# Package 'DivE'

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<b>Description</b> Contains functions for the 'DivE' estimator <a href="https://doi.org/10.1371/journal.pcbi.1003646">doi:10.1371/journal.pcbi.1003646</a> . The 'DivE' estimator is a heuristic approach to estimate the number of classes or the number of species (species richness) in a population.
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R topics documented:
DivE-package
Bact1
CombDM
Curvature
DiveMaster
DivSampleNum         11           DivSubsamples         13
FitSingleMod
ModelSet
ParamRanges
ParamSeeds
PopDiversity
ScoreSingleMod
Index 23

2 DivE-package

DivE-package

Diversity Estimator

## **Description**

R-package *DivE* contains functions for the DivE estimator (Laydon, D.J. *et al.*, Quantification of HTLV-1 clonality and TCR diversity, PLOS Comput. Biol. 2014). The *DivE* estimator is a heuristic approach to estimate the number of classes or the number of species (species richness) in a population.

*DivE* fits many mathematical models to multiple nested subsamples of individual-based rarefaction curves. These curves depict the expected number of species as a function of the number of individuals (e.g. T cells, virions, microbes). Each model is fitted to all nested subsamples, producing multiple model fits. Novel criteria are used to score each model in how consistently its fits reproduce the full observed rarefaction curve from the nested subsamples, i.e. from only incomplete data. The best performing models are extrapolated to a desired population size, and their estimates are aggregated to estimate the number of classes in the population.

The package contains:

- 1. functions to generate individual-based rarefaction (species-accumulation) data, and evaluate their curvature
- 2. functions to fit mathematical models to rarefaction data and nested subsamples thereof. These functions make extensive use of the R-package *FME* (http://cran.r-project.org/web/packages/FME/index.html)
- 3. functions to evaluate novel criteria for each model. These functions make use of the R-package *rgeos* (http://cran.r-project.org/web/packages/rgeos/index.html)
- 4. functions to score competing models
- 5. a function to produce final estimates of the number of classes (diversity)
- 6. example candidate models, fitted parameters, parameter ranges, and an example data set
- 7. an example script. We have attempted to make the code flexible to users who require varying levels of detail and control. The simplest way to use the package is the DiveMaster function. This function is a wrapper around other functions provided with the *DivE* package and will create subsamples (function DivSubsamples), fit models (function FitSingleMod), score models (function ScoreSingleMod) and produce final diversity/species richness estimates (function PopDiversity).

The novel criteria against which each model fit is scored are:

**Discrepancy** – the mean percentage error between data points and model prediction.

**Accuracy** – the percentage error between the full sample species richness, and the estimate of full sample species richness from a given subsample.

**Similarity** – the area between the curve fitted to a subsample and the curve fitted to the full sample, normalized to the area under the curve from the full data, on the interval [0, *Nobs*], where *Nobs* is the size of the full data.

**Plausibility** – the predicted number of species must either increase monotonically or plateau and the predicted rate of species accumulation must either decrease or plateau (i.e. for S(x) and  $x \ge 1$ , where x is the number of individuals,  $S'(x) \ge 0$ , and  $S''(x) \le 0$ ).

The rationale behind each criterion is as follows:

DivE-package 3

Discrepancy – the model must describe the data to which it was fitted.

Accuracy – from a subsample, the model should predict the full sample species richness.

Similarity – an ideal model will produce identical fits from all subsamples. The smaller the area between the model fits, the better the model.

*Plausibility* – this criterion requires that, as the observed number of individuals increases, the observed number of species does not decrease and the rate of species-accumulation does not increase; the former is impossible and the latter is implausible.

# **Population Size**

*DivE* requires an estimate of population size, i.e. the number of individuals in the population for which the number of species is desired. Population size is a necessary input for species richness estimation when it is not appropriate to assume a saturating relationship between population size and species richness.

In spatially homogeneous populations with equiprobable detection of individuals, population size can be estimated through scaling by area or volume e.g. scaling from cells in 50ml of blood to cells in the total blood volume. When population size estimates are unavailable, it is still usually possible to provide meaningful diversity estimates, e.g. the number of species per gram of tissue.

#### Requirements

Many deep sequencing data consist of relative abundance of classes or species. We caution that *DivE* requires data detailing the absolute counts of each class or species: relative abundances are insufficient. Rarefaction curves are highly sensitive to the scaling factor applied to relative abundances. Scaling factors that are too high greatly overestimate the degree of repetition of species in the sample, falsely implying that the sample contains a more comprehensive census, and ultimately affecting the resulting estimates of species richness. Absolute counts can usually be obtained when data are being collected (for further details, please see Laydon, D. *et al.*).

*DivE* requires data where each individual has been sampled randomly, independently and with an equal probability of detection, and where the underlying distribution of individuals is spatially homogeneous. Reliable extrapolation of rarefaction curves is only possible where these conditions are met. DivE is a heuristic estimator designed for use in immunological and microbiological populations, but can be used in any system where the above conditions are satisfied, and for which an estimate of population size is available (for further details, please see Laydon, D. *et al.*).

We have attempted to identify conditions under which DivE is prone to error and should not be applied. When the observed rarefaction curve is linear, the data imply a constant rate of species accumulation, and so provide little information on how quickly the rate of species accumulation will decrease. This is usually indicative of severe under-sampling. We quantified the deviation from linearity of the observed rarefaction curve using the curvature parameter Cp. This parameter can take values between 0 and 1, where 1 reflects perfect saturation and 0 reflects a constant rate of species accumulation. We recommend, based on our simulations, that DivE should not be applied when Cp < 0.1. Low curvatures suggest severe under-sampling and researchers should exercise caution when using any diversity estimator with such data. We have included a function Curvature to evaluate the approximate curvature of the rarefaction curve.

#### **Model Fitting Process**

The pseudo-random model fitting algorithm included with *DivE* (from R package *FME*) requires that parameter ranges and parameter seeding values be inputted. The runtime incurred in model fitting increases with the size of the parameter space. The need for parameter ranges small enough to yield precise parameter estimates in relatively short runtimes must be balanced against the need

4 Bact1

for parameter ranges that adequately encompass appropriate parameter values for data of different scales. We have included parameter ranges and seeding values that have performed well in our analyses, which the user can use or amend as required.

The performance of modFit (package FME) with the pseudorandom parameter search algorithm (package FME, pseudoOptim) used to estimated model parameter values, is sensitive to the choice of initial seeding values. We have provided the fitted parameters returned from our simulations to be used as initial seeding parameters. For each model, each initial parameter guess (i.e. each row of the model matrix in ModelSeeds) is evaluated by to modCost. The parameter guess returning the lowest cost is used as the seeding value in modFit.

