can be interpreted as which hypothesis best (relative to each other) predicts the observed data (Section 3.2 in Kass and Raftery 1995).

Interpretation of Conditional (In)dependence Models for Latent Data:

See BGGM-package for details about interpreting GGMs based on latent data (i.e, all data types besides "continuous")

References

Dablander F, Bergh Dvd, Ly A, Wagenmakers E (2020). "Default Bayes Factors for Testing the (In) equality of Several Population Variances." *arXiv preprint arXiv:2003.06278*.

Hoff PD (2007). "Extending the rank likelihood for semiparametric copula estimation." *The Annals of Applied Statistics*, **1**(1), 265–283. doi: 10.1214/07AOAS107.

Kass RE, Raftery AE (1995). "Bayes Factors." *Journal of the American Statistical Association*, **90**(430), 773–795.

Williams DR, Mulder J (2019). "Bayesian Hypothesis Testing for Gaussian Graphical Models: Conditional Independence and Order Constraints." *PsyArXiv*. doi: 10.31234/osf.io/ypxd8.

Examples

note: iter = 250 for demonstrative purposes

constrained_posterior 17

constrained_posterior Constrained Posterior Distribution

Description

Compute the posterior distribution with off-diagonal elements of the precision matrix constrained to zero.

Usage

```
constrained_posterior(
  object,
  adj,
  method = "direct",
  iter = 5000,
  progress = TRUE,
  ...
)
```

Arguments

object An object of class estimate or explore

adj A p by p adjacency matrix. The zero entries denote the elements that should be

constrained to zero.

method Character string. Which method should be used? Defaults to the "direct sam-

pler" (i.e., method = "direct") described in page 122, section 2.4, Lenkoski

(2013). The other option is a Metropolis-Hastings algorithm (MH). See details.

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iter	Number of iterations (posterior samples; defaults to 5000).
progress	Logical. Should a progress bar be included (defaults to TRUE) ?
	Currently ignored.

Value

An object of class contrained, including

- precision_mean The posterior mean for the precision matrix.
- pcor_mean The posterior mean for the precision matrix.
- precision_samps A 3d array of dimension p by p by iter including the sampled precision matrices.
- pcor_samps A 3d array of dimension p by p by iter including sampled partial correlations matrices.

References

Lenkoski A (2013). "A direct sampler for G-Wishart variates." Stat, 2(1), 119-128.

Examples

convergence

MCMC Convergence

Description

Monitor convergence of the MCMC algorithms.

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Usage

```
convergence(object, param = NULL, type = "trace", print_names = FALSE)
```

Arguments

object An object of class estimate or explore

param Character string. Names of parameters for which to monitor MCMC conver-

gence.

type Character string. Which type of convergence plot ? The current options are

trace (default) and acf.

print_names Logical. Should the parameter names be printed (defaults to FALSE)? This can

be used to first determine the parameter names to specify in type.

Value

A list of ggplot objects.

Note

An overview of MCMC diagnostics can be found here.

```
# note: iter = 250 for demonstrative purposes
# data
Y <- ptsd[,1:5]
##### continuous ######
############################
fit <- estimate(Y, iter = 250,</pre>
               progress = FALSE)
# print names first
convergence(fit, print_names = TRUE)
# trace plots
convergence(fit, type = "trace",
           param = c("B1--B2", "B1--B3"))[[1]]
# acf plots
convergence(fit, type = "acf",
           param = c("B1--B2", "B1--B3"))[[1]]
```

20 csws

CSWS

Data: Contingencies of Self-Worth Scale (CSWS)

Description

A dataset containing items from the Contingencies of Self-Worth Scale (CSWS) scale. There are 35 variables and 680 observations

Usage

```
data("csws")
```

Format

A data frame with 35 variables and 680 observations (7 point Likert scale)

Details

- 1 When I think I look attractive, I feel good about myself
- 2 My self-worth is based on God's love
- 3 I feel worthwhile when I perform better than others on a task or skill.
- 4 My self-esteem is unrelated to how I feel about the way my body looks.
- 5 Doing something I know is wrong makes me lose my self-respect
- 6 I don't care if other people have a negative opinion about me.
- 7 Knowing that my family members love me makes me feel good about myself.
- 8 I feel worthwhile when I have God's love.
- 9 I can't respect myself if others don't respect me.
- 10 My self-worth is not influenced by the quality of my relationships with my family members.
- 11 Whenever I follow my moral principles, my sense of self-respect gets a boost.
- 12 Knowing that I am better than others on a task raises my self-esteem.
- 13 My opinion about myself isn't tied to how well I do in school.
- 14 I couldn't respect myself if I didn't live up to a moral code.
- 15 I don't care what other people think of me.
- 16 When my family members are proud of me, my sense of self-worth increases.
- 17 My self-esteem is influenced by how attractive I think my face or facial features are.
- 18 My self-esteem would suffer if I didn't have God's love.
- 19 Doing well in school gives me a sense of selfrespect.
- 20 Doing better than others gives me a sense of self-respect.
- 21 My sense of self-worth suffers whenever I think I don't look good.
- 22 I feel better about myself when I know I'm doing well academically.

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- 23 What others think of me has no effect on what I think about myself.
- 24 When I don't feel loved by my family, my selfesteem goes down.
- 25 My self-worth is affected by how well I do when I am competing with others.
- 26 My self-esteem goes up when I feel that God loves me.
- 27 My self-esteem is influenced by my academic performance.
- 28 My self-esteem would suffer if I did something unethical.
- 29 It is important to my self-respect that I have a family that cares about me.
- 30 My self-esteem does not depend on whether or not I feel attractive.
- 31 When I think that I'm disobeying God, I feel bad about myself.
- 32 My self-worth is influenced by how well I do on competitive tasks.
- 33 I feel bad about myself whenever my academic performance is lacking.
- 34 My self-esteem depends on whether or not I follow my moral/ethical principles.
- 35 My self-esteem depends on the opinions others hold of me.
- gender "M" (male) or "F" (female)

Note

There are seven domains

FAMILY SUPPORT: items 7, 10, 16, 24, and 29.

COMPETITION: items 3, 12, 20, 25, and 32.

APPEARANCE: items 1, 4, 17, 21, and 30.

GOD'S LOVE: items 2, 8, 18, 26, and 31.

ACADEMIC COMPETENCE: items 13, 19, 22, 27, and 33.

VIRTUE: items 5, 11, 14, 28, and 34.

APPROVAL FROM OTHERS: items: 6, 9, 15, 23, and 35.

References

Briganti, G., Fried, E. I., & Linkowski, P. (2019). Network analysis of Contingencies of Self-Worth Scale in 680 university students. Psychiatry research, 272, 252-257.

Examples

data("csws")

Description

A data frame containing 403 observations (n = 403) and 16 variables (p = 16) measured on the 4-point likert scale (depression: 9; anxiety: 7).

Usage

```
data("depression_anxiety_t1")
```

Format

A data frame containing 403 observations (n = 7466) and 16 variables (p = 16) measured on the 4-point likert scale.

Details

Depression:

- PHQ1 Little interest or pleasure in doing things?
- PHQ2 Feeling down, depressed, or hopeless?
- PHQ3 Trouble falling or staying asleep, or sleeping too much?
- PHQ4 Feeling tired or having little energy?
- PHQ5 Poor appetite or overeating?
- PHQ6 Feeling bad about yourself or that you are a failure or have let yourself or your family down?
- PHQ7 Trouble concentrating on things, such as reading the newspaper or watching television?
- PHQ8 Moving or speaking so slowly that other people could have noticed? Or so fidgety or restless that you have been moving a lot more than usual?
- PHQ9 Thoughts that you would be better off dead, or thoughts of hurting yourself in some way?

Anxiety

- GAD1 Feeling nervous, anxious, or on edge
- GAD2 Not being able to stop or control worrying
- · GAD3 Worrying too much about different things
- GAD4 Trouble relaxing
- GAD5 Being so restless that it's hard to sit still
- · GAD6 Becoming easily annoyed or irritable
- GAD7 Feeling afraid as if something awful might happen

References

Forbes, M. K., Baillie, A. J., & Schniering, C. A. (2016). A structural equation modeling analysis of the relationships between depression, anxiety, and sexual problems over time. The Journal of Sex Research, 53(8), 942-954.

Forbes, M. K., Wright, A. G., Markon, K. E., & Krueger, R. F. (2019). Quantifying the reliability and replicability of psychopathology network characteristics. Multivariate behavioral research, 1-19.

Jones, P. J., Williams, D. R., & McNally, R. J. (2019). Sampling variability is not nonreplication: a Bayesian reanalysis of Forbes, Wright, Markon, & Krueger.

Examples

depression_anxiety_t2 Data: Depression and Anxiety (Time 2)

Description

A data frame containing 403 observations (n = 403) and 16 variables (p = 16) measured on the 4-point likert scale (depression: 9; anxiety: 7).

Usage

```
data("depression_anxiety_t2")
```

Format

A data frame containing 403 observations (n = 7466) and 16 variables (p = 16) measured on the 4-point likert scale.

Details

Depression:

- PHQ1 Little interest or pleasure in doing things?
- PHQ2 Feeling down, depressed, or hopeless?
- PHQ3 Trouble falling or staying asleep, or sleeping too much?
- PHQ4 Feeling tired or having little energy?

- PHQ5 Poor appetite or overeating?
- PHQ6 Feeling bad about yourself or that you are a failure or have let yourself or your family down?
- PHQ7 Trouble concentrating on things, such as reading the newspaper or watching television?
- PHQ8 Moving or speaking so slowly that other people could have noticed? Or so fidgety or restless that you have been moving a lot more than usual?
- PHQ9 Thoughts that you would be better off dead, or thoughts of hurting yourself in some way?

Anxiety

- GAD1 Feeling nervous, anxious, or on edge
- GAD2 Not being able to stop or control worrying
- GAD3 Worrying too much about different things
- GAD4 Trouble relaxing
- GAD5 Being so restless that it's hard to sit still
- · GAD6 Becoming easily annoyed or irritable
- GAD7 Feeling afraid as if something awful might happen

References

Forbes, M. K., Baillie, A. J., & Schniering, C. A. (2016). A structural equation modeling analysis of the relationships between depression, anxiety, and sexual problems over time. The Journal of Sex Research, 53(8), 942-954.

Forbes, M. K., Wright, A. G., Markon, K. E., & Krueger, R. F. (2019). Quantifying the reliability and replicability of psychopathology network characteristics. Multivariate behavioral research, 1-19.

Jones, P. J., Williams, D. R., & McNally, R. J. (2019). Sampling variability is not nonreplication: a Bayesian reanalysis of Forbes, Wright, Markon, & Krueger.

estimate GGM: Estimation

Description

Estimate the conditional (in)dependence with either an analytic solution or efficiently sampling from the posterior distribution. These methods were introduced in Williams (2018). The graph is selected with select.estimate and then plotted with plot.select.

Usage

```
estimate(
   Y,
   formula = NULL,
   type = "continuous",
   mixed_type = NULL,
   analytic = FALSE,
   prior_sd = 0.25,
   iter = 5000,
   impute = FALSE,
   progress = TRUE,
   seed = 1,
   ...
)
```

Arguments

Υ	Matrix (or data frame) of dimensions n (observations) by p (variables).
formula	An object of class formula. This allows for including control variables in the model (i.e., ~ gender). See the note for further details.
type	Character string. Which type of data for Y? The options include continuous, binary, ordinal, or mixed. Note that mixed can be used for data with only ordinal variables. See the note for further details.
mixed_type	Numeric vector. An indicator of length p for which variables should be treated as ranks. (1 for rank and 0 to assume normality). The default is currently to treat all integer variables as ranks when type = "mixed" and NULL otherwise. See note for further details.
analytic	Logical. Should the analytic solution be computed (default is FALSE)?
prior_sd	Scale of the prior distribution, approximately the standard deviation of a beta distribution (defaults to 0.50).
iter	Number of iterations (posterior samples; defaults to 5000).
impute	Logical. Should the missing values (NA) be imputed during model fitting (defaults to TRUE) $?$
progress	Logical. Should a progress bar be included (defaults to TRUE)?
seed	An integer for the random seed.
	Currently ignored.

Details

The default is to draw samples from the posterior distribution (analytic = FALSE). The samples are required for computing edge differences (see ggm_compare_estimate), Bayesian R2 introduced in Gelman et al. (2019) (see predictability), etc. If the goal is to *only* determine the non-zero effects, this can be accomplished by setting analytic = TRUE. This is particularly useful when a fast solution is needed (see the examples in ggm_compare_ppc)

Controlling for Variables:

When controlling for variables, it is assumed that Y includes *only* the nodes in the GGM and the control variables. Internally, only the predictors that are included in formula are removed from Y. This is not behavior of, say, 1m, but was adopted to ensure users do not have to write out each variable that should be included in the GGM. An example is provided below.

Mixed Type:

The term "mixed" is somewhat of a misnomer, because the method can be used for data including *only* continuous or *only* discrete variables. This is based on the ranked likelihood which requires sampling the ranks for each variable (i.e., the data is not merely transformed to ranks). This is computationally expensive when there are many levels. For example, with continuous data, there are as many ranks as data points!

The option mixed_type allows the user to determine which variable should be treated as ranks and the "emprical" distribution is used otherwise (Hoff 2007). This is accomplished by specifying an indicator vector of length p. A one indicates to use the ranks, whereas a zero indicates to "ignore" that variable. By default all integer variables are treated as ranks.

Dealing with Errors:

An error is most likely to arise when type = "ordinal". The are two common errors (although still rare):

- The first is due to sampling the thresholds, especially when the data is heavily skewed. This can result in an ill-defined matrix. If this occurs, we recommend to first try decreasing prior_sd (i.e., a more informative prior). If that does not work, then change the data type to type = mixed which then estimates a copula GGM (this method can be used for data containing **only** ordinal variable). This should work without a problem.
- The second is due to how the ordinal data are categorized. For example, if the error states that the index is out of bounds, this indicates that the first category is a zero. This is not allowed, as the first category must be one. This is addressed by adding one (e.g., Y + 1) to the data matrix.

Imputing Missing Values:

Missing values are imputed with the approach described in Hoff (2009). The basic idea is to impute the missing values with the respective posterior pedictive distribution, given the observed data, as the model is being estimated. Note that the default is TRUE, but this ignored when there are no missing values. If set to FALSE, and there are missing values, list-wise deletion is performed with na.omit.

Value

The returned object of class estimate contains a lot of information that is used for printing and plotting the results. For users of **BGGM**, the following are the useful objects:

- pcor_mat Partial correltion matrix (posterior mean).
- post_samp An object containing the posterior samples.

Note

Posterior Uncertainty:

A key feature of **BGGM** is that there is a posterior distribution for each partial correlation. This readily allows for visitualizing uncertainty in the estimates. This feature works with all data types and is accomplished by plotting the summary of the estimate object (i.e., plot(summary(fit))). Several examples are provided below.

