Package 'ICSNP'

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Author Klaus Nordhausen, Seija Sirkia, Hannu Oja, David E. Tyler

Maintainer Klaus Nordhausen <klaus.nordhausen@tuwien.ac.at>

Depends R (>= 2.4.0), mvtnorm, ICS

Description Tools for multivariate nonparametrics, as location tests based on marginal ranks, spatial median and spatial signs computation, Hotelling's T-test, estimates of shape are implemented.

License GPL (>= 2)

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ICSNP-package   *Tools for Multivariate Nonparametrics*

Description

This package contains functions and tools for multivariate nonparametric tests and estimation.

Details

Package:	ICSNP
Type:	Package
Version:	1.1-1
Date:	2018-03-10
License:	GPL (>= 2)

This package contains tools for nonparametric multivariate analysis, including the estimation of location and shape as well as some tests for location and independece. Shape matrices from this package can be used as one of the scatter matrices needed in the package ICS whereas the tests of this package can be used for testing in the framework of invariant coordinates or independent components obtained from the package ICS. The parametric Hotelling's T test serves as a reference for the nonparametric location tests.

Author(s)

Klaus Nordhausen, Seija Sirkiä, Hannu Oja and David E. Tyler

Maintainer: Klaus Nordhausen, <klaus.nordhausen@tuwien.ac.at>

See Also

ICS

---

duembgen.shape   *Duembgen's Shape Matrix*

Description

Iterative algorithm to estimate Dümbgen's shape matrix.

Usage

```
duembgen.shape(X, init = NULL, steps = Inf, eps = 1e-06,
               maxiter = 100, in.R = FALSE, na.action = na.fail, ...)
```

Arguments

X	numeric data matrix or dataframe.
init	an optional matrix giving the starting value for the iteration. Otherwise the regular covariance is used after transforming it to a shape matrix wit determinant 1.
steps	a fixed number of iteration steps to take. See details.
eps	convergence tolerance.
maxiter	maximum number of iterations.
in.R	logical. If TRUE R-code (and not C) is used in the iteration
na.action	a function which indicates what should happen when the data contain 'NA's. Default is to fail.
...	other arguments passed on to [tyler.shape]().

Details

Dümbgen's shape matrix can be seen as [tyler.shape]()'s matrix wrt to the origin for the pairwise differences of the observations. Therefore this shape matrix needs no location parameter.

The function is, however, slow if the dataset is large.

The algorithm also allows for a k-step version where the iteration is run for a fixed number of steps instead of until convergence. If `steps` is finite that number of steps is taken and `maxiter` is ignored.

A better implementation is available in the package fastM as the function `DUEMBGENshape`.

Value

A matrix.

Author(s)

Klaus Nordhausen, Seija Sirkiä, and some of the C++ is based on work by Jari Miettinen

References

Dümbgen, L. (1998), On Tyler's M-functional of scatter in high dimension, Annals of Institute of Statistical Mathematics, **50**, *471–491.*

See Also

[tyler.shape](), [duembgen.shape.wt]()

Examples

```
set.seed(654321)
cov.matrix <- matrix(c(3,2,1,2,4,-0.5,1,-0.5,2), ncol=3)
X <- rmvnorm(100, c(0,0,0), cov.matrix)
cov.matrix/det(cov.matrix)^(1/3)
duembgen.shape(X)
rm(.Random.seed)
```

---

duembgen.shape.wt	*Weighted Duembgen's Shape Matrix*

Description

Iterative algorithm to estimate the weighted version of Dümbgen's shape matrix.

Usage

```
duembgen.shape.wt(X, wt = rep(1, nrow(X)), init = NULL,
                  eps = 1e-06, maxiter = 100, na.action = na.fail)
```

Arguments

X	numeric data frame or matrix.
wt	vector of weights. Should be nonnegative and at least one larger than zero.
init	an optional matrix giving the starting value for the iteration.
eps	convergence tolerance.
maxiter	maximum number of iterations.
na.action	a function which indicates what should happen when the data contain 'NA's. Default is to fail.

