Package 'EcoEnsemble'

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```
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     'EnsemblePrior-class.R' 'EnsembleData-class.R'
     'EnsembleFit-class.R' 'EnsembleSample-class.R'
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```

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EcoEnsemble-package

A general framework for combining ecosystem models

Description

The EcoEnsemble package implements the framework for combining ecosystem models laid out in Spence et al (2018).

Details

The ensemble model can be implemented in three main stages:

- 1. Eliciting priors on discrepancy terms: This is done by using the EnsemblePrior constructor.
- 2. Fitting the ensemble model: Using fit_ensemble_model with simulator outputs, observations and prior information. The ensemble model can be fit, obtaining either the point estimate, which maximises the posterior density, or running Markov chain Monte Carlo to generate a sample from the posterior denisty of the ensemble model.
- 3. Sampling the latent variables from the fitted model: Using generate_sample with the fitted ensemble object, the discrepancy terms and the ensemble's best guess of the truth can be generated. Similarly to fit_ensemble_model, this can either be a point estimate or a full sample.

References

Stan Development Team (2020). RStan: the R interface to Stan. R package version 2.21.2. https://mc-stan.org

Spence, M. A., J. L. Blanchard, A. G. Rossberg, M. R. Heath, J. J. Heymans, S. Mackinson, N. Serpetti, D. C. Speirs, R. B. Thorpe, and P. G. Blackwell. 2018. "A General Framework for Combining Ecosystem Models." Fish and Fisheries 19: 1013-42. https://onlinelibrary.wiley.com/doi/abs/10.1111/faf.12310

EnsembleData

Constructor for the EnsembleData class

Description

A constructor for the EnsembleData class. This is used to convert input data into the required form for fit_ensemble_model.

Usage

EnsembleData(observations, simulators, priors)

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Arguments

observations A list of length 2 containing observations and a covariance matrix. The first

element is a data.frame or matrix with each column giving observations of each output of interest and each row a time. Rows should be named with the times and columns should be named the variables. The second element is is a $d\times d$ matrix where d is the number of columns of the observations data frame

/ matrix. This matrix is the covariance matrix of the observations.

simulators A list with length equal to the number of simulators. For each simulator, there

is a list of 2 objects containing the simulator output and covariance matrix. The first element is a data. frame or matrix with each column giving a simulator outputs of interest and each row a time. Rows should be named with the times and columns should be named the variables. The second element is a $n_k \times n_k$ matrix where n_k is the number of columns of the simulators output data frame

/ matrix. This matrix is the covariance matrix of the simulator outputs.

priors An EnsemblePrior object specifying the prior distributions for the ensemble.

Value

An object of class EnsembleData

See Also

EnsembleData, EnsemblePrior, fit_ensemble_model

Examples

EnsembleData-class

A class to hold the Ensemble data

Description

A class that holds the observation data, simulator outputs, and prior information to convert into the required form for fit_ensemble_model.

Slots

stan_input A list of parameters in the correct form to fit the ensemble model in Stan.

observations A list of length 2 containing observations and a covariance matrix. The first element is a data.frame or matrix with each column giving observations of each output of interest and each row a time. Rows should be named with the times and columns should be named the variables. The second element is the covariance matrix of the observations.

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simulators A list with length equal to the number of simulators. For each simulator, there is a list of 2 objects containing the simulator output and covariance matrix. The first element is a data. frame or matrix with each column giving a simulator outputs of interest and each row a time. Rows should be named with the times and columns should be named the variables. The second element is the covariance matrix of the simulator outputs.

priors An EnsemblePrior object specifying the prior distributions for the ensemble.

See Also

EnsembleData, EnsemblePrior, fit_ensemble_model

EnsembleFit

The constructor for the EnsembleFit object

Description

The constructor for an EnsembleFit object. This function need not be called as an EnsembleFit object is constructed automatically by the fit_ensemble_model function. The samples slot contains the samples from the MCMC if a full sampling was completed, otherwise the point_estimate slot contains information about a point estimate.

Usage

```
EnsembleFit(ensemble_data, samples = NULL, point_estimate = NULL)
```

Arguments

samples A stanfit object containing the samples drawn from the fitted model. The

default value is NULL.

point_estimate A list output of the optimised model. The default value is NULL.

Value

An object of class EnsembleFit

References

Stan Development Team (2020). RStan: the R interface to Stan. R package version 2.21.2. https://mc-stan.org

See Also

```
EnsembleFit, fit_ensemble_model,
```

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EnsembleFit-class	A class to hold the samples or point estimates from the ensemble model.
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Description

An EnsembleFit object is returned by the fit_ensemble_model function. The object contains a slot for the EnsembleData object originally used to fit the ensemble model. The samples slot contains the samples from the MCMC if a full sampling was completed, otherwise the point_estimate slot contains information about a point estimate.

Slots

ensemble_data An EnsembleData object encapsulating the data used to fit the ensemble model. samples A stanfit object containing the samples drawn from the fitted model. The default value is NULL.

point_estimate A list output of the optimised model. The default value is NULL.

References

Stan Development Team (2020). RStan: the R interface to Stan. R package version 2.21.2. https://mc-stan.org

See Also

```
EnsembleFit, fit_ensemble_model, generate_sample
```

EnsemblePrior-class A class to hold the priors for the ensemble model.

Description

An EnsemblePrior object encapsulates the prior information for the ensemble model.

