# Package 'FastCUB'

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Title Fast EM and Best-Subset Selection for CUB Models for Rating Data

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Description For ordinal rating data, consider the accelerated Expectation-Maximization algorithm to estimate and test models within the family of CUB models (where CUB stands for Combination of a discrete Uniform and a shifted Binomial distributions). The procedure is built upon Louis' identity for the observed information matrix. Best-subset variable selection for CUB regression models is then implemented on such basis. The methods here implemented are illustrated and discussed in the preprint available from Researchgate by Simone R. (2020) <https://tinyurl.com/vvk563e>.

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```
bestcub
```

Best-subset variable selection for CUB models via fast EM algorithm

## Description

Perform a best-subset search for CUB models on the basis of the BIC index, by combining all possible covariates' specification for feeling and for uncertainty parameters

## Usage

```
bestcub(ordinal,m,Y,W,toler=1e-4,maxiter=200,iterc=5,alpha=0.05,mix=FALSE,
tolmix=1e+2,fmix=NULL,invgen=TRUE,verbose=FALSE)
```

#### Arguments

ordina	Vector of ordinal responses	
m	Number of ordinal categories	
Y	Matrix of selected covariates for the uncertain	ty parameter
W	Matrix of selected covariates for the feeling p	arameter
toler	Fixed convergence tolerance for final estimate	es
maxit	Maximum number of iterations allowed for ru	nning the optimization algorithm
iterc	Iteration from which the acceleration strategy	starts
alpha	Significant level for Wald test	
mix	Logical: should a first preliminary standard E (default is FALSE)	M be run at toler equal to tolmix?

## bestcub

tolmix	Convergence tolerance for first preliminary EM (if mix=TRUE).
fmix	Fraction of iteration needed for first preliminary EM (if mix=TRUE). Default is null.
invgen	Logical: should the recursive formula for the inverse of the information matrix be considered? (Default is TRUE)
verbose	Logical: should messages about acceleration steps be printed out? (Default is FALSE)

## Value

A list containing the following results:

vsel	List of all estimated models (with the accelerated EM) as FastCUB objects
bestmodel	FastCUB object corresponding to the best CUB model (according to BIC), if not null
bestW	Names of covariates for feeling in the best model with all significant effect
bestY	Names of covariates for feeling in the best model with all significant effect
param	ML estimates of the best model
se	Estimated standard errors for the best model
bic	BIC index of the best (significant) model
mattime	Matrix of computational time for each of the estimated model
matiter	Matrix of number of iterations occurred for each of the estimated model

## See Also

fastCUB

## Examples

```
library(FastCUB)
data(univer)
ordinal<-univer$global
m<-7
Y<-univer[,c(2,3,4)]
W<-univer[,8:11]
## Search for the best CUB model with covariates only for feeling
best0q<-bestcub(ordinal,m,Y=NULL,W,toler=1e-4,maxiter=100,iterc=5,alpha=0.05,invgen=TRUE)
## Search for the best CUB model with covariates only for uncertainty
bestp0<-bestcub(ordinal,m,Y,W=NULL,toler=1e-4,maxiter=100,iterc=5,alpha=0.05,invgen=TRUE)
## Search for the best CUB model with covariates for both parameters
bestpq<-bestcub(ordinal,m,Y,W,toler=1e-4,maxiter=100,iterc=5,alpha=0.05,invgen=TRUE,
    mix=TRUE,tolmix=1e+3,fmix=1)
final<-bestpq$bestmodel; summary(final)</pre>
```

BIC.fastCUB

## Description

S3 BIC method for objects of class fastCUB.

## Usage

## S3 method for class 'fastCUB'
BIC(object, ...)

## Arguments

object	An object of class "fastCUB"
	Other arguments

## Value

BIC index for the fitted model.

## See Also

logLik, fastCUB

bi	tc	si
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Shifted Binomial probabilities of ordinal responses

## Description

Compute the shifted Binomial probabilities of ordinal responses.

#### Usage

bitcsi(m,ordinal,csi)

## Arguments

m	Number of ordinal categories
ordinal	Vector of ordinal responses
csi	Feeling parameter of the shifted Binomial distribution

#### Value

A vector of the same length as ordinal, where each entry is the shifted Binomial probability of the corresponding observation.

## bitgama

#### References

Piccolo D. (2003). On the moments of a mixture of uniform and shifted binomial random variables, *Quaderni di Statistica*, **5**, 85–104

## See Also

probcub00, probcubp0, probcub0q

## Examples