To obtain better parameter fits, the fitting process can be repeated. Fitted parameters from a single subsample may provide a better seeding guess for a fit to a subsequent subsample than the initial parameter seeds originally inputted, and thus better final model fits will be produced. In our analyses, two attempts of the fitting process (argument fitloops in DiveMaster) were usually sufficient.

#### Contact

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#### **Details**

Package: DivE Type: Package Version: 1.1

Date: 2019-08-17 License: GPL (>= 2)

The main function is DiveMaster, which combines the four functions DivSampleNum, DivSubsamples, FitSingleMod, and ScoreSingleMod. An example script using both DiveMaster and the four component functions can be found in the *demo* folder in the source.

## Author(s)

Daniel J. Laydon, Aaron Sim, Charles R.M. Bangham, Becca Asquith

## References

Laydon, D. J., Melamed, A., Sim, A., Gillet, N. A., Sim, K., Darko, S., Kroll, S., Douek, D. C., Price, D., Bangham, C. R. M., Asquith, B., Quantification of HTLV-1 clonality and TCR diversity, PLOS Comput. Biol. 2014

Bact1 5

#### **Description**

This gives a fictitious example of a sample of 7814 bacteria comprising of 144 unique species. Designed as a test dataset for the DivE diversity estimation algorithm.

#### Usage

data(Bact1)

#### **Format**

A data frame with 144 observations on the following 2 variables.

Bacteria a factor with levels Acetobacter\_aurantius Acinetobacter\_baumannii Actinomyces\_israelii Agrobacterium\_radiobacter Agrobacterium\_tumefaciens Anaplasma Azorhizobium\_caulinodans Azotobacter\_vinelandii Bacillus\_anthracis Bacillus\_brevis Bacillus\_cereus Bacillus\_fusiformis Bacillus\_licheniformis Bacillus\_megaterium Bacillus\_mycoides Bacillus\_stearothermophilus Bacillus\_subtilis Bacteroides\_fragilis Bacteroides\_gingivalis Bacteroides\_melaninogenicus Bartonella\_henselae Bartonella\_quintana Bordetella\_bronchiseptica Bordetella\_pertussis Borrelia\_burgdorferi Brucella\_abortus Brucella\_melitensis Brucella\_suis Burkholderia\_cepacia Burkholderia\_malleiBurkholderia\_pseudomalleiCalymmatobacterium\_granulomatis Campylobacter\_coli Campylobacter\_fetus Campylobacter\_jejuni Campylobacter\_pylori Chlamydia\_trachomatis Chlamydophila\_pneumoniae Chlamydophila\_psittaci Clostridium\_botulinum Clostridium\_difficile Clostridium\_perfringens Clostridium\_tetani Corynebacterium\_diphtheriae Corynebacterium\_fusiforme Coxiella\_burnetii Ehrlichia\_chaffeensis Enterobacter\_cloacae Enterococcus\_avium Enterococcus\_durans Enterococcus\_faecalis Enterococcus\_faecium Enterococcus\_galllinarum Enterococcus\_maloratus Escherichia coli Francisella tularensis Fusobacterium\_nucleatum Gardnerella\_vaginalis Haemophilus\_ducreyi Haemophilus\_influenzae Haemophilus\_parainfluenzae Haemophilus\_pertussis Haemophilus\_vaginalis Helicobacter\_pylori Klebsiella\_pneumoniae Lactobacillus\_Bulgaricus Lactobacillus\_acidophilus Lactobacillus\_caseiLactococcus\_lactisLegionella\_pneumophilaListeria\_monocytogenes Methanobacterium\_extroquens Microbacterium\_multiforme Micrococcus\_luteus Moraxella\_catarrhalis Mycobacterium Mycobacterium\_avium Mycobacterium\_bovis Mycobacterium\_diphtheriae Mycobacterium\_intracellulare Mycobacterium\_leprae Mycobacterium\_lepraemurium  ${\tt Mycobacterium\_phlei\ Mycobacterium\_smegmatis\ Mycobacterium\_tuberculosis\ Mycoplasma\_fermentans}$ Mycoplasma\_genitalium Mycoplasma\_hominis Mycoplasma\_penetrans Mycoplasma\_pneumoniae Neisseria\_gonorrhoeae Neisseria\_meningitidis Pasteurella\_multocida Pasteurella\_tularensis Peptostreptococcus Porphyromonas\_gingivalis Pseudomonas\_aeruginosa Rhizobium\_radiobacter Rickettsia\_prowazekii Rickettsia\_psittaci Rickettsia\_quintana Rickettsia\_rickettsii Rickettsia\_trachomae Rochalimaea\_Henselae Rochalimaea\_quintana Rothia\_dentocariosa Salmonella\_enteritidis Salmonella\_typhi Salmonella\_typhimurium Serratia\_marcescens Shigella\_dysenteriae Staphylococcus\_aureus Staphylococcus\_epidermidis Stenotrophomonas\_maltophil: Streptococcus\_agalactiae Streptococcus\_avium Streptococcus\_bovis Streptococcus\_cricetus Streptococcus\_faceiumStreptococcus\_faecalisStreptococcus\_ferusStreptococcus\_gallinarum Streptococcus\_lactis Streptococcus\_mitior Streptococcus\_mitis Streptococcus\_mutans Streptococcus\_oralisStreptococcus\_pneumoniaeStreptococcus\_pyogenesStreptococcus\_rattus Streptococcus\_salivarius Streptococcus\_sanguis Streptococcus\_sobrinus Treponema\_denticola Treponema\_pallidum Vibrio\_cholerae Vibrio\_comma Vibrio\_parahaemolyticus Vibrio\_vulnificus Wolbachia Yersinia\_enterocolitica Yersinia\_pestis Yersinia\_pseudotuberculosis

Count a numeric vector

6 CombDM

#### References

Laydon, D. J., Melamed, A., Sim, A., Gillet, N. A., Sim, K., Darko, S., Kroll, S., Douek, D. C., Price, D., Bangham, C. R. M., Asquith, B., Quantification of HTLV-1 clonality and TCR diversity, PLOS Comput. Biol. 2014

## **Examples**

```
data(Bact1)
hist(Bact1[,2], breaks=20, main="Bacterial diversity of a sample",
xlab="Number of bacteria of a given species", ylab="Number of bacterial species")
```

CombDM

CombDM

#### **Description**

Implements the DivE diversity estimator. Combines multiple objects of class *DiveMaster*.

# Usage

```
CombDM(dmlist)
```

## **Arguments**

dmlist

list of objects of class DiveMaster.

## **Details**

*CombDM* combines multiple objects of class *DiveMaster*. Function used if *DivE* estimation has been split into multiple, separate calls to DiveMaster.

