Package 'BNSP'

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Title Bayesian Non- And Semi-Parametric Model Fitting
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Description

Markov chain Monte Carlo algorithms for non- and semi-parametric models: 1. spike-slab variable selection in multivariate mean/variance regression models with function mvrm, 2. joint mean-covariance models for multivariate longitudinal responses with function 1mrm, and 3. Dirichlet process mixture models with function dpmj.

Details

Package: BNSP
Type: Package
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Papageorgiou, G., Richardson, S. and Best, N. (2015). Bayesian nonparametric models for spatially indexed data of mixed type. Journal of the Royal Statistical Society: Series B (Statistical Methodology), 77:973-999.

ami

Amitriptyline dataset from Johnson and Wichern

Description

Amitriptyline is a prescription antidepressant. The dataset consists of measurements on 17 patients who had over-dosed on amitriptyline.

Usage

data(ami)

Format

A data frame containing 17 rows and 7 columns. The columns represent

tot total blood plasma level.

ami amount of amitriptyline found in the plasma.

gen gender (1 for female).

amt amount of the drug taken.

pr PR wave measurement.

bp diastolic blood pressure.

qrs QRS wave measurement.

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Source

Johnson, R. A., and Wichern, D. W. (2007), Applied Multivariate Statistical Analysis, Essex: Pearson, page 426.

References

Johnson, R. A., and Wichern, D. W. (2007). Applied Multivariate Statistical Analysis, Essex: Pearson.

chol

The Cholesky and modified Cholesky decompositions

Description

Computes the Cholesky factorization and modified Cholesky factorizations of a real symmetric positive-definite square matrix.

Usage

```
chol(x, mod = TRUE, p = 1, ...)
```

Arguments

Х A symmetric, positive-definite matrix. mod Defaults to TRUE. With this choice, the function returns the modified Cholesky

decomposition. When mod = FALSE, the function returns the usual Cholesky

decomposition.

Relevant only when mod = TRUE. It determines the size of the blocks of the block р

diagonal matrix.

other arguments.

Details

The function computes the modified Cholesky decomposition of a real symmetric positive-definite square matrix Σ . This is given by

 $L\Sigma L^{\top} = D,$

where L is a lower tringular matrix with ones on its main diagonal and D is a block diagonal matrix with block size determined by argument p.

Value

The function returns matrices L and D.

Author(s)

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See Also

The default function from base, chol

Examples

```
Sigma <- matrix(c(1.21,0.18,0.13,0.41,0.06,0.23,
                  0.18, 0.64, 0.10, -0.16, 0.23, 0.07,
                  0.13,0.10,0.36,-0.10,0.03,0.18,
                  0.41,-0.16,-0.10,1.05,-0.29,-0.08,
                  0.06,0.23,0.03,-0.29,1.71,-0.10,
                  0.23,0.07,0.18,-0.08,-0.10,0.36),6,6)
LD <- chol(Sigma)
L <- LD$L
D <- LD$D
round(L,5)
round(D,5)
solve(L) %*% D %*% solve(t(L))
LD <- chol(Sigma, p = 2)
L <- LD$L
D <- LD$D
round(L, 5)
round(D, 5)
solve(L) %*% D %*% solve(t(L))
```

clustering

Computes the similarity matrix

Description

Computes the similarity matrix.

Usage

```
clustering(object, ...)
```

Arguments

```
object an object of class "mvrm", usually a result of a call to mvrm.
... other arguments.
```

Details

The function computes the similarity matrix for clustering based on corrrelations or variables.

Value

Similarity matrix.

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Author(s)

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See Also

mvrm

Examples

```
#see \code{mvrm} example
```

continue

Continues the sampler from where it stopped

Description

Allows the user to continue the sampler from the state it stopped in the previous call to mvrm.

Usage

```
continue(object, sweeps, burn = 0, thin, discard = FALSE,...)
```

Arguments

object	An object of class "mvrm", usually a result of a call to mvrm.
sweeps	The number of additional sweeps, maintaining the same thinning interval as specified in the original call to mvrm.
burn	length of burn-in period. Defaults to zero.
thin	thinning parameter. Defaults to the thinning parameter chosen for object.
discard	If set to true, the previous samples are discarded.
	other arguments.

Details

The function allows the sampler to continue from the state it last stopped.

Value

The function returns an object of class mvrm.

Author(s)

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See Also

mvrm

Examples

#see \code{mvrm} example

dpmj

Dirichlet process mixtures of joint models

Description

Fits Dirichlet process mixtures of joint response-covariate models, where the covariates are of mixed type while the discrete responses are represented utilizing continuous latent variables. See 'Details' section for a full model description and Papageorgiou (2018) for all technical details.

Usage

Arguments

O	
formula	a formula defining the response and the covariates e.g. y \sim x.
Fcdf	a description of the kernel of the response variable. Currently five options are supported: 1. "poisson", 2. "negative binomial", 3. "generalized poisson", 4. "binomial" and 5. "beta binomial". The first three kernels are used for count data analysis, where the third kernel allows for both over- and under-dispersion relative to the Poisson distribution. The last two kernels are used for binomial data analysis. See 'Details' section for some of the kernel details.
data	an optional data frame, list or environment (or object coercible by 'as.data.frame' to a data frame) containing the variables in the model. If not found in 'data', the variables are taken from 'environment(formula)'.
offset	this can be used to specify an a priori known component to be included in the model. This should be 'NULL' or a numeric vector of length equal to the sample size. One 'offset' term can be included in the formula, and if more are required, their sum should be used.
sampler	the MCMC algorithm to be utilized. The two options are sampler = "slice" which implements a slice sampler (Walker, 2007; Papaspiliopoulos, 2008) and sampler = "truncated" which proceeds by truncating the countable mixture at ncomp components (see argument ncomp).
Xpred	an optional design matrix the rows of which include the values of the covariates x for which the conditional distribution of $Y x, D$ (where D denotes the data)

included to obtain averaged effects.

is calculated. These are treated as 'new' covariates i.e. they do not contribute to the likelihood. The matrix shouldn't include a column of 1's. NA's can be

offsetPred

the offset term associated with the new covariates Xpred. It is of dimension one i.e. the same offset term is used for all rows of Xpred. If Fcdf is one of "poisson" or "negative binomial" or "generalized poisson", then offsetPred is the Poisson offset term. If Fcdf is one of "binomial" or "beta binomial", then offsetPred is the number of Binomial trials. If offsetPred is missing, it is taken to be the mean of offset, rounded to the nearest integer.

StorageDir

a directory to store files with the posterior samples of models parameters and other quantities of interest. If a directory is not provided, files are created in the current directory and removed when the sampler completes.

ncomp

number of mixture components. It defines where the countable mixture of densities [in (1) below] is truncated. Even if sampler="slice" is chosen, ncomp needs to be specified as it is used in the initialization process.

sweeps

total number of posterior samples, including those discarded in burn-in period (see argument burn) and those discarded by the thinning process (see argument thin).

burn

length of burn-in period.

thin

thinning parameter.

seed

optional seed for the random generator.

Н

optional scale matrix of the Wishart-like prior assigned to the restricted covariance matrices Σ_h^* . See 'Details' section.

Hdf

optional degrees of freedom of the prior Wishart-like prior assigned to the restricted covariance matrices Σ_h^* . See 'Details' section.

d

optional prior mean of the mean vector μ_h . See 'Details' section.

D

optional prior covariance matrix of the mean vector μ_h . See 'Details' section.

Alpha.xi an optional parameter that depends on the specified Fcdf argument.

- 1. If Fcdf = "poisson", this argument is parameter $\alpha_{\mathcal{E}}$ of the prior of the Poisson rate: $\xi \sim \text{Gamma}(\alpha_{\xi}, \beta_{\xi})$.
- 2. If Fcdf = "negative binomial", this argument is a two-dimensional vector that includes parameters $\alpha_{1\xi}$ and $\alpha_{2\xi}$ of the priors: $\xi_1 \sim \text{Gamma}(\alpha_{1\xi}, \beta_{1\xi})$ and $\xi_2 \sim \text{Gamma}(\alpha_{2\xi}, \beta_{2\xi})$, where ξ_1 and ξ_2 are the two parameters of the Negative Binomial pmf.
- 3. If Fcdf = "generalized poisson", this argument is a two-dimensional vector that includes parameters $\alpha_{1\xi}$ and $\alpha_{2\xi}$ of the priors: $\xi_1 \sim \text{Gamma}(\alpha_{1\xi}, \beta_{1\xi})$ and $\xi_2 \sim N(\alpha_{2\xi}, \beta_{2\xi})I[\xi_2 \in R_{\xi_2}]$, where ξ_1 and ξ_2 are the two parameters of the Generalized Poisson pmf. Parameter ξ_2 is restricted in the range $R_{\xi_2} = (0.05, \infty)$ as it is a dispersion parameter.
- 4. If Fcdf = "binomial", this argument is parameter α_{ξ} of the prior of the Binomial probability: $\xi \sim \text{Beta}(\alpha_{\xi}, \beta_{\xi})$.
- 5. If Fcdf = "beta binomial", this argument is a two-dimensional vector that includes parameters $\alpha_{1\xi}$ and $\alpha_{2\xi}$ of the priors: $\xi_1 \sim \text{Gamma}(\alpha_{1\xi}, \beta_{1\xi})$ and $\xi_2 \sim \text{Gamma}(\alpha_{2\xi}, \beta_{2\xi})$, where ξ_1 and ξ_2 are the two parameters of the Beta Binomial pmf.