Details

The weighted Dümbgen shape matrix can be seen as [tyler.shape]()'s matrix wrt to the origin for the weighted pairwise differences of the observations. Therefore this shape matrix needs no location parameter.

Note that this function is memory comsuming and slow for large data sets since the matrix is based on all pairwise difference of the observations.

Value

a matrix.

Author(s)

Klaus Nordhausen

References

Sirkiä, S., Taskinen, S. and Oja, H. (2007), Symmetrised M-estimators of scatter. Journal of Multi-variate Analysis, **98**, *1611–1629.*

See Also

[duembgen.shape](#)

Examples

```
set.seed(1)
cov.matrix.1 <- matrix(c(3,2,1,2,4,-0.5,1,-0.5,2), ncol = 3)
X.1 <- rmvnorm(100, c(0,0,0), cov.matrix.1)
cov.matrix.2 <- diag(1,3)
X.2 <- rmvnorm(50, c(1,1,1), cov.matrix.2)
X <- rbind(X.1, X.2)

D1 <-  duembgen.shape.wt(X, rep(c(0,1), c(100,50)))
D2 <-  duembgen.shape.wt(X, rep(c(1,0), c(100,50)))

D1
D2

rm(.Random.seed)
```

---

hl.loc	*Hodges - Lehmann Estimator of Location*

Description

Function to compute the Hodges - Lehmann estimator of location in the one sample case.

Usage

```
hl.loc(x, na.action = na.fail)
```

Arguments

x	a numeric vector.
na.action	a function which indicates what should happen when the data contain 'NA's. Default is to fail.

Details

The Hodges - Lehmann estimator is the median of the combined data points and Walsh averages. It is the same as the Pseudo Median returned as a by-product of the function `wilcox.test`.

Value

the Hodges - Lehmann estimator of location.

Author(s)

Klaus Nordhausen

References

Hettmansperger, T.P. and McKean, J.W. (1998), Robust Nonparametric Statistical Methods, *London, Arnold.*

Hodges, J.L., and Lehmann, E.L. (1963), Estimates of location based on rank tests. The Annals of Mathematical Statistics, **34**, *598–611.*

See Also

`wilcox.test`

Examples

```
set.seed(1)
x <- rt(100, df = 3)
hl.loc(x)
# same as
wilcox.test(x,  conf.int = TRUE)$estimate
rm(.Random.seed)
```

HotellingsT2   *Hotelling's T2 Test*

Description

Hotelling's T2 test for the one and two sample case.

Usage

```
 HotellingsT2(X, ...)

## Default S3 method:
HotellingsT2(X, Y = NULL, mu = NULL, test = "f",
             na.action = na.fail, ...)

## S3 method for class 'formula'
HotellingsT2(formula, na.action = na.fail, ...)
```

Arguments

X	a numeric data frame or matrix.
Y	an optional numeric data frame or matrix for the two sample test. If NULL a one sample test is performed.
mu	a vector indicating the hypothesized value of the mean (or difference in means if a two sample test is performed). NULL represents origin or no difference between the groups.
test	if 'f', the decision is based on the F-distribution, if 'chi' a chi-squared approximation is used.
formula	a formula of the form X ~ g where X is a numeric matrix giving the data values and g a factor with two levels giving the corresponding groups.
na.action	a function which indicates what should happen when the data contain 'NA's. Default is to fail.
...	further arguments to be passed to or from methods.

Details

The classical test for testing the location of a multivariate population or for testing the mean difference for two multivariate populations. When test = "f" the F-distribution is used for the test statistic and it is assumed that the data are normally distributed. If the chisquare approximation is used, the normal assumption can be relaxed to existence of second moments. In the two sample case both populations are assumed to have the same covariance matrix.