Slots

d A numeric specifying the number of variables of interest in the ensemble.

ind_st_params A list containing a prior specification for the individual short-term discrepancies $z_k^{(t)}$. See details of the EnsemblePrior() constructor.

ind_lt_params A list containing a prior specification for the individual long-term discrepancies γ_k . See details of the EnsemblePrior() constructor.

sha_st_params A list containing a prior specification for the shared short-term discrepancies $\eta^{(t)}$. See details of the EnsemblePrior() constructor.

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sha_lt_params A numeric containing the standard deviations for the normal prior used on the shared short-term discrepancy μ . If a single value is supplied, this is repeated for each variable

truth_params A list containing a prior specification for the processes on the truth $y^{(t)}$. See details of the EnsemblePrior() constructor. The default value is TruthPrior(d).

priors_stan_input A list containing the prior data in the correct form to fit the model in Stan. This information is automatically generated by the constructor.

References

Stan Development Team (2020). RStan: the R interface to Stan. R package version 2.21.2. https://mc-stan.org

Lewandowski, Daniel, Dorota Kurowicka, and Harry Joe. 2009. "Generating Random Correlation Matrices Based on Vines and Extended Onion Method." Journal of Multivariate Analysis 100: 1989–2001.

EnsembleSample

A constructor for the EnsembleSample object

Description

A constructor for the EnsembleSample class. These objects are generated automatically using the generate_sample function.

Usage

EnsembleSample(ensemble_fit, mle, samples)

Arguments

ensemble_fit An EnsembleFit object containing the fitted ensemble model.

mle

An array of dimension $T \times (M+2) \times N_{sample}$ containing MLE point estimates from the ensemble_fit object, where T is the total time, M is the number of simulators and N_{sample} is the number of samples. For each time step, the tth element of the array is a matrix where each column is a sample and the rows are the variables:

$$\left(y^{(t)}, \eta^{(t)}, z_1^{(t)}, z_2^{(t)}, \dots, z_M^{(t)}\right)'$$

where $y^{(t)}$ is the ensemble model's prediction of the latent truth value at time t, $\eta^{(t)}$ is the shared short-term discrepancy at time t, $z_i^{(t)}$ is the individual short-term discrepancy of simulator i at time t.

samples

An array of dimension $T \times (M+2) \times N_{sample}$ containing samples from the ensemble_fit object, where T is the total time, M is the number of simulators and N_{sample} is the number of samples. For each time step, the tth element of the array is a matrix where each column is a sample and the rows are the variables:

$$\left(y^{(t)}, \eta^{(t)}, z_1^{(t)}, z_2^{(t)}, \dots, z_M^{(t)}\right)'$$

where $y^{(t)}$ is the ensemble model's prediction of the latent truth value at time t, $\eta^{(t)}$ is the shared short-term discrepancy at time t, $z_i^{(t)}$ is the individual short-term discrepancy of simulator i at time t.

Value

An object of class EnsembleSample

See Also

EnsembleSample, generate_sample

EnsembleSample-class A class to hold samples of the ensemble model

Description

EnsembleSample objects are generated using the generate_sample function.

Slots

ensemble_fit An EnsembleFit object containing the fitted ensemble model.

mle An array of dimension $T \times (M+2) \times N_{sample}$ containing MLE point estimates from the ensemble_fit object, where T is the total time, M is the number of simulators and N_{sample} is the number of samples. For each time step, the tth element of the array is a matrix where each column is a sample and the rows are the variables:

$$\left(y^{(t)}, \eta^{(t)}, z_1^{(t)}, z_2^{(t)}, \dots, z_M^{(t)}\right)'$$

where $y^{(t)}$ is the ensemble model's prediction of the latent truth value at time t, $\eta^{(t)}$ is the shared short-term discrepancy at time t, $z_i^{(t)}$ is the individual short-term discrepancy of simulator i at time t.

samples An array of dimension $T \times (M+2) \times N_{sample}$ containing samples from the ensemble_fit object, where T is the total time, M is the number of simulators and N_{sample} is the number of samples. For each time step, the tth element of the array is a matrix where each column is a sample and the rows are the variables:

$$\left(y^{(t)}, \eta^{(t)}, z_1^{(t)}, z_2^{(t)}, \dots, z_M^{(t)}\right)'$$

where $y^{(t)}$ is the ensemble model's prediction of the latent truth value at time t, $\eta^{(t)}$ is the shared short-term discrepancy at time t, $z_i^{(t)}$ is the individual short-term discrepancy of simulator i at time t.

See Also

EnsembleSample, generate_sample

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fit_ensemble_model

Fits the ensemble model

Description

fit_ensemble_model runs an MCMC of the ensemble model. This process can take a long time depending on the size of the datasets.

Usage

```
fit_ensemble_model(
  observations,
  simulators,
  priors,
  full_sample = TRUE,
  control = list(adapt_delta = 0.95),
  ...
)
```

Arguments

observations

A list of length 2 containing observations and a covariance matrix. The first element is a data. frame or matrix with each column giving observations of each output of interest and each row a time. Rows should be named with the times and columns should be named the variables. The second element is is a $d \times d$ matrix where d is the number of columns of the observations data frame / matrix. This matrix is the covariance matrix of the observations.

simulators

A list with length equal to the number of simulators. For each simulator, there is a list of 2 objects containing the simulator output and covariance matrix. The first element is a data. frame or matrix with each column giving a simulator outputs of interest and each row a time. Rows should be named with the times and columns should be named the variables. The second element is a $n_k \times n_k$ matrix where n_k is the number of columns of the simulators output data frame / matrix. This matrix is the covariance matrix of the simulator outputs.

priors

An EnsemblePrior object specifying the prior distributions for the ensemble.

full_sample

A logical that runs a full sampling of the posterior density of the ensemble model if TRUE. If FALSE, returns the point estimate which maximises the poste-

rior density of the ensemble model.

control

If creating a full sample, this is a named list of paramaters to control Stan's sampling behaviour. See the documentation of the stan() function in the rstan package for details. The default value is list(adapt_delta = 0.95). If opti-

mizing, this value is ignored.