See 'Details' section.

Beta.xi an optional parameter that depends on the specified family.

- 1. If Fcdf = "poisson", this argument is parameter β_{ξ} of the prior of the Poisson rate: $\xi \sim \text{Gamma}(\alpha_{\xi}, \beta_{\xi})$.
- 2. If Fcdf = "negative binomial", this argument is a two-dimensional vector that includes parameters $\beta_{1\xi}$ and $\beta_{2\xi}$ of the priors: $\xi_1 \sim \text{Gamma}(\alpha_{1\xi}, \beta_{1\xi})$ and $\xi_2 \sim \text{Gamma}(\alpha_{2\xi}, \beta_{2\xi})$, where ξ_1 and ξ_2 are the two parameters of the Negative Binomial pmf.
- 3. If Fcdf = "generalized poisson", this argument is a two-dimensional vector that includes parameters $\beta_{1\xi}$ and $\beta_{2\xi}$ of the priors: $\xi_1 \sim \operatorname{Gamma}(\alpha_{1\xi},\beta_{1\xi})$ and $\xi_2 \sim \operatorname{Normal}(\alpha_{2\xi},\beta_{2\xi})I[\xi_2 \in R_{\xi_2}]$, where ξ_1 and ξ_2 are the two parameters of the Generalized Poisson pmf. Parameter ξ_2 is restricted in the range $R_{\xi_2} = (0.05,\infty)$ as it is a dispersion parameter. Note that $\beta_{2\xi}$ is a standard deviation.
- 4. If Fcdf = "binomial", this argument is parameter β_{ξ} of the prior of the Binomial probability: $\xi \sim \text{Beta}(\alpha_{\xi}, \beta_{\xi})$.
- 5. If Fcdf = "beta binomial", this argument is a two-dimensional vector that includes parameters $\beta_{1\xi}$ and $\beta_{2\xi}$ of the priors: $\xi_1 \sim \text{Gamma}(\alpha_{1\xi}, \beta_{1\xi})$ and $\xi_2 \sim \text{Gamma}(\alpha_{2\xi}, \beta_{2\xi})$, where ξ_1 and ξ_2 are the two parameters of the Beta Binomial pmf.

See 'Details' section.

Alpha. alpha optional shape parameter α_{α} of the Gamma prior assigned to the concentration parameter α . See 'Details' section.

Beta.alpha optional rate parameter β_{α} of the Gamma prior assigned to concentration parameter α . See 'Details' section.

Trunc.alpha optional truncation point c_{α} of the Gamma prior assigned to concentration parameter α . See 'Details' section.

... Other options that will be ignored.

Details

Function dpmj returns samples from the posterior distributions of the parameters of the model:

$$f(y_i, x_i) = \sum_{h=1}^{\infty} \pi_h f(y_i, x_i | \theta_h), \tag{1}$$

where y_i is a univariate discrete response, x_i is a p-dimensional vector of mixed type covariates, and $\pi_h, h \geq 1$, are obtained according to Sethuraman's (1994) stick-breaking construction: $\pi_1 = v_1$, and for $l \geq 2, \pi_l = v_l \prod_{i=1}^{l-1} (1-v_j)$, where v_k are iid samples $v_k \sim \text{Beta } (1, \alpha), k \geq 1$.

Let Z denote a discrete variable (response or covariate). It is represented as discretized version of a continuous latent variable Z^* . Observed discrete Z and continuous latent variable Z^* are connected by:

$$z = q \iff c_{q-1} < z^* < c_q, q = 0, 1, 2, \dots,$$

where the cut-points are obtained as: $c_{-1} = -\infty$, while for $q \ge 0$, $c_q = c_q(\lambda) = \Phi^{-1}\{F(q;\lambda)\}$. Here $\Phi(.)$ is the cumulative distribution function (cdf) of a standard normal variable and F() denotes an appropriate cdf. Further, latent variables are assumed to independently follow a N(0,1) distribution, where the mean and variance are restricted to be zero and one as they are non-identifiable by the data. Choices for F() are described next.

For counts, three options are supported. First, $F(.;\lambda_i)$ can be specified as the cdf of a Poisson $(H_i\xi_h)$ variable. Here $\lambda_i=(\xi_h,H_i)^T,\xi_h$ denotes the Poisson rate associated with cluster h, and H_i the offset term associated with sampling unit i. Second, $F(.;\lambda_i)$ can be specified as the negative binomial cdf, where $\lambda_i=(\xi_{1h},\xi_{2h},H_i)^T$. This option allows for overdispersion within each cluster relative to the Poisson distribution. Third, $F(.;\lambda_i)$ can be specified as the Generalized Poisson cdf, where, again, $\lambda_i=(\xi_{1h},\xi_{2h},H_i)^T$. This option allows for both over- and under-dispersion within each cluster.

For Binomial data, two options are supported. First, $F(.; \lambda_i)$ may be taken to be the cdf of a Binomial (H_i, ξ_h) variable, where ξ_h denotes the success probability of cluster h and H_i the number of trials associated with sampling unit i. Second, $F(.; \lambda_i)$ may be specified to be the beta-binomial cdf, where $\lambda = (\xi_{1h}, \xi_{2h}, H_i)^T$.

The special case of Binomial data is treated as

$$Z = 0 \iff z^* < 0, z^* \sim N(\mu_z^*, 1).$$

Details on all kernels are provided in the two tables below. The first table provides the probability mass functions and the mean in the presence of an offset term (which may be taken to be one). The column 'Sample' indicates for which parameters the routine provides posterior samples. The second table provides information on the assumed priors along with the default values of the parameters of the prior distributions and it also indicates the function arguments that allow the user to alter these.

Kernel	PMF	Offset	Mean	Sample
Poisson	$\exp(-H\xi)(H\xi)^y/y!$	H	$H\xi$	ξ
Negative Binomial	$\frac{\Gamma(y+\xi_1)}{\Gamma(\xi_1)\Gamma(y+1)} \left(\frac{\xi_2}{H+\xi_2}\right)^{\xi_1} \left(\frac{H}{H+\xi_2}\right)^y$	H	$H\xi_1/\xi_2$	ξ_1, ξ_2
Generalized Poisson	$\xi_1 \{ \xi_1 + (\xi_2 - 1)y \}^{y-1} \xi_2^{-y} \times$	H	$H\xi_1$	ξ_1, ξ_2
	$\exp\{-[\xi_1 + (\xi_2 - 1)y]/\xi_2\}/y!$			
Binomial	$\binom{N}{y}\xi^y(1-\xi)^{N-y}$	N	$N\xi$	ξ
Beta Binomial	$\binom{N}{y} \frac{Beta(y+\xi_1,N-y+\xi_2)}{Beta(\xi_1,\xi_2)}$	N	$N\xi_1/(\xi_1+\xi_2)$	ξ_1, ξ_2

Kernel	Priors	Default Values
Poisson	$\xi \sim \text{Gamma}(\alpha_{\xi}, \beta_{\xi})$	Alpha. $xi = 1.0$, Beta. $xi = 0.1$
Negative Binomial	$\xi_i \sim \text{Gamma}(\alpha_{\xi_i}, \beta_{\xi_i}), i = 1, 2$	Alpha.xi = $c(1.0,1.0)$, Beta.xi = $c(0.1,0.1)$
Generalized Poisson	$\xi_1 \sim Gamma(\alpha_{\xi_1}, \beta_{\xi_1})$	
	$\xi_2 \sim N(\alpha_{\xi_2}, \beta_{\xi_2}) I[\xi_2 > 0.05]$	Alpha.xi = $c(1.0,1.0)$, Beta.xi = $c(0.1,1.0)$
	where β_{ξ_2} denotes st.dev.	
Binomial	$\xi \sim \text{Beta}(\alpha_{\xi}, \beta_{\xi})$	Alpha. $xi = 1.0$, Beta. $xi = 1.0$
Beta Binomial	$\xi_i \sim \text{Gamma}(\alpha_{\xi_i}, \beta_{\xi_i}), i = 1, 2$	Alpha.xi = $c(1.0,1.0)$, Beta.xi = $c(0.1,0.1)$

Let $z_i = (y_i, x_i^T)^T$ denote the joint vector of observed continuous and discrete variables and z_i^* the corresponding vector of continuous observed and latent variables. With θ_h denoting model parameters associated with the hth cluster, the joint density $f(z_i|\theta_h)$ takes the form

$$f(z_i|\theta_h) = \int_{R(y)} \int_{R(x_d)} N_q(z_i^*; \mu_h^*, \Sigma_h^*) dx_d^* dy^*,$$

where

$$\mu_h^* = \begin{pmatrix} 0 \\ \mu_h \end{pmatrix}, \quad \Sigma_h^* = \begin{bmatrix} C_h & \nu_h^T \\ \nu_h & \Sigma_h \end{bmatrix},$$

where C_h is the covariance matrix of the latent continuous variables and it has diagonal elements equal to one i.e. it is a correlation matrix.