```
data(univer)
m<-7
csi<-0.7
ordinal<-univer$informat
pr<-bitcsi(m,ordinal,csi)</pre>
```

```
bitgama
```

Shifted Binomial distribution with covariates

### Description

Return the shifted Binomial probabilities of ordinal responses where the feeling component is explained by covariates via a logistic link.

#### Usage

bitgama(m,ordinal,W,gama)

#### Arguments

m	Number of ordinal categories
ordinal	Vector of ordinal responses
W	Matrix of covariates for the feeling component
gama	Vector of parameters for the feeling component, with length equal to NCOL(W)+1 to account for an intercept term (first entry of gama)

## Value

A vector of the same length as ordinal, where each entry is the shifted Binomial probability for the corresponding observation and feeling value.

#### See Also

logis, probcub0q, probcubpq

## Examples

```
n<-100
m<-7
W<-sample(c(0,1),n,replace=TRUE)
gama<-c(0.2,-0.2)
csivett<-logis(W,gama)
ordinal<-rbinom(n,m-1,csivett)+1
pr<-bitgama(m,ordinal,W,gama)</pre>
```

coef.fastCUB

## S3 Method: coef for class "fastCUB"

## Description

S3 method: coef for objects of class fastCUB.

## Usage

## S3 method for class 'fastCUB'
coef(object, ...)

## Arguments

object	An object of class fastCUB
	Other arguments

## Details

Returns estimated values of coefficients of the fitted model

## Value

ML estimates of parameters of the fitted CUB model.

## See Also

fastCUB, summary

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cormat

## Description

Compute parameter correlation matrix for estimated model as returned by an object of class "fastCUB".

## Usage

```
cormat(object,digits=options()$digits)
```

## Arguments

object	An object of class "fastCUB"
digits	Number of significant digits to be printed. Default is options()\$digits

## Value

Parameters correlation matrix for fitted fastCUB models.

## See Also

fastCUB, vcov

dissim

Normalized dissimilarity measure

## Description

Compute the normalized dissimilarity measure between observed relative frequencies and estimated (theoretical) probabilities of a discrete distribution.

#### Usage

dissim(proba,probb)

## Arguments

proba	Vector of observed relative frequencies
probb	Vector of estimated (theoretical) probabilities

#### Value

Numeric value of the dissimilarity index, assessing the distance to a perfect fit.

## Examples

```
proba<-c(0.01,0.03,0.08,0.07,0.27,0.37,0.17)
probb<-c(0.04,0.04,0.05,0.10,0.21,0.32,0.24)
dissim(proba,probb)
```

fastCUB

Main function for fast estimation CUB models

## Description

Main function to estimate and validate a CUB model for explaining uncertainty and feeling for given ratings, with or without covariates, on the basis of Louis' identity for the information matrix and the derived accelerated estimation.

## Usage

```
fastCUB(Formula, data, mix=FALSE, tolmix=1e+2,fmix= NULL,...)
```

#### Arguments

Formula	Object of class Formula with two right-hand side: the first for uncertainty co- variates, the second for feeling covariates.
data	Data frame from which model matrices and response variables are taken.
mix	Logical: should a first preliminary standard EM be run at toler equal to tolmix? (default is FALSE).
tolmix	Convergence tolerance for first preliminary EM (if mix=TRUE).
fmix	Fraction of iteration needed for preliminary EM (if mix=TRUE). Default is null.
	Additional arguments to be passed for the specification of the model and the acceleration steps.

## Details

This is the main function for CUB models, which calls for the corresponding functions whenever covariates are specified. It performs maximum likelihood estimation via the E-M algorithm for CUB models and extensions based on the Louis' identity for the observed information matrix.

#### Value

An object of the class "fastCUB": returns a list containing the following results:

estimates	Maximum likelihood estimates of model parameters
loglik	Log-likelihood function at the final estimates
varmat	Variance-covariance matrix of final estimates
niter	Number of executed iterations
BIC	BIC index for the estimated model
parnames	Names for model parameters

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## fastCUB\_package

## See Also

probcub00, probcubp0, probcub0q, probcubpq

#### Examples