Interpretation of Conditional (In)dependence Models for Latent Data:

See BGGM-package for details about interpreting GGMs based on latent data (i.e, all data types besides "continuous")

References

Gelman A, Goodrich B, Gabry J, Vehtari A (2019). "R-squared for Bayesian Regression Models." *American Statistician*, **73**(3), 307–309. ISSN 15372731, doi: 10.1080/00031305.2018.1549100.

Hoff PD (2007). "Extending the rank likelihood for semiparametric copula estimation." *The Annals of Applied Statistics*, **1**(1), 265–283. doi: 10.1214/07AOAS107.

Hoff PD (2009). A first course in Bayesian statistical methods, volume 580. Springer.

Williams DR (2018). "Bayesian Estimation for Gaussian Graphical Models: Structure Learning, Predictability, and Network Comparisons." *arXiv*. doi: 10.31234/OSF.IO/X8DPR.

```
# select the graph
E <- select(fit)</pre>
# plot the selected graph
plt_E <- plot(select(fit))</pre>
# ordinal
# fit model (note + 1, due to zeros)
fit <- estimate(Y + 1, type = "ordinal",</pre>
                iter = 250)
# summarize the partial correlations
summ <- summary(fit)</pre>
# plot the summary
plt <- plot(summary(fit))</pre>
# select the graph
E <- select(fit)</pre>
# plot the selected graph
plt_E <- plot(select(fit))</pre>
## example 2: analytic solution ##
# (only continuous)
# data
Y <- ptsd
# fit model
fit <- estimate(Y, analytic = TRUE)</pre>
# summarize the partial correlations
summ <- summary(fit)</pre>
# plot summary
plt_summ <- plot(summary(fit))</pre>
# select graph
E <- select(fit)</pre>
# plot the selected graph
plt_E <- plot(select(fit))</pre>
```

explore 29

explore

GGM: Exploratory Hypothesis Testing

Description

Learn the conditional (in)dependence structure with the Bayes factor using the matrix-F prior distribution (Mulder and Pericchi 2018). These methods were introduced in Williams and Mulder (2019). The graph is selected with select.explore and then plotted with plot.select.

Usage

```
explore(
   Y,
   formula = NULL,
   type = "continuous",
   mixed_type = NULL,
   analytic = FALSE,
   prior_sd = 0.25,
   iter = 5000,
   progress = TRUE,
   impute = TRUE,
   seed = 1,
   ...
)
```

Arguments

Υ	Matrix (or data frame) of dimensions n (observations) by p (variables).
formula	An object of class formula. This allows for including control variables in the model (i.e., \sim gender).
type	Character string. Which type of data for Y? The options include continuous, binary, ordinal, or mixed (semi-parametric copula). See the note for further details.
mixed_type	Numeric vector. An indicator of length p for which varibles should be treated as ranks. (1 for rank and 0 to assume normality). The default is to treat all integer variables as ranks when type = "mixed" and NULL otherwise. See note for further details.
analytic	Logical. Should the analytic solution be computed (default is FALSE)? (currently not implemented)
prior_sd	Scale of the prior distribution, approximately the standard deviation of a beta distribution (defaults to 0.25).
iter	Number of iterations (posterior samples; defaults to 5000).
progress	Logical. Should a progress bar be included (defaults to TRUE)?
impute	Logicial. Should the missing values (NA) be imputed during model fitting (defaults to TRUE) $?$

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An integer for the random seed.
... Currently ignored (leave empty).

Details

Controlling for Variables:

When controlling for variables, it is assumed that Y includes *only* the nodes in the GGM and the control variables. Internally, only the predictors that are included in formula are removed from Y. This is not behavior of, say, lm, but was adopted to ensure users do not have to write out each variable that should be included in the GGM. An example is provided below.

Mixed Type:

The term "mixed" is somewhat of a misnomer, because the method can be used for data including *only* continuous or *only* discrete variables. This is based on the ranked likelihood which requires sampling the ranks for each variable (i.e., the data is not merely transformed to ranks). This is computationally expensive when there are many levels. For example, with continuous data, there are as many ranks as data points!

The option mixed_type allows the user to determine which variable should be treated as ranks and the "emprical" distribution is used otherwise. This is accomplished by specifying an indicator vector of length *p*. A one indicates to use the ranks, whereas a zero indicates to "ignore" that variable. By default all integer variables are handled as ranks.

Dealing with Errors:

An error is most likely to arise when type = "ordinal". The are two common errors (although still rare):

- The first is due to sampling the thresholds, especially when the data is heavily skewed. This can result in an ill-defined matrix. If this occurs, we recommend to first try decreasing prior_sd (i.e., a more informative prior). If that does not work, then change the data type to type = mixed which then estimates a copula GGM (this method can be used for data containing **only** ordinal variable). This should work without a problem.
- The second is due to how the ordinal data are categorized. For example, if the error states that the index is out of bounds, this indicates that the first category is a zero. This is not allowed, as the first category must be one. This is addressed by adding one (e.g., Y + 1) to the data matrix.

Imputing Missing Values:

Missing values are imputed with the approach described in Hoff (2009). The basic idea is to impute the missing values with the respective posterior pedictive distribution, given the observed data, as the model is being estimated. Note that the default is TRUE, but this ignored when there are no missing values. If set to FALSE, and there are missing values, list-wise deletion is performed with na.omit.

Value

The returned object of class explore contains a lot of information that is used for printing and plotting the results. For users of **BGGM**, the following are the useful objects:

- pcor_mat partial correltion matrix (posterior mean).
- post_samp an object containing the posterior samples.

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Note

Posterior Uncertainty:

A key feature of **BGGM** is that there is a posterior distribution for each partial correlation. This readily allows for visiualizing uncertainty in the estimates. This feature works with all data types and is accomplished by plotting the summary of the explore object (i.e., plot(summary(fit))). Note that in contrast to estimate (credible intervals), the posterior standard deviation is plotted for explore objects.

"Default" Prior:

In Bayesian statistics, a default Bayes factor needs to have several properties. I refer interested users to section 2.2 in Dablander et al. (2020). In Williams and Mulder (2019), some of these propteries were investigated including model selection consistency. That said, we would not consider this a "default" (or "automatic") Bayes factor and thus we encourage users to perform sensitivity analyses by varying the scale of the prior distribution.

Furthermore, it is important to note there is no "correct" prior and, also, there is no need to entertain the possibility of a "true" model. Rather, the Bayes factor can be interpreted as which hypothesis best (**relative** to each other) predicts the observed data (Section 3.2 in Kass and Raftery 1995).

Interpretation of Conditional (In)dependence Models for Latent Data:

See BGGM-package for details about interpreting GGMs based on latent data (i.e, all data types besides "continuous")

References

Dablander F, Bergh Dvd, Ly A, Wagenmakers E (2020). "Default Bayes Factors for Testing the (In) equality of Several Population Variances." *arXiv preprint arXiv:2003.06278*.

Hoff PD (2009). A first course in Bayesian statistical methods, volume 580. Springer.

Kass RE, Raftery AE (1995). "Bayes Factors." *Journal of the American Statistical Association*, **90**(430), 773–795.

Mulder J, Pericchi L (2018). "The Matrix-F Prior for Estimating and Testing Covariance Matrices." *Bayesian Analysis*, 1–22. ISSN 19316690, doi: 10.1214/17BA1092.

Williams DR, Mulder J (2019). "Bayesian Hypothesis Testing for Gaussian Graphical Models: Conditional Independence and Order Constraints." *PsyArXiv*. doi: 10.31234/osf.io/ypxd8.

32 fisher_r_to_z

fisher_r_to_z

Fisher Z Transformation

Description

Tranform correlations to Fisher's Z

Usage

```
fisher_r_to_z(r)
```

Arguments

r

correlation (can be a vector)

Value

Fisher Z transformed correlation(s)

```
fisher_r_to_z(0.5)
```

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fisher_z_to_r

Fisher Z Back Transformation

Description

Back tranform Fisher's Z to correlations

Usage

```
fisher_z_to_r(z)
```

Arguments

Z

Fisher Z

Value

Correlation (s) (backtransformed)

Examples

```
fisher_z_to_r(0.5)
```

gen_ordinal

Generate Ordinal and Binary data

Description

Generate Multivariate Ordinal and Binary data.

Usage

```
gen_ordinal(n, p, levels = 2, cor_mat, empirical = FALSE)
```

Arguments

n Number of observations (n).
p Number of variables (p).

levels Number of categories (defaults to 2; binary data).

cor_mat A p by p matrix including the true correlation structure.

empirical Logical. If true, cor_mat specifies the empirical not population covariance ma-

trix.

Value

A n by p data matrix.

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Note

In order to allow users to enjoy the functionality of **BGGM**, we had to make minor changes to the function rmvord_naiv from the R package **orddata** (Leisch et al. 2010). All rights to, and credit for, the function rmvord_naiv belong to the authors of that package.

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References

Leisch F, Kaiser AWS, Hornik K (2010). *orddata: Generation of Artificial Ordinal and Binary Data*. R package version 0.1/r4, https://R-Forge.R-project.org/projects/orddata/.

```
######## example 1 ##########
#####################################
main <- ptsd_cor1[1:5,1:5]
p <- ncol(main)</pre>
pcors <- -(cov2cor(solve(main)) -diag(p))</pre>
diag(pcors) <- 1
pcors <- ifelse(abs(pcors) < 0.05, 0, pcors)</pre>
inv <- -pcors
diag(inv) <- 1
cors <- cov2cor( solve(inv))</pre>
# example data
Y \leftarrow BGGM::gen\_ordinal(n = 500, p = 5,
                       levels = 2,
                       cor_mat = cors,
                       empirical = FALSE)
#####################################
######## example 2 ##########
#####################################
# empirical = TRUE
Y <- gen_ordinal(n = 500,
                  p = 16,
                  levels = 5,
                  cor_mat = ptsd_cor1,
                  empirical = TRUE)
```

 ${\tt ggm_compare_confirm}$

GGM Compare: Confirmatory Hypothesis Testing

Description

Confirmatory hypothesis testing for comparing GGMs. Hypotheses are expressed as equality and/or inequality contraints on the partial correlations of interest. Here the focus is *not* on determining the graph (see explore) but testing specific hypotheses related to the conditional (in)dependence structure. These methods were introduced in Williams and Mulder (2019) and in Williams et al. (2020)

Usage

```
ggm_compare_confirm(
    ...,
    hypothesis,
    formula = NULL,
    type = "continuous",
    mixed_type = NULL,
    prior_sd = 0.25,
    iter = 25000,
    impute = TRUE,
    progress = TRUE,
    seed = 1
)
```

Arguments

• • •	At least two matrices (or data frame) of dimensions n (observations) by p (nodes).
hypothesis	Character string. The hypothesis (or hypotheses) to be tested. See notes for futher details.
formula	an object of class formula. This allows for including control variables in the model (i.e., \sim gender).
type	Character string. Which type of data for Y? The options include continuous, binary, ordinal, or mixed. Note that mixed can be used for data with only ordinal variables. See the note for further details.
mixed_type	numeric vector. An indicator of length p for which varibles should be treated as ranks. (1 for rank and 0 to assume normality). The default is currently (dev version) to treat all integer variables as ranks when type = "mixed" and NULL otherwise. See note for further details.
prior_sd	Numeric. The scale of the prior distribution (centered at zero), in reference to a beta distribution (defaults to 0.25).
iter	Number of iterations (posterior samples; defaults to 25,000).

impute Logicial. Should the missing values (NA) be imputed during model fitting (de-

faults to TRUE)?

progress Logical. Should a progress bar be included (defaults to TRUE)?

seed An integer for the random seed.

Details

The hypotheses can be written either with the respective column names or numbers. For example, g1_1--2 denotes the relation between the variables in column 1 and 2 for group 1. The g1_ is required and the only difference from confirm (one group). Note that these must correspond to the upper triangular elements of the correlation matrix. This is accomplished by ensuring that the first number is smaller than the second number. This also applies when using column names (i.e., in reference to the column number).

One Hypothesis:

To test whether a relation in larger in one group, while both are expected to be positive, this can be written as

• hyp
$$<-c(g1_1--2>g2_1--2>0)$$

This is then compared to the complement.

More Than One Hypothesis:

The above hypothesis can also be compared to, say, a null model by using ";" to seperate the hypotheses, for example,

• hyp
$$<-c(g1_1--2>g2_1--2>0; g1_1--2=g2_1--2=0).$$

Any number of hypotheses can be compared this way.

Using "&"

It is also possible to include &. This allows for testing one constraint **and** another contraint as one hypothesis.

• hyp
$$<-c("g1_A1--A2 > g2_A1--A2 & g1_A1--A3 = g2_A1--A3")$$

Of course, it is then possible to include additional hypotheses by separating them with ";".

Testing Sums

It might also be interesting to test the sum of partial correlations. For example, that the sum of specific relations in one group is larger than the sum in another group.

Potential Delays:

There is a chance for a potentially long delay from the time the progress bar finishes to when the function is done running. This occurs when the hypotheses require further sampling to be tested, for example, when grouping relations $c("(g1_A1--A2, g2_A2--A3)) > (g2_A1--A2, g2_A2--A3)"$. This is not an error.

Controlling for Variables:

When controlling for variables, it is assumed that Y includes *only* the nodes in the GGM and the control variables. Internally, only the predictors that are included in formula are removed from Y. This is not behavior of, say, lm, but was adopted to ensure users do not have to write out each variable that should be included in the GGM. An example is provided below.

Mixed Type:

The term "mixed" is somewhat of a misnomer, because the method can be used for data including *only* continuous or *only* discrete variables (Hoff 2007). This is based on the ranked likelihood which requires sampling the ranks for each variable (i.e., the data is not merely transformed to ranks). This is computationally expensive when there are many levels. For example, with continuous data, there are as many ranks as data points!

The option mixed_type allows the user to determine which variable should be treated as ranks and the "emprical" distribution is used otherwise. This is accomplished by specifying an indicator vector of length *p*. A one indicates to use the ranks, whereas a zero indicates to "ignore" that variable. By default all integer variables are handled as ranks.

Dealing with Errors:

An error is most likely to arise when type = "ordinal". The are two common errors (although still rare):

- The first is due to sampling the thresholds, especially when the data is heavily skewed. This can result in an ill-defined matrix. If this occurs, we recommend to first try decreasing prior_sd (i.e., a more informative prior). If that does not work, then change the data type to type = mixed which then estimates a copula GGM (this method can be used for data containing only ordinal variable). This should work without a problem.
- The second is due to how the ordinal data are categorized. For example, if the error states that the index is out of bounds, this indicates that the first category is a zero. This is not allowed, as the first category must be one. This is addressed by adding one (e.g., Y + 1) to the data matrix.