In addition to the priors defined in the table above, we specify the following:

- 1. The restricted covariance matrix Σ_h* is assigned a prior distribution that is based on the Wishart distribution with degrees of freedom set by default to dimension of matrix plus two and diagonal scale matrix, with the sub-matrix that corresponds to discrete variables taken to be the identity matrix and with sub-matrix that corresponds to continuous variables having entries equal to 1/8 of the square of the observed data range. Default values can be changed using arguments H and Hdf.
- 2. The prior on μ_h , the non-zero part of μ_h^* , is taken to be multivariate normal $\mu_h \sim N(d,D)$. The mean d is taken to be equal to the center of the dataset. The covariance matrix D is taken to be diagonal. Its elements that correspond to continuous variables are set equal to 1/8 of the square of the observed data range while the elements that correspond to binary variables are set equal to 5. Arguments Mu.mu and Sigma.mu allow the user to change the default values.
- 3. The concentration parameter α is assigned a $\operatorname{Gamma}(\alpha_{\alpha},\beta_{\alpha})$ prior over the range (c_{α},∞) , that is, $f(\alpha) \propto \alpha^{\alpha_{\alpha}-1} \exp\{-\alpha\beta_{\alpha}\}I[\alpha>c_{\alpha}]$, where I[.] is the indicator function. The default values are $\alpha_{\alpha}=2.0,\beta_{\alpha}=5.0$, and $c_{\alpha}=0.25$. Users can alter the default using using arguments Alpha. alpha, Beta. alpha and Turnc. alpha.

Value

Function dpmj returns the following:

call	the matched call.
seed	the seed that was used (in case replication of the results is needed).
meanReg	if Xpred is specified, the function returns the posterior mean of the conditional expectation of the response y given each new covariate x .
medianReg	if Xpred is specified, the function returns the posterior mean of the conditional 50% quantile of the response y given each new covariate x .
q1Reg	if Xpred is specified, the function returns the posterior mean of the conditional 25% quantile of the response y given each new covariate x .
q3Reg	if Xpred is specified, the function returns the posterior mean of the conditional 75% quantile of the response y given each new covariate x .
modeReg	if Xpred is specified, the function returns the posterior mean of the conditional mode of the response y given each new covariate x .
denReg	if Xpred is specified, the function returns the posterior mean conditional density of the response y given each new covariate x . Results are presented in a matrix the rows of which correspond to the different x s.
denVar	if Xpred is specified, the function returns the posterior variance of the conditional density of the response y given each new covariate x . Results are pre-

sented in a matrix the rows of which correspond to the different xs.

Further, function dpmj creates files where the posterior samples are written. These files are (with all file names preceded by 'BNSP.'):

alpha.txt this file contains samples from the posterior of the concentration parameters α . The file is arranged in (sweeps-burn)/thin lines and one column, each line including one posterior sample.

compAlloc.txt this file contains the allocations to clusters obtained during posterior sampling. It consists of (sweeps-burn)/thin lines, that represent the posterior samples, and n columns, that represent the sampling units. Clusters are represented by integers ranging from 0 to ncomp-1.

MeanReg.txt this file contains the conditional means of the response y given covariates x obtained during posterior sampling. The rows represent the (sweeps-burn)/thin posterior samples. The columns represent the various covariate values x for which the means are obtained.

MedianReg.txt this file contains the 50% conditional quantile of the response y given covariates x obtained during posterior sampling. The rows represent the (sweeps-burn)/thin posterior samples. The columns represent the various covariate values x for which the medians are obtained.

muh.txt this file contains samples from the posteriors of the p-dimensional mean vectors $\mu_h, h=1,2,\ldots$,ncomp. The file is arranged in ((sweeps-burn)/thin)*ncomp lines and p columns. In more detail, sweeps create ncomp lines representing samples $\mu_h^{(sw)}, h=1,\ldots$,ncomp, where superscript sw represents a particular sweep. The elements of $\mu_h^{(sw)}$ are written in the columns of the file.

nmembers.txt this file contains (sweeps-burn)/thin lines and ncomp columns, where the lines represent posterior samples while the columns represent the components or clusters. The entries represent the number of sampling units allocated to each component.

Q05Reg.txt this file contains the 5% conditional quantile of the response y given covariates x obtained during posterior sampling. The rows represent the (sweeps-burn)/thin posterior samples. The columns represent the various covariate values x for which the quantiles are obtained.

as above, for the 10% conditional quantile. Q10Reg.txt Q15Reg.txt as above, for the 15% conditional quantile. Q20Reg.txt as above, for the 20% conditional quantile. as above, for the 25% conditional quantile. Q25Reg.txt as above, for the 75% conditional quantile. Q75Reg.txt Q80Reg.txt as above, for the 80% conditional quantile. Q85Reg.txt as above, for the 85% conditional quantile. Q90Reg.txt as above, for the 90% conditional quantile. Q95Reg.txt as above, for the 95% conditional quantile.

Sigmah.txt this file contains samples from the posteriors of the $q \times q$ restricted covariance matrices $\Sigma_h^*, h = 1, 2, \ldots$, ncomp. The file is arranged in ((sweeps-burn)/thin)*ncomp lines and q^2 columns. In more detail, sweeps create ncomp lines representing samples $\Sigma_h^{(sw)}, h = 1, \ldots$, ncomp, where superscript sw represents a particular sweep. The elements of $\Sigma_h^{(sw)}$ are written in the columns of the file.

this file contains samples from the posteriors of parameters $\xi_h, h=1,2,\ldots$, ncomp. The file is arranged in ((sweeps-burn)/thin)*ncomp lines and one or two columns, depending on the number of parameters in the selected Fcdf. Sweeps write in the file ncomp lines representing samples $\xi_h^{(sw)}, h=1,\ldots$, ncomp, where superscript sw represents a particular sweep.

Updated.txt this file contains (sweeps-burn)/thin lines with the number of components updated at each iteration of the sampler (relevant for slice sampling).

Author(s)

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Walker, S. G. (2007). Sampling the Dirichlet mixture model with slices. Communications in Statistics Simulation and Computation, 36(1), 45-54.

Examples

```
#Bayesian nonparametric joint model with binomial response Y and one predictor X
data(simD)
pred<-seq(with(simD,min(X))+0.1,with(simD,max(X))-0.1,length.out=30)</pre>
npred<-length(pred)</pre>
# fit1 and fit2 define the same model but with different numbers of
# components and posterior samples
fit1 <- dpmj(cbind(Y,(E-Y))~X, Fcdf="binomial", data=simD, ncomp=10, sweeps=20,</pre>
             burn=10, sampler="truncated", Xpred=pred, offsetPred=30)
fit2 <- dpmj(cbind(Y,(E-Y))~X, Fcdf="binomial", data=simD, ncomp=50, sweeps=5000,
               burn=1000, sampler="truncated", Xpred=pred, offsetPred=30)
plot(with(simD,X),with(simD,Y)/with(simD,E))
lines(pred, fit2$medianReg/30, col=3, lwd=2)
# with discrete covariate
simD<-data.frame(simD, Xd=sample(c(0,1),300,replace=TRUE))</pre>
pred < -c(0,1)
fit3 <- dpmj(cbind(Y,(E-Y))~Xd, Fcdf="binomial", data=simD, ncomp=10, sweeps=20,
             burn=10, sampler="truncated", Xpred=pred, offsetPred=30)
```

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histCorr

Creates plots of correlation matrices

Description

This function plots the posterior distribution of the elements of correlation matrices.

Usage

```
histCorr(x, term = "R", plotOptions = list(),...)
```

Arguments

x an object of class 'mvrm', as generated by function mvrm.

term Admits two possible values: "R" to plot samples from the posterior of the cor-

relation matrix R, and "muR" to plot samples from the posterior of the means

 μ_R .

plotOptions ggplot type options.

... other arguments.

Details

Use this function to visualize the elements of a correlation matrix.

Value

Posterior distributions of elements of correlation matrices.

Author(s)

Georgios Papageorgiou <gpapageo@gmail.com>

See Also

mvrm

Examples

```
#see \code{mvrm} example
```

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lmrm	Bayesian semiparametric modelling of covariance matrices for multi-
	variate longitudinal data

Description

Implements an MCMC algorithm for posterior sampling based on a semiparametric model for continuous longitudinal multivariate responses. The overall model consists of 5 regression submodels and it utilizes spike-slab priors for variable selection and function regularization. See 'Details' section for a full description of the model.