#### Value

An object of class *DiveMaster*, i.e. a list of objects

model.score a matrix of aggregated model scores

fmm a list of fitsingMod objects corresponding to the list of fitted models

a matrix of scores of the fit of the models corresponding to the list of fitted

models

estimate the estimate of species richness (number of species/classes or diversity) at popu-

lation size tot.pop. This is the geometric average of the models corresponding to the top-five model scores. This is recalculated based on the combined list of

models

lower\_estimate

as per estimate value, but the lowest prediction amongst the models having the

top-five scores. This is recalculated based on the combined list of models

Curvature 7

upper\_estimate

as per estimate value, but the highest prediction amongst the models having the

top-five scores. This is recalculated based on the combined list of models

models list of original input models

m number of topscoring models used for diversity estimate. This is set as the

smallest m value of each of the *DiveMaster* objects in the list

#### Author(s)

Daniel J. Laydon, Aaron Sim, Charles R.M. Bangham, Becca Asquith

#### References

Laydon, D. J., Melamed, A., Sim, A., Gillet, N. A., Sim, K., Darko, S., Kroll, S., Douek, D. C., Price, D., Bangham, C. R. M., Asquith, B., Quantification of HTLV-1 clonality and TCR diversity, PLOS Comput. Biol. 2014

## See Also

DiveMaster

## **Examples**

# See DiveMaster documentation for examples.

Curvature

Curvature

## **Description**

Calculates the curvature of the rarefaction curve of the full observed data.

## Usage

Curvature(dss)

# **Arguments**

dss

list of objects of class DivSubsamples.

# **Details**

Curvature calculates the curvature of the full observed data. If dss contains more than one subsample (i.e. if length(dss)>1), the curvature of the largest subsample is calculated. If the curvature value is < 0.1, researchers should exercise caution as this is indicative of severe under-sampling, in which case DivE is prone to error.

8 DiveMaster

#### Value

numeric, between 0 and 1

#### Author(s)

Daniel J. Laydon, Aaron Sim, Charles R.M. Bangham, Becca Asquith

#### References

Laydon, D. J., Melamed, A., Sim, A., Gillet, N. A., Sim, K., Darko, S., Kroll, S., Douek, D. C., Price, D., Bangham, C. R. M., Asquith, B., Quantification of HTLV-1 clonality and TCR diversity, PLOS Comput. Biol. 2014

#### See Also

DivSubsamples

# **Examples**

# See DivSubsamples documentation for examples.

DiveMaster

DiveMaster

# Description

Implements the DivE diversity estimator.

## Usage

## **Arguments**

models list of models; each model is written as a function: function(x, params) { with(as.list(params),

<function of params>)}. Examples are given in the ModelSet data file as part of

the DivE package.

init.params list of matrices of initial seed model parameters. For each matrix, each row rep-

resents a given parameter set; each column represents a parameter value. Column names must match parameter names (params) in the corresponding model in the list models. Examples are given in the ParamSeeds data file as part of the

DivE package.

DiveMaster 9

param.ranges	list of matrices of lower and upper model parameters bounds. Used for the modFit function. The first and second row corresponds to the lower and upper bounds respectively; each column represents a parameter value. Column names must match parameter names (params) in the corresponding model in the list models. Examples are given in the param.ranges data file as part of the DivE package.
main.samp	the main sample, either as a 2-column data.frame (species ID, count of species), or a vector of species IDs.
tot.pop	total population (integer); default set to 100x the main.samp size.
numit	control argument passed to optimisation routine; the maximum number of iterations that modFit will perform. See modFit for details.
varleft	control argument passed to optimisation routine; see modFit for details.
subsizes	either number of nested subsamples (integer, must be 2 or greater), or a vector of nested sample lengths. If the former, then the vector of sample lengths will be created using the <i>DivSampleNum</i> function.
dssamps	list of user specified rarefaction data <i>DivSubsamples</i> objects. The length of each component vector of each object in the list must correspond to the vector of nested sample lengths (as defined by the user in subsizes).
nrf	difference between lengths of successive rarefaction datapoints.
minrarefac	minimum rarefaction x-axis value. This argument is not used if list of <i>DivSub-samples</i> object is specified in dssamps.
NResamples	number of resamples used to calculate the rarefaction data. This parameter is not used if list of <i>DivSubsamples</i> object is specified in dssamps.
minplaus	lower x-axis bound for plausibility check.
precision.lv	vector of precision level values for each criterion: 1. discrepancy – mean percentage error between rarefaction data points and model predicion, 2. Sample accuracy – percentage error between observed diversity of full rarefaction data and estimated diversity of full data from subsample, 3. local similarity. The scores for each criteria are defined as 1 + (multiples of bin sizes)
plaus.pen	penalty score for breaking the plausibility criterion: a model fit should be monotonically increasing and should have a slowing rate of species accumulation.
crit.wts	vector of weights of each of the four scoring criteria – fit, accuracy, similarity, plausibility. Default is $c(1,1,1,1)$ .
fitloops	number of fitting rounds performed for each model. In each round of fitting, the initial seed parameter values for each model will be the fitted parameters of the previous fitting run. This parameter has a significant impact on the computational time. The 'sweet spot' is 2.
numpred	number of topscoring models used for diversity prediction. Default is 5.

# **Details**

This is the master function of the DivE estimator. The default operation is a combination of four steps. 1. Generate a list of nested samples lengths from the main sample. 2. For each nested subsample, generate a vector of rarefaction data and their associated mean species diversity. 3. Fit

10 DiveMaster

to the generated data a set of models. 4. Evaluate the fits according to the DivE diversity estimation methodology and compare the scores across models and fitting criteria.

A list of DiveMaster objects, each representing the fits to different sets of models, can combined into a single DiveMaster object using the CombDM function. This is useful when running the DivE estimator with the full set of 58 models in a single run is not possible.

One can estimate the diversity for a given population using the PopDiversity function where the arguments are the Diversater object and the population size respectively.