Imputing Missing Values:

Missing values are imputed with the approach described in Hoff (2009). The basic idea is to impute the missing values with the respective posterior pedictive distribution, given the observed data, as the model is being estimated. Note that the default is TRUE, but this ignored when there are no missing values. If set to FALSE, and there are missing values, list-wise deletion is performed with na.omit.

Value

The returned object of class confirm contains a lot of information that is used for printing and plotting the results. For users of **BGGM**, the following are the useful objects:

- out_hyp_prob Posterior hypothesis probabilities.
- info An object of class BF from the R package **BFpack** (Mulder et al. 2019)

Note

"Default" Prior:

In Bayesian statistics, a default Bayes factor needs to have several properties. I refer interested users to section 2.2 in Dablander et al. (2020). In Williams and Mulder (2019), some of these propteries were investigated (e.g., model selection consistency). That said, we would not consider this a "default" or "automatic" Bayes factor and thus we encourage users to perform sensitivity analyses by varying the scale of the prior distribution (prior_sd).

Furthermore, it is important to note there is no "correct" prior and, also, there is no need to entertain the possibility of a "true" model. Rather, the Bayes factor can be interpreted as which hypothesis best (relative to each other) predicts the observed data (Section 3.2 in Kass and Raftery 1995).

Interpretation of Conditional (In)dependence Models for Latent Data:

See BGGM-package for details about interpreting GGMs based on latent data (i.e, all data types besides "continuous")

References

Dablander F, Bergh Dvd, Ly A, Wagenmakers E (2020). "Default Bayes Factors for Testing the (In) equality of Several Population Variances." *arXiv preprint arXiv:2003.06278*.

Hoff PD (2007). "Extending the rank likelihood for semiparametric copula estimation." *The Annals of Applied Statistics*, **1**(1), 265–283. doi: 10.1214/07AOAS107.

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Mulder J, Gu X, Olsson-Collentine A, Tomarken A, Böing-Messing F, Hoijtink H, Meijerink M, Williams DR, Menke J, Fox J, others (2019). "BFpack: Flexible Bayes Factor Testing of Scientific Theories in R." *arXiv preprint arXiv:1911.07728*.

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Williams DR, Rast P, Pericchi LR, Mulder J (2020). "Comparing Gaussian graphical models with the posterior predictive distribution and Bayesian model selection." *Psychological Methods*. doi: 10.1037/met0000254.

test

```
# males
Ymale <- subset(Y, gender == 1,</pre>
                select = -c(education,
                            gender))[,1:5]
# females
Yfemale <- subset(Y, gender == 2,</pre>
                   select = -c(education,
                               gender))[,1:5]
# exhaustive
hypothesis <- c("g1\_A1--A2 > g2\_A1--A2;
                g1_A1--A2 < g2_A1--A2;
                 g1_A1--A2 = g2_A1--A2")
# test hyp
test <- ggm_compare_confirm(Ymale, Yfemale,</pre>
                          hypothesis = hypothesis,
                          iter = 250,
                          progress = FALSE)
# print (evidence not strong)
test
#### example 2: sensitivity to prior ####
# continued from example 1
# decrease prior SD
test <- ggm_compare_confirm(Ymale,</pre>
                          prior_sd = 0.1,
                          hypothesis = hypothesis,
                          iter = 250,
                          progress = FALSE)
# print
test
# indecrease prior SD
test <- ggm_compare_confirm(Ymale,</pre>
                          Yfemale,
                          prior_sd = 0.5,
                          hypothesis = hypothesis,
                          iter = 250,
                          progress = FALSE)
# print
```

```
#### example 3: mixed data #####
hypothesis <- c("g1\_A1--A2 > g2\_A1--A2;
              g1_A1--A2 < g2_A1--A2;
              g1_A1--A2 = g2_A1--A2")
# test (1000 for example)
test <- ggm_compare_confirm(Ymale,</pre>
                       Yfemale,
                       type = "mixed",
                       hypothesis = hypothesis,
                       iter = 250,
                       progress = FALSE)
# print
test
################################
##### example 4: control #####
# control for education
# data
Y <- bfi
# males
Ymale <- subset(Y, gender == 1,</pre>
               select = -c(gender))[,c(1:5, 26)]
# females
Yfemale <- subset(Y, gender == 2,
               select = -c(gender))[,c(1:5, 26)]
# test
test <- ggm_compare_confirm(Ymale,</pre>
                        formula = ~ education,
                        hypothesis = hypothesis,
                        iter = 250,
                        progress = FALSE)
# print
test
##### example 5: many relations #####
# data
Y <- bfi
```

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```
hypothesis <- c("g1_A1--A2 > g2_A1--A2 & g1_A1--A3 = g2_A1--A3;
                 g1_A1-A2 = g2_A1-A2 & g1_A1-A3 = g2_A1-A3;
                 g1_A1-A2 = g2_A1-A2 = g1_A1-A3 = g2_A1-A3"
Ymale
       <- subset(Y, gender == 1,
                  select = -c(education,
                              gender))[,1:5]
# females
Yfemale <- subset(Y, gender == 2,
                     select = -c(education,
                                 gender))[,1:5]
test <- ggm_compare_confirm(Ymale,</pre>
                            Yfemale,
                             hypothesis = hypothesis,
                             iter = 250,
                             progress = FALSE)
# print
test
```

Description

Compare partial correlations that are estimated from any number of groups. This method works for continuous, binary, ordinal, and mixed data (a combination of categorical and continuous variables). The approach (i.e., a difference between posterior distributions) was described in Williams (2018).

Usage

```
ggm_compare_estimate(
    ...,
    formula = NULL,
    type = "continuous",
    mixed_type = NULL,
    analytic = FALSE,
    prior_sd = 0.5,
    iter = 5000,
    impute = TRUE,
    progress = TRUE,
    seed = 1
)
```

Arguments

•••	Matrices (or data frames) of dimensions n (observations) by p (variables). Requires at least two.
formula	An object of class formula. This allows for including control variables in the model (i.e., ~ gender). See the note for further details.
type	Character string. Which type of data for \mathbf{Y} ? The options include continuous, binary, ordinal, or continuous. See the note for further details.
<pre>mixed_type</pre>	Numeric vector. An indicator of length p for which varibles should be treated as ranks. (1 for rank and 0 to use the 'empirical' or observed distribution). The default is currently to treat all integer variables as ranks when type = "mixed" and NULL otherwise. See note for further details.
analytic	Logical. Should the analytic solution be computed (default is FALSE)? This is only available for continuous data. Note that if type = "mixed" and analytic = TRUE, the data will automatically be treated as continuous.
prior_sd	The scale of the prior distribution (centered at zero), in reference to a beta distribution (defaults to 0.50). See note for further details.
iter	Number of iterations (posterior samples; defaults to 5000).
impute	Logicial. Should the missing values (NA) be imputed during model fitting (defaults to TRUE) $?$
progress	Logical. Should a progress bar be included (defaults to TRUE)?
seed	An integer for the random seed.

Details

This function can be used to compare the partial correlations for any number of groups. This is accomplished with pairwise comparisons for each relation. In the case of three groups, for example, group 1 and group 2 are compared, then group 1 and group 3 are compared, and then group 2 and group 3 are compared. There is a full distibution for each difference that can be summarized (i.e., summary.ggm_compare_estimate) and then visualized (i.e., plot.summary.ggm_compare_estimate). The graph of difference is selected with select.ggm_compare_estimate).

Controlling for Variables:

When controlling for variables, it is assumed that Y includes *only* the nodes in the GGM and the control variables. Internally, only the predictors that are included in formula are removed from Y. This is not behavior of, say, 1m, but was adopted to ensure users do not have to write out each variable that should be included in the GGM. An example is provided below.

Mixed Type:

The term "mixed" is somewhat of a misnomer, because the method can be used for data including *only* continuous or *only* discrete variables. This is based on the ranked likelihood which requires sampling the ranks for each variable (i.e., the data is not merely transformed to ranks). This is computationally expensive when there are many levels. For example, with continuous data, there are as many ranks as data points!

The option mixed_type allows the user to determine which variable should be treated as ranks and the "emprical" distribution is used otherwise. This is accomplished by specifying an indicator vector

of length p. A one indicates to use the ranks, whereas a zero indicates to "ignore" that variable. By default all integer variables are handled as ranks.

Dealing with Errors:

An error is most likely to arise when type = "ordinal". The are two common errors (although still rare):

- The first is due to sampling the thresholds, especially when the data is heavily skewed. This can result in an ill-defined matrix. If this occurs, we recommend to first try decreasing prior_sd (i.e., a more informative prior). If that does not work, then change the data type to type = mixed which then estimates a copula GGM (this method can be used for data containing **only** ordinal variable). This should work without a problem.
- The second is due to how the ordinal data are categorized. For example, if the error states that the index is out of bounds, this indicates that the first category is a zero. This is not allowed, as the first category must be one. This is addressed by adding one (e.g., Y + 1) to the data matrix.

Imputing Missing Values:

Missing values are imputed with the approach described in Hoff (2009). The basic idea is to impute the missing values with the respective posterior pedictive distribution, given the observed data, as the model is being estimated. Note that the default is TRUE, but this ignored when there are no missing values. If set to FALSE, and there are missing values, list-wise deletion is performed with na.omit.

Value

A list of class ggm_compare_estimate containing:

- pcor_diffs partial correlation differences (posterior distribution)
- p number of variable
- info list containing information about each group (e.g., sample size, etc.)
- iter number of posterior samples
- call match.call

Note

Mixed Data:

The mixed data approach was introduced in Hoff (2007) (our paper describing an extension to Bayesian hypothesis testing if forthcoming). This is a semi-paramateric copula model based on the ranked likelihood. This is computationally expensive when treating continuous data as ranks. The current default is to treat only integer data as ranks. This should of course be adjusted for continuous data that is skewed. This can be accomplished with the argument mixed_type. A 1 in the numeric vector of length *p*indicates to treat that respective node as a rank (corresponding to the column number) and a zero indicates to use the observed (or "emprical") data.

It is also important to note that type = "mixed" is not restricted to mixed data (containing a combination of categorical and continuous): all the nodes can be ordinal or continuous (but again this will take some time).

Interpretation of Conditional (In)dependence Models for Latent Data:

See BGGM-package for details about interpreting GGMs based on latent data (i.e, all data types besides "continuous")

Additional GGM Compare Methods

Bayesian hypothesis testing is implemented in ggm_compare_explore and ggm_compare_confirm (Williams and Mulder 2019). The latter allows for confirmatory hypothesis testing. An approach based on a posterior predictive check is implemented in ggm_compare_ppc (Williams et al. 2020). This provides a 'global' test for comparing the entire GGM and a 'nodewise' test for comparing each variable in the network Williams (2018).

References

Hoff PD (2007). "Extending the rank likelihood for semiparametric copula estimation." *The Annals of Applied Statistics*, **1**(1), 265–283. doi: 10.1214/07AOAS107.

Hoff PD (2009). A first course in Bayesian statistical methods, volume 580. Springer.

Williams DR (2018). "Bayesian Estimation for Gaussian Graphical Models: Structure Learning, Predictability, and Network Comparisons." *arXiv*. doi: 10.31234/OSF.IO/X8DPR.

Williams DR, Mulder J (2019). "Bayesian Hypothesis Testing for Gaussian Graphical Models: Conditional Independence and Order Constraints." *PsyArXiv*. doi: 10.31234/osf.io/ypxd8.

Williams DR, Rast P, Pericchi LR, Mulder J (2020). "Comparing Gaussian graphical models with the posterior predictive distribution and Bayesian model selection." *Psychological Methods*. doi: 10.1037/met0000254.

```
# note: iter = 250 for demonstrative purposes
# data
Y <- bfi
# males and females
Ymale <- subset(Y, gender == 1,</pre>
                   select = -c(gender,
                                education))[,1:10]
Yfemale <- subset(Y, gender == 2,
                     select = -c(gender,
                                  education))[,1:10]
# fit model
fit <- ggm_compare_estimate(Ymale, Yfemale,</pre>
                            type = "ordinal",
                            iter = 250,
                            prior_sd = 0.25,
                            progress = FALSE)
```

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ggm_compare_explore

GGM Compare: Exploratory Hypothesis Testing

Description

Compare Gaussian graphical models with exploratory hypothesis testing using the matrix-F prior distribution (Mulder and Pericchi 2018). A test for each partial correlation in the model for any number of groups. This provides evidence for the null hypothesis of no difference and the alternative hypothesis of difference. With more than two groups, the test is for *all* groups simultaneously (i.e., the relation is the same or different in all groups). This method was introduced in Williams et al. (2020). For confirmatory hypothesis testing see confirm_groups.

Usage