Usage

```
lmrm(formula, data = list(), centre=TRUE, id, time,
sweeps, burn = 0, thin = 1, seed, StorageDir,
c.betaPrior = "IG(0.5,0.5*n*p)", pi.muPrior = "Beta(1,1)",
c.alphaPrior = "IG(1.1,1.1)", pi.phiPrior = "Beta(1,1)", c.psiPrior = "HN(2)",
sigmaPrior = "HN(2)", pi.sigmaPrior = "Beta(1,1)",
corr.Model = c("common", nClust = 1), DP.concPrior = "Gamma(5,2)",
c.etaPrior = "IG(0.5,0.5*samp)", pi.nuPrior = "Beta(1,1)",
pi.fiPrior = "Beta(1,1)", c.omegaPrior = "IG(1.1,1.1)", sigmaCorPrior = "HN(2)",
tuneCalpha, tuneSigma2, tuneCbeta, tuneAlpha, tuneSigma2R, tuneR, tuneCpsi,
tuneCbCor, tuneOmega, tuneComega, tau, FT = 1,...)
```

Arguments

formula	a formula defining the responses and the covariates in the 5 regression models e.g. $y1 \mid y2 \sim x \mid w \mid z \mid t \mid t$ or for smooth effects $y1 \mid y2 \sim sm(x) \mid sm(w) \mid sm(z) \mid sm(t) \mid sm(t)$. The package uses the extended formula notation, where the responses are defined on the left of \sim and the models on the right.
data	a data frame.
centre	Binary indicator. If set equal to TRUE, the design matrices are centred, to have column mean equl to zero, otherwise, if set to FALSE, the columns are not centred.
id	identifiers of the individuals or other sampling units that are observed over time.
time	a vector input that specifies the time of observation
sweeps	total number of posterior samples, including those discarded in burn-in period (see argument burn) and those discarded by the thinning process (see argument thin).
burn	length of burn-in period.
thin	thinning parameter.
seed	optional seed for the random generator.
StorageDir	a required directory to store files with the posterior samples of models parameters.

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c.betaPrior The inverse Gamma prior of c_{β} . The default is "IG(0.5,0.5*n*p)", that is, an inverse Gamma with parameters 1/2 and np/2, where n is the number of sampling units and p is the length of the response vector. The Beta prior of π_{μ} . The default is "Beta(1,1)". It can be of dimension 1, of pi.muPrior dimension K (the number of effects that enter the mean model), or of dimension The inverse Gamma prior of c_{α}^2 . The default is "IG(1.1,1.1)". Half-normal priors c.alphaPrior for c_{α} are also available, declared using "HN(a)", where "a" is a positive number. It can be of dimension 1 or p (the length of the multivariate response). The Beta prior of π_{ϕ} . The default is "Beta(1,1)". It can be of dimension 1, pi.phiPrior of dimension B (the number of effects that enter the dependence model), or of dimension p^2B The prior of c_{ψ}^2 . The default is "HN(2)", a half-normal prior for c_{ψ} with variance c.psiPrior equal to two, $c_{\psi} \sim N(0,2)I[c_{\psi} > 0]$. Inverse Gamma priors for c_{ψ}^2 are also available, declared using "IG(a,b)". It can be of dimension 1 or p^2 (the number of dependence models). The prior of $\sigma_k^2, k = 1, \dots, p$. The default is "HN(2)", a half-normal prior for sigmaPrior σ_k with variance equal to two, $\sigma_k \sim N(0,2)I[\sigma > 0]$. Inverse Gamma priors for σ_k^2 are also available, declared using "IG(a,b)". It can be of dimension 1 or p (the length of the multivariate response). pi.sigmaPrior The Beta prior of π_{σ} . The default is "Beta(1,1)". It can be of dimension 1, of dimension L (the number of effects that enter the variance model), or of dimension pLSpecifies the model for the correlation matrices R_t . The three choices supported corr.Model are "common", that specifies a common correlations model, "groupC", that specifies a grouped correlations model, and "groupV", that specifies a grouped variables model. When the model chosen is either "groupC" or "groupV", the upper limit on the number of clusters can also be specified, using corr.Model = c("groupC", nClust = d) or corr.Model = c("groupV", nClust = p). If the number of clusters is left unspecified, for the "groupV" model, it is taken to be p, the number of responses. For the "groupC" model, it is taken to be d = p(p-1)/2, the number of free elements in the correlation matrices. DP.concPrior The Gamma prior for the Dirichlet process concentration parameter. The inverse Gamma prior of c_n . The default is "IG(0.5,0.5*samp)", that is, an c.etaPrior inverse Gamma with parameters 1/2 and samp/2, where samp is the number of correlations observed over time, that is \$samp=M*d\$ where \$M\$ is the number of unique observation time points and \$d\$ is the number of non-redundant elements of \$R\$. The Beta prior of π_{ν} . The default is "Beta(1,1)". It can be of dimension 1. pi.nuPrior The Beta prior of π_{φ} . The default is "Beta(1,1)". It can be of dimension 1. pi.fiPrior The prior of c_ω^2 . The default is "HN(2)", a half-normal prior for c_ω with variance c.omegaPrior equal to two, $c_{\omega} \sim N(0,2)I[c_{\omega}>0]$. Inverse Gamma priors for c_{ω}^2 are also available, declared using "IG(a,b)". It can be of dimension 1. The prior of σ^2 . The default is "HN(2)", a half-normal prior for σ^2 with variance sigmaCorPrior

equal to two, $\sigma \sim N(0,2)I[\sigma > 0]$. Inverse Gamma priors for σ^2 are also

available, declared using "IG(a,b)". It can be of dimension 1.

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tuneCalpha	Starting value of the tuning parameter for sampling $c_{\alpha k}, k = 1,, p$. Defaults at a vector of \$p\$ ones. It could be of dimension p .
tuneSigma2	Starting value of the tuning parameter for sampling $\sigma_k^2, k=1,\ldots,p$. Defaults at a vector of \$p\$ ones. It could be of dimension p .
tuneCbeta	Starting value of the tuning parameter for sampling c_{β} . Defaults at 100.
tuneAlpha	Starting value of the tuning parameter for sampling regression coefficients of the variance models $\alpha_k, k=1,\ldots,p$. Defaults at a vector of 5s. It could be of dimension Lp
tuneSigma2R	Starting value of the tuning parameter for sampling σ^2 . Defaults at 1.
tuneR	Starting value of the tuning parameter for sampling correlation matrices. Defaults at $40*(p+2)^3$. Can be of dimension 1 or M is the number of unique observation time points.
tuneCpsi	Starting value of the tuning parameter for sampling variances c_{ψ}^2 . Defaults at 5. Can be of dimension 1 or p^2 .
tuneCbCor	Starting value of the tuning parameter for sampling c_{η}^2 . Defaults at 10.
tuneOmega	Starting value of the tuning parameter for sampling regression coefficients of the variance models ω . Defaults at 5.
tuneComega	Starting value of the tuning parameter for sampling c_{ω} . Defaults at 1.
tau	The tau of the shadow prior. Defaults at 0.01.
FT	Binary indicator. If set equal to 1, the Fisher's z transform of the correlations is modelled, otherwise if set equal to 0, the untransformed correlations are modelled.
	Other options that will be ignored.

Details

Function 1mrm returns samples from the posterior distributions of the parameters of a regression model with normally distributed multivariate longitudinal responses. To describe the model, let $Y_{ij} = (Y_{ij1}, \ldots, Y_{ijp})^{\top}$ denote the vector of p responses observed on individual $i, i = 1, \ldots, n$, at time point $t_{ij}, j = 1, \ldots, n_i$. The observational time points t_{ij} are allowed to be unequally spaced. Further, let u_{ij} denote the covariate vector that is observed along with Y_{ij} and that may include time, other time-dependent covariates and time-independent ones. In addition, let $Y_i = (Y_{i1}^{\top}, \ldots, Y_{in_i}^{\top})^{\top}$ denote the ith response vector. With $\mu_i = E(Y_i)$ and $\Sigma_i = \text{cov}(Y_i)$, the model assumes multivariate normality, $Y_i \sim N(\mu_i, \Sigma_i), i = 1, 2, \ldots, n$. The means μ_i and covariance matrices Σ_i are modelled semiparametrically in terms of covariates. For the means one can specify semiparametric models,

$$\mu_{ijk} = \beta_{k0} + \sum_{l=1}^{K_1} u_{ijl} \beta_{kl} + \sum_{l=K_1+1}^{K} f_{\mu,k,l}(u_{ijl}).$$

This is the first of the 5 regression submodels.