#### Value

## A list of objects:

model.score a matrix of aggregated model scores

fmm a list of *fitsingMod* objects corresponding to the list of fitted models

a matrix of scores of the fit of the models corresponding to the list of fitted

models

estimate the estimate of species richness (number of species/classes or diversity) at popu-

lation size tot.pop. This is the geometric average of the models corresponding

to the top-five model scores

lower\_estimate

as per estimate value, but the lowest prediction amongst the models having the

top-five scores

upper\_estimate

as per estimate value, but the highest prediction amongst the models having the

top-five scores

models list of original input models

m number of topscoring models used for diversity estimate

#### Author(s)

Daniel J. Laydon, Aaron Sim, Charles R.M. Bangham, Becca Asquith

#### References

Laydon, D. J., Melamed, A., Sim, A., Gillet, N. A., Sim, K., Darko, S., Kroll, S., Douek, D. C., Price, D., Bangham, C. R. M., Asquith, B., Quantification of HTLV-1 clonality and TCR diversity, PLOS Comput. Biol. 2014

## See Also

FitSingleMod, ScoreSingleMod

DivSampleNum 11

## **Examples**

```
require(DivE)
data(Bact1)
data(ModelSet)
data(ParamSeeds)
data(ParamRanges)
testmodels <- list()</pre>
testmeta <- list()</pre>
paramranges <- list()</pre>
# Choose a single model
testmodels <- c(testmodels, ModelSet[1])</pre>
#testmeta[[1]] <- (ParamSeeds[[1]]) # Commented out for sake of brevity)</pre>
testmeta[[1]] < -matrix(c(0.9451638, 0.007428265, 0.9938149, 1.0147441, 0.009543598, 0.9870419),
                nrow=2, byrow=TRUE, dimnames=list(c(), c("a1", "a2", "a3"))) # Example seeds
paramranges[[1]] <- ParamRanges[[1]]</pre>
# Create DivSubsamples object (NB: For quick illustration only -- not default parameters)
dss_1 <- DivSubsamples(Bact1, nrf=2, minrarefac=1, maxrarefac=40, NResamples=5)
dss_2 <- DivSubsamples(Bact1, nrf=2, minrarefac=1, maxrarefac=65, NResamples=5)
dss <- list(dss_2, dss_1)
# Implement the function (NB: For quick illustration only -- not default parameters)
out <- DiveMaster(models=testmodels, init.params=testmeta, param.ranges=paramranges,</pre>
                  main.samp=Bact1, subsizes=c(65, 40), NResamples=5, fitloops=1,
                  dssamp=dss, numit=2, varleft=10)
# DiveMaster Outputs
out$estimate
out$fmm$logistic
out$fmm$logistic$global
out$ssm
summary(out)
## Combining two DiveMaster objects (assuming a second object 'out2'):
# out3 <- CombDM(list(out, out2))</pre>
## To calculate the diversity for a different population size
# PopDiversity(dm=out, popsize=10^5, TopX=1)
```

12 DivSampleNum

# **Description**

Function to generate an integer sequence representing the lengths of nested samples of sample

# Usage

```
DivSampleNum(ms, n)
```

# **Arguments**

ms the main sample, either as a 2-column data.frame (species ID, count of species),

or a vector of species IDs.

n desired number of nested samples (integer)

#### **Details**

This function produces the default list of nested sample lengths for the DivE algorithm. For the vector representation of the main sample (ms) it is equivalent to sort(round(seq(from=length(ms)/n), to=length(ms), by=length(ms)/n)), decreasing=TRUE).

#### Value

A decreasing sequence of nested sample lengths.

## Author(s)

Daniel J. Laydon, Aaron Sim, Charles R.M. Bangham, Becca Asquith

# References

Laydon, D. J., Melamed, A., Sim, A., Gillet, N. A., Sim, K., Darko, S., Kroll, S., Douek, D. C., Price, D., Bangham, C. R. M., Asquith, B., Quantification of HTLV-1 clonality and TCR diversity, PLOS Comput. Biol. 2014

# **Examples**

```
require(DivE)
data(Bact1)

DivSampleNum(Bact1, 3)
DivSampleNum(Bact1, 6)
```

DivSubsamples 13

DivSubsamples DivSubsamples
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#### **Description**

Function to generate the rarefaction data from a given sample

# Usage

```
DivSubsamples(mainsamp, nrf, minrarefac=1,
maxrarefac=length(FormatInput(mainsamp)), NResamples=1000)
```

# **Arguments**

mainsamp the main sample, either as a 2-column data.frame (species ID, count of species),

or a vector of species IDs.

nrf difference between lengths of successive rarefaction datapoints.

minrarefac minimum rarefaction data x-axis value. Default is 1.

maxrarefac maximum rarefaction data x-axis value. Default is length of the sample mainsamp.

NResamples number of resamples used to calculate the rarefaction data.

## **Details**

This function produces a vector of subsamples diversity values with subsample lengths evenly distributed between a specified minimum and maximum number. The curvature of the rarefaction curve can be obtained with the function Curvature.

#### Value

a list of class *DivSubsamples* containing resampling results (i.e. the diversity data). This includes the following:

RarefacXAxis vector of x-axis rarefaction data RarefacYAxis vector of y-axis rarefaction data

div\_sd vector of y-axis rarefaction data standard deviations

NResamples number of sampling iterations used to calculate sample means of each subsam-

ple diversity

# Author(s)

Daniel J. Laydon, Aaron Sim, Charles R.M. Bangham, Becca Asquith

#### References

Laydon, D. J., Melamed, A., Sim, A., Gillet, N. A., Sim, K., Darko, S., Kroll, S., Douek, D. C., Price, D., Bangham, C. R. M., Asquith, B., Quantification of HTLV-1 clonality and TCR diversity, PLOS Comput. Biol. 2014

14 FitSingleMod

## **Examples**

FitSingleMod

FitSingleMod

## **Description**

Function to fit a model to the diversity values of subsamples of a given sample and its nested samples.

## Usage

## **Arguments**

model.list

model; written as a function: function(x, params) with(as.list(params), < function of params>). Examples are given in the ModelSet data file as part of the DivE package. Used in the modFit function.

init.param

matrix of of initial seed model parameters. For each matrix, each row represents a given parameter set; each column represents a parameter value. Column names must match parameter names (params) in the corresponding model in the list models. Examples are given in the ParamSeeds data file as part of the DivE package.

FitSingleMod 15

param.range	matrix of lower and upper model parameters bounds. Used for the modFit function. The first and second row corresponds to the lower and upper bounds respectively; each column represents a parameter value. Column names must match parameter names (params) in the corresponding model in the list models. Examples are given in the ParamRanges data file as part of the DivE package.
main.samp	the main sample, either as a 2-column data.frame (species ID, count of species), or a vector of species IDs.
tot.pop	total population (integer); default set to 100x the main.samp size.
numit	control argument passed to optimisation routine; the maximum number of iterations that modFit will perform. See modFit for details.
varleft	control argument passed to optimisation routine; see modFit for details.
data.default	if True, then the list of vectors of nested rarefaction data (divsubsample objects) generated by the <i>DivSampleNum</i> and <i>divsubsample</i> functions; if False, then the function uses the user-specified list of nested rarefaction data, <i>dssamps</i>
subsizes	either number of subsamples of main.samp (integer), or a vector of subsample lengths. If the former, then the vector of sample lengths will be created using the <i>DivSampleNum</i> function.
dssamps	list of user specified rarefaction data <i>DivSubsamples</i> objects. The length of each component vector of each object in the list must correspond to the vector of subsample lengths (as defined by the user in subsizes).
nrf	difference between lengths of successive rarefaction datapoints.
minrarefac	minimum rarefaction x-axis value. This argument is not used if list of <i>DivSub-samples</i> object is specified in <i>dssamps</i> .
NResamples	number of resamples used to calculate the rarefaction data. This parameter is not used if list of <i>DivSubsamples</i> object is specified in dssamps. NB: different from numit parameter, which is specific to the fitting process.
minplaus	lower x-axis bound for plausibility check.
fitloops	number of fitting rounds performed for each model. In each round of fitting, the initial seed parameter values for each model will be the fitted parameters of the

# **Details**

This function fits a single specified model to the diversity values of the subsamples of a set of nested samples. The output is a list of raw fitting results (pre-scoring). The user should use this function if he or she is interested in fitting a specific parametric rarefraction curve to a sample (rather than selecting the most appropriate model) and examining its performance.

previous fitting run. This parameter has a significant impact on the computa-

## Value

A list of class *FitSingleMod* containing the results of the fit of the model to the diversity samples. This includes the following:

param matrix of fitted parameters for each nested sample

tional time. The 'sweet spot' is 2.