```
ggm_compare_explore(
    ...,
    formula = NULL,
    type = "continuous",
    mixed_type = NULL,
    analytic = FALSE,
    prior_sd = 0.2,
    iter = 5000,
    progress = TRUE,
    seed = 1
)
```

Arguments

At least two matrices (or data frame) of dimensions n (observations) by p (variables). An object of class formula. This allows for including control variables in the formula model (i.e., ~ gender). Character string. Which type of data for Y? The options include continuous, type binary, or ordinal. See the note for further details. Numeric vector. An indicator of length p for which varibles should be treated mixed_type as ranks. (1 for rank and 0 to assume normality). The default is currently (dev version) to treat all integer variables as ranks when type = "mixed" and NULL otherwise. See note for further details. logical. Should the analytic solution be computed (default is FALSE)? See note analytic for details. Numeric. The scale of the prior distribution (centered at zero), in reference to a prior_sd beta distribtuion. The 'default' is 0.20. See note for further details. iter number of iterations (posterior samples; defaults to 5000). Logical. Should a progress bar be included (defaults to TRUE)? progress

Details

seed

Controlling for Variables:

When controlling for variables, it is assumed that Y includes *only* the nodes in the GGM and the control variables. Internally, only the predictors that are included in formula are removed from Y. This is not behavior of, say, lm, but was adopted to ensure users do not have to write out each variable that should be included in the GGM. An example is provided below.

An integer for the random seed.

Mixed Type:

The term "mixed" is somewhat of a misnomer, because the method can be used for data including *only* continuous or *only* discrete variables. This is based on the ranked likelihood which requires sampling the ranks for each variable (i.e., the data is not merely transformed to ranks). This is computationally expensive when there are many levels. For example, with continuous data, there are as many ranks as data points!

The option mixed_type allows the user to determine which variable should be treated as ranks and the "emprical" distribution is used otherwise. This is accomplished by specifying an indicator vector of length *p*. A one indicates to use the ranks, whereas a zero indicates to "ignore" that variable. By default all integer variables are handled as ranks.

Dealing with Errors:

An error is most likely to arise when type = "ordinal". The are two common errors (although still rare):

• The first is due to sampling the thresholds, especially when the data is heavily skewed. This can result in an ill-defined matrix. If this occurs, we recommend to first try decreasing prior_sd (i.e., a more informative prior). If that does not work, then change the data type to type = mixed which then estimates a copula GGM (this method can be used for data containing only ordinal variable). This should work without a problem.

• The second is due to how the ordinal data are categorized. For example, if the error states that the index is out of bounds, this indicates that the first category is a zero. This is not allowed, as the first category must be one. This is addressed by adding one (e.g., Y + 1) to the data matrix.

Value

The returned object of class ggm_compare_explore contains a lot of information that is used for printing and plotting the results. For users of **BGGM**, the following are the useful objects:

- BF_01 A p by p matrix including the Bayes factor for the null hypothesis.
- pcor_diff A p by p matrix including the difference in partial correlations (only for two groups).
- samp A list containing the fitted models (of class explore) for each group.

Note

"Default" Prior:

In Bayesian statistics, a default Bayes factor needs to have several properties. I refer interested users to section 2.2 in Dablander et al. (2020). In Williams and Mulder (2019), some of these propteries were investigated, such model selection consistency. That said, we would not consider this a "default" Bayes factor and thus we encourage users to perform sensitivity analyses by varying the scale of the prior distribution.

Furthermore, it is important to note there is no "correct" prior and, also, there is no need to entertain the possibility of a "true" model. Rather, the Bayes factor can be interpreted as which hypothesis best (relative to each other) predicts the observed data (Section 3.2 in Kass and Raftery 1995).

Interpretation of Conditional (In)dependence Models for Latent Data:

See BGGM-package for details about interpreting GGMs based on latent data (i.e, all data types besides "continuous")

References

Dablander F, Bergh Dvd, Ly A, Wagenmakers E (2020). "Default Bayes Factors for Testing the (In) equality of Several Population Variances." *arXiv preprint arXiv:2003.06278*.

Kass RE, Raftery AE (1995). "Bayes Factors." *Journal of the American Statistical Association*, **90**(430), 773–795.

Mulder J, Pericchi L (2018). "The Matrix-F Prior for Estimating and Testing Covariance Matrices." *Bayesian Analysis*, 1–22. ISSN 19316690, doi: 10.1214/17BA1092.

Williams DR, Mulder J (2019). "Bayesian Hypothesis Testing for Gaussian Graphical Models: Conditional Independence and Order Constraints." *PsyArXiv*. doi: 10.31234/osf.io/ypxd8.

Williams DR, Rast P, Pericchi LR, Mulder J (2020). "Comparing Gaussian graphical models with the posterior predictive distribution and Bayesian model selection." *Psychological Methods*. doi: 10.1037/met0000254.

Examples

```
# note: iter = 250 for demonstrative purposes
# data
Y <- bfi
# males and females
Ymale <- subset(Y, gender == 1,</pre>
                 select = -c(gender,
                             education))[,1:10]
Yfemale <- subset(Y, gender == 2,
                   select = -c(gender,
                               education))[,1:10]
### example 1: ordinal ###
# fit model
fit <- ggm_compare_explore(Ymale, Yfemale,</pre>
                         type = "ordinal",
                         iter = 250,
                         progress = FALSE)
# summary
summ <- summary(fit)</pre>
# edge set
E <- select(fit)
```

ggm_compare_ppc

GGM Compare: Posterior Predictive Check

Description

Compare GGMs with a posterior predicitve check (Gelman et al. 1996). This method was introduced in Williams et al. (2020). Currently, there is a global (the entire GGM) and a nodewise test. The default is to compare GGMs with respect to the posterior predictive distribution of Kullback Leibler divergence and the sum of squared errors. It is also possible to compare the GGMs with a user defined test-statistic.

Usage

```
ggm_compare_ppc(
    ...,
```

```
test = "global",
iter = 5000,
FUN = NULL,
custom_obs = NULL,
loss = TRUE,
progress = TRUE
)
```

Arguments

•••	At least two matrices (or data frames) of dimensions n (observations) by p (variables).
test	Which test should be performed (defaults to "global")? The options include global and nodewise.
iter	Number of replicated datasets used to construct the predictivie distribution (defaults to 5000).
FUN	An optional function for comparing GGMs that returns a number. See Details .
custom_obs	Number corresponding to the observed score for comparing the GGMs. This is required if a function is provided in FUN. See Details .
loss	Logical. If a function is provided, is the measure a "loss function" (i.e., a large score is bad thing). This determines how the <i>p</i> -value is computed. See Details .
progress	Logical. Should a progress bar be included (defaults to TRUE)?

Details

The FUN argument allows for a user defined test-statistic (the measure used to compare the GGMs). The function must include only two agruments, each of which corresponds to a dataset. For example, $f \leftarrow function(Yg1, Yg2)$, where each Y is dataset of dimensions n by p. The groups are then compare within the function, returning a single number. An example is provided below.

Further, when using a custom function care must be taken when specifying the argument loss. We recommended to visualize the results with plot to ensure the *p*-value was computed in the right direction.

Value

The returned object of class ggm_compare_ppc contains a lot of information that is used for printing and plotting the results. For users of **BGGM**, the following are the useful objects:

```
test = "global"
```

- ppp_jsd posterior predictive *p*-values (JSD).
- ppp_sse posterior predictive *p*-values (SSE).
- predictive_jsd list containing the posterior predictive distributions (JSD).
- predictive_sse list containing the posterior predictive distributions (SSE).
- obs_jsd list containing the observed error (JSD).
- obs_sse list containing the observed error (SSE).

test = "nodewise"

- ppp_jsd posterior predictive *p*-values (JSD).
- predictive_jsd list containing the posterior predictive distributions (JSD).
- obs_jsd list containing the observed error (JSD).

FUN = f()

- ppp_custom posterior predictive p-values (custom).
- predictive_custom posterior predictive distributions (custom).
- obs_custom observed error (custom).

Note

Interpretation:

The primary test-statistic is symmetric KL-divergence that is termed Jensen-Shannon divergence (JSD). This is in essence a likelihood ratio that provides the "distance" between two multivariate normal distributions. The basic idea is to (1) compute the posterior predictive distribution, assuming group equality (the null model). This provides the error that we would expect to see under the null model; (2) compute JSD for the observed groups; and (3) compare the observed JSD to the posterior predictive distribution, from which a posterior predictive *p*-value is computed.

For the global check, the sum of squared error is also provided. This is computed from the partial correlation matrices and it is analogous to the strength test in van Borkulo et al. (2017). The nodewise test compares the posterior predictive distribution for each node. This is based on the correspondence between the inverse covariance matrix and multiple regression (Kwan 2014; Stephens 1998).

If the null model is not rejected, note that this does not provide evidence for equality! Further, if the null model is rejected, this means that the assumption of group equality is not tenable—the groups are different.

Alternative Methods:

There are several methods in **BGGM** for comparing groups. See ggm_compare_estimate (posterior differences for the partial correlations), ggm_compare_explore (exploratory hypothesis testing), and ggm_compare_confirm (confirmatory hypothesis testing).

References

Gelman A, Meng X, Stern H (1996). "Posterior predictive assessment of model fitness via realized discrepancies." *Statistica sinica*, 733–760.

Kwan CC (2014). "A regression-based interpretation of the inverse of the sample covariance matrix." *Spreadsheets in Education*, **7**(1), 4613.

Stephens G (1998). "On the Inverse of the Covariance Matrix in Portfolio Analysis." *The Journal of Finance*, **53**(5), 1821–1827.

Williams DR, Rast P, Pericchi LR, Mulder J (2020). "Comparing Gaussian graphical models with the posterior predictive distribution and Bayesian model selection." *Psychological Methods*.

doi: 10.1037/met0000254.

van Borkulo CD, Boschloo L, Kossakowski J, Tio P, Schoevers RA, Borsboom D, Waldorp LJ (2017). "Comparing network structures on three aspects: A permutation test." *Manuscript submitted for publication*.

```
# note: iter = 250 for demonstrative purposes
# data
Y <- bfi
####### global ##########
# males
Ym <- subset(Y, gender == 1,</pre>
          select = - c(gender, education))
# females
Yf <- subset(Y, gender == 2,
           select = - c(gender, education))
global_test <- ggm_compare_ppc(Ym, Yf,</pre>
                          iter = 250)
global_test
##### custom function #####
# example 1
# maximum difference van Borkulo et al. (2017)
f <- function(Yg1, Yg2){</pre>
# remove NA
x <- na.omit(Yg1)</pre>
y <- na.omit(Yg2)
# nodes
p <- ncol(Yg1)
```

```
# identity matrix
I_p <- diag(p)</pre>
# partial correlations
pcor_1 <- -(cov2cor(solve(cor(x))) - I_p)</pre>
pcor_2 <- -(cov2cor(solve(cor(y))) - I_p)</pre>
# max difference
max(abs((pcor_1[upper.tri(I_p)] - pcor_2[upper.tri(I_p)])))
# observed difference
obs <- f(Ym, Yf)
global_max <- ggm_compare_ppc(Ym, Yf,</pre>
                                 iter = 250,
                                 FUN = f,
                                 custom_obs = obs,
                                 progress = FALSE)
global_max
# example 2
# Hamming distance (squared error for adjacency)
f <- function(Yg1, Yg2){</pre>
# remove NA
x <- na.omit(Yg1)</pre>
y <- na.omit(Yg2)
# nodes
p \leftarrow ncol(x)
# identity matrix
I_p <- diag(p)</pre>
fit1 <- estimate(x, analytic = TRUE)</pre>
fit2 <- estimate(y, analytic = TRUE)</pre>
sel1 <- select(fit1)</pre>
sel2 <- select(fit2)</pre>
sum((sel1\$adj[upper.tri(I_p)] - sel2\$adj[upper.tri(I_p)])^2)
}
# observed difference
obs <- f(Ym, Yf)
```

gss 53

gss

Data: 1994 General Social Survey

Description

A data frame containing 1002 rows and 7 variables measured on various scales, including binary and ordered cateogrical (with varying numbers of categories). There are also missing values in each variable

- Inc Income of the respondent in 1000s of dollars, binned into 21 ordered categories.
- DEG Highest degree ever obtained (none, HS, Associates, Bachelors, or Graduate)
- CHILD Number of children ever had.
- PINC Financial status of respondent's parents when respondent was 16 (on a 5-point scale).
- PDEG Maximum of mother's and father's highest degree
- PCHILD Number of siblings of the respondent plus one
- AGE Age of the respondent in years.

Usage

```
data("gss")
```

Format

A data frame containing 1190 observations (n = 1190) and 6 variables (p = 6) measured on the binary scale (Fowlkes et al. 1988). The variable descriptions were copied from section 4, Hoff (2007)

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References

Fowlkes EB, Freeny AE, Landwehr JM (1988). "Evaluating logistic models for large contingency tables." *Journal of the American Statistical Association*, **83**(403), 611–622. doi: 10.1080/01621459.1988.10478640.

Hoff PD (2007). "Extending the rank likelihood for semiparametric copula estimation." *The Annals of Applied Statistics*, **1**(1), 265–283. doi: 10.1214/07AOAS107.

Examples

```
data("gss")
```

ifit

Data: ifit Intensive Longitudinal Data

Description

A data frame containing 8 variables and nearly 200 observations. There are two subjects, each of which provided data every data for over 90 days. Six variables are from the PANAS scale (positive and negative affect), the daily number of steps, and the subject id.

- · id Subject id
- interested
- disinterested
- excited
- upset
- strong
- stressed
- steps steps recorded by a fit bit

Usage

```
data("ifit")
```

Format

A data frame containing 197 observations and 8 variables. The data have been used in (O'Laughlin et al. 2020) and (Williams et al. 2019)

References

O'Laughlin KD, Liu S, Ferrer E (2020). "Use of Composites in Analysis of Individual Time Series: Implications for Person-Specific Dynamic Parameters." *Multivariate Behavioral Research*, 1–18. doi: 10.1080/00273171.2020.1716673.

Williams DR, Liu S, Martin SR, Rast P (2019). "Bayesian Multivariate Mixed-Effects Location Scale Modeling of Longitudinal Relations among Affective Traits, States, and Physical Activity." *PsyArXiv*. doi: 10.31234/osf.io/4kfjp.

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Examples

```
data("ifit")
```

impute_data

Obtain Imputed Datasets

Description

Impute missing values, assuming a multivariate normal distribution, with the posterior predictive distribution. For binary, ordinal, and mixed (a combination of discrete and continuous) data, the values are first imputed for the latent data and then converted to the original scale.

Usage

```
impute_data(
   Y,
   type = "continuous",
   lambda = NULL,
   mixed_type = NULL,
   iter = 1000,
   progress = TRUE
)
```

Arguments

Υ	Matrix (or data frame) of dimensions n (observations) by p (variables).
type	Character string. Which type of data for Y? The options include continuous, binary, ordinal, or mixed. Note that mixed can be used for data with only ordinal variables. See the note for further details.
lambda	Numeric. A regularization parameter, which defaults to $p + 2$. A larger value results in more shrinkage.
mixed_type	Numeric vector. An indicator of length p for which variables should be treated as ranks. (1 for rank and 0 to assume the observed marginal distribution). The default is currently to treat all integer variables as ranks when type = "mixed" and NULL otherwise. See note for further details.
iter	Number of iterations (posterior samples; defaults to 1000).

Details

progress

Missing values are imputed with the approach described in Hoff (2009). The basic idea is to impute the missing values with the respective posterior pedictive distribution, given the observed data, as the model is being estimated. Note that the default is TRUE, but this ignored when there are no missing values. If set to FALSE, and there are missing values, list-wise deletion is performed with na.omit.

Logical. Should a progress bar be included (defaults to TRUE)?

56 impute_data

Value

An object of class mvn_imputation:

• imputed_datasets An array including the imputed datasets.

References

Hoff PD (2009). A first course in Bayesian statistical methods, volume 580. Springer.