To model the covariance matrix, first consider the modified Cholesky decomposition, $L_i \Sigma_i L_i^{\top} = D_i$, where L_i is a unit block lower triangular matrix and D_i is a block diagonal matrix,

$$L_{i} = \begin{bmatrix} I & 0 & \dots & 0 \\ -\Phi_{i21} & I & \dots & 0 \\ \vdots & \vdots & \ddots & \vdots \\ -\Phi_{in_{i}1} & -\Phi_{in_{i}1} & \dots & I \end{bmatrix}, \quad D_{i} = \begin{bmatrix} D_{1} & 0 & \dots & 0 \\ 0 & D_{2} & 0 & 0 \\ \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & 0 & D_{n_{i}} \end{bmatrix},$$

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For modelling D_{ij} , $i=1,\ldots,n,j=1,\ldots,n_i$ in terms of covariates, first we separate the variances and the correlations $D_{ij}=S_{ij}^{1/2}R_{ij}S_{ij}^{1/2}$. It is easy to model matrix S_{ij} in terms of covariates as the only requirement on its diagonal elements is that they are nonnegative,

$$\log \sigma_{ijk}^2 = \alpha_{k0} + \sum_{l=1}^{L_1} w_{ijl} \alpha_{kl} + \sum_{l=L_1+1}^{L} f_{\sigma,k,l}(w_{ijl})$$

This is the second of the 5 regression submodels.

For ϕ_{ijklm} , the (l,m) element of Φ_{ijk} , $l,m=1,\ldots,p$, one can specify semiparametric models

$$\phi_{ijklm} = \psi_{lm0} + \sum_{b=1}^{B_1} v_{ijkb} \psi_{lmb} + \sum_{b=B_1+1}^{B} f_{\phi,l,m,b}(v_{ijkb})$$

This is the third of the 5 regression submodels.

The elements of the correlations matrices R_{ij} are modelled in terms of covariate time only, hence they are denoted by R_t . Subject to the positive definiteness constraint, the elements of R_t are modelled using a normal distribution with location and scale parameters, μ_{ct} and σ_{ct}^2 , modelled as

$$\mu_{ct} = \eta_0 + f_{\mu}(t),$$

$$\log \sigma_{ct}^2 = \omega_0 + f_{\sigma}(t),$$

and these are the last 2 of the 5 submodels.

Value

Function 1mrm returns samples from the posteriors of the model parameters.

Author(s)

Georgios Papageorgiou <gpapageo@gmail.com>

References

Papageorgiou, G. (2020). Bayesian semiparametric modelling of covariance matrices for multivariate longitudinal data. arXiv:2012.09833.

Examples

```
# Fit a joint mean-covariance model on the simulated dataset simD2
require(ggplot2)
data(simD2)
model <- Y1 | Y2 ~ time | sm(time) | sm(lag) | sm(time) | 1
# the above defines the responses and the regression models on the left and
# right of "~", respectively
# the first model, for the mean, is a linear function of time, this is sufficient as
# the 2 responses have constant mean.
# the second model, for the variances, is a smooth function of time
# the third model, for the dependence structure, is a smooth function of lag,
# that lmrm figures out and it does not need to be computed by the user</pre>
```

mvrm

Bayesian semiparametric analysis of multivariate continuous responses, with variable selection

Description

Implements an MCMC algorithm for posterior sampling based on a semiparametric model for continuous multivariate responses and additive models for the mean and variance functions. The model utilizes spike-slab priors for variable selection and regularization. See 'Details' section for a full description of the model.

Usage

```
mvrm(formula, distribution = "normal", data = list(), centre = TRUE, sweeps,
burn = 0, thin = 1, seed, StorageDir, c.betaPrior = "IG(0.5, 0.5 * n * p)",
pi.muPrior = "Beta(1, 1)", c.alphaPrior = "IG(1.1, 1.1)", sigmaPrior = "HN(2)",
pi.sigmaPrior = "Beta(1, 1)", c.psiPrior = "HN(1)", phiPrior = "HN(2)",
pi.omegaPrior = "Beta(1, 1)", mu.RPrior = "N(0, 1)", sigma.RPrior = "HN(1)",
corr.Model = c("common", nClust = 1), DP.concPrior = "Gamma(5, 2)",
tuneCbeta, tuneCalpha, tuneAlpha, tuneSigma2, tuneCpsi, tunePsi,
tunePhi, tuneR, tuneSigma2R, tuneHar, tau, FT = 1, compDeviance = FALSE, ...)
```

Arguments

formula	a formula defining the responses and the covariates in the mean and variance models e.g. y1 y2 \sim x z or for smooth effects y1 y2 \sim sm(x) sm(z). The package uses the extended formula notation, where the responses are defined on the left of \sim and the mean and variance models on the right.
distribution	The distribution for the response variables. Currently two options are supported: "normal" and "t".
data	a data frame.
centre	Binary indicator. If set equal to TRUE, the design matrices are centred, to have column mean equl to zero, otherwise, if set to FALSE, the columns are not centred.
sweeps	total number of posterior samples, including those discarded in burn-in period (see argument burn) and those discarded by the thinning process (see argument thin).

burn length of burn-in period. thin thinning parameter. seed optional seed for the random generator. StorageDir a required directory to store files with the posterior samples of models parame-The inverse Gamma prior of c_{β} . The default is "IG(0.5,0.5*n*p)", that is, an inc.betaPrior verse Gamma with parameters 1/2 and np/2, where n is the number of sampling units and p is the length of the response vector. pi.muPrior The Beta prior of π_{μ} . The default is "Beta(1,1)". It can be of dimension 1, of dimension K (the number of effects that enter the mean model), or of dimension pKc.alphaPrior The prior of c_{α} . The default is "IG(1.1,1.1)". Half-normal priors for $\sqrt{c_{\alpha}}$ are also available, declared using "HN(a)", where "a" is a positive number. It can be of dimension 1 or p (the length of the multivariate response). The prior of σ . The default is "HN(2)", a half-normal prior for σ with variance sigmaPrior equal to two, $\sigma \sim N(0,2)I[\sigma > 0]$. Inverse Gamma priors for σ^2 are also available, declared using "IG(a,b)". It can be of dimension 1 or p (the length of the multivariate response). pi.sigmaPrior The Beta prior of π_{σ} . The default is "Beta(1,1)". It can be of dimension 1, of dimension Q (the number of effects that enter the variance model), or of dimension pQc.psiPrior The prior of c_{ψ} . The default is half-normal for $\sqrt{c_{\psi}}$, declared using "HN(a)", where "a" is a positive number. The default value for "a" is one. Inverse-gamma priors are also available and they can be declared using "IG(a,b)", where "a" and "b" are positive constants. The prior can be of dimension 1 or p (the length of the multivariate response). The prior of $varphi^2$. The default is half-normal for varphi, declared usphiPrior ing "HN(a)", where "a" is a positive number. The default value for "a" is two. Inverse-gamma priors are also available and they can be declared using "IG(a,b)", where "a" and "b" are positive constants. The prior can be of dimension 1 or p (the length of the multivariate response). pi.omegaPrior The Beta prior of π_{ω} . The default is "Beta(1,1)". It can be of dimension 1, of dimension B (the number of effects that enter the shape parameter model), or of dimension pBmu.RPrior The normal prior for μ_R . The default is the standard normal distribution. sigma.RPrior The half normal prior for σ_R . The default is the half normal distribution with variance one. corr.Model Specifies the model for the correlation matrix R. The three choices supported are "common", that specifies a common correlations model, "groupC", that specifies

a grouped correlations model, and "groupV", that specifies a grouped variables model. When the model chosen is either "groupC" or "groupV", the upper limit on the number of clusters can also be specified, using corr.Model = c("groupC", nClust = d) or corr.Model = c("groupV", nClust = p). If the number of clusters is left unspecified, for the "groupV" model, it is taken to be p, the number of responses. For the "groupC" model, it is taken to be d = p(p-1)/2, the number

of free elements in the correlation matrix.

DP.concPrior The Gamma prior for the Dirichlet process concentration parameter. tuneCbeta Starting value of the tuning parameter for sampling c_{β} . Defaults at 20. tuneCalpha Starting value of the tuning parameter for sampling c_{α} . Defaults at 1. tuneAlpha Starting value of the tuning parameter for sampling regression coefficients of the variance model α . Defaults at 5. tuneSigma2 Starting value of the tuning parameter for sampling variances σ_i^2 . Defaults at 1. tuneCpsi Starting value of the tuning parameter for sampling c_{ψ} . Defaults at 1. tunePsi Starting value of the tuning parameter for sampling ψ . Defaults at 5. tunePhi Starting value of the tuning parameter for sampling φ . Defaults at 0.5. tuneR Starting value of the tuning parameter for sampling correlation matrices. Defaults at $40 * (p + 2)^3$. Starting value of the tuning parameter for sampling σ_R^2 . Defaults at 1. tuneSigma2R Starting value of the tuning parameter for sampling the regression coefficients tuneHar of the harmonics. Defaults at 100. The tau of the shadow prior. Defaults at 0.01. tau Binary indicator. If set equal to 1, the Fisher's z transform of the correlations is FΤ modelled, otherwise if set equal to 0, the untransformed correlations are modelled.