.. Additional arguments passed to the function rstan::sampling or rstan::optimizing.

Value

An EnsembleFit object.

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References

Stan Development Team (2020). RStan: the R interface to Stan. R package version 2.21.2. https://mc-stan.org

See Also

```
EnsembleFit, EnsembleSample
```

Examples

generate_sample

Generate samples from a fitted ensemble model.

Description

Methods to generates samples of the latent variables from a fitted ensemble model.

Usage

```
generate_sample(fit, num_samples = 1)
get_transformed_data(fit)
get_parameters(ex.fit, x = 1)
get_mle(x = 1, ex.fit, transformed_data, time)
gen_sample(x = 1, ex.fit, transformed_data, time)
```

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Arguments

fit An EnsembleFit object.

num_samples A numeric specifying the number of samples to be generated. The default is 1.

ex.fit A list containing the samples / point estimate from the EnsembleFit object.

x A numeric specifying which sample from the posterior to use. The default is 1.

transformed data

A list of transformed input data.

time A numeric specifying the time for which the ensemble model was run.

Details

The samples are created using the methods described in Strickland et. al. (2009) and Durbin and Koopman (2002).

Value

generate_sample gives a list of length 2, the first element being the MLE of latent variables and the second element being a set of samples of the latent variables.

- If fit is a sampling of the ensemble model parameters, then:
 - mle is a time $\times(3M+2)\times$ num_samples array, where M is the number of simulators and num_samples is the number of samples from the ensemble model, giving the MLE of the latent variables for each available sample from the ensemble model.
 - sample is a time $\times(3M+2)\times$ num_samples array, giving a sample of the latent variables for each available sample of the ensemble model.
- If fit is a point estimate of the ensemble model parameters, then:
 - mle is a time $\times (3M+2) \times 1$ array giving the MLE of the latent variables for the point estimate of the ensemble model.
 - sample is a time $\times (3M+2) \times$ num_samples array, giving num_samples samples of the latent variables for the single point estimate of the ensemble model.

get_transformed_data gives a list of transformed input data.

get_parameters gives a list of ensemble parameters from the requested sample.

get_mle If fit is a sampling of the ensemble model parameters, then this is a time $\times(3M+2)\times$ num_samples array. If fit is a point estimate of the ensemble model parameters, then this is a time $\times(3M+2)\times$ 1 array giving the MLE of the latent variables for the point estimate of the ensemble model.

gen_sample If fit is a sampling of the ensemble model parameters, then this is a time $\times (3M+2) \times$ num_samples array, giving a sample of the latent variables for each available sample of the ensemble model. If fit is a point estimate of the ensemble model parameters, then this is a time $\times (3M+2) \times$ num_samples array.

References

J. Durbin, S. J. Koopman (2002) A simple and efficient simulation smoother for state space time series analysis Biometrika, Volume 89, Issue 3, August 2002, Pages 603–616,

Chris M.Strickland, Ian. W.Turner, RobertDenhamb, Kerrie L.Mengersena. Efficient Bayesian estimation of multivariate state space models Computational Statistics & Data Analysis Volume 53, Issue 12, 1 October 2009, Pages 4116-4125

Examples

get_mcmc_ensemble_model

Return the compiled ensemble model Stan object.

Description

Gets the unfit, compiled stanmodel object encoding the ensemble model. This allows for manual fitting of the ensemble model directly using.

Usage

```
get_mcmc_ensemble_model()
```

Value

The stanmodel object encoding the ensemble model.

Examples

```
mod <- get_mcmc_ensemble_model()
priors <- EnsemblePrior(4)
ensemble_data <- EnsembleData(observations = list(SSB_obs, Sigma_obs),</pre>
```

 ${\tt IndLTPrior}$

Constructor for the EnsemblePrior class

Description

Constructors for the EnsemblePrior class and related classes. These functions are used to encode prior information for the ensemble model. The IndSTPrior, IndLTPrior, ShaSTPrior, and TruthPrior constructors encapsulate prior information.

Usage

```
IndLTPrior(
  parametrisation_form = "lkj",
  var_params = list(1, 1),
  cor_params = 1
)
IndSTPrior(
  parametrisation_form = "hierarchical",
  var_params = list(-3, 1, 8, 4),
  cor_params = list(0.1, 0.1, 0.1, 0.1),
  AR_params = c(2, 2)
)
ShaSTPrior(
  parametrisation_form = "lkj",
  var_params = list(1, 10),
  cor_params = 1,
  AR_params = c(2, 2)
)
TruthPrior(
  d,
  initial_mean = 0,
  initial_var = 100,
  rw_covariance = list(2 * d, diag(d))
)
EnsemblePrior(
```

```
d,
  ind_st_params = IndSTPrior(),
  ind_lt_params = IndLTPrior(),
  sha_st_params = ShaSTPrior(),
  sha_lt_params = 5,
  truth_params = TruthPrior(d)
)
```