```
library(FastCUB)
data(univer)
ordinal<-univer$global
m<-7
effe<-with(univer, Formula(global~0|gender+freqserv+age +changefa))
cub0q<-fastCUB(effe,data=univer,m=7, maxiter=100,toler=1e-8,mix=TRUE,verbose=FALSE)
summary(cub0q)
## Fast EM for CUB model with covariates only for uncertainty
effe<-with(univer, Formula(global~gender+freqserv+age +changefa|0))
cubp0<-fastCUB(effe,data=univer,m=7, maxiter=100,toler=1e-8,iterc=5,verbose=TRUE)
## Fast EM for CUB model with covariates for both feeling and uncertainty
effe<-with(univer, Formula(global~gender+freqserv+age +changefa|gender+freqserv+age +changefa))
cubpq<-fastCUB(effe,data=univer,m=7, maxiter=100,toler=1e-8,iterc=5)
summary(cubpq)
BIC(cubpq)</pre>
```

fastCUB\_package fastCUB package

#### Description

The package implements Louis' identity for CUB models for rating data, to retrieve the observed information matrix within the Expectation-Maximization algorithm. On this basis, an acceleration strategy is derived and then a best-subset search through the covariate space for feeling and uncertainty is implemented.

## Details

Package:	fastCUB
Туре:	Package
Version:	0.0.2
Date:	2019-03-05
License: GPL-2   GPL-3	

#### Author(s)

Rosaria Simone

#### References

Louis T.A. (1982). Finding the Observed Information Matrix when Using the EM Algorithm, *Journal of the Royal Statistical Society, Series B*, **44**, 226–233

Simone R. (2020). An Accelerated EM algorithm for mixture models with uncertainty for rating data. *under Review* 

fitted.fastCUB S3 method "fitted" for class "fastCUB"

#### Description

S3 method fitted for objects of class fastCUB.

#### Usage

## S3 method for class 'fastCUB'
fitted(object, ...)

#### Arguments

object	An object of class fastCUB
	Other arguments

## Details

Returns the fitted probability distribution for GEM models with no covariates. If only one dichotomous covariate is included in the model to explain some components, it returns the fitted probability distribution for each profile.

#### See Also

fastCUB

inibest

Preliminary estimators for CUB models without covariates

#### Description

Compute preliminary parameter estimates of a CUB model without covariates for given ordinal responses. These preliminary estimators are used within the package code to start the E-M algorithm.

#### Usage

inibest(m,freq)

## inibestgama

#### Arguments

m	Number of ordinal categories
freq	Vector of the absolute frequencies of given ordinal responses

## Value

A vector  $(\pi, \xi)$  of the initial parameter estimates for a CUB model without covariates, given the absolute frequency distribution of ordinal responses

## References

Iannario M. (2009). A comparison of preliminary estimators in a class of ordinal data models, *Statistica & Applicazioni*, **VII**, 25–44

Iannario M. (2012). Preliminary estimators for a mixture model of ordinal data, *Advances in Data Analysis and Classification*, **6**, 163–184

## See Also

#### inibestgama

## Examples

```
m<-9
freq<-c(10,24,28,36,50,43,23,12,5)
estim<-inibest(m,freq)
pai<-estim[1]
csi<-estim[2]</pre>
```

inibestgama	Preliminary parameter estimates of a CUB model with covariates for
	feeling

#### Description

Compute preliminary parameter estimates for the feeling component of a CUB model fitted to ordinal responses These estimates are set as initial values for parameters to start the E-M algorithm.

## Usage

inibestgama(m,ordinal,W)

#### Arguments

m	Number of ordinal categories
ordinal	Vector of ordinal responses
W	Matrix of selected covariates for explaining the feeling component

## Value

A vector of length equal to NCOL(W)+1, whose entries are the preliminary estimates of the parameters for the feeling component, including an intercept term as first entry.

#### References

Iannario M. (2008). Selecting feeling covariates in rating surveys, *Rivista di Statistica Applicata*, **20**, 103–116

Iannario M. (2009). A comparison of preliminary estimators in a class of ordinal data models, *Statistica & Applicazioni*, **VII**, 25–44

Iannario M. (2012). Preliminary estimators for a mixture model of ordinal data, *Advances in Data Analysis and Classification*, **6**, 163–184

#### See Also

#### inibest

#### Examples