Details

compDeviance

Function mvrm returns samples from the posterior distributions of the parameters of a regression model with normally distributed multivariate responses and mean and variance functions modeled in terms of covariates. For instance, in the presence of two responses (y_1, y_2) and two covariates in the mean model (u_1, u_2) and two in the variance model (w_1, w_2) , we may choose to fit

Binary indicator. If set equal to 1, the deviance is computed.

$$\mu_u = \beta_0 + \beta_1 u_1 + f_{\mu}(u_2),$$

 $\log(\sigma_W^2) = \alpha_0 + \alpha_1 w_1 + f_{\sigma}(w_2),$

parametrically modelling the effects of u_1 and w_1 and non-parametrically modelling the effects of u_2 and w_2 . Smooth functions, such as f_{μ} and f_{σ} , are represented by basis function expansion,

$$f_{\mu}(u_2) = \sum_{j} \beta_j \phi_j(u_2),$$

$$f_{\sigma}(w_2) = \sum_j \alpha_j \phi_j(w_2),$$

where ϕ are the basis functions and β and α are regression coefficients.

Other options that will be ignored.

The variance model can equivalently be expressed as

$$\sigma_W^2 = \exp(\alpha_0) \exp(\alpha_1 w_1 + f_\sigma(w_2)) = \sigma^2 \exp(\alpha_1 w_1 + f_\sigma(w_2)),$$

where $\sigma^2 = \exp(\alpha_0)$. This is the parameterization that we adopt in this implementation.

Positive prior probability that the regression coefficients in the mean model are exactly zero is achieved by defining binary variables γ that take value $\gamma=1$ if the associated coefficient $\beta\neq 0$ and $\gamma=0$ if $\beta=0$. Indicators δ that take value $\delta=1$ if the associated coefficient $\alpha\neq 0$ and $\delta=0$ if $\alpha=0$ for the variance function are defined analogously. We note that all coefficients in the mean and variance functions are subject to selection except the intercepts, β_0 and α_0 .

Prior specification:

For the vector of non-zero regression coefficients β_{γ} we specify a g-prior

$$\beta_{\gamma}|c_{\beta}, \sigma^2, \gamma, \alpha, \delta \sim N(0, c_{\beta}\sigma^2(\tilde{X}_{\gamma}^{\top}\tilde{X}_{\gamma})^{-1}).$$

where \tilde{X} is a scaled version of design matrix X of the mean model.

For the vector of non-zero regression coefficients α_{δ} we specify a normal prior

$$\alpha_{\delta}|c_{\alpha}, \delta \sim N(0, c_{\alpha}I).$$

Independent priors are specified for the indicators variables γ and δ as $P(\gamma=1|\pi_{\mu})=\pi_{\mu}$ and $P(\delta=1|\pi_{\sigma})=\pi_{\sigma}$. Further, Beta priors are specified for π_{μ} and π_{σ}

$$\pi_{\mu} \sim Beta(c_{\mu}, d_{\mu}), \pi_{\sigma} \sim Beta(c_{\sigma}, d_{\sigma}).$$

We note that blocks of regression coefficients associated with distinct covariate effects have their own probability of selection (π_{μ} or π_{σ}) and this probability has its own prior distribution.

Further, we specify inverse Gamma priors for c_{β} and c_{α}

$$c_{\beta} \sim IG(a_{\beta}, b_{\beta}), c_{\alpha} \sim IG(a_{\alpha}, b_{\alpha})$$

For σ^2 we consider inverse Gamma and half-normal priors

$$\sigma^2 \sim IG(a_{\sigma}, b_{\sigma}), |\sigma| \sim N(0, \phi_{\sigma}^2).$$

Lastly, for the elements of the correlation matrix, we specify normal distributions with mean μ_R and variance σ_R^2 , with the priors on these two parameters being normal and half-normal, respectively. This is the common correlations model. Further, the grouped correlations model can be specified. It considers a mixture of normal distributions for the means μ_R . The grouped correlations model can also be specified. It clusters the variables instead of the correlations.

Value

Function mvrm returns the following:

call the matched call. formula model formula.

seed the seed that was used (in case replication of the results is needed).

data the dataset

X the mean model design matrix.
Z the variance model design matrix.

LG	the length of the vector of indicators	γ.
LD	the length of the vector of indicators	δ .

mcpar the MCMC parameters: length of burn in period, total number of samples, thin-

ning period.

nSamples total number of posterior samples

DIR the storage directory

deviance.txt

Further, function mvrm creates files where the posterior samples are written. These files are (with all file names preceded by 'BNSP.'):

alpha.txt	contains samples from the posterior of vector α . Rows represent posterior samples and columns represent the regression coefficient, and they are in the same order as the columns of design matrix Z .
beta.txt	contains samples from the posterior of vector β . Rows represent posterior samples and columns represent the regression coefficients, and they are in the same order as the columns of design matrix X .
gamma.txt	contains samples from the posterior of the vector of the indicators γ . Rows represent posterior samples and columns represent the indicator variables, and they are in the same order as the columns of design matrix X .
delta.txt	contains samples from the posterior of the vector of the indicators δ . Rows represent posterior samples and columns represent the indicator variables, and they are in the same order as the columns of design matrix Z .
sigma2.txt	contains samples from the posterior of the error variance σ^2 of each response.
cbeta.txt	contains samples from the posterior of c_{β} .
calpha.txt	contains samples from the posterior of c_{α} .
R.txt	contains samples from the posterior of the correlation matrix R .
theta.txt	contains samples from the posterior of θ of the shadow prior (probably not needed).
muR.txt	contains samples from the posterior of μ_R .
sigma2R.txt	contains samples from the posterior of σ_R^2 .

In addition to the above, for models that cluster the correlations we have

values of the parameters.

compAlloc.txt	The cluster at which the correlations were allocated, λ_{kl} . These are integers from zero to the specified number of clusters minus one.	
nmembers.txt	The numbers of correlations assigned to each cluster.	
DPconc.txt	Contains samples from the posterior of the Dirichlet process concentration parameter.	

contains the deviance, minus twice the log likelihood evaluated at the sampled

In addition to the above, for models that cluster the variables we have

compAllocV.txt The cluster at which the variables were allocated, λ_k . These are integers from zero to the specified number of clusters minus one.

nmembersV.txt The numbers of variables assigned to each cluster.

Author(s)

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References

Papageorgiou, G. and Marshall, B.C. (2019). Bayesian semiparametric analysis of multivariate continuous responses, with variable selection. arXiv.

Papageorgiou, G. (2018). BNSP: an R Package for fitting Bayesian semiparametric regression models and variable selection. The R Journal, 10(2):526-548.

Chan, D., Kohn, R., Nott, D., & Kirby, C. (2006). Locally adaptive semiparametric estimation of the mean and variance functions in regression models. Journal of Computational and Graphical Statistics, 15(4), 915-936.

Examples

```
# Fit a mean/variance regression model on the cps71 dataset from package np.
#This is a univariate response model
require(np)
require(ggplot2)
data(cps71)
model \leftarrow logwage \sim sm(age,k=30,bs="rd") \mid sm(age,k=30,bs="rd")
## Not run: m1 <- mvrm(formula=model,data=cps71,sweeps=10000,burn=5000,thin=2, seed=1,StorageDir=DIR)
#Print information and summarize the model
print(m1)
summary(m1)
#Summarize and plot one parameter of interest
alpha<-mvrm2mcmc(m1,"alpha")</pre>
summary(alpha)
plot(alpha)
#Obtain a plot of a term in the mean model
wagePlotOptions<-list(geom_point(data=cps71,aes(x=age,y=logwage)))</pre>
plot(x=m1,model="mean",term="sm(age)",plotOptions=wagePlotOptions)
plot(m1)
#Obtain predictions for new values of the predictor "age"
predict(m1,data.frame(age=c(21,65)),interval="credible")
# Fit a bivariate mean/variance model on the marks dataset from package ggm
# two responses: marks mechanics and vectors, and one covariate: marks on algebra
model2 <- mechanics | vectors ~ sm(algebra,k=5) | sm(algebra,k=3)</pre>
m2 <- mvrm(formula=model2, data=marks, sweeps = 100000, burn = 50000,
                        thin = 2, seed = 1, StorageDir = DIR)
plot(m2)
## End(Not run)
```

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mvrm2mcmc	Convert posterior samples from function mvrm into an object of class 'mcmc'

Description

Reads in files where the posterior samples were written and creates an object of class 'mcmc' so that functions like summary and plot from package coda can be used

Usage

```
mvrm2mcmc(mvrmObj, labels)
```

Arguments

mvrm0bj An object of class 'mvrm' as created by a call to function mvrm.

labels The labels of the files to be read in. These can be one or more of: "alpha",

"beta", "gamma", "delta", "sigma2", "cbeta", "calpha", "R", "muR", "sigma2R", "nmembers", "nmembersV", "compAlloc", "compAllocV", and "DPconc" and they correspond to the parameters of the model that a call to functions mvrm fits. In addition, "deviance" can be read in. If left unspecified, all files are read in.

Value

An object of class 'mcmc' that holds the samples from the posterior of the selected parameter.

Author(s)

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See Also

mvrm

Examples

```
#see \code{mvrm} example
```

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plot.mvrm	Creates plots of terms in the mean and/or variance models

Description

This function plots estimated terms that appear in the mean and variance models.