Arguments

parametrisation_form

The parametrisation by which the covariance matrix of the noise of the AR process (in the case of IndSTPrior and ShaSTPrior objects or the covariance of the distribution of long-term discrepancies for IndLTPrior objects) is decomposed. The default is hierarchical for IndSTPrior objects, and lkj otherwise. See details.

var_params The parameters characterising the variance of the AR process (in the case of

> IndSTPrior and ShaSTPrior objects or the variance of the distribution of longterm discrepancies for IndLTPrior objects) on the discrepancy. The default value is list(-3, 1, 8, 4) for IndSTPrior objects, list(1, 1) for IndLTPrior

objects, and list(1, 10) for ShaSTPrior objects. See details.

cor_params The parameters characterising the correlations of the AR process (or the distri-

bution of long-term discrepancies) on the short-term discrepancies. The default value is list (0.1,0.1,0.1,0.1) for IndSTPrior objects, and 1 for IndLTPrior

and ShaSTPrior objects. See details.

The parameters giving the beta parameters for the prior distribution on the au-AR_params

to regressive parameter of the AR(1) process. The default is c(2,2). See details.

A numeric specifying the number of variables of interest in the ensemble.

A numeric giving the mean of the normal distribution giving the prior on the initial_mean

initial value of the random walk. This is the same value for each variable Default

value is 0.

A numeric giving the variance of the normal distribution giving the prior on the initial_var

initial value of the random walk. This is the same value for each variable Default

value is 100.

A list of length 2 containing the inverse-Wishart parameters for the covariance rw_covariance

of the random walk of the truth. The default value is list(2*d, diag(d)).

ind_st_params An IndSTPrior object specifying priors for the individual short-term discrep-

ancies $z_k^{(t)}.$ The default value is IndSTPrior("hierarchical", list(-3, 1,

8, 4), list(0.1, 0.1, 0.1, 0.1), c(2, 2)).

ind_lt_params An IndLTPrior object specifying priors for the individual long-term discrepan-

cies γ_k . The default value is IndLTPrior("lkj", list(1, 1), 1).

A ShaSTPrior object specifying priors for the shared short-term discrepancies sha_st_params

 $\eta^{(t)}$. The default value is ShaSTPrior("lkj", list(1, 10), 1, c(2,2)).

A numeric of length d or 1 containing the standard deviations for the normal sha_lt_params prior used on the shared short-term discrepancy μ . If a single value is supplied,

this is repeated for each variable of interest. The default value is 5.

truth_params A TruthPrior object specifying priors for the processes on the truth $y^{(t)}$. The default value is TruthPrior(d).

Details

IndSTPrior and ShaSTPrior discrepancy prior parameter objects contain 4 slots corresponding to:

- parametrisation_form A character specifying how the priors are parametrised. Currently supported priors are 'LKJ', 'inv_wishart', 'beta', or 'hierarchical' ('hierarchical' is only supported for IndSTPrior objects).
- 2. var_params The prior parameters for the discrepancy variances, either a list of length 2 or a numeric of length 4. See below.
- cor_params The correlation matrix parameters, either a list of length 2 or a numeric of length 4. See below.
- 4. AR_params Parameters for the autoregressive parameter as a numeric of length 2.

IndLTPrior discrepancy prior parameter objects contain the slots parametrisation_form, var_params, and cor_params.

There are currently four supported prior distributions on covariance matrices. As in Spence et. al. (2018), the individual and shared short-term discrepancy covariances, Λ_k and Λ_η , as well as the individual long-term discrepancy covariance, Λ_γ , are decomposed into a vector of variances and a correlation matrix

$$\Lambda = \sqrt{\operatorname{diag}(\pi)} P \sqrt{\operatorname{diag}(\pi)},$$

where π is the vector of variances for each variable of interest (VoI), and P is the correlation matrix.

Selecting 'lkj', 'inv_wishart', 'beta', or 'hierarchical' refers to setting LKJ, inverse Wishart, beta, or hierarchical prior distributions on the covariance matrix respectively. The variance parameters should be passed through as the var_params slot of the object and the correlation parameters should be passed through as the cor_params. For 'lkj', 'inv_wishart', and 'beta' selections, variances are parameterised by gamma distributions, so the var_params slot should be a list of length two, where each element gives the shape and rate parameters for each VoI (either as a single value which is the same for each VoI or a numeric with the same length as the number of VoI). For example, setting var_params = list(c(5,6,7,8), c(4,3,2,1)) would correspond to a Gamma(5, 4) prior on the variance of the first VoI, a Gamma(6, 3) prior on the variance of the second VoI, etc... The correlations should be in the following form:

• If '1kj' is selected, then cor_params should be a numeric η giving the LKJ shape parameter, such that the probability density is given by (Lewandowski et. al. 2009)

$$f(\Sigma|\eta) \propto \det(\Sigma)^{\eta-1}$$
.

Variances are parameterised by gamma distributions.

• If 'inv_wishart' is selected, then cor_params should be a list containing a scalar value ν (giving the degrees of freedom) and a symmetric, positive definite matrix Σ (giving the scale matrix). The dimensions of Σ should be the same as the correlation matrix it produces (i.e $d \times d$ where d is the number of VoI). The density of an inverse Wishart is given by

$$f(W|\eta,S) = \frac{1}{2^{\eta d/2} \Gamma_N\left(\frac{\eta}{2}\right)} |S|^{\eta/2} |W|^{-(\eta+d+1)/2} \exp\left(-\frac{1}{2} \mathrm{tr}\left(SW^{-1}\right)\right),$$

where Γ_N is the multivariate gamma function and $\operatorname{tr}(X)$ is the trace of X. Note that inverse Wishart distributions act over the space of all covariance matrices. When used for a correlation matrix, only the subset of valid covariance matrices that are also valid correlation matrices are considered. Variances are parameterised by gamma distributions.