```
data(univer)
m<-7; ordinal<-univer$global; cov<-univer$gender
ini<-inibestgama(m,ordinal,W=cov)</pre>
```

invmatge	n

Recursive computation of the inverse of a matrix

#### Description

Compute the variance-covariance matrix of the incomplete score vector involved in Louis' identity for the observed information matrix

## Usage

invmatgen(G,H,listE)

#### Arguments

G	Primary matrix for the sum decomposition of \$G+H\$
Н	Secondary matrix for the sum decomposition of $G+H$
listE	Auxiliary matrices that sum up to H

#### Value

The inverse of matrix G + H computed recursively thanks to matrices listed in listE

## logis

## References

Miller K. (1981). On the inverse of the sum of matrices, Mathematics Magazine, 54, 67-72

#### See Also

fastCUB

logis

The logistic transform

## Description

Create a matrix YY binding array Y with a vector of ones, placed as the first column of YY. It applies the logistic transform componentwise to the standard matrix multiplication between YY and param.

#### Usage

logis(Y,param)

#### Arguments

Y	A generic matrix or one dimensional array
param	Vector of coefficients, whose length is $NCOL(Y) + 1$ (to consider also an intercept term)

## Value

Return a vector whose length is NROW(Y) and whose i-th component is the logistic function at the scalar product between the i-th row of YY and the vector param.

## Examples

```
n<-50
Y<-sample(c(1,2,3),n,replace=TRUE)
param<-c(0.2,0.7)
logis(Y,param)</pre>
```

logLik.fastCUB

#### Description

S3 method: logLik() for objects of class "fastCUB".

## Usage

```
## S3 method for class 'fastCUB'
logLik(object, ...)
```

#### Arguments

object	An object of class "fastCUB"
	Other arguments

## Value

Log-likelihood at the final ML estimates for parameters of the fitted fastCUB model.

### See Also

fastCUB

makeplot

Plot facilities for fastCUB objects

## Description

Plot facilities for objects of class "fastCUB".

#### Usage

makeplot(object)

## Arguments

object An object of class "fastCUB"

## Details

Returns a plot comparing fitted probabilities and observed relative frequencies for GEM models without covariates. If only one explanatory dichotomous variable is included in the model for one or all components, then the function returns a plot comparing the distributions of the responses conditioned to the value of the covariate.

print.fastCUB

## Description

S3 method print for objects of class fastCUB.

#### Usage

```
## S3 method for class 'fastCUB'
print(x, ...)
```

## Arguments

х	An object of class fastCUB
	Other arguments

## Value

Brief summary results of the fitting procedure, including parameter estimates, their standard errors and the executed call.

probbit	Probability distribution of a shifted Binomial random variable
---------	--

## Description

Return the shifted Binomial probability distribution.

## Usage

probbit(m,csi)

## Arguments

m	Number of ordinal categories
csi	Feeling parameter

## Value

The vector of the probability distribution of a shifted Binomial model.

## See Also

bitcsi, probcub00

## Examples

```
m<-7
csi<-0.7
pr<-probbit(m,csi)
plot(1:m,pr,type="h",main="Shifted Binomial probability distribution",xlab="Categories")
points(1:m,pr,pch=19)</pre>
```

```
probcub00
```

Probability distribution of a CUB model without covariates

#### Description

Compute the probability distribution of a CUB model without covariates.

#### Usage

probcub00(m,pai,csi)

## Arguments

m	Number of ordinal categories
pai	Uncertainty parameter
csi	Feeling parameter

### Value

The vector of the probability distribution of a CUB model.

## References

Piccolo D. (2003). On the moments of a mixture of uniform and shifted binomial random variables. *Quaderni di Statistica*, **5**, 85–104

## See Also

bitcsi, probcub0q, probcubp0, probcubpq

## Examples