The formula interface is only applicable for the 2-sample tests.

Value

A list with class 'htest' containing the following components:

statistic	the value of the T2-statistic. (That is the scaled value of the statistic that has an F distribution or a chisquare distribution depending on the value of test).
parameter	the degrees of freedom for the T2-statistic.
p.value	the p-value for the test.
null.value	the specified hypothesized value of the mean or mean difference depending on whether it was a one-sample test or a two-sample test.
alternative	a character string with the value 'two.sided'.
method	a character string indicating what type of test was performed.
data.name	a character string giving the name of the data (and grouping vector).

Author(s)

Klaus Nordhausen

References

Anderson, T.W. (2003), An introduction to multivariate analysis, *New Jersey: Wiley.*

Examples

```
# one sample test:

data(pulmonary)

HotellingsT2(pulmonary)
HotellingsT2(pulmonary, mu = c(0,0,2), test = "chi")

# two sample test:

set.seed(123456)
X <- rmvnorm(20, c(0, 0, 0, 0), diag(1:4))
Y <- rmvnorm(30, c(0.5, 0.5, 0.5, 0.5), diag(1:4))
Z <- rbind(X, Y)
g <- factor(rep(c(1,2),c(20,30)))

HotellingsT2(X, Y)
HotellingsT2(Z ~ g, mu = rep(-0.5,4))

rm(.Random.seed)
```

HP.loc.test   *Hallin and Paindaveine Signed-Rank Tests*

Description

This function implements the signed-rank location tests as suggested by Hallin and Paindaveine (2002a, 2002b).

Usage

```
HP.loc.test(X, mu = NULL, score = "rank", angles = "tyler",
            method = "approximation", n.perm = 1000,
            na.action = na.fail)
```

Arguments

X	a numeric data frame or matrix.
mu	a vector indicating the hypothesized value of the location. NULL represents the origin.
score	score for the pseudo mahalanobis distance. Options are 'rank', 'sign' and 'normal' scores.
angles	which angle to use. Possible are 'tyler' for spatial sign type anlges or 'interdirections'. Note however that currently only 'tyler' is implemented.
method	defines the method used for the computation of the p-value. The possibilites are 'approximation' or 'permutation'.

n.perm	if method="permutation" specifies this the number of replications used in the permutation procedure.
na.action	a function which indicates what should happen when the data contain 'NA's. Default is to fail.

Details

The test based on interdirections is described in Hallin and Paindaveine (2002a) and the test based on Tyler's angles is described in Hallin and Paindaveine (2002b). The two different tests are asymptotically equivalent and in both cases is assumed that the data comes from an elliptic distribution.

Value

A list with class 'htest' containing the following components:

statistic	the value of the Q-statistic.
parameter	the degrees of freedom for the Q-statistic.
p.value	the p-value for the test.
null.value	the specified hypothesized value of the location.
alternative	a character string with the value 'two.sided'.
method	a character string indicating what type of test was performed.
data.name	a character string giving the name of the data.

Author(s)

Klaus Nordhausen

References

Hallin, M. and Paindaveine, D. (2002a), Optimal tests for multivariate location based on interdirections and pseudo-Mahalanobis ranks, Annals of Statistics, **30**, *1103–1133.*

Hallin, M. and Paindaveine, D. (2002b), Randles' interdirections or Tyler's angles?, In Y. Dodge, Ed. Statistical data analysis based on the L1-norm and related methods, *271–282.*

See Also

tyler.shape, spatial.sign

Examples

```
X <- rmvnorm(100, c(0,0,0.1))
HP.loc.test(X)
HP.loc.test(X, score="s")
HP.loc.test(X, score="n")
```

HP1.shape   *One Step Rank Scatter Estimator*

Description

one step M-estimator of the scatter matrix based on ranks.