16 FitSingleMod

sum-of-squared residuals for the fits for each nested sample ssr mean sum-of-squared residuals for the fits for each nested sample ms goodness-of-fit values for the fits for each nested sample; this expressed as the discrep average across the subsamples in each nested sample of all the percentage residlocal prediction of main sample sizes according to fitted curves for each of the nested global prediction of population diversity at popsize according to fitted curves for each of the nested subsamples AccuracyToObserved vector of percentage errors between the observed diversity of full sample data and the estimated diversity of full sample data from subsamples subsamplesizes vector of nested subsample sizes the list of divsubsample objects used in the fitting. The length of the list is equal datapoints to number of samples modelname name of the model used number of parameters in the model numparam the mean squared distances between subsample curves, local and global sampvar mono.local matrix of logical values: is the curve monotonically increasing, up to the main sample size? mono.global matrix of logical values: is the curve monotonically increasing, up to the population size? slowing.local matrix of logical values: is the rate of increase in the curve slowing (decreasing second derivative), up to the main sample size? slowing.global matrix of logical values: is the rate of increase in the curve slowing (decreasing second derivative), from minplaus to the population size (popsize? matrix of logical values: is the curve plausible (i.e. monotonically increasing plausibility and with decreasing second derivative)? dist.local matrix of distances between curves fitted to the nested samples. Distances are calculated as areas between curves bounded by 0 and the main sample size dist.global similar to dist.local, but with curve upper bound the population size local.ref.dist distances of nested curves to the curve fitted to the whole sample, with the curves bounded by 0 and the main sample size global.ref.dist similar to local.ref.dist but with curve upper bound the population size user defined population size popsize

the function corresponding to the user-selected modelname

## Author(s)

the model

Daniel J. Laydon, Aaron Sim, Charles R.M. Bangham, Becca Asquith

ModelSet 17

#### References

Laydon, D. J., Melamed, A., Sim, A., Gillet, N. A., Sim, K., Darko, S., Kroll, S., Douek, D. C., Price, D., Bangham, C. R. M., Asquith, B., Quantification of HTLV-1 clonality and TCR diversity, PLOS Comput. Biol. 2014

#### See Also

ScoreSingleMod

## **Examples**

# See documentation of \code{ScoreSingleMod} for examples

ModelSet

List of 58 candidate models to fit to data

## **Description**

ModelSet is an example list of candidate models used in the reference below to calculate the DivE estimate

## Usage

data(ModelSet)

## Format

A list of 58 named functions (with named parameters). Each model in the list must be provided as a function, and must be of the following form: function(x, params) with(as.list(params), <function of params>). The parameter names are a1, a2, a3, etc. These must match the names of the parameter values given in ParamSeeds and ParamRanges.

# **Details**

Each model is written as a function: function(x, params) with(as.list(params), <function of params>). Examples are given in the *ModelSet* data file as part of the *DivE* package. The user can amend *ModelSet* and input additional models as required. The analytical form of all the models provided in *ModelSet* can be found in the reference below, in Text S1: List of *DivE* candidate models. All models were obtained from *zunzun.org*, an online curve fitting repository

## References

Laydon, D. J., Melamed, A., Sim, A., Gillet, N. A., Sim, K., Darko, S., Kroll, S., Douek, D. C., Price, D., Bangham, C. R. M., Asquith, B., Quantification of HTLV-1 clonality and TCR diversity, PLOS Comput. Biol. 2014

# **Examples**

data(ModelSet)

18 ParamSeeds

ParamRanges	List of 58 sets of upper and lower bounds for models evaluated by DivE

# Description

A list of 58 matrices. Each matrix corresponds to a model in ModelSet, for which it contains suggested upper and lower bounds for each parameter.

# Usage

```
data(ParamRanges)
```

#### **Format**

A list of 58 matrices. Each matrix has 2 rows (lower bounds, upper bounds) and columns corresponding to the parameters of the matching model in ModelSet.

## **Details**

There is a trade-off between specifying parameter ranges that are large enough to encompass likely fitted values for a variety of data sets, and specifying parameter ranges that are suitably small so that parameter estimation is sufficiently precise and runtime is managable. We have aimed to balance these competing concerns. The parameter ranges provided performed well in our simulations. The user can amend if required.

## References

Laydon, D. J., Melamed, A., Sim, A., Gillet, N. A., Sim, K., Darko, S., Kroll, S., Douek, D. C., Price, D., Bangham, C. R. M., Asquith, B., Quantification of HTLV-1 clonality and TCR diversity, PLOS Comput. Biol. 2014

## **Examples**

data(ParamRanges)

## **Description**

The performance of *modFit* (package *FME*) with the pseudorandom parameter search algorithm (package *FME*, pseudoOptim) used to estimated model parameter values, is sensitive to the choice of initial seeding values. We have provided the fitted parameters returned from our simulations to be used as initial seeding parameters.

PopDiversity 19

## Usage

data(ParamSeeds)

#### **Format**

A list of 58 matrices. Each matrix has columns corresponding to the parameters of the matching model in *ModelSet*. Each row is set of potential seeding parameters

#### **Details**

For each model, each initial parameter guess (i.e. each row of the model matrix in *ParamRanges*) is evaluated by to *modCost*. The parameter guess returning the lowest cost is used as the seeding value in *modFit*. If the user wishes to input alternative initial seeding parameter values, then for each model and parameter, all values must be finite (not NA or NaN), and within the upper and lower bounds set in *ParamRanges*. Column names must match parameter names (params) in the corresponding model in ModelSet (i.e. models argument in DivEMaster).

#### References

Laydon, D. J., Melamed, A., Sim, A., Gillet, N. A., Sim, K., Darko, S., Kroll, S., Douek, D. C., Price, D., Bangham, C. R. M., Asquith, B., Quantification of HTLV-1 clonality and TCR diversity, PLOS Comput. Biol. 2014

# **Examples**

data(ParamSeeds)

PopDiversity

**PopDiversity** 

# Description

Calculates the species richness at a specified population size, taking an object of class *DiveMaster* as an input.