```
m<-9
pai<-0.3
csi<-0.8
pr<-probcub00(m,pai,csi)
plot(1:m,pr,type="h",main="CUB probability distribution",xlab="Ordinal categories")
points(1:m,pr,pch=19)</pre>
```

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probcub0q

#### Description

Compute the probability distribution of a CUB model with covariates for the feeling component.

#### Usage

probcub0q(m,ordinal,W,pai,gama)

#### Arguments

m	Number of ordinal categories
ordinal	Vector of ordinal responses
W	Matrix of covariates for explaining the feeling component NCOL(Y)+1 to include an intercept term in the model (first entry)
pai	Uncertainty parameter
gama	Vector of parameters for the feeling component, whose length equals NCOL(W)+1 to include an intercept term in the model (first entry)

## Value

A vector of the same length as ordinal, whose i-th component is the probability of the i-th observation according to a CUB distribution with the corresponding values of the covariates for the feeling component and coefficients specified in gama.

#### References

Piccolo D. (2006). Observed Information Matrix for MUB Models, *Quaderni di Statistica*, **8**, 33–78

Piccolo D. and D'Elia A. (2008). A new approach for modelling consumers' preferences, *Food Quality and Preference*, **18**, 247–259

Iannario M. and Piccolo D. (2012). CUB models: Statistical methods and empirical evidence, in: Kenett R. S. and Salini S. (eds.), *Modern Analysis of Customer Surveys: with applications using R*, J. Wiley and Sons, Chichester, 231–258

## See Also

bitgama, probcub00, probcubp0, probcubpq

## Examples

```
data(relgoods)
m<-10
naord<-which(is.na(relgoods$Physician))
nacov<-which(is.na(relgoods$Gender))
na<-union(naord,nacov)
ordinal<-relgoods$Physician[-na]
W<-relgoods$Gender[-na]
pai<-0.44; gama<-c(-0.91,-0.7)
pr<-probcub0q(m,ordinal,W,pai,gama)</pre>
```

probcubp0 Probability distribution of a CUB model with covariates for the uncertainty component

## Description

Compute the probability distribution of a CUB model with covariates for the uncertainty component.

## Usage

probcubp0(m,ordinal,Y,bet,csi)

## Arguments

m	Number of ordinal categories
ordinal	Vector of ordinal responses
Υ	Matrix of covariates for explaining the uncertainty component
bet	Vector of parameters for the uncertainty component, whose length equals NCOL(Y) + 1 to include an intercept term in the model (first entry)
csi	Feeling parameter

## Value

A vector of the same length as ordinal, whose i-th component is the probability of the i-th observation according to a CUB model with the corresponding values of the covariates for the uncertainty component and coefficients for the covariates specified in bet.

#### References

Piccolo D. (2006). Observed Information Matrix for MUB Models, *Quaderni di Statistica*, **8**, 33–78

Piccolo D. and D'Elia A. (2008). A new approach for modelling consumers' preferences, *Food Quality and Preference*, **18**, 247–259

Iannario M. and Piccolo D. (2012). CUB models: Statistical methods and empirical evidence, in: Kenett R. S. and Salini S. (eds.), *Modern Analysis of Customer Surveys: with applications using R*, J. Wiley and Sons, Chichester, 231–258

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#### probcubpq

## See Also

bitgama, probcub00, probcubpq, probcub0q

## Examples

```
data(relgoods)
m<-10
naord<-which(is.na(relgoods$Physician))
nacov<-which(is.na(relgoods$Gender))
na<-union(naord,nacov)
ordinal<-relgoods$Physician[-na]
Y<-relgoods$Gender[-na]
bet<-c(-0.81,0.93); csi<-0.20
probi<-probcubp0(m,ordinal,Y,bet,csi)</pre>
```