Usage

```
HP1.shape(X, location = "Estimate", na.action = na.fail, ...)
```

Arguments

X   a numeric data frame or matrix.

location   if 'Estimate' the location and scatter matrix used for computing the spatial signs are estimated simultaneously using `HR.Mest`, if 'Origin' or numeric `tyler.shape` is used with respect to origin or the given value, respectively, to obtain the spatial signs.

na.action   a function which indicates what should happen when the data contain 'NA's. Default is to fail.

...   arguments that can be passed on to `tyler.shape` or `HR.Mest`.

Details

This is a one step M-estimator of shape which is standardized in such a way that the determinant is 1.

The exact formula is:

$$V = V_0^{\frac{1}{2}} ave\{a(\frac{R_i}{n+1})u_i'u_i\}V_0^{\frac{1}{2}}.$$

where V_0 is Tyler's shape matrix, $u_i = ||z_i||^{-1}z_i$ is the spatial sign of $z_i = (x_i - \mu)V_0^{-\frac{1}{2}}$ and R_i gives the rank of $||z_i||$ among $||z_1||, \ldots, ||z_n||$. The van der Warden score function $a(.)$ is the inverse of the cdf of a chi-squared distribution with p degrees of freedom.

This scatter matrix is based on the test for shape developed in the paper by Hallin and Paindaveine (2006), its usage with respect to the origin is demonstrated in Nordhausen et al. (2006).

Author(s)

Klaus Nordhausen

References

Hallin, M. and Paindaveine, D. (2006), *Semiparametrically efficient rank-based inference for shape. I. Optimal rank-based tests for sphericity*, Annals of Statistics, **34**, 2707–2756.

Nordhausen, K., Oja, H. and Paindaveine, D. (2009), *Signed-rank tests for location in the symmetric independent component model*, Journal of Multivariate Analysis, **100**, 821–834.

Examples

```
set.seed(654321)
cov.matrix <- matrix(c(3,2,1,2,4,-0.5,1,-0.5,2), ncol=3)
X <- rmvnorm(100, c(0,0,0), cov.matrix)
HP1.shape(X)
HP1.shape(X, location="Origin")
cov.matrix/det(cov.matrix)^(1/3)
rm(.Random.seed)
```

HR.Mest	*Simultaneous Affine Equivariant Estimation of Multivariate Median and Tyler's Shape Matrix*

Description

iterative algorithm that finds the affine equivariant multivariate median by estimating `tyler.shape` simultaneously.

Usage

```
HR.Mest(X, maxiter = 100, eps.scale = 1e-06, eps.center = 1e-06,
        na.action = na.fail)
```

Arguments

X	a numeric data frame or matrix.
maxiter	maximum number of iterations.
eps.scale	convergence tolerance for the Tyler's shape matrix subroutine.
eps.center	convergence tolerance for the location estimate.
na.action	a function which indicates what should happen when the data contain 'NA's. Default is to fail.

Details

The algorithm follows the idea of Hettmansperger and Randles (2002). There are, however, some differences. This algorithm has the vector of marginal medians as starting point for the location and the starting shape matrix is Tyler's shape matrix based on the vector of marginal medians and has then a location step and a shape step which are:

location step k+1: transforming the data as $y = xV_k^{-\frac{1}{2}}$ and computing the spatial median μ_y of y using the function `spatial.median`. Then retransforming μ_y to the original scale $\mu_{x,k+1} = \mu_y V_k^{\frac{1}{2}}$.

shape step k+1: computing Tyler's shape matrix V_{k+1} with respect to $\mu_{x,k+1}$ by using the function `tyler.shape`.

The algorithm stops when the difference between two subsequent location estimates is smaller than
`eps.center`.

There is no proof that the algorithm converges.

Value

A list containing:

center   vector with the estimated loaction.

scatter   matrix of the estimated scatter.