• If 'beta' is selected, then cor_params should be a list containing two symmetric $d \times d$ matrices A and B giving the prior success parameters and prior failure parameters respectively. The correlation between the ith and jth VoI is $\rho_{i,j}$ with

$$\frac{1}{\pi} \tan^{-1} \frac{\rho_{i,j}}{\sqrt{1 - \rho_{i,j}^2}} + \frac{1}{2} \sim \text{beta}(A_{i,j}, B_{i,j}).$$

Variances are parameterised by gamma distributions.

• If 'hierarchical' is selected, then variances are parameterised by log-normal distributions:

$$\log \pi_{k,i} \sim N(\mu_i, \sigma_i^2)$$

with priors

$$\mu_i \sim N(\alpha_{\pi}, \beta_{\pi}),$$

$$\sigma_i^2 \sim \text{InvGamma}(\gamma_\pi, \delta_\pi).$$

The var_params slot should then be a numeric of length 4, giving the α_{π} , β_{π} , γ_{π} , δ_{π} hyperparameters respectively. Correlations ($\rho_{k,i,j}$ where $\rho_{k,i,j}$ is the correlation between VoI i and j for the kth simulator) are parameterised by hierarchical beta distributions.

$$\frac{\rho_{k,i,j}+1}{2} \sim \text{beta}(c_{k,i,j}, d_{k,i,j})$$

with priors

$$c_{k,i,j} \sim \operatorname{gamma}(\alpha_{\rho}, \beta_{\rho}),$$

$$d_{k,i,j} \sim \operatorname{gamma}(\gamma_{\rho}, \delta_{\rho}).$$

The cor_params slot should be a numeric of length 4 giving the $\alpha_{\rho}, \beta_{\rho}, \gamma_{\rho}, \delta_{\rho}$ hyperparameters. respectively. NOTE: This options is only supported for the individual short-term discrepancy terms.

Priors may also be specified for the autoregressive parameters for discrepancies modelled using autoregressive processes (i.e. for IndSTPrior and ShaSTPrior objects). These are parametrised via beta distributions such that the autoregressive parameter $R \in (-1, 1)$ satisfies

$$\frac{R+1}{2} \sim \text{Beta}(\alpha, \beta)$$

.

In addition to priors on the discrepancy terms, it is also possible to add prior information on the truth. We require priors on the truth at t=0. By default, a N(0,10) prior is used on the initial values., however this can be configured by the truth_params argument. The covariance matrix of the random walk of the truth Λ_y can be configured using an inverse-Wishart prior. The truth_params argument should be a TruthPrior object.

Value

EnsemblePrior returns an object of class EnsemblePrior. IndSTPrior returns an object of class IndSTPrior. IndLTPrior returns an object of class IndLTPrior. ShaSTPrior returns an object of class ShaSTPrior. TruthPrior returns an object of class TruthPrior.

References

Spence et. al. (2018). A general framework for combining ecosystem models. *Fish and Fisheries*, 19(6):1031-1042.

Examples

```
##### Different forms of the individual long term discrepancy priors
#LKJ(10) priors on correlation matrices and gamma(5, 3) priors on the variances
ist_lkj <- IndSTPrior("lkj", list(5, 3), 10)#</pre>
#Same as above but with an additional beta(2, 4) prior on
#the autoregressive parameter of the AR process.
ist_lkj <- IndSTPrior("lkj", list(5, 3), 10, AR_params = c(2, 4))</pre>
#Same as above but with different variance priors for 5 different variables of interest.
#This encodes that there is a gamma(1, 1) prior on the variance of the first variable,
#a gamma(23, 1) on the second variable etc...
ist_lkj \leftarrow IndSTPrior("lkj", list(c(1,23,24,6,87), c(1,1,1,1,5)), 10, AR_params = c(2, 4))
#Hierarchical priors with gamma(1,2) and gamma(10, 1) on the variance hyperparameters and
\#gamma(3,4), gamma(5,6) on the correlation hyperparameters
ist_hie <- IndSTPrior("hierarchical", list(1,2,10,1), list(3,4,5,6))</pre>
#Beta priors via the method of concordance. We have gamma(5,3) priors on the variance
# and beta(40,40) on each of the correlations in the correlation matrix.
ist_bet <- IndSTPrior("beta", list(5, 3), list(matrix(40, 5, 5), matrix(40, 5, 5)))</pre>
#Inverse Wishart correlation priors. Gamma(2, 1/3) priors are on the variances and
#inv-Wishart(5, diag(5)) on the correlation matrices.
ist_inW <- IndSTPrior("inv_wishart", list(2, 1/3), list(5, diag(5)))</pre>
##### TruthPrior
#Simple default truth prior with 7 variables of interest
truth_def <- TruthPrior(7)</pre>
# A more fine-tuned truth prior for an ensemble with 7 species.
truth_cus <- TruthPrior(7, initial_mean = 2, initial_var = 10, rw_covariance = list(10, diag(7)))</pre>
#The default priors for an ensemble with 8 variables of interest
priors <- EnsemblePrior(8)</pre>
#With 4 variables of interest.
priors <- EnsemblePrior(4)</pre>
#Defining custom priors for a model with 4 species.
num_species <- 5</pre>
priors <- EnsemblePrior(</pre>
```

18 IndLTPrior-class

IndLTPrior-class

A class to hold the priors for the ensemble model.