```
# obs
n <- 5000
# n missing
n_{missing} < -1000
# variables
p <- 16
# data
Y <- MASS::mvrnorm(n, rep(0, p), ptsd_cor1)
# for checking
Ymain <- Y
# all possible indices
indices <- which(matrix(0, n, p) == 0,
                 arr.ind = TRUE)
# random sample of 1000 missing values
na_indices <- indices[sample(5:nrow(indices),</pre>
                              size = n_missing,
                              replace = FALSE),]
# fill with NA
Y[na_indices] <- NA
# missing = 1
Y_miss <- ifelse(is.na(Y), 1, 0)
# true values (to check)
true <- unlist(sapply(1:p, function(x)</pre>
        Ymain[which(Y_miss[,x] == 1),x]))
# impute
fit_missing <- impute_data(Y, progress = FALSE, iter = 250)</pre>
# impute
fit_missing <- impute_data(Y,</pre>
                            progress = TRUE,
```

iter = 250)

iri

Data: Interpersonal Reactivity Index (IRI)

Description

A dataset containing items from the Interpersonal Reactivity Index (IRI; an empathy measure). There are 28 variables and 1973 observations

Usage

```
data("iri")
```

Format

A data frame with 28 variables and 1973 observations (5 point Likert scale)

Details

- 1 I daydream and fantasize, with some regularity, about things that might happen to me.
- 2 I often have tender, concerned feelings for people less fortunate than me.
- 3 I sometimes find it difficult to see things from the "other guy's" point of view.
- 4 Sometimes I don't feel very sorry for other people when they are having problems.
- 5 I really get involved with the feelings of the characters in a novel.
- 6 In emergency situations, I feel apprehensive and ill-at-ease.
- 7 I am usually objective when I watch a movie or play, and I don't often get completely caught up in it.
- 8 I try to look at everybody's side of a disagreement before I make a decision.
- 9 When I see someone being taken advantage of, I feel kind of protective towards them.
- 10 I sometimes feel helpless when I am in the middle of a very emotional situation.
- 11 I sometimes try to understand my friends better by imagining how things look from their perspective
- 12 Becoming extremely involved in a good book or movie is somewhat rare for me.
- 13 When I see someone get hurt, I tend to remain calm.
- 14 Other people's misfortunes do not usually disturb me a great deal.
- 15 If I'm sure I'm right about something, I don't waste much time listening to other people's arguments.
- 16 After seeing a play or movie, I have felt as though I were one of the characters.
- 17 Being in a tense emotional situation scares me.

58 map

• 18 When I see someone being treated unfairly, I sometimes don't feel very much pity for them.

- 19 I am usually pretty effective in dealing with emergencies.
- 20 I am often quite touched by things that I see happen.
- 21 I believe that there are two sides to every question and try to look at them both.
- 22 I would describe myself as a pretty soft-hearted person.
- 23 When I watch a good movie, I can very easily put myself in the place of a leading character
- 24 I tend to lose control during emergencies.
- 25 When I'm upset at someone, I usually try to "put myself in his shoes" for a while.
- 26 When I am reading an interesting story or novel, I imagine how I would feel if the events in the story were happening to me.
- 27 When I see someone who badly needs help in an emergency, I go to pieces.
- 28 Before criticizing somebody, I try to imagine how I would feel if I were in their place.
- gender "M" (male) or "F" (female)

Note

There are four domains

Fantasy: items 1, 5, 7, 12, 16, 23, 26

Perspective taking: items 3, 8, 11, 15, 21, 25, 28 Empathic concern: items 2, 4, 9, 14, 18, 20, 22 Personal distress: items 6, 10, 13, 17, 19, 24, 27,

References

Briganti, G., Kempenaers, C., Braun, S., Fried, E. I., & Linkowski, P. (2018). Network analysis of empathy items from the interpersonal reactivity index in 1973 young adults. Psychiatry research, 265, 87-92.

Examples

```
data("iri")
```

map

Maximum A Posteriori Precision Matrix

Description

Maximum A Posteriori Precision Matrix

Usage

map(Y)

pcor_mat 59

Arguments

Υ

Matrix (or data frame) of dimensions n (observations) by p (variables).

Value

An object of class map, including the precision matrix, partial correlation matrix, and regression parameters.

Examples

```
Y <- BGGM::bfi[, 1:5]
# map
map <- map(Y)
map</pre>
```

pcor_mat

Extract the Partial Correlation Matrix

Description

Extract the partial correlation matrix (posterior mean) from estimate, explore, ggm_compare_estimate, and ggm_compare_explore objects. It is also possible to extract the partial correlation differences for ggm_compare_estimate and ggm_compare_explore objects.

Usage

```
pcor_mat(object, difference = FALSE, ...)
```

Arguments

object A model estimated with **BGGM**. All classes are supported, assuming there is

matrix to be extracted.

difference Logical. Should the difference be returned (defaults to FALSE)? Note that this

assumes there is a difference (e.g., an object of class ggm_compare_estimate)

and ignored otherwise.

... Currently ignored.

Value

The estimated partial correlation matrix.

pcor_sum

Examples

pcor_sum

Partial Correlation Sum

Description

Compute and test partial correlation sums either within or between GGMs (e.g., different groups), resulting in a posterior distribution.

Usage

```
pcor_sum(..., iter = NULL, relations)
```

Arguments

... An object of class estimate. This can be either one or two fitted objects.

iter Number of iterations (posterior samples; defaults to the number in the object).

relations Character string. Which partial correlations should be summed?

Details

Some care must be taken when writing the string for partial_sum. Below are several examples

Just a Sum: Perhaps a sum is of interest, and not necessarily the difference of two sums. This can be written as

```
partial_sum <- c("A1--A2 + A1--A3 + A1--A4")</li>
```

which will sum those relations.

Comparing Sums: When comparing sums, each must be seperated by ";". For example,

```
• partial_sum <- c("A1--A2 + A1--A3; A1--A2 + A1--A4")
```

pcor_sum 61

which will sum both and compute the difference. Note that there cannot be more than two sums, such that c("A1--A2 + A1--A3; A1--A2 + A1--A4; A1--A2 + A1--A5") will result in an error.

Comparing Groups:

When more than one fitted object is suppled to object it is assumed that the groups should be compared for the same sum. Hence, in this case, only the sum needs to be written.

```
• partial_sum <- c("A1--A2 + A1--A3 + A1--A4")
```

The above results in that sum being computed for each group and then compared.

Value

An object of class posterior_sum, including the sum and possibly the difference for two sums.

```
# data
Y <- bfi
# males
Y_{males} \leftarrow subset(Y, gender == 1, select = -c(education, gender))[,1:5]
Y_{\text{females}} \leftarrow \text{subset}(Y, \text{gender} == 2, \text{select} = -c(\text{education}, \text{gender}))[,1:5]
# males
fit_males <- estimate(Y_males, seed = 1,</pre>
                          progress = FALSE)
# fit females
fit_females <- estimate(Y_females, seed = 2,</pre>
                            progress = FALSE)
sums <- pcor_sum(fit_males,</pre>
                    fit_females,
                    relations = "A1--A2 + A1--A3")
# print
sums
# plot difference
plot(sums)[[3]]
```

62 pcor_to_cor

pcor_to_cor

Compute Correlations from the Partial Correlations

Description

Convert the partial correlation matrices into correlation matrices. To our knowledge, this is the only Bayesian implementation in R that can estiamte Pearson's, tetrachoric (binary), polychoric (ordinal with more than two cateogries), and rank based correlation coefficients.

Usage

```
pcor_to_cor(object, iter = NULL)
```

Arguments

object An object of class estimate or explore

iter numeric. How many iterations (i.e., posterior samples) should be used? The

default uses all of the samples, but note that this can take a long time with large

matrices.

Value

- R An array including the correlation matrices (of dimensions p by p by iter)
- R_mean Posterior mean of the correlations (of dimensions p by p)

Note

The 'default' prior distributions are specified for partial correlations in particular. This means that the implied prior distribution will not be the same for the correlations.

plot.confirm 63

```
##### ordinal #######
# first level must be 1 !
Y < - Y + 1
# estimate the model
fit <- estimate(Y, type = "ordinal",</pre>
             iter = 250,
             progress = FALSE)
# compute correlations
cors <- pcor_to_cor(fit)</pre>
###### mixed
              ######
# rank based correlations
# estimate the model
fit <- estimate(Y, type = "mixed",</pre>
             iter = 250,
             progress = FALSE)
# compute correlations
cors <- pcor_to_cor(fit)</pre>
```

plot.confirm

Plot confirm objects

Description

Plot the posterior hypothesis probabilities as a pie chart, with each slice corresponding the probability of a given hypothesis.

Usage

```
## S3 method for class 'confirm' plot(x, ...)
```

Arguments

x An object of class confirm

... Currently ignored.

Value

A ggplot object.

Examples

```
##### example 1: many relations #####
# data
Y <- bfi
hypothesis <- c("g1_A1--A2 > g2_A1--A2 & g1_A1--A3 = g2_A1--A3;
              g1_A1-A2 = g2_A1-A2 & g1_A1-A3 = g2_A1-A3;
              g1_A1-A2 = g2_A1-A2 = g1_A1-A3 = g2_A1-A3"
     <- subset(Y, gender == 1,
Ymale
               select = -c(education,
                         gender))[,1:5]
# females
Yfemale <- subset(Y, gender == 2,
                  select = -c(education,
                            gender))[,1:5]
test <- ggm_compare_confirm(Ymale,</pre>
                        Yfemale,
                        hypothesis = hypothesis,
                        iter = 250,
                        progress = FALSE)
# plot
plot(test)
```

```
plot.ggm_compare_ppc Plot ggm_compare_ppc Objects
```

Description

Plot the predictive check with ggridges

Usage

```
## S3 method for class 'ggm_compare_ppc'
plot(
    x,
    critical = 0.05,
    col_noncritical = "#84e184A0",
    col_critical = "red",
    point_size = 2,
    ...
)
```

Arguments

Value

An object (or list of objects) of class ggplot.

Note

See ggridges for many examples.

See Also

```
ggm_compare_ppc
```

plot.pcor_sum

plot.pcor_sum

Plot pcor_sum Object

Description

Plot pcor_sum Object

Usage

```
## S3 method for class 'pcor_sum'
plot(x, fill = "#CC79A7", ...)
```

Arguments

x An object of class posterior_sum

fill Character string. What fill for the histogram (defaults to colorblind "pink")?

... Currently ignored.

Value

A list of ggplot objects

Note

Examples:

See Also

pcor_sum

plot.predictability 67

```
plot.predictability Plot predictability Objects
```

Description

Plot predictability Objects

Usage

```
## S3 method for class 'predictability'
plot(
    x,
    type = "error_bar",
    cred = 0.95,
    alpha = 0.5,
    scale = 1,
    width = 0,
    size = 1,
    color = "blue",
    ...
)
```

Arguments

X	An object of class predictability
type	Character string. Which type of plot ? The options are "error_bar" or "ridgeline" (defaults to "error_bar").
cred	Numeric. The credible interval width for summarizing the posterior distributions (defaults to 0.95; must be between 0 and 1).
alpha	Numeric. Transparancey of the ridges
scale	Numeric. This controls the overlap of densities for type = "ridgeline" (defaults to 1).
width	Numeric. The width of error bar ends (defaults to \emptyset) for type = "error_bar".
size	Numeric. The size for the points (defaults to 2) for type = "error_bar".
color	Character string. What color for the point (type = "error_bar") or tail region (type = "ridgeline")? Defaults to "blue".
	Currently ignored.

Value

An object of class ggplot.

68 plot.roll_your_own

Examples

plot.roll_your_own

Plot roll_your_own Objects

Description

```
Plot roll_your_own Objects
```

Usage

```
## S3 method for class 'roll_your_own'
plot(x, fill = "#CC79A7", alpha = 0.5, ...)
```

Arguments

X	An object of class roll_your_own
fill	Character string specifying the color for the ridges.
alpha	Numeric. Transparancey of the ridges
	Currently ignored

Value

An object of class ggplot

plot.select 69

```
# fit model
fit <- estimate(Y = Y, iter = 250,</pre>
                 progress = FALSE)
# membership
membership <- c(rep("a", 5), rep("c", 5))</pre>
# define function
f <- function(x,...){</pre>
 assortment.discrete(x, ...)r
net_stat <- roll_your_own(object = fit,</pre>
                            FUN = f,
                            types = membership,
                            weighted = TRUE,
                            SE = FALSE, M = 1,
                            progress = FALSE)
# plot
plot(net_stat)
```

plot.select

Network Plot for select Objects

Description

Visualize the conditional (in)dependence structure.

Usage

```
## S3 method for class 'select'
plot(
    x,
    layout = "circle",
    pos_col = "#009E73",
    neg_col = "#D55E00",
    node_size = 10,
    edge_magnify = 1,
    groups = NULL,
    palette = "Set3",
    ...
)
```

70 plot.select

Arguments

x	An object of class select.
layout	Character string. Which graph layout (defaults is circle)? See gplot.layout.
pos_col	Character string. Color for the positive edges (defaults to green).
neg_col	Character string. Color for the negative edges (defaults to green).
node_size	Numeric. The size of the nodes (defaults to 10).
edge_magnify	Numeric. A value that is multiplied by the edge weights. This increases (> 1) or decrease (< 1) the line widths (defaults to 1).
groups	A character string of length p (the number of nodes in the model). This indicates groups of nodes that should be the same color (e.g., "clusters" or "communities").
palette	A character string sepcifying the palette for the groups. (default is Set 3). See palette options here.
	Additional options passed to ggnet2

Value

An object (or list of objects) of class ggplot that can then be further customized.

Note

A more extensive example of a custom plot is provided here

```
### example 1: one ggm ##
#####################################
# data
Y <- bfi[,1:25]
# estimate
fit <- estimate(Y, iter = 250,</pre>
                progress = FALSE)
# "communities"
comm <- substring(colnames(Y), 1, 1)</pre>
# edge set
E <- select(fit)
# plot edge set
plt_E <- plot(E, edge_magnify = 5,</pre>
              palette = "Set1",
              groups = comm)
```

plot.summary.estimate 71

```
### example 2: ggm compare ##
# compare males vs. females
# data
Y <- bfi[,1:26]
Ym <- subset(Y, gender == 1,</pre>
            select = -gender)
Yf <- subset(Y, gender == 2,
             select = -gender)
# estimate
fit <- ggm_compare_estimate(Ym, Yf, iter = 250,</pre>
                          progress = FALSE)
# "communities"
comm <- substring(colnames(Ym), 1, 1)</pre>
# edge set
E <- select(fit)
# plot edge set
plt_E <- plot(E, edge_magnify = 5,</pre>
             palette = "Set1",
             groups = comm)
```

plot.summary.estimate *Plot* summary.estimate *Objects*

Description

Visualize the posterior distributions for each partial correlation.

Usage

```
## S3 method for class 'summary.estimate'
plot(x, color = "black", size = 2, width = 0, ...)
```

Arguments

```
x An object of class summary.estimatecolor Character string. The color for the error bars. (defaults to "black").
```

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```
size Numeric. The size for the points (defaults to 2). width Numeric. The width of error bar ends (defaults to \emptyset). Currently ignored
```

Value

A ggplot object.

See Also

estimate

Examples

```
plot.summary.explore Plot summary.explore Objects
```

Description

Visualize the posterior distributions for each partial correlation.

Usage

```
## S3 method for class 'summary.explore'
plot(x, color = "black", size = 2, width = 0, ...)
```

Arguments

Х	An object of class summary.explore
color	Character string. The color for the error bars. (defaults to "black").
size	Numeric. The size for the points (defaults to 2).
width	Numeric. The width of error bar ends (defaults to 0).
	Currently ignored

Value

```
A ggplot object
```

See Also

```
explore
```

Examples

```
plot. \verb| summary.ggm_compare_estimate| \\ Plot \verb| summary.ggm_compare_estimate| Objects|
```

Description

Visualize the posterior distribution differences.