Author(s)

Klaus Nordhausen and Seija Sirkiä

References

Hettmansperger, T.P. and Randles, R.H. (2002), A practical affine equivariant multivariate median,
Biometrika, **89**, *851–860.*

Examples

```
set.seed(654321)
cov.matrix <- matrix(c(3,2,1,2,4,-0.5,1,-0.5,2), ncol=3)
X <- rmvnorm(100, c(0,0,0), cov.matrix)
res <- HR.Mest(X)
colMeans(X)
res$center
cov.matrix/det(cov.matrix)^(1/3)
res$scatter
rm(.Random.seed)
```

---

ind.ctest   *Test of Independece based on Marginal Ranks*

Description

Performs the test that a group of variables is independent of an other based on marginal ranks. Three
different score functions are available.

Usage

```
ind.ctest(X, index1, index2 = NULL, scores = "rank",
          na.action = na.fail)
```

Arguments

X	a data frame or matrix.
index1	integer vector that selects the columns of X that form group one. Only numeric columns can be selected.
index2	integer vector that selects the columns of X that form group two. Only numeric columns can be selected. If NULL, all remaining columns of X will be selected.
scores	if 'sign', a sign test is performed, if 'rank' a rank test is performed or if 'normal' a normal score test is performed.
na.action	a function which indicates what should happen when the data contain 'NA's. Default is to fail.

Details

The test tests if X[, index1] is independent of X[, index2] and is described in great detail in Puri and Sen (1971).

Value

A list with class 'htest' containing the following components:

statistic	the value of the W-statistic.
parameter	the degrees of freedom for the W-statistic.
p.value	the p-value for the test.
method	a character string indicating what type of test was performed.
data.name	a character string giving the name of the data.

Author(s)

Klaus Nordhausen

References

Puri , M.L. and Sen, P.K. (1971), Nonparametric Methods in Multivariate Analysis, *New York: Wiley.*

Examples

```
A1 <- matrix(c(4, 4, 5, 4, 6, 6, 5, 6, 7), ncol = 3)
A2 <- matrix(c(0.5, -0.3, -0.3, 0.7), ncol = 2)
X <- cbind(rmvnorm(100, c(-1, 0, 1), A1), rmvnorm(100, c(0, 0), A2))
ind.ctest(X,1:3)
ind.ctest(X, c(1, 5), c(2, 3), scores = "normal")
```

---

ind.ictest   *Test of Independence based on Marginal Ranks in a Symmetric IC*
                                    Model

Description

Performs the test that a group of variables is independent of an other based on marginal ranks. It is
assumed that the data follows a symmetric IC model. Three different score functions are available.

Usage

```
ind.ictest(X, index1, index2 = NULL, scores = "rank",
          method = "approximation", n.simu = 1000,
          ..., na.action = na.fail)
```

Arguments

X	a data frame or matrix.
index1	integer vector that selects the columns of X that form group one. Only numeric columns can be selected.
index2	integer vector that selects the columns of X that form group two. Only numeric columns can be selected. If NULL, all remaining columns of X will be selected.
scores	if 'sign', a sign test is performed, if 'rank' a signed rank test is performed or if 'normal' a normal score test is performed.
method	defines the method used for the computation of the p-value. The possobilites are "approximation" (default), "simulation" or "permutation". Details below.
n.simu	if 'method = "simulation"' or 'method = "permutation"' this specifies the number of replications used in the simulation or permutation procedure.
...	further arguments to be passed to the function ics
na.action	a function which indicates what should happen when the data contain 'NA's. Default is to fail.

Details

Assumed is here that X[, index1] comes from a symmetric independent component model which
in turn is independent from X[, index2] which has also an underlying symmetric independent
component model. This function recovers the independent components using the function ics,
centers them by a marginal loaction estimate based on the same scores that will be used in the
actual test. The test is described in Oja, Paindaveine and Taskinen (2009). The asymptotic chi-
square distibution is however even for large sample sizes inadequat and therefore p-values can be
simulated by resampling the test statistic under the null hypothesis or by permuting the rows of the
independent components of X[, index2]. Both alternatives are also described in Oja, Paindaveine
and Taskinen (2009).