Description

An IndLTPrior object encapsulates the prior information for the long-term discrepancies of the individual simulators within the ensemble model.

Details

Individual long-term discrepancies γ_k are drawn from a distribtion

$$\gamma_k \sim N(0, C_{\gamma}).$$

Accepted parametrisation forms for this discrepancy are lkj, beta, or inv_wishart. See details of the EnsemblePrior() constructor for more details.

Slots

parametrisation_form The parametrisation by which the covariance matrix of the noise of the AR process is decomposed.

var_params The parameters characterising the variance of the distribution of the individual longterm discrepancy.

cor_params The parameters characterising the correlations of the distribution of the individual long-term discrepancy.

See Also

IndSTPrior, ShaSTPrior, TruthPrior,

IndSTPrior-class 19

IndSTPrior-class

A class to hold the priors for the ensemble model.

Description

An IndSTPrior object encapsulates the prior information for the short-term discrepancies of the individual simulators within the ensemble model.

Details

Individual short-term discrepancies $z_k^{(t)}$ are modelled as an AR(1) process so that

$$z_k^{(t+1)} \sim N(R_k z_k^{(t)}, \Lambda_k).$$

Accepted parametrisation forms for this discrepancy are lkj, beta, inv_wishart, or hierarchical. See details of the EnsemblePrior() constructor for more details.

Slots

AR_param The parameters giving the beta parameters for the autoregressive parameter of the AR(1) process.

parametrisation_form The parametrisation by which the covariance matrix of the noise of the AR process is decomposed.

var_params The parameters characterising the variance of the AR process on the individual short-term discrepancy.

cor_params The parameters characterising the correlations of the AR process on the individual short-term discrepancy.

See Also

IndLTPrior, ShaSTPrior, TruthPrior,

plot.EnsembleSample

Plot the ensemble output

Description

Plots the latent variables predicted by the ensemble model, along with simulator outputs and observations.

Usage

```
## S3 method for class 'EnsembleSample'
plot(x, variable = NULL, quantiles = c(0.05, 0.95), ...)
```

Arguments

X	An EnsembleSample object.
variable	The name of the variable to plot. This can either be a character string in the same form as the observation variable, or an index for the column in the observations data frame.
quantiles	A numeric vector of length 2 giving the quantiles for which to plot ribbons if doing a full sampling of the ensemble model. The default is $c(0.05,0.95)$.
	Other arguments passed on to methods. Not currently used.

Value

The ggplot object.

Examples

```
fit <- fit_ensemble_model(observations = list(SSB_obs, Sigma_obs),</pre>
                           simulators = list(list(SSB_ewe, Sigma_ewe, "EwE"),
                                              list(SSB_fs, Sigma_fs, "FishSUMS"),
                                               list(SSB_lm, Sigma_lm, "LeMans"),
                                               list(SSB_miz, Sigma_miz, "Mizer")),
                           priors = EnsemblePrior(4))
samples <- generate_sample(fit)</pre>
plot(samples)
plot(samples, variable = "Cod", quantiles=c(0.2, 0.8))
fit_point <-fit_ensemble_model(observations = list(SSB_obs, Sigma_obs),</pre>
                                simulators = list(list(SSB_ewe, Sigma_ewe, "EwE"),
                                              list(SSB_fs, Sigma_fs, "FishSUMS"),
list(SSB_lm, Sigma_lm, "LeMans"),
                                               list(SSB_miz, Sigma_miz, "Mizer")),
                                 priors = EnsemblePrior(4),
                                 full_sample = FALSE)
samples1 <- generate_sample(fit_point)</pre>
plot(samples1, variable="Herring")
```

prior_ensemble_model Generate samples of parameters from prior distribution

Description

Methods to generates samples of the parameters from the prior distribution of the ensemble model.

prior_ensemble_model 21

Usage

```
prior_ensemble_model(
  priors,
  M = 1,
  full_sample = TRUE,
  control = list(adapt_delta = 0.95),
  ...
)
```

Arguments

priors An EnsemblePrior object specifying the prior distributions for the ensemble.

M A numeric that represents the number of simulators. The default is 1.

full_sample A logical that runs a full sampling of the prior density of the ensemble model

if TRUE. If FALSE, returns the point estimate which maximises the prior density

of the ensemble model.

control If creating a full sample, this is a named list of paramaters to control Stan's

sampling behaviour. See the documentation of the stan() function in the rstan package for details. The default value is list(adapt_delta = 0.95). If opti-

mizing, this value is ignored.

... Additional arguments passed to the function rstan::sampling or rstan::optimizing.

Value

A list containing two items named samples and point_estimate. If full_sample==TRUE, samples is a stanfit and point_estimate is a NULL object, else samples is a NULL and point_estimate is a list object.

References

Stan Development Team (2020). RStan: the R interface to Stan. R package version 2.21.2. https://mc-stan.org

See Also

```
EnsembleFit
```

Examples

```
priors <- EnsemblePrior(4)
prior_density <- prior_ensemble_model(priors, M = 4)</pre>
```

22 sample_prior

sample_prior

Generate samples of latent variables from prior predictive distribution

Description

Methods to generates samples of the latent variables from the prior predictive distribution of the ensemble model.