Usage

```
## S3 method for class 'mvrm' plot(x, model, term, response, response2, intercept = TRUE, grid = 30, centre = mean, quantiles = c(0.1, 0.9), contour = TRUE, static = TRUE, centreEffects = FALSE, plotOptions = list(), nrow, ask = FALSE, plotEmptyCluster = FALSE, combine = FALSE, ...)
```

Arguments

x	an object of class 'mvrm' as generated by function mvrm.
model	one of "mean", "stdev", or "both", specifying which model to be visualized.
term	the term in the selected model to be plotted.
response	integer number denoting the response variable to be plotted (in case there is more than one).
response2	only relevant for multivariate longitudinal data.
intercept	specifies if an intercept should be included in the calculations.
grid	the length of the grid on which the term will be evaluated.
centre	a description of how the centre of the posterior should be measured. Usually mean or median.
quantiles	the quantiles to be used when plotting credible regions. Plots without credible intervals may be obtained by setting this argument to NULL.
contour	relevant for 3D plots only. If contour=TRUE then plot.mvrm creates contour plots. contour=FALSE is allowed only for creating one plot at a time. The plot can be static or dynamic. See argument 'static'.
static	relevant for 3D plots only. If static=TRUE then plot.mvrm calls function ribbon3D from package plot3D to create the plot. If static=FALSE then plot.mvrm calls function scatterplot3js from package threejs to create the plot.
centreEffects	if TRUE then the effects in the mean functions are centred around zero over the range of the predictor while the effects in the variance function are scaled around one.
plotOptions	for plots of univariate smooth terms or for plots of bivariate smooth terms where one of the two covariates is discrete, this is a list of plot elements to give to ggplot. For smooths of bivariate continuous covariates, this is a list of plot elements to give to ribbon3D (if static=FALSE) or to scatterplot3js (if

static=TRUE).

plotCorr 27

nrow the number of rows in the figure with the plots.

ask if set to TRUE, plots will be displayed one at a time.

plotEmptyCluster

if set to TRUE, plots of empty clusters will be displayed. Relevant for multivari-

ate longitudinal datasets.

combine Binary indicator. It can be set to TRUE to simultaneously plot two terms. One of

the terms must be continuous and the other must be discrete. This makes sense to set to TRUE when wanting to visualize groups that have a common slope.

... other arguments.

Details

Use this function to obtain predictions.

Value

Predictions along with credible/pediction intervals

Author(s)

Georgios Papageorgiou <gpapageo@gmail.com>

See Also

mvrm

Examples

```
#see \code{mvrm} example
```

plotCorr

Creates plots of the correlation matrices

Description

This function plots the posterior mean and credible intervals of the elements of correlation matrices.

Usage

```
plotCorr(x, term = "R", centre = mean, quantiles = c(0.1, 0.9), ...)
```

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Arguments

x an object of class 'mvrm' as generated by function mvrm.

term R or muR,

centre a description of how the centre of the posterior should be measured. Usually

mean or median.

quantiles the quantiles to be used when plotting credible regions. Plots without credible

intervals may be obtained by setting this argument to NULL.

... other arguments.

Details

Use this function to visualize the elements of a correlation matrix.

Value

Posterior means and credible intervals of elements of correlation matrices.

Author(s)

Georgios Papageorgiou <gpapageo@gmail.com>

See Also

mvrm

Examples

```
#see \code{mvrm} example
```

predict.mvrm

Model predictions

Description

Provides predictions and posterior credible/prediction intervals for given feature vectors.

Usage

predict.mvrm 29

Arguments

object an object of class "mvrm", usually a result of a call to mvrm.

newdata data frame of feature vectors to obtain predictions for. If newdata is missing,

the function will use the feature vectors in the data frame used to fit the mvrm

object.

interval type of interval calculation.

level tolerance level.

nSamples number of samples to obtain from the posterior predictive distribution (for each

sweep of the MCMC). Only relevant for "prediction intervals".

ind.preds Binary indicator. If set to TRUE the function returns additionally the predictions

per individual MCMC sample.

... other arguments.

Details

The function returns predictions of new responses or the means of the responses for given feature vectors. Predictions for new responses or the means of new responses are the same. However, the two differ in the associated level of uncertainty: response predictions are associated with wider (prediction) intervals than mean response predictions. To obtain prediction intervals (for new responses) the function samples from the normal distributions with means and variances as sampled during the MCMC run.

Value

Predictions for given covariate/feature vectors.

Author(s)

Georgios Papageorgiou <gpapageo@gmail.com>

See Also

mvrm

Examples

#see \code{mvrm} example

30 print.mvrm

print.mvrm

Prints an mvrm fit

Description

Provides basic information from an myrm fit.

Usage

```
## S3 method for class 'mvrm'
print(x, digits = 5, ...)
```

Arguments

```
x an object of class "mvrm", usually a result of a call to mvrm.digits the number of significant digits to use when printing.other arguments.
```

Details

The function prints information about mvrm fits.

Value

The function provides a matched call, the number of posterior samples obtained and marginal inclusion probabilities of the terms in the mean and variance models.

Author(s)

Georgios Papageorgiou <gpapageo@gmail.com>

See Also

mvrm

Examples

```
#see \code{mvrm} example
```

s 31

mgcv constructor s

Description

Provides interface between mgcv::s and BNSP.s(...) calls mgcv::smoothCon(mgcv::s(...),...

Usage

s

```
s(..., data, knots = NULL, absorb.cons = FALSE, scale.penalty = TRUE, n = nrow(data), dataX = NULL, null.space.penalty = FALSE, sparse.cons = 0, diagonal.penalty = FALSE, apply.by = TRUE, modCon = 0, k = -1, fx = FALSE, bs = "tp", m = NA, by = NA, xt = NULL, id = NULL, sp = NULL, pc = NULL)
```

Arguments

```
a list of variables. See mgcv::s
. . .
data
                 see mgcv::smoothCon
knots
                 see mgcv::knots
absorb.cons
                 see mgcv::smoothCon
scale.penalty
                 see mgcv::smoothCon
                 see mgcv::smoothCon
n
dataX
                 see mgcv::smoothCon
null.space.penalty
                 see mgcv::smoothCon
sparse.cons
                 see mgcv::smoothCon
diagonal.penalty
                 see mgcv::smoothCon
apply.by
                 see mgcv::smoothCon
modCon
                 see mgcv::smoothCon
k
                 see mgcv::s
fx
                 see mgcv::s
bs
                 see mgcv::s
                 see mgcv::s
m
by
                 see mgcv::s
хt
                 see mgcv::s
id
                 see mgcv::s
                 see mgcv::s
sp
                 see mgcv::s
рс
```

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Details

The most relevant arguments for BNSP users are the list of variables ..., knots, absorb.cons, bs, and by.

Value

A design matrix that specifies a smooth term in a model.

Author(s)

Georgios Papageorgiou <gpapageo@gmail.com>

simD

Simulated dataset

Description

Just a simulated dataset to illustrate the DO mixture model. The success probability and the covariate have a non-linear relationship.

Usage

data(simD)

Format

A data frame with 300 independent observations. Three numerical vectors contain information on

- Y number of successes.
- E number of trials.
- X explanatory variable.

simD2

Simulated dataset

Description

A simulated dataset to illustrate the multivariate longitudinal model. It consists of a bivariate vector of responses observed over 6 time points.

Usage

data(simD2)

sinusoid 33

Format

A data frame that includes observations on 50 sampling units. The data frame has 300 rows for the 50 sampling units observed over 6 time points. It has 4 columns

Y1 first response.

Y2 second response.

time the time of observation.

id unique sampling unit identifier.

sinusoid

Sinusoid terms in mvrm formulae

Description

Function used to define sinusoidal curves in the mean formula of function mvrm. The function is used internally to construct design matrices.

Usage

```
sinusoid(..., harmonics = 1, amplitude = 1, period = 1, knots = NULL)
```

Arguments

... a single covariate that the sinusoid term is a function of.

harmonics an integer value that denotes the number of sins and cosines to be utilized in the

representation of a sinusoidal curve.

amplitude a positive integer. If set equal to one, it denotes a fixed amplitude. Otherwise,

if set to an integer that is greater than one, it denotes the number of knots to be

utilized in the representation of the time-varying amplitude.

period the period of the sinusoidal wave.

knots the knots to be utilized in the representation of the time-varying amplitude. Rel-

evant only when amplitude is greater than 1.

Details

Use this function within calls to function mvrm to specify sinusoidal waves in the mean function of a regression model.

Consider the sinusoidal curve

$$y_t = \beta_0 + A(t)\sin(2\pi t/\omega + \varphi) + \epsilon_t,$$

where y_t is the response at time t, β_0 is an intercept term, A(t) is a time-varying amplitude, $\varphi \in [0, 2\pi]$ is the phase shift parameter, ω is the period taken to be known, and ϵ_t is the error term.

The period ω is defined by the argument period.