#### Usage

PopDiversity(dm, popsize, TopX=NULL)

## Arguments

dm list of objects of class *DiveMaster*.

popsize positive real number. Population size.

TopX a positive integer, less than the number of models contained in dm, representing

the number of best-performing models used for the aggregated estimate of the population diversity. If NULL (default), then dm\$m models are aggregated. If TopX is larger than the the number of models fitted, then min(5, length(dm\$fmm))

models are aggregated.

20 ScoreSingleMod

## **Details**

*CombDM* combines multiple objects of class *DiveMaster*. Function used if *DivE* estimation has been split into multiple, separate calls to DiveMaster.

#### Value

A list of objects:

estimate point estimate of diversity (species richness)

upper\_estimate

estimate upper bound

lower\_estimate

estimate lower bound

# Author(s)

Daniel J. Laydon, Aaron Sim, Charles R.M. Bangham, Becca Asquith

#### References

Laydon, D. J., Melamed, A., Sim, A., Gillet, N. A., Sim, K., Darko, S., Kroll, S., Douek, D. C., Price, D., Bangham, C. R. M., Asquith, B., Quantification of HTLV-1 clonality and TCR diversity, PLOS Comput. Biol. 2014

# See Also

DiveMaster

## **Examples**

# See DiveMaster documentation for examples.

ScoreSingleMod

ScoreSingleMod

# **Description**

Determines the set of scores corresponding to a single model fit to a diversity values of subsamples of a given sample and its nested samples.

## Usage

```
ScoreSingleMod(fsm, precision.lv=c(0.0001, 0.005, 0.005), plaus.pen=500)
```

ScoreSingleMod 21

## Arguments

fsm FitSingleMod object

precision.lv vector of precision level values for each criterion: 1. discrepancy – mean per-

centage error between rarefaction data points and model predicion, 2. Sample accuracy – percentage error between observed diversity of full rarefaction data and estimated diversity of full data from subsample, 3. local similarity. The

scores for each criteria are defined as 1 + (multiples of bin sizes)

plaus.pen penalty score for breaking the plausibility criterion: a model fit should be mono-

tonically increasing and should have a slowing rate of species accumulation.

# **Details**

The score for a given model is only meaningful when compared with scores of other models. Lower score = better for predicting the population diversity. To assess the performance of a single model, it is more informative to use FitSingleMod function.

#### Value

A list of class *ScoreSingleMod* containing the scores of the fit of the model to the diversity samples. This includes the following:

discrepancy score for discrepancy, aggregated across all nested subsamples

accuracy score for accuracy of full sample prediction, aggregated across all nested sub-

samples

similarity score for similarity of curves for different samples

plausibility score for plausibility criterion

binsize vector of user-specified precision values used to translate values associated with

each criterion into scores

plausibility.penalty

penalty score for implausible diversity curve

modname model name

## Author(s)

Daniel J. Laydon, Aaron Sim, Charles R.M. Bangham, Becca Asquith

#### References

Laydon, D. J., Melamed, A., Sim, A., Gillet, N. A., Sim, K., Darko, S., Kroll, S., Douek, D. C., Price, D., Bangham, C. R. M., Asquith, B., Quantification of HTLV-1 clonality and TCR diversity, PLOS Comput. Biol. 2014

#### See Also

FitSingleMod

ScoreSingleMod ScoreSingleMod

## **Examples**

```
require(DivE)
data(Bact1)
data(ModelSet)
data(ParamSeeds)
data(ParamRanges)
testmodels <- list()</pre>
testmeta <- list()</pre>
paramranges <- list()</pre>
# Choose a single model
testmodels <- c(testmodels, ModelSet[1])</pre>
# testmeta <- (ParamSeeds[[1]]) # Commented out for sake of brevity)</pre>
testmeta <- matrix(c(0.9451638, 0.007428265, 0.9938149, 1.0147441, 0.009543598, 0.9870419),
                 nrow=2, byrow=TRUE, dimnames=list(c(), c("a1", "a2", "a3"))) # Example seeds
paramranges <- ParamRanges[[1]]</pre>
# Create DivSubsamples object (NB: For quick illustration only -- not default parameters)
dss_1 <- DivSubsamples(Bact1, nrf=2, minrarefac=1, maxrarefac=40, NResamples=5)
dss_2 <- DivSubsamples(Bact1, nrf=2, minrarefac=1, maxrarefac=65, NResamples=5)
dss <- list(dss_2, dss_1)</pre>
# Fit the model (NB: For quick illustration only -- not default parameters)
fsm <- FitSingleMod(model.list=testmodels, init.param=testmeta, param.range=paramranges,</pre>
                     main.samp=Bact1, dssamps=dss, fitloops=1, data.default=FALSE,
                     subsizes=c(65, 40),
                     numit=2) # numit chosen to be extremely small to speed up example
# Score the model
ssm <- ScoreSingleMod(fsm)</pre>
ssm
summary(ssm)
```