Usage

```
sample_prior(
  observations,
  simulators,
  priors,
  sam_priors,
  num_samples = 1,
  full_sample = TRUE,
  ...
)
```

Arguments

observations

A list of length 2 containing observations and a covariance matrix. The first element is a data.frame or matrix with each column giving observations of each output of interest and each row a time. Rows should be named with the times and columns should be named the variables. The second element is is a $d \times d$ matrix where d is the number of columns of the observations data frame / matrix. This matrix is the covariance matrix of the observations.

simulators

A list with length equal to the number of simulators. For each simulator, there is a list of 2 objects containing the simulator output and covariance matrix. The first element is a data. frame or matrix with each column giving a simulator outputs of interest and each row a time. Rows should be named with the times and columns should be named the variables. The second element is a $n_k \times n_k$ matrix where n_k is the number of columns of the simulators output data frame / matrix. This matrix is the covariance matrix of the simulator outputs.

priors

An EnsemblePrior object specifying the prior distributions for the ensemble.

sam_priors

A list containing two items named samples and point_estimate. samples is either a NULL or a stanfit object containing the samples drawn from the prior distribution of the ensemble model and point_estimate is either a NULL or a list object containing the optimised prior distribution of the ensemble model. If this object is missing then sample_prior generates it.

num_samples
full_sample

A numeric specifying the number of samples to be generated. The default is 1. A logical that runs a full sampling of the prior density of the ensemble model if TRUE. If FALSE, returns the point estimate which maximises the prior density of the ensemble model.

. . .

Additional arguments passed to the function rstan::sampling or rstan::optimizing.

ShaSTPrior-class 23

Details

The samples are created using the methods described in Strickland et. al. (2009) and Durbin and Koopman (2002).

Value

An EnsembleSample object.

References

J. Durbin, S. J. Koopman (2002) A simple and efficient simulation smoother for state space time series analysis Biometrika, Volume 89, Issue 3, August 2002, Pages 603-616,

Chris M.Strickland, Ian. W.Turner, RobertDenhamb, Kerrie L.Mengersena. Efficient Bayesian estimation of multivariate state space models Computational Statistics & Data Analysis Volume 53, Issue 12, 1 October 2009, Pages 4116-4125

See Also

EnsembleFit, EnsembleSample, generate_sample, prior_ensemble_model

Examples

ShaSTPrior-class

A class to hold the priors for the ensemble model.

Description

An ShaSTPrior object encapsulates the prior information for the short-term discrepancies of the shared discrepancy of the ensemble model.

Details

Shared short-term discrepancies $\eta^{(t)}$ are modelled as an AR(1) process so that

$$\eta^{(t+1)} \sim N(R_{\eta}\eta, \Lambda_{\eta}).$$

Accepted parametrisation forms for this discrepancy are lkj, beta, or inv_wishart. See details of the EnsemblePrior() constructor for more details.

24 Sigma_fs

Slots

AR_param The parameters giving the beta parameters for the main parameter of the AR(1) process.

parametrisation_form The parametrisation by which the covariance matrix of the noise of the AR process is decomposed.

var_params The parameters characterising the variance of the AR process on the shared short-term discrepancy.

cor_params The parameters characterising the correlations of the AR process on the shared short-term discrepancy.

Sigma_ewe

Ecopath with EcoSim Sigma

Description

A 4x4 covariance matrix quantifying the parameter uncertainty of Ecopath with EcoSim

Usage

Sigma_ewe

Format

A 4x4 matrix.

References

Mackinson, S., Platts, M., Garcia, C., and Lynam, C. (2018). Evaluating the fishery and ecological consequences of the proposed North Sea multi-annual plan. PLOS ONE, 13(1), 1–23.

Sigma_fs

FishSUMS Sigma

Description

A 3x3 covariance matrix quantifying the parameter uncertainty of FishSUMS

Usage

Sigma_fs

Format

A 3x3 matrix.

Sigma_lm 25

References

Spence, M. A., Blanchard, J. L., Rossberg, A. G., Heath, M. R., Heymans, J. J., Mackinson, S., Serpetti, N., Speirs, D. C., Thorpe, R. B., and Blackwell, P. G. (2018). A general framework for combining ecosystem models. Fish and Fisheries, 19(6), 1031–1042.

Sigma_lm

LeMans Sigma

Description

LeMans Sigma

Usage

Sigma_lm

Format

A 4x4 matrix. A 4x4 covariance matrix quantifying the parameter uncertainty of LeMans

References

Thorpe, R. B., Le Quesne, W. J. F., Luxford, F., Collie, J. S., and Jennings, S. (2015). Evaluation and management implications of uncertainty in a multispecies size-structured model of population and community responses to fishing. Methods in Ecology and Evolution, 6(1), 49–58.

Sigma_miz

mizer Sigma

Description

mizer Sigma

Usage

Sigma_miz

Format

A 4x4 matrix. A 4x4 covariance matrix quantifying the parameter uncertainty of mizer

References

Spence, M. A., Blackwell, P. G., and Blanchard, J. L. (2016). Parameter uncertainty of a dynamic multispecies size spectrum model. Canadian Journal of Fisheries and Aquatic Sciences, 73(4), 589–59

SSB_ewe

Sigma_obs

Stock assessment Sigma

Description

A 4x4 covariance matrix quantifying the covariances of the stock assessment estimates of biomass.

Usage

Sigma_obs

Format

A 4x4 matrix.

References

Herring Assessment Working Group for the Area South of 62 N (HAWG). Technical report, ICES Scientific Reports. ACOM:07. 960 pp, ICES, Copenhagen.