Usage

```
## S3 method for class 'summary.ggm_compare_estimate'
plot(x, color = "black", size = 2, width = 0, ...)
```

Arguments

x	An object of class ggm_compare_estimate.
color	Character string. The color of the points (defaults to "black").
size	Numeric. The size of the points (defaults to 2).
width	Numeric. The width of error bar ends (defaults to θ).
	Currently ignored.

Value

An object of class ggplot

See Also

```
ggm_compare_estimate
```

Examples

```
# note: iter = 250 for demonstrative purposes
# data
Y <- bfi
# males and females
Ymale <- subset(Y, gender == 1,</pre>
                select = -c(gender,
                             education))[,1:5]
Yfemale <- subset(Y, gender == 2,
                  select = -c(gender,
                               education))[,1:5]
# fit model
fit <- ggm_compare_estimate(Ymale, Yfemale,</pre>
                             type = "ordinal",
                             iter = 250,
                             prior_sd = 0.25,
                             progress = FALSE)
plot(summary(fit))
```

```
{\it plot.summary.ggm\_compare\_explore} \\ {\it Plot.summary.ggm\_compare\_explore} \ Objects
```

Description

Visualize the posterior hypothesis probabilities.

Usage

```
## S3 method for class 'summary.ggm_compare_explore'
plot(x, size = 2, color = "black", ...)
```

Arguments

x	An object of class summary.ggm_compare_explore
size	Numeric. The size of the points (defaults to 2).
color	Character string. The color of the points (defaults to "black").
	Currently ignored.

Value

```
A ggplot object
```

See Also

```
ggm_compare_explore
```

Examples

```
# note: iter = 250 for demonstrative purposes
# data
Y <- bfi
# males and females
Ymale <- subset(Y, gender == 1,</pre>
                 select = -c(gender,
                            education))[,1:10]
Yfemale <- subset(Y, gender == 2,
                   select = -c(gender,
                              education))[,1:10]
### example 1: ordinal ###
# fit model
fit <- ggm_compare_explore(Ymale, Yfemale,</pre>
                         type = "ordinal",
                         iter = 250,
                         progress = FALSE)
# summary
summ <- summary(fit)</pre>
plot(summ)
```

```
{\it plot.} {\it summary.} {\it select.} {\it explore} \\ {\it Plot.} {\it summary.} {\it select.} {\it explore} {\it Objects}
```

Description

Visualize the posterior hypothesis probabilities.

Usage

```
## S3 method for class 'summary.select.explore'
plot(x, size = 2, color = "black", ...)
```

Arguments

x An object of class summary.select.explore
 size Numeric. The size for the points (defaults to 2).
 color Character string. The Color for the points
 ... Currently ignored

Value

A ggplot object

Examples

```
{\it plot.} {\it summary.} {\it var\_estimate} \\ {\it Plot.} {\it summary.} {\it var\_estimate} \ {\it Objects} \\
```

Description

Visualize the posterior distributions of each partial correlation and regression coefficient.

Usage

```
## S3 method for class 'summary.var_estimate'
plot(x, color = "black", size = 2, width = 0, param = "all", order = TRUE, ...)
```

plot_prior 77

Arguments

X	An object of class summary.var_estimate
color	Character string. The color for the error bars. (defaults to "black").
size	Numeric. The size for the points (defaults to 2).
width	Numeric. The width of error bar ends (defaults to 0).
param	Character string. Which parameters should be plotted? The options are pcor, beta, or all (default).
order	Logical. Should the relations be ordered by size (defaults to TRUE) ?
	Currently ignored

Value

A list of ggplot objects.

Examples

```
# data
Y <- subset(ifit, id == 1)[,-1]
# fit model with alias (var_estimate also works)
fit <- var_estimate(Y, progress = FALSE)

plts <- plot(summary(fit))
plts$pcor_plt</pre>
```

plot_prior Plot: Prior Distribution

Description

Visualize the implied prior distribution for the partial correlations. This is particularly useful for the Bayesian hypothesis testing methods.

Usage

```
plot_prior(prior_sd = 0.2, iter = 5000)
```

Arguments

prior_sd	Scale of the prior distribution, approximately the standard deviation of a beta distribution (defaults to 0.25).
iter	Number of iterations (prior samples; defaults to 5000).

78 posterior_predict

Value

A ggplot object.

Examples

```
# note: iter = 250 for demonstrative purposes
plot_prior(prior_sd = 0.25, iter = 250)
```

posterior_predict

Posterior Predictive Distribution

Description

Draw samples from the posterior predictive distribution.

Usage

```
posterior_predict(object, iter = 1000, progress = TRUE)
```

Arguments

object An object of class estimate or explore

iter Numeric. Number of samples from the predictive distributionprogress Logical. Should a progress bar be included (defaults to TRUE)

Value

A 3D array containing the predicted datasets

Note

Currently only implemented for type = "mixed", type = "ordinal", and type = "binary". Note the term mixed is confusing, in that it can be used with only, say, ordinal data. In this case, reestimate the model with type = "mixed" until all data types are supported.

posterior_samples 79

posterior_samples

Extract Posterior Samples

Description

Extract posterior samples for all parameters.

Usage

```
posterior_samples(object, ...)
```

Arguments

```
object an object of class estimate or explore.
... currently ignored.
```

Value

A matrix of posterior samples for the partial correlation. Note that if controlling for variables (e.g., formula ~ age), the matrix also includes the coefficients from each multivariate regression.

```
# note: iter = 250 for demonstrative purposes
### example 1: control with formula ###
# (the following works with all data types)
# controlling for gender
Y <- bfi
# to control for only gender
# (remove education)
Y <- subset(Y, select = - education)
# fit model
fit <- estimate(Y, formula = ~ gender,</pre>
             iter = 250)
# note regression coefficients
samps <- posterior_samples(fit)</pre>
hist(samps[,1])
```

80 precision

precision

Precision Matrix Posterior Distribution

Description

Transform the sampled correlation matrices to precision matrices (i.e., inverse covariance matrices).

Usage

```
precision(object, progress = TRUE)
```

Arguments

object An object of class estimate.

progress Logical. Should a progress bar be included (defaults to TRUE)?

Value

- precision_mean The mean of the precision matrix (p by p matrix).
- precision 3d array of dimensions p by p by iter including **unconstrained** (i.e., from th full graph) precision matrices.

Note

The estimated precision matrix is the inverse of the **correlation** matrix.

```
# data
Y <- ptsd
# fit model
fit <- estimate(Y)
# precision matrix
Theta <- precision(fit)</pre>
```

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predict.estimate

Model Predictions for estimate Objects

Description

Model Predictions for estimate Objects

Usage

```
## S3 method for class 'estimate'
predict(
   object,
   newdata = NULL,
   summary = TRUE,
   cred = 0.95,
   iter = NULL,
   progress = TRUE,
   ...
)
```

Arguments

```
object object of class estimate

newdata an optional data frame for obtaining predictions (e.g., on test data)

summary summarize the posterior samples (defaults to TRUE).

cred credible interval used for summarizing

iter number of posterior samples (defaults to all in the object).

progress Logical. Should a progress bar be included (defaults to TRUE)?

currently ignored
```

Value

summary = TRUE: 3D array of dimensions n (observations), 4 (posterior summary), p (number of nodes). summary = FALSE: list containing predictions for each variable

82 predict.explore

predict.explore

Model Predictions for explore Objects

Description

Model Predictions for explore Objects

Usage

```
## $3 method for class 'explore'
predict(
  object,
  newdata = NULL,
  summary = TRUE,
  cred = 0.95,
  iter = NULL,
  progress = TRUE,
  ...
)
```

Arguments

```
object object of class explore

newdata an optional data frame for obtaining predictions (e.g., on test data)

summary summarize the posterior samples (defaults to TRUE).

cred credible interval used for summarizing

iter number of posterior samples (defaults to all in the object).

progress Logical. Should a progress bar be included (defaults to TRUE)?

currently ignored
```

Value

summary = TRUE: 3D array of dimensions n (observations), 4 (posterior summary), p (number of nodes). summary = FALSE: list containing predictions for each variable

predict.var_estimate 83

Description

Model Predictions for var_estimate Objects

Usage

```
## S3 method for class 'var_estimate'
predict(object, summary = TRUE, cred = 0.95, iter = NULL, progress = TRUE, ...)
```

Arguments

object object of class var_estimate
summary summarize the posterior samples (defaults to TRUE).

cred credible interval used for summarizing
iter number of posterior samples (defaults to all in the object).

progress Logical. Should a progress bar be included (defaults to TRUE)?

... Currently ignored

Value

The predicted values for each regression model.

```
# data
Y <- subset(ifit, id == 1)[,-1]
# fit model with alias (var_estimate also works)
fit <- var_estimate(Y, progress = FALSE)
# fitted values
pred <- predict(fit, progress = FALSE)
# predicted values (1st outcome)
pred[,,1]</pre>
```

84 predictability

Predictability: Bayesian Variance Explained (R2)
--

Description

Compute nodewise predictability or Bayesian variance explained (R2 Gelman et al. 2019). In the context of GGMs, this method was described in Williams (2018).

Usage

```
predictability(
  object,
  select = FALSE,
  cred = 0.95,
  BF_cut = 3,
  iter = NULL,
  progress = TRUE,
  ...
)
```

Arguments

object	object of class estimate or explore
select	logical. Should the graph be selected? The default is currently FALSE.
cred	numeric. credible interval between 0 and 1 (default is 0.95) that is used for selecting the graph.
BF_cut	numeric. evidentiary threshold (default is 3).
iter	interger. iterations (posterior samples) used for computing R2.
progress	Logical. Should a progress bar be included (defaults to TRUE)?
	currently ignored.

Value

An object of classes bayes_R2 and metric, including

• scores A list containing the posterior samples of R2. The is one element for each node.

Note

Binary and Ordinal Data:

R2 is computed from the latent data.

Mixed Data:

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The mixed data approach is somewhat ad-hoc see for example p. 277 in Hoff (2007). This is becaue uncertainty in the ranks is not incorporated, which means that variance explained is computed from the 'empirical' *CDF*.

Model Selection:

Currently the default to include all nodes in the model when computing R2. This can be changed (i.e., select = TRUE), which then sets those edges not detected to zero. This is accomplished by subsetting the correlation matrix according to each neighborhood of relations.

References

Gelman A, Goodrich B, Gabry J, Vehtari A (2019). "R-squared for Bayesian Regression Models." *American Statistician*, **73**(3), 307–309. ISSN 15372731, doi: 10.1080/00031305.2018.1549100.

Hoff PD (2007). "Extending the rank likelihood for semiparametric copula estimation." *The Annals of Applied Statistics*, **1**(1), 265–283. doi: 10.1214/07AOAS107.

Williams DR (2018). "Bayesian Estimation for Gaussian Graphical Models: Structure Learning, Predictability, and Network Comparisons." *arXiv*. doi: 10.31234/OSF.IO/X8DPR.

Examples

predicted_probability Predicted Probabilities

Description

Compute the predicted probabilities for discrete data, with the possibility of conditional predictive probabilities (i.e., at fixed values of other nodes)

Usage

```
predicted_probability(object, outcome, Y, ...)
```

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Arguments

object	An object of class posterior_predict
outcome	Character string. Node for which the probabilities are computed.
Υ	Matrix (or data frame) of dimensions n (observations) by p (variables). This must include the column names.
	Compute conditional probabilities by specifying a column name in Y (besides the outcome) and a fixed value. This can include any number of nodes. See example below. Leave this blank to compute unconditional probabilities for outcome.

Value

A list containing a matrix with the computed probabilities (a row for each predictive sample and a column for each category).

Note

There are no checks that the conditional probability exists, i.e., suppose you wish to condition on, say, B3 = 2 and B4 = 1, yet there is no instance in which B3 is 2 AND B4 is 1. This will result in an uninformative error.

Examples

print.BGGM

Print method for BGGM objects

Description

Print method for BGGM objects

Usage

```
## S3 method for class 'BGGM'
print(x, ...)
```

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Arguments

x An object of class BGGM

... currently ignored

ptsd

Data: Post-Traumatic Stress Disorder

Description

A dataset containing items that measure Post-traumatic stress disorder symptoms (Armour et al. 2017). There are 20 variables (p) and 221 observations (n).

Usage

```
data("ptsd")
```

Format

A dataframe with 221 rows and 20 variables

- Intrusive Thoughts
- Nightmares
- Flashbacks
- Emotional cue reactivity
- Psychological cue reactivity
- Avoidance of thoughts
- Avoidance of reminders
- Trauma-related amnesia
- Negative beliefs
- Negative trauma-related emotions
- Loss of interest
- Detachment
- · Restricted affect
- Irritability/anger
- Self-destructive/reckless behavior
- Hypervigilance
- Exaggerated startle response
- Difficulty concentrating
- Sleep disturbance

88 ptsd_cor1

References

Armour C, Fried EI, Deserno MK, Tsai J, Pietrzak RH (2017). "A network analysis of DSM-5 posttraumatic stress disorder symptoms and correlates in US military veterans." *Journal of anxiety disorders*, **45**, 49–59. doi: 10.31234/osf.io/p69m7.

ptsd_cor1

Data: Post-Traumatic Stress Disorder (Sample # 1)

Description

A correlation matrix that includes 16 variables. The correlation matrix was estimated from 526 individuals (Fried et al. 2018).

Format

A correlation matrix with 16 variables

Details

- Intrusive Thoughts
- Nightmares
- Flashbacks
- · Physiological/psychological reactivity
- Avoidance of thoughts
- Avoidance of situations
- Amnesia
- Disinterest in activities
- · Feeling detached
- · Emotional numbing
- Foreshortened future
- · Sleep problems
- · Irritability
- Concentration problems
- Hypervigilance
- Startle response

References

Fried EI, Eidhof MB, Palic S, Costantini G, Huisman-van Dijk HM, Bockting CL, Engelhard I, Armour C, Nielsen AB, Karstoft K (2018). "Replicability and generalizability of posttraumatic stress disorder (PTSD) networks: a cross-cultural multisite study of PTSD symptoms in four trauma patient samples." *Clinical Psychological Science*, **6**(3), 335–351.

ptsd_cor2 89

Examples

ptsd_cor2

Data: Post-Traumatic Stress Disorder (Sample # 2)

Description

A correlation matrix that includes 16 variables. The correlation matrix was estimated from 365 individuals (Fried et al. 2018).

Format

A correlation matrix with 16 variables

- Intrusive Thoughts
- Nightmares
- Flashbacks
- Physiological/psychological reactivity
- Avoidance of thoughts
- Avoidance of situations
- Amnesia
- Disinterest in activities
- · Feeling detached
- Emotional numbing
- Foreshortened future
- · Sleep problems
- Irritability
- Concentration problems
- Hypervigilance
- Startle response

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References

Fried EI, Eidhof MB, Palic S, Costantini G, Huisman-van Dijk HM, Bockting CL, Engelhard I, Armour C, Nielsen AB, Karstoft K (2018). "Replicability and generalizability of posttraumatic stress disorder (PTSD) networks: a cross-cultural multisite study of PTSD symptoms in four trauma patient samples." *Clinical Psychological Science*, **6**(3), 335–351.