Value

A list with class 'htest' containing the following components:

`statistic`	the value of the Q-statistic.
`parameter`	the degrees of freedom for the Q-statistic or the number of replications depending on the chosen method.
`p.value`	the p-value for the test.
`method`	a character string indicating what type of test was performed.
`data.name`	a character string giving the name of the data.

Author(s)

Klaus Nordhausen

References

Oja, H. and Paindaveine, D. and Taskinen, S. (2016), Affine-invariant rank tests for multivariate independence in independent component models, Electronic Journal of Statistics, **10**, *2372–2419.*

Examples

```
Z1<-cbind(rt(500,5),rnorm(500),runif(500))
Z2<-cbind(rt(500,8),rbeta(500,2,2))
A1 <- matrix(c(4, 4, 5, 4, 6, 6, 5, 6, 7), ncol = 3)
A2 <- matrix(c(0.5, -0.3, -0.3, 0.7), ncol = 2)

X <- cbind(Z1 %*% t(A1), Z2 %*% t(A2))

ind.ictest(X,1:3)
ind.ictest(X,1:3,method="simu")

ind.ictest(X,1:2,3:5,method="perm", S1=tyler.shape,S2=cov)
```

LASERI	*Cardiovascular Responses to Head-up Tilt*

Description

This data set contains the cardiovascular responses to a passive head-up tilt for 223 subjects.

Usage

```
data(LASERI)
```

Format

A data frame with 223 observations on the following 32 variables.

`Sex` a factor with levels `Female` and `Male`.

`Age` Age in years.

`Height` Height in cm.

`Weight` Weight in kg.

`Waist` Waist circumference in cm.

`Hip` Hip circumference in cm.

`BMI` Body mass index.

`WHR` Waist hip ratio.

`HRT1` Average heart rate in the tenth minute of rest.

`HRT2` Average heart rate in the second minute during the tilt.

`HRT3` Average heart rate in the fifth minute during the tilt.

`HRT4` Average heart rate in the fifth minute after the tilt.

`COT1` Average cardiac output in the tenth minute of rest.

`COT2` Average cardiac output in the second minute during the tilt.

`COT3` Average cardiac output in the fifth minute during the tilt.

`COT4` Average cardiac output in the fifth minute after the tilt.

`SVRIT1` Average systemic vascular resistance index in the tenth minute of rest.

`SVRIT2` Average systemic vascular resistance index in the second minute during the tilt.

`SVRIT3` Average systemic vascular resistance index in the fifth minute during the tilt.

`SVRIT4` Average systemic vascular resistance index in the fifth minute after the tilt.

`PWVT1` Average pulse wave velocity in the tenth minute of rest.

`PWVT2` Average pulse wave velocity in the second minute during the tilt.

`PWVT3` Average pulse wave velocity in the fifth minute during the tilt.

`PWVT4` Average pulse wave velocity in the fifth minute after the tilt.

`HRT1T2` Difference `HRT1 - HRT2`.

`COT1T2` Difference `COT1 - COT2`.

`SVRIT1T2` Difference `SVRIT1 - SVRIT2`.

`PWVT1T2` Difference `PWVT1 - PWVT2`.

`HRT1T4` Difference `HRT1 - HRT4`.

`COT1T4` Difference `COT1 - COT4`.

`SVRIT1T4` Difference `SVRIT1 - SVRIT4`.

`PWVT1T4` Difference `PWVT1 - PWVT4`.

Details

This data is a subset of hemodynamic data collected as a part of the LASERI study (English title: "Cardivascular risk in young Finns study") using whole-body impedance cardiography and plethysmographic blood pressure recordings from fingers. The data given here comes from 223 healthy subjects between 26 and 42 years of age, who participated in the recording of the hemodynamic variables both in a supine position and during a passive head-up tilt on a motorized table. During that experiment the subject spent the first ten minutes in a supine position, then the motorized table was tilted to a head-up position (60 degrees) for five minutes, and for the last five minutes the table was again returned to the supine position.