Report of the Working Group on the Assessment of Demersal Stocks in the North Sea and Skagerrak. Technical report, ICES Scientific Reports. ACOM:22.pp, ICES, Copenhagen.

SSB_ewe

Ecopath with EcoSim SSB

Description

A dataset containing the predictions for spawning stock biomass of Norway Pout, Herring, Cod, and Sole in the North Sea between 1991-2050 under an MSY fishing scenario from EcoPath with EcoSim.

Usage

SSB_ewe

Format

A data. frame with 60 rows and 4 variables:

N. pout Spawning stock biomass of Norway Pout, in log tonnes.

Herring Spawning stock biomass of Herring, in log tonnes.

Cod Spawning stock biomass of Cod, in log tonnes.

Sole Spawning stock biomass of Sole, in log tonnes.

SSB_fs 27

References

ICES (2016). Working Group on Multispecies Assessment Methods (WGSAM). Technical report, International Council for Exploration of the Seas.

SSB_fs

FishSUMS SSB

Description

A data frame containing the predictions for spawning stock biomass of Norway Pout, Herring, and Cod in the North Sea between 1984-2050 under an MSY fishing scenario from FishSUMS. Note that FishSUMS does not produce outputs for Sole.

Usage

SSB_fs

Format

A data. frame with 67 rows and 3 variables:

N. pout Spawning stock biomass of Norway Pout, in log tonnes.

Herring Spawning stock biomass of Herring, in log tonnes.

Cod Spawning stock biomass of Cod, in log tonnes.

References

Speirs, D., Greenstreet, S., and Heath, M. (2016). Modelling the effects of fishing on the North Sea fish community size composition. Ecological Modelling, 321, 35–45

 SSB_1m

LeMans SSB

Description

A data.frame containing the predictions for spawning stock biomass of Norway Pout, Herring, Cod, and Sole in the North Sea between 1986-2050 under an MSY fishing scenario from the LeMaRns package.

Usage

 SSB_1m

28 SSB_miz

Format

A data. frame with 65 rows and 4 variables:

N. pout Spawning stock biomass of Norway Pout, in log tonnes.

Herring Spawning stock biomass of Herring, in log tonnes.

Cod Spawning stock biomass of Cod, in log tonnes.

Sole Spawning stock biomass of Sole, in log tonnes.

References

Thorpe, R. B., Le Quesne, W. J. F., Luxford, F., Collie, J. S., and Jennings, S. (2015). Evaluation and management implications of uncertainty in a multispecies size-structured model of population and community responses to fishing. Methods in Ecology and Evolution, 6(1), 49–58.

SSB_miz

mizer SSB

Description

A data.frame containing the predictions for spawning stock biomass of Norway Pout, Herring, Cod, and Sole in the North Sea between 1984-2050 under an MSY fishing scenario from mizer.

Usage

SSB_miz

Format

A data frame with 67 rows and 4 variables:

N. pout Spawning stock biomass of Norway Pout, in log tonnes.

Herring Spawning stock biomass of Herring, in log tonnes.

Cod Spawning stock biomass of Cod, in log tonnes.

Sole Spawning stock biomass of Sole, in log tonnes.

References

Blanchard, J. L., Andersen, K. H., Scott, F., Hintzen, N. T., Piet, G., and Jennings, S. (2014). Evaluating targets and trade-offs among fisheries and conservation objectives using a multispecies size spectrum model. Journal of Applied Ecology, 51(3), 612–622

SSB_obs 29

SSB_obs	Stock assessment SSB	

Description

A data. frame containing the single species stock assessment estimates of spawning stock biomass of Norway Pout, Herring, Cod, and Sole in the North Sea between 1984-2017.

Usage

SSB_obs

Format

A data frame with 34 rows and 4 variables:

N. pout Spawning stock biomass of Norway Pout, in log tonnes.

Herring Spawning stock biomass of Herring, in log tonnes.

Cod Spawning stock biomass of Cod, in log tonnes.

Sole Spawning stock biomass of Sole, in log tonnes.

References

Herring Assessment Working Group for the Area South of 62 N (HAWG)(2020). Technical report, ICES Scientific Reports. ACOM:07. 960 pp, ICES, Copenhagen.

Report of the Working Group on the Assessment of Demersal Stocks in the North Sea and Skagerrak (2020). Technical report, ICES Scientific Reports. ACOM:22.pp, ICES, Copenhagen.

TruthPrior-class A class to hold the priors for the truth model in the ensemble framework

Description

An TruthPrior object encapsulates the prior information for the short-term discrepancies of the shared discrepancy of the ensemble model.

Details

The truth $\mathbf{y}^{(t)}$ is modelled as a random walk such that

$$\mathbf{y}^{(t+1)} \sim N(\mathbf{y}^{(t)}, \Lambda_y).$$

The covariance matrix Λ_y is parameterised by an inverse Wishart distribution (contained in the rw_covariance slot) and the initial value is modelled as drawn from a normal distribution.

Slots

- d A numeric giving the number of variables of interest in the ensemble model.
- initial_mean A numeric giving the standard deviation of the normal prior on the initial mean value of the random walk. This is the same standard deviation for each variable of interest.
- initial_var A list of length 2 containing the shape and scale parameters (respectively) for the gamma priors on the variance of the initial value of the truth.
- rw_covariance A list of length 2 containing the inverse-Wishart parameters for the covariance of the random walk of the truth.

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