Examples

ptsd_cor3

Data: Post-Traumatic Stress Disorder (Sample # 3)

Description

A correlation matrix that includes 16 variables. The correlation matrix was estimated from 926 individuals (Fried et al. 2018).

Format

A correlation matrix with 16 variables

- Intrusive Thoughts
- · Nightmares
- Flashbacks
- Physiological/psychological reactivity
- Avoidance of thoughts
- Avoidance of situations
- Amnesia
- Disinterest in activities
- · Feeling detached
- Emotional numbing
- Foreshortened future
- Sleep problems
- Irritability
- Concentration problems
- Hypervigilance
- · Startle response

ptsd_cor4 91

References

Fried EI, Eidhof MB, Palic S, Costantini G, Huisman-van Dijk HM, Bockting CL, Engelhard I, Armour C, Nielsen AB, Karstoft K (2018). "Replicability and generalizability of posttraumatic stress disorder (PTSD) networks: a cross-cultural multisite study of PTSD symptoms in four trauma patient samples." *Clinical Psychological Science*, **6**(3), 335–351.

Examples

ptsd_cor4

Data: Post-Traumatic Stress Disorder (Sample # 4)

Description

A correlation matrix that includes 16 variables. The correlation matrix was estimated from 965 individuals (Fried et al. 2018).

Format

A correlation matrix with 16 variables

- Intrusive Thoughts
- Nightmares
- · Flashbacks
- Physiological/psychological reactivity
- Avoidance of thoughts
- Avoidance of situations
- Amnesia
- Disinterest in activities
- · Feeling detached
- · Emotional numbing
- Foreshortened future
- · Sleep problems
- Irritability
- Concentration problems
- Hypervigilance
- · Startle response

92 regression_summary

References

Fried EI, Eidhof MB, Palic S, Costantini G, Huisman-van Dijk HM, Bockting CL, Engelhard I, Armour C, Nielsen AB, Karstoft K (2018). "Replicability and generalizability of posttraumatic stress disorder (PTSD) networks: a cross-cultural multisite study of PTSD symptoms in four trauma patient samples." *Clinical Psychological Science*, **6**(3), 335–351.

Examples

regression_summary

Summarary Method for Multivariate or Univarate Regression

Description

Summarary Method for Multivariate or Univarate Regression

Usage

```
regression_summary(object, cred = 0.95, ...)
```

Arguments

object An object of class estimate
cred Numeric. The credible interval width for summarizing the posterior distributions

(defaults to 0.05, must be between 0 and 1)

(defaults to 0.95; must be between 0 and 1).

.. Currently ignored

Value

A list of length p including the summaries for each regression.

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roll_your_own

Compute Custom Network Statistics

Description

This function allows for computing custom network statistics for weighted adjacency matrices (partial correlations). The statistics are computed for each of the sampled matrices, resulting in a distribution.

Usage

```
roll_your_own(
  object,
  FUN,
  iter = NULL,
  select = FALSE,
  cred = 0.95,
  progress = TRUE,
  ...
)
```

Arguments

object	An object of class estimate.
FUN	A custom function for computing the statistic. The first argument must be a partial correlation matrix.
iter	Number of iterations (posterior samples; defaults to the number in the object).
select	Logical. Should the graph be selected? The default is currently FALSE.
cred	Numeric. Credible interval between 0 and 1 (default is 0.95) that is used for selecting the graph.
progress	Logical. Should a progress bar be included (defaults to TRUE)?
	Arguments passed to the function.

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Details

The user has complete control of this function. Hence, care must be taken as to what FUN returns and in what format. The function should return a single number (one for the entire GGM) or a vector (one for each node). This ensures that the print and plot.roll_your_own will work.

When select = TRUE, the graph is selected and then the network statistics are computed based on the weighhed adjacency matrix. This is accomplished internally by multiplying each of the sampled partial correlation matrices by the adjacency matrix.

Value

An object defined by FUN.

```
##### example 1: assortment ######
# assortment
library(assortnet)
Y <- BGGM::bfi[,1:10]
membership \leftarrow c(rep("a", 5), rep("c", 5))
# fit model
fit <- estimate(Y = Y, iter = 250,</pre>
            progress = FALSE)
# membership
membership <- c(rep("a", 5), rep("c", 5))</pre>
# define function
f \leftarrow function(x,...)
assortment.discrete(x, ...)$r
}
net_stat <- roll_your_own(object = fit,</pre>
                     FUN = f,
                     types = membership,
                     weighted = TRUE,
                     SE = FALSE, M = 1,
                     progress = FALSE)
# print
net_stat
##### example 2: expected influence ######
```

rsa 95

```
# expected influence from this package
library(networktools)
# data
Y <- depression
# fit model
fit <- estimate(Y = Y, iter = 250)</pre>
# define function
f <- function(x,...){</pre>
     expectedInf(x,...)$step1
}
# compute
net_stat <- roll_your_own(object = fit,</pre>
                         FUN = f,
                         progress = FALSE)
### example 3: mixed data & bridge ####
# bridge from this package
library(networktools)
# data
Y <- ptsd[,1:7]
fit <- estimate(Y,</pre>
               type = "mixed",
               iter = 250)
# clusters
communities <- substring(colnames(Y), 1, 1)</pre>
# function is slow
f <- function(x, ...){</pre>
bridge(x, ...)$`Bridge Strength`
net_stat <- roll_your_own(fit,</pre>
                         FUN = f,
                         select = TRUE,
                         communities = communities,
                         progress = FALSE)
```

96 rsa

Description

A dataset containing items from the Resilience Scale of Adults (RSA). There are 33 items and 675 observations

Usage

```
data("rsa")
```

Format

A data frame with 28 variables and 1973 observations (5 point Likert scale)

- 1 My plans for the future are
- 2 When something unforeseen happens
- 3 My family understanding of what is important in life is
- 4 I feel that my future looks
- 5 My goals
- 6 I can discuss personal issues with
- 7 I feel
- 8 I enjoy being
- 9 Those who are good at encouraging are
- 10 The bonds among my friends
- 11 My personal problems
- 12 When a family member experiences a crisis/emergency
- 13 My family is characterised by
- 14 To be flexible in social settings
- 15 I get support from
- 16 In difficult periods my family
- 17 My judgements and decisions
- 18 New friendships are something
- 19 When needed, I have
- 20 I am at my best when I
- 21 Meeting new people is
- 22 When I am with others
- 23 When I start on new things/projects
- 24 Facing other people, our family acts
- 25 Belief in myself
- 26 For me, thinking of good topics of conversation is
- 27 My close friends/family members

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- 28 I am good at
- 29 In my family, we like to
- 30 Rules and regular routines
- 31 In difficult periods I have a tendency to
- 32 My goals for the future are
- 33 Events in my life that I cannot influence
- gender "M" (male) or "F" (female)

Note

There are 6 domains

Planned future: items 1, 4, 5, 32

Perception of self: items 2, 11, 17, 25, 31, 33 Family cohesion: items 3, 7, 13, 16, 24, 29 Social resources: items 6, 9, 10, 12, 15, 19, 27 Social Competence: items 8, 14, 18, 21, 22, 26,

Structured style: items 23, 28, 30

References

Briganti, G., & Linkowski, P. (2019). Item and domain network structures of the Resilience Scale for Adults in 675 university students. Epidemiology and psychiatric sciences, 1-9.

Examples

data("rsa")

Sachs

Data: Sachs Network

Description

Protein expression in human immune system cells

Usage

data("Sachs")

Format

A data frame containing 7466 cells (n=7466) and flow cytometry measurements of 11 (p=11) phosphorylated proteins and phospholipids

@references Sachs, K., Gifford, D., Jaakkola, T., Sorger, P., & Lauffenburger, D. A. (2002). Bayesian network approach to cell signaling pathway modeling. Sci. STKE, 2002(148), pe38-pe38.

98 select.estimate

Examples

```
data("Sachs")
```

select

S3 select method

Description

S3 select method

Usage

```
select(object, ...)
```

Arguments

object of class estimate or explore ... not currently used

Value

select works with the following methods:

- select.estimate
- select.explore
- select.ggm_compare_estimate

select.estimate

Graph Selection for estimate Objects

Description

Provides the selected graph based on credible intervals for the partial correlations that did not contain zero (Williams 2018).

Usage

```
## S3 method for class 'estimate'
select(object, cred = 0.95, alternative = "two.sided", ...)
```

select.estimate 99

Arguments

object	An object of class estimate.default.
cred	Numeric. The credible interval width for selecting the graph (defaults to 0.95; must be between 0 and 1).
alternative	A character string specifying the alternative hypothesis. It must be one of "two.sided" (default), "greater" or "less". See note for futher details.
	Currently ignored.

Details

This package was built for the social-behavioral sciences in particular. In these applications, there is strong theory that expects *all* effects to be positive. This is known as a "positive manifold" and this notion has a rich tradition in psychometrics. Hence, this can be incorporated into the graph with alternative = "greater". This results in the estimated structure including only positive edges.

Value

The returned object of class select.estimate contains a lot of information that is used for printing and plotting the results. For users of **BGGM**, the following are the useful objects:

- pcor_adj Selected partial correlation matrix (weighted adjacency).
- adj Adjacency matrix for the selected edges
- object An object of class estimate (the fitted model).

References

Williams DR (2018). "Bayesian Estimation for Gaussian Graphical Models: Structure Learning, Predictability, and Network Comparisons." *arXiv*. doi: 10.31234/OSF.IO/X8DPR.

See Also

estimate and ggm_compare_estimate for several examples.

100 select.explore

select.explore

Graph selection for explore Objects

Description

Provides the selected graph based on the Bayes factor (Williams and Mulder 2019).

Usage

```
## S3 method for class 'explore'
select(object, BF_cut = 3, alternative = "two.sided", ...)
```

Arguments

object An object of class explore.default

BF_cut Numeric. Threshold for including an edge (defaults to 3).

alternative A character string specifying the alternative hypothesis. It must be one of

"two.sided" (default), "greater", "less", or "exhuastive". See note for futher de-

tails.

... Currently ignored.

Details

Exhaustive provides the posterior hypothesis probabilities for a positive, negative, or null relation (see Table 3 in Williams and Mulder 2019).

Value

The returned object of class select.explore contains a lot of information that is used for printing and plotting the results. For users of **BGGM**, the following are the useful objects:

```
alternative = "two.sided"
```

- pcor_mat_zero Selected partial correlation matrix (weighted adjacency).
- pcor_mat Partial correlation matrix (posterior mean).
- Adj_10 Adjacency matrix for the selected edges.
- Adj_01 Adjacency matrix for which there was evidence for the null hypothesis.

```
alternative = "greater" and "less"
```

- pcor_mat_zero Selected partial correlation matrix (weighted adjacency).
- pcor_mat Partial correlation matrix (posterior mean).
- Adj_20 Adjacency matrix for the selected edges.

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• Adj_02 Adjacency matrix for which there was evidence for the null hypothesis (see note).

alternative = "exhaustive"

- post_prob A data frame that included the posterior hypothesis probabilities.
- neg_mat Adjacency matrix for which there was evidence for negative edges.
- pos_mat Adjacency matrix for which there was evidence for positive edges.
- neg_mat Adjacency matrix for which there was evidence for the null hypothesis (see note).
- pcor_mat Partial correlation matrix (posterior mean). The weighted adjacency matrices can be computed by multiplying pcor_mat with an adjacency matrix.

Note

Care must be taken with the options alternative = "less" and alternative = "greater". This is because the full parameter space is not included, such, for alternative = "greater", there can be evidence for the "null" when the relation is negative. This inference is correct: the null model better predicted the data than the positive model. But note this is relative and does **not** provide absolute evidence for the null hypothesis.

References

Williams DR, Mulder J (2019). "Bayesian Hypothesis Testing for Gaussian Graphical Models: Conditional Independence and Order Constraints." *PsyArXiv*. doi: 10.31234/osf.io/ypxd8.

See Also

explore and ggm_compare_explore for several examples.

```
{\it Select.ggm\_compare\_estimate} \\ {\it Graph Selection for ggm\_compare\_estimate} \ {\it Objects}
```

Description

Provides the selected graph (of differences) based on credible intervals for the partial correlations that did not contain zero (Williams 2018).

Usage

```
## S3 method for class 'ggm_compare_estimate'
select(object, cred = 0.95, ...)
```

Arguments

object An object of class estimate.default.

cred Numeric. The credible interval width for selecting the graph (defaults to 0.95; must be between 0 and 1).

... not currently used

Value

The returned object of class select.ggm_compare_estimate contains a lot of information that is used for printing and plotting the results. For users of **BGGM**, the following are the useful objects:

- mean_diff A list of matrices for each group comparsion (partial correlation differences).
- pcor_adj A list of weighted adjacency matrices for each group comparsion.
- adj A list of adjacency matrices for each group comparsion.

```
{\it Select.ggm\_compare\_explore} \\ {\it Graph\ selection\ for\ ggm\_compare\_explore\ Objects}
```

Description

Provides the selected graph (of differences) based on the Bayes factor (Williams et al. 2020).

Usage

```
## S3 method for class 'ggm_compare_explore'
select(object, BF_cut = 3, ...)
```

Arguments

```
object An object of class ggm_compare_explore.

BF_cut Numeric. Threshold for including an edge (defaults to 3).

... Currently ignored.
```

Value

The returned object of class select.ggm_compare_explore contains a lot of information that is used for printing and plotting the results. For users of **BGGM**, the following are the useful objects:

- adj_10 Adjacency matrix for which there was evidence for a difference.
- adj_10 Adjacency matrix for which there was evidence for a null relation
- pcor_mat_10 Selected partial correlation matrix (weighted adjacency; only for two groups).

See Also

explore and ggm_compare_explore for several examples.

104 select.var_estimate

Examples

```
####################
### example 1: ###
####################
# data
Y <- bfi
# males and females
Ymale <- subset(Y, gender == 1,</pre>
                    select = -c(gender,
                                education))[,1:10]
Yfemale <- subset(Y, gender == 2,
                      select = -c(gender,
                                   education))[,1:10]
# fit model
fit <- ggm_compare_explore(Ymale, Yfemale,</pre>
                             iter = 250,
                             type = "continuous",
                             progress = FALSE)
E <- select(fit, post_prob = 0.50)</pre>
```

select.var_estimate Graph Selection for var.estimate Object

Description

Graph Selection for var.estimate Object

Usage

```
## S3 method for class 'var_estimate'
select(object, cred = 0.95, alternative = "two.sided", ...)
```

Arguments

object	An object of class VAR.estimate.
cred	Numeric. The credible interval width for selecting the graph (defaults to 0.95 ; must be between 0 and 1).
alternative	A character string specifying the alternative hypothesis. It must be one of "two.sided" (default), "greater" or "less". See note for futher details.
• • •	Currently ignored.