# **Index**

Bact1, 4 ModelSet, 17 ParamRanges, 18 ParamSeeds, 18 ParamSeeds, 18 * diversity CombDM, 6 Curvature, 7 DiveMaster, 8 DivSampleNum, 11 DivSubsamples, 13 FitSingleMod, 20 * print.summary.DiveMaster (DiveMaster), 8 print.summary.DivSubsamples, 13 FitSingleMod, 14 PopDiversity, 19 ScoreSingleMod, 20 * print.summary.DivSubsamples, 13 ScoreSingleMod, 10, 17, 20 summary.DiveMaster (DiveMaster), 8 summary.DiveMaster (DiveMaster), 8 summary.DivSubsamples, 13 summary.DivSubsamples (DivSubsamples), 13 summary.FitSingleMod (FitSingleMod), 14 summary.ScoreSingleMod, 20 (ScoreSingleMod, 20 * print.summary.DivSubsamples, 13 FitSingleMod, 14 print.summary.DivSubsampleMod (ScoreSingleMod), 20 ScoreSingleMod, 20 summary.DivSubsamples (DivSubsamples), 13 summary.FitSingleMod (FitSingleMod), 14 summary.ScoreSingleMod, 20 (ScoreSingleMod, 20 ScoreSingleMod, 14 summary.ScoreSingleMod, 10 ScoreSingleMod, 10, 14, 21 ModelSet, 17 modFit, 9, 15
ParamRanges, 18 ParamSeeds, 18 PoivSubsamples, 13 PitSingleMod, 14 PopDiversity, 19 ScoreSingleMod, 20 ParamSeeds, 18 PopDiversity, 19 ScoreSingleMod, 20 Paramseeds, 18 PopDiversity, 19 ScoreSingleMod, 20 Paramseeds, 2  Paramseeds, 18 Print. summary. DivSubsamples (FitSingleMod (ScoreSingleMod, 20 ScoreSingleMod, 10, 17, 20 Summary. DivSubsamples (DivSubsamples), 13 Summary. FitSingleMod (FitSingleMod), 14 Summary. ScoreSingleMod (ScoreSingleMod), 20 Paramseeds, 13 ScoreSingleMod (FitSingleMod), 14 Summary. DivSubsamples, 2 Summary. DivSubsamples, 2 Summary. FitSingleMod (FitSingleMod), 14 Summary. ScoreSingleMod (ScoreSingleMod), 20 Paramseeds, 18 PoivSubsamples, 2 PoivE-package, 2 PoivE-
ParamSeeds, 18  * diversity CombDM, 6 Curvature, 7 DiveMaster, 8 DivSampleNum, 11 DivSubsamples, 13 FitSingleMod, 14 PopDiversity, 19 ScoreSingleMod, 20  * package DivE-package, 2 DivE(DivE-package, 2 DivE(DivE-package, 2 DivE-package, 2 DivSampleNum, 11 DivSubsamples, 8, 13 FitSingleMod, 10, 14, 21 ModelSet, 17 modFit, 9, 15
* diversity CombDM, 6 Curvature, 7 DiveMaster, 8 DivSampleNum, 11 DivSubsamples, 13 FitSingleMod, 14 PopDiversity, 19 ScoreSingleMod, 20 * package DivE-package, 2 DivE(DivE-package), 2 DivE(DivE-package), 2 DivSampleNum, 11 DivSubsamples, 8, 13 FitSingleMod, 10, 17, 20 Summary. DiveMaster (DiveMaster), 8 Summary. DivSubsamples (DivSubsamples), 13 Summary. FitSingleMod (FitSingleMod), 14 Summary. ScoreSingleMod, 20 (ScoreSingleMod, 20 (ScoreSingleMod), 20  Sact1, 4 Bact2 (Bact1), 4 CombDM, 6 Curvature, 7 DivE (DivE-package), 2 DivE-package, 2 DivSampleNum, 11 DivSubsamples, 8, 13 FitSingleMod, 10, 14, 21 ModelSet, 17 modFit, 9, 15
CombDM, 6 Curvature, 7 DiveMaster, 8 DivSampleNum, 11 DivSubsamples, 13 FitSingleMod, 14 PopDiversity, 19 ScoreSingleMod, 20 * package DivE-package, 2 DivE(DivE-package, 2 DivSampleNum, 11 DivSubsamples, 8, 13 FitSingleMod, 14 PopDiversity, 19 ScoreSingleMod, 20 * package DivE-package, 2 DivE-package, 2 DivE-package, 2 DivE-package, 2 DivSampleNum, 11 DivSubsamples, 8, 13 FitSingleMod, 10, 14, 21 ModelSet, 17 modFit, 9, 15
Curvature, 7 DiveMaster, 8 DivSampleNum, 11 DivSubsamples, 13 FitSingleMod, 14 PopDiversity, 19 ScoreSingleMod, 20 * package DivE-package, 2  Bact1, 4 Bact2 (Bact1), 4  CombDM, 6 Curvature, 7  DivE (DivE-package), 2 DivSampleNum, 11 DivSubsamples, 8, 13  FitSingleMod, 10, 17, 20 summary. DiveMaster (DiveMaster), 8 summary. DivSubsamples (DivSubsamples), 13 summary. FitSingleMod (FitSingleMod), 14 summary. ScoreSingleMod (ScoreSingleMod), 20  ScoreSingleMod, 10 ScoreSingleMod, 14 Summary. ScoreSingleMod (ScoreSingleMod, 14 Summary. FitSingleMod, 14 Summary. ScoreSingleMod (ScoreSingleMod, 14 Summary. ScoreSingleMod (ScoreSingleMod, 14 Summary. ScoreSingleMod (ScoreSingleMod, 14 Summary. FitSingleMod, 14 Summary. ScoreSingleMod (ScoreSingleMod, 14 Summary. ScoreSingleMod (ScoreSingleMod, 14 Summary. FitSingleMod, 14 Summary. ScoreSingleMod (ScoreSingleMod, 14 Summary. FitSingleMod, 16 StoreSingleMod Summary. FitSingleMod StoreSingleMod Summary. FitSingleMod Summary. FitSingle
DiveMaster, 8 DivSampleNum, 11 DivSubsamples, 13 FitSingleMod, 14 PopDiversity, 19 ScoreSingleMod, 20 * package DivE-package, 2  Bact1, 4 Bact2 (Bact1), 4  CombDM, 6 Curvature, 7  DivE (DivE-package), 2 DivSampleNum, 11 DivSubsamples, 8, 13  FitSingleMod, 10, 17, 20 ScoreSingleMod, 10, 17, 20 Summary DiveMaster (DiveMaster), 8 Summary DivSubsamples (DivSubsamples), 13 Summary FitSingleMod (FitSingleMod), 14 Summary ScoreSingleMod (ScoreSingleMod), 20  ScoreSingleMod, 14 Summary FitSingleMod, 14 Summary FitSingleMod, 12 ScoreSingleMod, 14 Summary FitSingleMod, 12 ScoreSingleMod, 14 Summary FitSingleMod, 14 Summary FitSingleMod, 12 ScoreSingleMod, 14 Summary FitSingleMod, 12 ScoreSingleMod, 12 Summary FitSingleMod, 12 ScoreSingleMod, 12 Summary FitSingleMod, 14 S