```
probcubpq
```

*Probability distribution of a CUB model with covariates for both feeling and uncertainty* 

## Description

Compute the probability distribution of a CUB model with covariates for both the feeling and the uncertainty components.

#### Usage

probcubpq(m,ordinal,Y,W,bet,gama)

## Arguments

m	Number of ordinal categories
ordinal	Vector of ordinal responses
Υ	Matrix of covariates for explaining the uncertainty component
W	Matrix of covariates for explaining the feeling component
bet	Vector of parameters for the uncertainty component, whose length equals NCOL(Y) + 1 to include an intercept term in the model (first entry)
gama	Vector of parameters for the feeling component, whose length equals NCOL(W)+1 to include an intercept term in the model (first entry)

#### Value

A vector of the same length as ordinal, whose i-th component is the probability of the i-th rating according to a CUB distribution with given covariates for both uncertainty and feeling, and specified coefficients vectors bet and gama, respectively.

#### References

Piccolo D. (2006). Observed Information Matrix for MUB Models, *Quaderni di Statistica*, **8**, 33–78

Piccolo D. and D'Elia A. (2008). A new approach for modelling consumers' preferences, *Food Quality and Preference*, **18**, 247–259

Iannario M. and Piccolo D. (2012). CUB models: Statistical methods and empirical evidence, in: Kenett R. S. and Salini S. (eds.), *Modern Analysis of Customer Surveys: with applications using R*, J. Wiley and Sons, Chichester, 231–258

#### See Also

bitgama, probcub00, probcubp0, probcub0q

## Examples

```
data(relgoods)
m<-10
naord<-which(is.na(relgoods$Physician))
nacov<-which(is.na(relgoods$Gender))
na<-union(naord,nacov)
ordinal<-relgoods$Physician[-na]
W<-Y<-relgoods$Gender[-na]
gama<-c(-0.91,-0.7); bet<-c(-0.81,0.93)
probi<-probcubpq(m,ordinal,Y,W,bet,gama)</pre>
```

relgoods

Relational goods and Leisure time dataset

## Description

Dataset consists of the results of a survey aimed at measuring the evaluation of people living in the metropolitan area of Naples, Italy, with respect to of relational goods and leisure time collected in December 2014. Every participant was asked to assess on a 10 point ordinal scale his/her personal score for several relational goods (for instance, time dedicated to friends and family) and to leisure time. In addition, the survey asked respondents to self-evaluate their level of happiness by marking a sign along a horizontal line of 110 millimeters according to their feeling, with the left-most extremity standing for "extremely unhappy", and the right-most extremity corresponding to the status "extremely happy".

#### Usage

data(relgoods)

#### relgoods

#### Format

The description of subjects' covariates is the following:

ID An identification number

Gender A factor with levels: 0 = man, 1 = woman

BirthMonth A variable indicating the month of birth of the respondent

BirthYear A variable indicating the year of birth of the respondent

Family A factor variable indicating the number of members of the family

- Year.12 A factor with levels: 1 = if there is any child aged less than 12 in the family, 0 = otherwise
- EducationDegree A factor with levels: 1 = compulsory school, 2 = high school diploma, 3 = Graduated-Bachelor degree, 4 = Graduated-Master degree, 5 = Post graduated
- MaritalStatus A factor with levels: 1 = Unmarried, 2 = Married/Cohabitee, 3 = Separated/Divorced, 4 = Widower
- Residence A factor with levels: 1 = City of Naples, 2 = District of Naples, 3 = Others Campania, 4 = Others Italia, 5 = Foreign countries

Glasses A factor with levels: 1 = wearing glasses or contact lenses, 0 = otherwise

RightHand A factor with levels: 1 = right-handed, 0 = left-handed

Smoking A factor with levels: 1 =smoker, 0 =not smoker

WalkAlone A factor with levels: 1 = usually walking alone, 0 = usually walking in company

- job A factor with levels: 1 = Not working, 2 = Retired, 3 = occasionally, 4 = fixed-term job, 5 = permanent job
- PlaySport A factor with levels: 1 = Not playing any sport, 2 = Yes, individual sport, 3 = Yes, team sport

Pets A factor with levels: 1 =owning a pet, 0 =not owning any pet

1) Respondents were asked to evaluate the following items on a 10 point Likert scale, ranging from 1 = "never, at all" to 10 = "always, a lot":

WalkOut How often the respondent goes out for a walk

Parents How often respondent talks at least to one of his/her parents

MeetRelatives How often respondent meets his/her relatives

Association Frequency of involvement in volunteering or different kinds of associations/parties, etc

RelFriends Quality of respondent's relationships with friends

RelNeighbours Quality of the relationships with neighbors

NeedHelp Easiness in asking help whenever in need

Environment Level of comfort with the surrounding environment

Safety Level of safety in the streets

EndofMonth Family making ends meet

MeetFriend Number of times the respondent met his/her friends during the month preceding the interview

Physician Importance of the kindness/simpathy in the selection of respondent's physician

Happiness Each respondent was asked to mark a sign on a 110mm horizontal line according to his/her feeling of happiness (left endpoint corresponding to completely unhappy, right-most endpoint corresponding to extremely happy

2) The same respondents were asked to score the activities for leisure time listed below, according to their involvement/degree of amusement, on a 10 point Likert scale ranging from 1 = "At all, nothing, never" to 10 = "Totally, extremely important, always":

Videogames Reading Cinema Drawing Shopping Writing Bicycle Τv StayWFriend Spending time with friends Groups Taking part to associations, meetings, etc. Walking HandWork Hobby, gardening, sewing, etc. Internet Sport SocialNetwork Gym Quiz Crosswords, sudoku, etc. MusicInstr Playing a musical instrument GoAroundCar Hanging out by car Dog Walking out the dog GoOutEat Go to restaurants/pubs

## Details

Period of data collection: December 2014 Mode of collection: questionnaire Number of observations: 2459 Number of subjects' covariates: 16 Number of analyzed items: 34 Warning: with a limited number of missing values

#### Source

http://www.labstat.it/home/wp-content/uploads/2015/09/relgoods.txt

summary.fastCUB

#### Description

S3 method summary for objects of class fastCUB.

## Usage