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Value

An object of class select.var_estimate, including

- pcor_adj Adjacency matrix for the partial correlations.
- beta_adj Adjacency matrix for the regression coefficients.
- pcor_weighted_adj Weighted adjacency matrix for the partial correlations.
- beta_weighted_adj Weighted adjacency matrix for the regression coefficients.
- pcor_mu Partial correlation matrix (posterior mean).
- beta_mu A matrix including the regression coefficients (posterior mean).

Examples

```
# data
Y <- subset(ifit, id == 1)[,-1]
# fit model with alias (var_estimate also works)
fit <- var_estimate(Y, progress = FALSE)
# select graphs
select(fit, cred = 0.95)</pre>
```

summary.coef

Summarize coef Objects

Description

Summarize regression parameters with the posterior mean, standard deviation, and credible interval.

Usage

```
## S3 method for class 'coef'
summary(object, cred = 0.95, ...)
```

Arguments

object An object of class coef.

cred Numeric. The credible interval width for summarizing the posterior distributions (defaults to 0.95; must be between 0 and 1).

... Currently ignored

Value

A list of length *p* including the summaries for each multiple regression.

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Note

See coef.estimate and coef.explore for examples.

summary.estimate	Summary method for estimate.default objects	

Description

Summarize the posterior distribution of each partial correlation with the posterior mean and standard deviation.

Usage

```
## S3 method for class 'estimate'
summary(object, col_names = TRUE, cred = 0.95, ...)
```

Arguments

object An object of class estimate

col_names Logical. Should the summary include the column names (default is TRUE)? Setting to FALSE includes the column numbers (e.g., 1--2).

cred Numeric. The credible interval width for summarizing the posterior distributions (defaults to 0.95; must be between 0 and 1).

... Currently ignored.

Value

A dataframe containing the summarized posterior distributions.

See Also

```
estimate
```

summary.explore 107

summary.explore

Summary Method for explore.default Objects

Description

Summarize the posterior distribution for each partial correlation with the posterior mean and standard deviation.

Usage

```
## S3 method for class 'explore'
summary(object, col_names = TRUE, ...)
```

Arguments

object An object of class estimate

col_names Logical. Should the summary include the column names (default is TRUE)? Set-

ting to FALSE includes the column numbers (e.g., 1--2).

... Currently ignored

Value

A dataframe containing the summarized posterior distributions.

See Also

```
select.explore
```

```
summary.ggm_compare_estimate
```

Summary method for ggm_compare_estimate objects

Description

Summarize the posterior distribution of each partial correlation difference with the posterior mean and standard deviation.

Usage

```
## S3 method for class 'ggm_compare_estimate'
summary(object, col_names = TRUE, cred = 0.95, ...)
```

Arguments

object	An object of class ggm_compare_estimate.
col_names	Logical. Should the summary include the column names (default is TRUE)? Setting to FALSE includes the column numbers (e.g., 12).
cred	Numeric. The credible interval width for summarizing the posterior distributions (defaults to 0.95 ; must be between 0 and 1).
	Currently ignored.

Value

A list containing the summarized posterior distributions.

See Also

```
ggm_compare_estimate
```

```
summary.ggm_compare_explore
```

Summary Method for ggm_compare_explore Objects

Description

Summarize the posterior hypothesis probabilities

Usage

```
## S3 method for class 'ggm_compare_explore'
summary(object, col_names = TRUE, ...)
```

Arguments

object An object of class ggm_compare_explore.

col_names Logical. Should the summary include the column names (default is TRUE)? Set-

ting to FALSE includes the column numbers (e.g., 1--2).

... Currently ignored.

Value

An object of class summary.ggm_compare_explore

See Also

```
ggm_compare_explore
```

summary.predictability

Summary Method for predictability Objects

Description

Summary Method for predictability Objects

Usage

```
## S3 method for class 'predictability'
summary(object, cred = 0.95, ...)
```

Arguments

object An object of class predictability.

cred Numeric. The credible interval width for summarizing the posterior distributions

(defaults to 0.95; must be between 0 and 1).

... Currently ignored

summary.select.explore 111

```
progress = FALSE)
summary(r2)
```

```
summary.select.explore
```

Summary Method for select.explore Objects

Description

Summary Method for select.explore Objects

Usage

```
## S3 method for class 'select.explore'
summary(object, col_names = TRUE, ...)
```

Arguments

Value

a data frame including the posterior mean, standard deviation, and posterior hypothesis probabilities for each relation.

112 summary.var_estimate

```
summary.var_estimate Summary Method for var_estimate Objects
```

Description

Summarize the posterior distribution of each partial correlation and regression coefficient with the posterior mean, standard deviation, and credible intervals.

Usage

```
## S3 method for class 'var_estimate'
summary(object, cred = 0.95, ...)
```

Arguments

object An object of class var_estimate

cred Numeric. The credible interval width for summarizing the posterior distributions
(defaults to 0.95; must be between 0 and 1).

... Currently ignored.

Value

A dataframe containing the summarized posterior distributions, including both the partial correlations and the regression coefficients.

- pcor_results A data frame including the summarized partial correlations
- beta_results A list containing the summarized regression coefficients (one data frame for each outcome)

See Also

```
var_estimate
```

```
# data
Y <- subset(ifit, id == 1)[,-1]
# fit model with alias (var_estimate also works)
fit <- var_estimate(Y, progress = FALSE)
# summary ('pcor')
print(
summary(fit, cred = 0.95),
param = "pcor",
)</pre>
```

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```
# summary ('beta')
print(
summary(fit, cred = 0.95),
param = "beta",
)
```

tas

Data: Toronto Alexithymia Scale (TAS)

Description

A dataset containing items from the Toronto Alexithymia Scale (TAS). There are 20 variables and 1925 observations

Usage

```
data("tas")
```

Format

A data frame with 20 variables and 1925 observations (5 point Likert scale)

Details

- 1 I am often confused about what emotion I am feeling
- 2 It is difficult for me to find the right words for my feelings
- 3 I have physical sensations that even doctors don't understand
- 4 I am able to describe my feelings easily
- 5 I prefer to analyze problems rather than just describe them
- 6 When I am upset, I don't know if I am sad, frightened, or angry
- 7 I am often puzzled by sensations in my body
- 8 I prefer just to let things happen rather than to understand why they turned out that way
- 9 I have feelings that I can't quite identify
- 10 Being in touch with emotions is essential
- 11 I find it hard to describe how I feel about people
- 12 People tell me to describe my feelings more
- 13 I don't know what's going on inside me
- 14 I often don't know why I am angry
- 15 I prefer talking to people about their daily activities rather than their feelings
- 16 I prefer to watch "light" entertainment shows rather than psychological dramas

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- 17 It is difficult for me to reveal my innermost feelings, even to close friends
- 18 I can feel close to someone, even in moments of silence
- 19 I find examination of my feelings useful in solving personal problems
- 20 Looking for hidden meanings in movies or plays distracts from their enjoyment
- gender "M" (male) or "F" (female)

Note

There are three domains

Difficulty identifying feelings: items 1, 3, 6, 7, 9, 13, 14 Difficulty describing feelings: items 2, 4, 11, 12, 17 Externally oriented thinking: items 10, 15, 16, 18, 19

References

Briganti, G., & Linkowski, P. (2019). Network approach to items and domains from the Toronto Alexithymia Scale. Psychological reports.

Examples

```
data("tas")
```

var_estimate

VAR: Estimation

Description

Estimate VAR(1) models by efficiently sampling from the posterior distribution. This provides two graphical structures: (1) a network of undirected relations (the GGM, controlling for the lagged predictors) and (2) a network of directed relations (the lagged coefficients). Note that in the graphical modeling literature, this model is also known as a time series chain graphical model (Abegaz and Wit 2013).

Usage

```
var_estimate(
    Y,
    rho_sd = 0.5,
    beta_sd = 1,
    iter = 5000,
    progress = TRUE,
    seed = 1,
    ...
)
```

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Arguments

Υ	Matrix (or data frame) of dimensions n (observations) by p (variables).
rho_sd	Numeric. Scale of the prior distribution for the partial correlations, approximately the standard deviation of a beta distribution (defaults to 0.50).
beta_sd	Numeric. Standard deviation of the prior distribution for the regression coefficients (defaults to 1). The prior is by default centered at zero and follows a normal distribution (Equation 9, Sinay and Hsu 2014)
iter	Number of iterations (posterior samples; defaults to 5000).
progress	Logical. Should a progress bar be included (defaults to TRUE)?
seed	An integer for the random seed (defaults to 1).
	Currently ignored.

Details

Each time series in Y is standardized (mean = 0; standard deviation = 1).

Value

An object of class var_estimate containing a lot of information that is used for printing and plotting the results. For users of **BGGM**, the following are the useful objects:

- beta_mu A matrix including the regression coefficients (posterior mean).
- pcor_mu Partial correlation matrix (posterior mean).
- fit A list including the posterior samples.

Note

Regularization:

A Bayesian ridge regression can be fitted by decreasing beta_sd (e.g., beta_sd = 0.25). This could be advantageous for forecasting (out-of-sample prediction) in particular.

References

Abegaz F, Wit E (2013). "Sparse time series chain graphical models for reconstructing genetic networks." *Biostatistics*, **14**(3), 586–599. doi: 10.1093/biostatistics/kxt005.

Sinay MS, Hsu JS (2014). "Bayesian inference of a multivariate regression model." *Journal of Probability and Statistics*, **2014**.

```
# data
Y <- subset(ifit, id == 1)[,-1]
# use alias (var_estimate also works)
fit <- var_estimate(Y, progress = FALSE)</pre>
```

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fit

weighted_adj_mat

Extract the Weighted Adjacency Matrix

Description

Extract the weighted adjacency matrix (posterior mean) from estimate, explore, ggm_compare_estimate, and ggm_compare_explore objects.

Usage

```
weighted_adj_mat(object, ...)
```

Arguments

object A model estimated with **BGGM**. All classes are supported, assuming there is

matrix to be extracted.

... Currently ignored.

Value

The weighted adjacency matrix (partial correlation matrix with zeros).

women_math

women_math

Data: Women and Mathematics

Description

A data frame containing 1190 observations (n = 1190) and 6 variables (p = 6) measured on the binary scale.

Usage

```
data("women_math")
```

Format

A data frame containing 1190 observations (n = 1190) and 6 variables (p = 6) measured on the binary scale (Fowlkes et al. 1988). These data have been analyzed in Tarantola (2004) and in (Madigan and Raftery 1994). The variable descriptions were copied from (section 5.2) (section 5.2, Talhouk et al. 2012)

Details

- 1 Lecture attendance (attend/did not attend)
- 2 Gender (male/female)
- 3 School type (urban/suburban)
- 4 "I will be needing Mathematics in my future work" (agree/disagree)
- 5 Subject preference (math/science vs. liberal arts)
- 6 Future plans (college/job)

References

Fowlkes EB, Freeny AE, Landwehr JM (1988). "Evaluating logistic models for large contingency tables." *Journal of the American Statistical Association*, **83**(403), 611–622. doi: 10.1080/01621459.1988.10478640.

Madigan D, Raftery AE (1994). "Model selection and accounting for model uncertainty in graphical models using Occam's window." *Journal of the American Statistical Association*, **89**(428), 1535–1546.

Talhouk A, Doucet A, Murphy K (2012). "Efficient Bayesian inference for multivariate probit models with sparse inverse correlation matrices." *Journal of Computational and Graphical Statistics*, **21**(3), 739–757. doi: 10.1080/10618600.2012.679239.

Tarantola C (2004). "MCMC model determination for discrete graphical models." *Statistical Modelling*, **4**(1), 39–61. doi: 10.1191/1471082x04st063oa.

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Examples

```
data("women_math")
```

zero_order_cors

Zero-Order Correlations

Description

Estimate zero-order correlations for any type of data. Note zero-order refers to the fact that no variables are controlled for (i.e., bivariate correlations). To our knowledge, this is the only Bayesian implementation in R that can estiamte Pearson's, tetrachoric (binary), polychoric (ordinal with more than two cateogries), and rank based correlation coefficients.

Usage

```
zero_order_cors(
  Υ,
  type = "continuous",
  iter = 5000,
 mixed_type = NULL,
 progress = TRUE
)
```

Arguments

Matrix (or data frame) of dimensions n (observations) by p (variables).

Character string. Which type of data for Y? The options include continuous, type

binary, ordinal, or mixed. See the note for further details.

iter Number of iterations (posterior samples; defaults to 5000).

mixed_type

Numeric vector. An indicator of length p for which varibles should be treated as

ranks. (1 for rank and 0 to assume normality). The default is currently to treat all integer variables as ranks when type = "mixed" and NULL otherwise. See

note for further details.

Logical. Should a progress bar be included (defaults to TRUE)? progress

Details

The term "mixed" is somewhat of a misnomer, because the method can be used for data including only continuous or only discrete variables. This is based on the ranked likelihood which requires sampling the ranks for each variable (i.e., the data is not merely transformed to ranks). This is computationally expensive when there are many levels. For example, with continuous data, there are as many ranks as data points!

The option mixed_type allows the user to determine which variable should be treated as ranks and the "emprical" distribution is used otherwise (Hoff 2007). This is accomplished by specifying an zero_order_cors 119

indicator vector of length p. A one indicates to use the ranks, whereas a zero indicates to "ignore" that variable. By default all integer variables are treated as ranks.

Dealing with Errors:

An error is most likely to arise when type = "ordinal". The are two common errors (although still rare):

- The first is due to sampling the thresholds, especially when the data is heavily skewed. This can result in an ill-defined matrix. If this occurs, we recommend to first try decreasing prior_sd (i.e., a more informative prior). If that does not work, then change the data type to type = mixed which then estimates a copula GGM (this method can be used for data containing **only** ordinal variable). This should work without a problem.
- The second is due to how the ordinal data are categorized. For example, if the error states that the index is out of bounds, this indicates that the first category is a zero. This is not allowed, as the first category must be one. This is addressed by adding one (e.g., Y + 1) to the data matrix.

Value

- R An array including the correlation matrices (of dimensions p by p by iter)
- R_mean Posterior mean of the correlations (of dimensions p by p)

```
# note: iter = 250 for demonstrative purposes
Y <- ptsd[,1:3]
###### example 1: Pearson's ####
fit <- zero_order_cors(Y, type = "continuous",
                  iter = 250.
                  progress = FALSE)
##### example 2: polychoric ####
fit <- zero_order_cors(Y+1, type = "ordinal",
                  iter = 250,
                  progress = FALSE)
###############################
##### example 3: rank #####
#####################################
fit <- zero_order_cors(Y+1, type = "mixed",
```

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