DivSampleNum, 11 DivSubsamples, 13 FitSingleMod, 14 PopDiversity, 19 ScoreSingleMod, 20 ** package DivE-package, 2 Bact1, 4 Bact2 (Bact1), 4  CombDM, 6 Curvature, 7  DivE (DivE-package), 2 DivE-package, 2 DivSampleNum, 11 DivSubsamples, (DivSubsamples), 3 Summary. DivSubsamples (DivSubsamples), 13 Summary. FitSingleMod (FitSingleMod), 14 Summary. ScoreSingleMod (ScoreSingleMod), 20  ScoreSingleMod, 10, 14 Summary. FitSingleMod (FitSingleMod), 20 ScoreSingleMod, 10 ScoreSingleMod, 10 ScoreSingleMod, 11 Summary. DivSubsamples, 2 Summary. FitSingleMod (ScoreSingleMod, 14 Summary. DivSubsamples, 2 Summary. DivSubsamples, 2 Summary. DivSubsamples, 3 Summary. DivSubsamples, 2 Summary. DivSubsamples, 2 Summary. DivSubsamples, 2 Summary. DivSubsamples, 3 Summary. FitSingleMod, 14 Summary. ScoreSingleMod, 14 Summary. ScoreSingleMod, 14 Summary. ScoreSingleMod, 14 Summary. ScoreSingleMod, 14 Summary. DivSubsamples, 8 Summary
DivSubsamples, 13 FitSingleMod, 14 PopDiversity, 19 ScoreSingleMod, 20 * package DivE-package, 2  Bact1, 4 Bact2 (Bact1), 4  CombDM, 6 Curvature, 7  DivE (DivE-package, 2  DivSampleNum, 11 DivSubsamples, 13 Summary. DivSubsamples (DivSubsamples), 13 Summary. FitSingleMod (FitSingleMod), 14 Summary. ScoreSingleMod (ScoreSingleMod), 20  Bact1, 4 Bact2 (Bact1), 4  CombDM, 6 Curvature, 7  DivE (DivE-package), 2 DivE-package, 2 DiveMaster, 7, 8, 20 DivSampleNum, 11 DivSubsamples, 8, 13  FitSingleMod, 10, 14, 21  ModelSet, 17 modFit, 9, 15
FitSingleMod, 14 PopDiversity, 19 ScoreSingleMod, 20 * package DivE-package, 2  Bact1, 4 Bact2 (Bact1), 4  CombDM, 6 Curvature, 7  DivE (DivE-package, 2  DivE-package, 2  DivSampleNum, 11  DivSubsamples, 8, 13  FitSingleMod, 10, 14, 21  ModelSet, 17 modFit, 9, 15
PopDiversity, 19 ScoreSingleMod, 20 * package DivE-package, 2  Bact1, 4 Bact2 (Bact1), 4  CombDM, 6 Curvature, 7  DivE (DivE-package), 2  DivE-package, 2  DivE-package, 2  DivE-package, 2  DivE (DivE-package), 2  DivE (DivE-package), 2  DivE (DivSubsamples), 13  Summary. FitSingleMod (FitSingleMod), 14  summary. ScoreSingleMod), 20  (ScoreSingleMod), 20  ScoreSingleMod, 20  ScoreSing
ScoreSingleMod, 20 * package DivE-package, 2  Bact1, 4 Bact2 (Bact1), 4  CombDM, 6 Curvature, 7  DivE (DivE-package, 2  DivE-package, 2  DivE-package, 2  DivE-package, 2  DivE-package, 2  DivEMaster, 7, 8, 20  DivSampleNum, 11  DivSubsamples, 8, 13  FitSingleMod, 10, 14, 21  ModelSet, 17 modFit, 9, 15
ScoreSingleMod, 20 * package DivE-package, 2  Bact1, 4 Bact2 (Bact1), 4  CombDM, 6 Curvature, 7  DivE (DivE-package, 2  DivSampleNum, 11 DivSubsamples, 8, 13  FitSingleMod, 10, 14, 21  ModelSet, 17 modFit, 9, 15
* package DivE-package, 2  Bact1, 4 Bact2 (Bact1), 4  CombDM, 6 Curvature, 7  DivE (DivE-package), 2 DivE-package, 2 DiveMaster, 7, 8, 20 DivSampleNum, 11 DivSubsamples, 8, 13  FitSingleMod, 10, 14, 21  ModelSet, 17 modFit, 9, 15
Bact1, 4 Bact2 (Bact1), 4  CombDM, 6 Curvature, 7  DivE (DivE-package), 2 DivE-package, 2 DiveMaster, 7, 8, 20 DivSampleNum, 11 DivSubsamples, 8, 13  FitSingleMod, 10, 14, 21  ModelSet, 17 modFit, 9, 15
Bact1, 4 Bact2 (Bact1), 4  CombDM, 6 Curvature, 7  DivE (DivE-package), 2 DivE-package, 2 DiveMaster, 7, 8, 20 DivSampleNum, 11 DivSubsamples, 8, 13  FitSingleMod, 10, 14, 21  ModelSet, 17 modFit, 9, 15
Bact2 (Bact1), 4  CombDM, 6  Curvature, 7  DivE (DivE-package), 2  DivE-package, 2  DiveMaster, 7, 8, 20  DivSampleNum, 11  DivSubsamples, 8, 13  FitSingleMod, 10, 14, 21  ModelSet, 17  modFit, 9, 15
CombDM, 6 Curvature, 7  DivE (DivE-package), 2 DivE-package, 2 DiveMaster, 7, 8, 20 DivSampleNum, 11 DivSubsamples, 8, 13  FitSingleMod, 10, 14, 21  ModelSet, 17 modFit, 9, 15
Curvature, 7  DivE (DivE-package), 2  DivE-package, 2  DiveMaster, 7, 8, 20  DivSampleNum, 11  DivSubsamples, 8, 13  FitSingleMod, 10, 14, 21  ModelSet, 17  modFit, 9, 15
Curvature, 7  DivE (DivE-package), 2  DivE-package, 2  DiveMaster, 7, 8, 20  DivSampleNum, 11  DivSubsamples, 8, 13  FitSingleMod, 10, 14, 21  ModelSet, 17  modFit, 9, 15
DivE (DivE-package), 2 DivE-package, 2 DiveMaster, 7, 8, 20 DivSampleNum, 11 DivSubsamples, 8, 13 FitSingleMod, 10, 14, 21 ModelSet, 17 modFit, 9, 15
DivE-package, 2 DiveMaster, 7, 8, 20 DivSampleNum, 11 DivSubsamples, 8, 13 FitSingleMod, 10, 14, 21 ModelSet, 17 modFit, 9, 15
DivE-package, 2 DiveMaster, 7, 8, 20 DivSampleNum, 11 DivSubsamples, 8, 13 FitSingleMod, 10, 14, 21 ModelSet, 17 modFit, 9, 15
DiveMaster, 7, 8, 20 DivSampleNum, 11 DivSubsamples, 8, 13 FitSingleMod, 10, 14, 21 ModelSet, 17 modFit, 9, 15
DivSampleNum, 11 DivSubsamples, 8, 13 FitSingleMod, 10, 14, 21 ModelSet, 17 modFit, 9, 15
DivSubsamples, 8, 13 FitSingleMod, 10, 14, 21 ModelSet, 17 modFit, 9, 15
FitSingleMod, 10, 14, 21  ModelSet, 17  modFit, 9, 15
$\begin{array}{c} \text{ModelSet, } 17 \\ \text{modFit, } 9, 15 \end{array}$
modFit, 9, 15
ParamRanges, 18
ParamSeeds, 18
plot.FitSingleMod(FitSingleMod), 14
PopDiversity, 19
print.DiveMaster(DiveMaster), 8
print.DivSubsamples (DivSubsamples), 13
print.FitSingleMod(FitSingleMod), 14