Of interest in this data is for example if the values 5 minutes after the tilt are already returned to their pre-tilt levels.

Source

Data courtesy of the LASERI study
(<http://youngfinnsstudy.utu.fi/>).

Examples

```
# for example testing if the location before the tilt is the same as
# 5 minutes after the tilt:
data(LASERI)
DIFFS.T1T4 <- subset(LASERI,select=c(HRT1T4,COT1T4,SVRIT1T4))
rank.ctest(DIFFS.T1T4)
rank.ctest(DIFFS.T1T4, score="s")
```

---

pair.diff	*Pairwise Differences*

Description

Computes pairwise differences.

Usage

```
pair.diff(X)
```

Arguments

X   a numeric matrix.

Details

The function computes all differences of row i and row j with i < j. The function is a wrapper to a C function to do the computation quickly and does no checks concerning the input.

Value

Matrix containing the differences.

Author(s)

Seija Sirkiä

See Also

[pair.prod](), [pair.sum]()

Examples

```
X <- matrix(1:10, ncol = 2, byrow = FALSE)
pair.diff(X)
```

---

pair.prod	*Pairwise Products*

Description

Computes pairwise elementwise products.

Usage

```
pair.prod(X)
```

Arguments

X   a numeric matrix.

Details

The function computes all elementwise products of row i and row j with i < j. The function is a
wrapper to a C function to do the computation quickly and does no checks concerning the input.

Value

Matrix containing the products.

Author(s)

Klaus Nordhausen

See Also

[pair.diff](), [pair.sum]()

Examples

```
X <- matrix(1:10, ncol = 2, byrow = FALSE)
pair.prod(X)
```

---

pair.sum	*Pairwise Sums*

Description

Computes pairwise sums.

Usage

```
pair.sum(X)
```

Arguments

X   a numeric matrix.

Details

The function computes all sums of row i and row j with i < j. The function is a wrapper to a C function to do the computation quickly and does no checks concerning the input.

Value

Matrix containing the sums.

Author(s)

Seija Sirkiä

See Also

[pair.diff](), [pair.prod]()

Examples

```
X <- matrix(1:10, ncol = 2, byrow = FALSE)
pair.sum(X)
```

---

pulmonary   *Change in Pulmonary Response after Exposure to Cotton Dust*

Description

Changes in pulmonary function of 12 workers after 6 hours of exposure to cotton dust.

Usage

```
data(pulmonary)
```

Format

A data frame with 12 observations on the following 3 variables.

FVC change in FVC (forced vital capacity) after 6 hours.

FEV change in FEV_3 (forced expiratory volume) after 6 hours.

CC change in CC (closing capacity) after 6 hours.

Note

There is also a different version of this data set around. In the different version the FVC value of subject 11 is -0.01 instead of -0.10.

Source

Merchant, J. A., Halprin, G. M., Hudson, A. R. Kilburn, K. H., McKenzie, W. N., Hurst, D. J. and Bermazohnm P. (1975), Responses to cotton dust, Archives of Environmental Health, ***30***, *222–229, Table 5.*

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References

Hettmansperger, T. P. and McKean, J. W. (1998), Robust Nonparametric Statistical Methods, *London: Arnold.*

Examples

```
data(pulmonary)
plot(pulmonary)
```

| rank.ctest | *One, Two and C Sample Rank Tests for Location based on Marginal Ranks* |

Description

Performs the one, two or c sample location test based on marginal ranks. Three different score functions are available.