```
## S3 method for class 'fastCUB'
summary(object, correlation = FALSE,
    pnames = object$parnames, ...)
```

#### Arguments

object	An object of class fastCUB
correlation	Logical: should the estimated correlation matrix be returned? Default is FALSE
pnames	A vector of character for names to be assigned to estimated parameters
	Other arguments

## Value

Extended summary results of the fitting procedure, including parameter estimates, their standard errors and Wald statistics, maximized log-likelihood compared with that of the saturated model and of a Uniform sample. AIC, BIC and ICOMP indeces are also displayed for model selection. Execution time and number of exectued iterations for the fitting procedure are aslo returned.

univer

Evaluation of the Orientation Services 2002

#### Description

A sample survey on students evaluation of the Orientation services was conducted across the 13 Faculties of University of Naples Federico II in five waves: participants were asked to express their ratings on a 7 point scale (1 = "very unsatisfied", 7 = "extremely satisfied"). Here dataset collected during 2002 is loaded.

#### Usage

data(univer)

The description of subjects' covariates is:

- Faculty A factor variable, with levels ranging from 1 to 13 indicating the coding for the different university faculties
- Freqserv A factor with levels: 0 =for not regular users, 1 =for regular users

Age Variable indicating the age of the respondent in years

Gender A factor with levels: 0 = man, 1 = woman

Diploma A factor with levels: 1 = classic studies, 2 = scientific studies, 3 = linguistic, 4 = Professional, 5 = Technical/Accountancy, 6 = others

Residence A factor with levels: 1 = city NA, 2 = district NA, 3 = others

ChangeFa A factor with levels: 1 = changed faculty, 2 = not changed faculty

Analyzed ordinal variables (Likert ordinal scale): 1 = "extremely unsatisfied", 2 = "very unsatisfied", 3 = "unsatisfied", 4 = "indifferent", 5 = "satisfied", 6 = "very satisfied", 7 = "extremely satisfied"

Informat Level of satisfaction about the collected information

Willingn Level of satisfaction about the willingness of the staff

Officeho Judgment about the Office hours

Competen Judgement about the competence of the staff

Global Global satisfaction

#### Details

Period of data collection: 2002 Mode of collection: questionnaire Number of observations: 2179 Number of subjects' covariates: 7 Number of analyzed items: 5

#### Source

http://www.labstat.it/home/wp-content/uploads/2016/12/univer2002.txt

vcov.fastCUB S3 method vcov() for class "fastCUB"	
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## Description

S3 method: vcov for objects of class fastCUB.

#### Usage

## S3 method for class 'fastCUB'
vcov(object, ...)

## vcov.fastCUB

## Arguments

object	An object of class fastCUB
	Other arguments

## Value

Variance-covariance matrix of the final ML estimates for parameters of the fitted CUB model, according to the logit transform also when covariates are not included for uncertainty or feeling parameters. It is computed on the basis of Louis' identity within the EM algorithm.

## See Also

fastCUB

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