34 sinusoid

The time-varying amplitude is represented using $A(t) = \sum_{j=1}^K \beta_{Aj} \phi_{Aj}(t)$, where K, the number of knots, is defined by argument amplitude. If amplitude = 1, then the amplitude is taken to be fixed: A(t) = A.

Further, $\sin(2\pi t/\omega + \varphi)$ is represented utilizing $\sin(2\pi t/\omega + \varphi) = \sum_{k=1}^{L} a_k \sin(2k\pi t/\omega) + b_k \cos(2k\pi t/\omega)$, where L, the number of harmonics, is defined by argument harmonics.

Value

Specifies the design matrices of an mvrm call

Author(s)

Georgios Papageorgiou <gpapageo@gmail.com>

See Also

mvrm

Examples

```
# Simulate and fit a sinusoidal curve
# First load releveant packages
require(BNSP)
require(ggplot2)
require(gridExtra)
require(Formula)
# Simulate the data
mu \leftarrow function(u)\{cos(0.5*u)*sin(2 * pi * u + 1)\}
set.seed(1)
n <- 100
u <- sort(runif(n,min=0,max=2*pi))</pre>
y \leftarrow rnorm(n, mu(u), 0.1)
data <- data.frame(y, u)</pre>
# Define the model and call function \code{mvrm} that perfomes posterior sampling for the given
# dataset and defined model
model \leftarrow y \sim sinusoid(u, harmonics = 2, amplitude = 20, period = 1)
m1 <- mvrm(formula = model, data = data, sweeps = 10000, burn = 5000, thin = 2, seed = 1,
            StorageDir = getwd())
# Plot
x1 \leftarrow seq(min(u), max(u), length.out = 100)
plotOptionsM <- list(geom_line(aes_string(x = x1, y = mu(x1)), col = 2, alpha = 0.5, lty = 2),</pre>
                      geom_point(data = data, aes(x = u, y = y)))
plot(x = m1, term = 1, plotOptions = plotOptionsM, intercept = TRUE,
     quantiles = c(0.005, 0.995), grid = 100, combine = 100)
## End(Not run)
```

sm 35

Smooth terms in mvrm formulae

Description

Function used to define smooth effects in the mean and variance formulae of function mvrm. The function is used internally to construct the design matrices.

Usage

$$sm(..., k = 10, knots = NULL, bs = "rd")$$

Arguments

one or two covariates that the smooth term is a function of. If two covariates are used, they may be both continuous or one continuous and one discrete. Discrete

variables should be defined as factor in the data argument of the calling mvrm

function.

k the number of knots to be utilized in the basis function expansion.

knots the knots to be utilized in the basis function expansion.

bs a two letter character indicating the basis functions to be used. Currently, the

options are "rd" that specifies radial basis functions and is available for univariate and bivariate smooths, and "pl" that specifies thin plate splines that are

available for univariate smooths.

Details

Use this function within calls to function mvrm to specify smooth terms in the mean and/or variance function of the regression model.

Univariate radial basis functions with q basis functions or q-1 knots are defined by

$$\mathcal{B}_1 = \left\{ \phi_1(u) = u, \phi_2(u) = ||u - \xi_1||^2 \log \left(||u - \xi_1||^2 \right), \dots, \phi_q(u) = ||u - \xi_{q-1}||^2 \log \left(||u - \xi_{q-1}||^2 \right) \right\},$$

where ||u|| denotes the Euclidean norm of u and ξ_1, \ldots, ξ_{q-1} are the knots that are chosen as the quantiles of the observed values of explanatory variable u, with $\xi_1 = \min(u_i), \xi_{q-1} = \max(u_i)$ and the remaining knots chosen as equally spaced quantiles between ξ_1 and ξ_{q-1} .

Thin plate splines are defined by

$$\mathcal{B}_2 = \{\phi_1(u) = u, \phi_2(u) = (u - \xi_1)_+, \dots, \phi_q(u) = (u - \xi_q)_+\},\$$

where $(a)_{+} = \max(a, 0)$.

Radial basis functions for bivariate smooths are defined by

$$\mathcal{B}_3 = \left\{ u_1, u_2, \phi_3(u) = ||u - \xi_1||^2 \log \left(||u - \xi_1||^2 \right), \dots, \phi_q(u) = ||u - \xi_{q-1}||^2 \log \left(||u - \xi_{q-1}||^2 \right) \right\}.$$

Value

Specifies the design matrices of an mvrm call

sm

36 summary.mvrm

Author(s)

Georgios Papageorgiou <gpapageo@gmail.com>

See Also

mvrm

Examples

```
#see \code{mvrm} example
```

summary.mvrm

Summary of an mvrm fit

Description

Provides basic information from an mvrm fit.

Usage

```
## S3 method for class 'mvrm'
summary(object, nModels = 5, digits = 5, printTuning = FALSE, ...)
```

Arguments

object an object of class "mvrm", usually a result of a call to mvrm.

nModels integer number of models with the highest posterior probability to be displayed.

digits the number of significant digits to use when printing.

printTuning if set to TRUE, the starting and finishig values of the tuninf parameters are dis-

played.

... other arguments.

Details

Use this function to summarize myrm fits.

Value

The functions provides a detailed description of the specified model and priors. In addition, the function provides information about the Markov chain ran (length, burn-in, thinning) and the folder where the files with posterior samples are stored. Lastly, the function provides the mean posterior and null deviance and the mean/variance models visited most often during posterior sampling.

Author(s)

Georgios Papageorgiou <gpapageo@gmail.com>

te 37

See Also

mvrm

Examples

```
#see \code{mvrm} example
```

te

mgcv constructor te

Description

Provides interface between mgcv::te and BNSP. te(...) calls mgcv::smoothCon(mgcv::te(...),...

Usage

```
te(..., data, knots = NULL, absorb.cons = FALSE, scale.penalty = TRUE, n = nrow(data), dataX = NULL, null.space.penalty = FALSE, sparse.cons = 0, diagonal.penalty = FALSE, apply.by = TRUE, modCon = 0, k = NA, bs = "cr", m = NA, d = NA, by = NA, fx = FALSE, np = TRUE, xt = NULL, id = NULL, sp = NULL, pc = NULL)
```

Arguments

```
a list of variables. See mgcv::te
. . .
                 see mgcv::smoothCon
data
                 see mgcv::knots
knots
absorb.cons
                 see mgcv::smoothCon
scale.penalty
                 see mgcv::smoothCon
                 see mgcv::smoothCon
dataX
                 see mgcv::smoothCon
null.space.penalty
                 see mgcv::smoothCon
sparse.cons
                 see mgcv::smoothCon
diagonal.penalty
                 see mgcv::smoothCon
apply.by
                 see mgcv::smoothCon
modCon
                 see mgcv::smoothCon
k
                 see mgcv::te
bs
                 see mgcv::te
                 see mgcv::te
m
d
                 see mgcv::te
```

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by	see mgcv::te
fx	see mgcv::te
np	see mgcv::te
xt	see mgcv::te
id	see mgcv::te
sp	see mgcv::te
рс	see mgcv::te

Details

The most relevant arguments for BNSP users are the list of variables \dots , knots, absorb.cons, bs, and by.

Value

A design matrix that specifies a smooth term in a model.

Author(s)

Georgios Papageorgiou <gpapageo@gmail.com>

ti mgcv constructor ti

Description

Provides interface between mgcv::ti and BNSP.ti(...) calls mgcv::smoothCon(mgcv::ti(...),...

Usage

```
ti(..., data, knots = NULL, absorb.cons = FALSE, scale.penalty = TRUE, n = nrow(data), dataX = NULL, null.space.penalty = FALSE, sparse.cons = 0, diagonal.penalty = FALSE, apply.by = TRUE, modCon = 0, k = NA, bs = "cr", m = NA, d = NA, by = NA, fx = FALSE, np = TRUE, xt = NULL, id = NULL, sp = NULL, mc = NULL, pc = NULL)
```

Arguments

```
a list of variables. See mgcv::ti
data see mgcv::smoothCon
knots see mgcv::knots
absorb.cons see mgcv::smoothCon
scale.penalty see mgcv::smoothCon
n see mgcv::smoothCon
```

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```
dataX
                 see mgcv::smoothCon
null.space.penalty
                 see mgcv::smoothCon
sparse.cons
                  see mgcv::smoothCon
diagonal.penalty
                 see mgcv::smoothCon
apply.by
                 see mgcv::smoothCon
modCon
                 see mgcv::smoothCon
k
                 see mgcv::ti
                 see mgcv::ti
bs
                 see mgcv::ti
m
d
                 see mgcv::ti
                 see mgcv::ti
by
                 see mgcv::ti
fx
np
                 see mgcv::ti
                 see mgcv::ti
хt
                 see mgcv::ti
id
                 see mgcv::ti
sp
                 see mgcv::ti
\mathsf{mc}
                  see mgcv::ti
рс
```

Details

The most relevant arguments for BNSP users are the list of variables \dots , knots, absorb.cons, bs, and by.

Value

A design matrix that specifies a smooth term in a model.

Author(s)

Georgios Papageorgiou <gpapageo@gmail.com>

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