Usage

```
rank.ctest(X, ...)

## Default S3 method:
rank.ctest(X, Y = NULL, mu = NULL, scores = "rank",
           na.action = na.fail, ...)

## S3 method for class 'formula'
rank.ctest(formula, na.action = na.fail, ...)

## S3 method for class 'ics'
rank.ctest(X, g = NULL, index = NULL, na.action = na.fail, ...)
```

Arguments

X	a numeric data frame or matrix or an ics object.
Y	an optional numeric data frame or matrix for the two sample test. If NULL a one sample test is performed.
mu	a vector indicating the hypothesized value of the mean (or difference in means if you are performing a two sample test). NULL represents origin or no difference between the groups. For more than two groups mu should be 0 or not be specified at all.
scores	if 'sign', a sign test is performed, if 'rank' a signed rank test is performed or if 'normal' a normal score test is performed.
formula	a formula of the form X ~ g where X is a numeric matrix giving the data values and g a factor with at least two levels giving the corresponding groups.
g	a grouping factor with at least two levels.
index	an integer vector that gives the columns to choose the invariant coordinates form the 'ics' object. The default uses all columns.
na.action	a function which indicates what should happen when the data contain 'NA's. Default is to fail.
...	further arguments to be passed to or from methods.

Details

These tests are well described in Puri and Sen (1971). The tests are based on the marginal ranks
for which three score functions are available. The scores are also used to estimate the covariance
matrices. In the multisample case it is assumed that the distribution of the different populations
differs only in their location.

The ics interface provides an invariant test based on the invariant coordinate selection. The assymp-
totic distribution is however still an open question when more than one component is used, though
the chi-square approximation works well also for several components as shown in Nordhausen, Oja
and Tyler (2006).

Value

A list with class 'htest' containing the following components:

statistic	the value of the T-statistic.
parameter	the degrees of freedom for the T-statistic.
p.value	the p-value for the test.
null.value	the specified hypothesized value of the mean or mean difference depending on whether it was a one-sample test or a two-sample test.
alternative	a character string with the value 'two.sided'.
method	a character string indicating what type of test was performed.
data.name	a character string giving the name of the data (and grouping vector).

Author(s)

Klaus Nordhausen

References

Puri , M.L. and Sen, P.K. (1971), Nonparametric Methods in Multivariate Analysis, *New York:
Wiley.*

*Nordhausen, K., Oja, H. and Tyler, D.E. (2006), On the Efficiency of Invariant Multivariate Sign
and Rank Tests, in* Festschrift of Tarmo Pukkila on his 60th Birthday, *217–231.*

Examples

```
# one sample tests:

data(pulmonary)

rank.ctest(pulmonary, scores = "sign")
rank.ctest(pulmonary, mu = c(0,0,2))

# two sample tests:

set.seed(123456)
X <- rmvnorm(20, c(0,0,0,0), diag(1:4))
Y <- rmvnorm(30, c(0.5,0.5,0.5,0.5), diag(1:4))
```

```
Z <- rbind(X,Y)
g <- factor(rep(c(1,2), c(20,30)))

rank.ctest(X, Y, scores = "normal")
rank.ctest(Z~g, scores = "sign", mu = rep(-0.5,4))

# c sample test:

W <- rmvnorm(30, c(0,0,0,0), diag(1:4))
Z2 <- rbind(X,Y,W)
g2 <- factor(rep(1:3, c(20,30,30)))

rank.ctest(Z2~g2, scores = "normal")

# in an invariant coordinate system

rank.ctest(ics(Z2,covOrigin, cov4, S2args=list(location =
           "Origin")), index = c(1,4), scores = "sign")

rank.ctest(ics(Z), g, index = 4)

rank.ctest(ics(Z2), g2, scores = "normal",index = 4)

rm(.Random.seed)
```

---

rank.ictest	*One Sample Location Test based on Marginal Ranks in the Independent Component Model*

Description

marginal rank test for the location problem in the one sample case when the margins are assumed independent.

Usage

```
rank.ictest(X, ...)

## Default S3 method:
rank.ictest(X, mu = NULL, scores = "rank", method = "approximation",
            n.simu = 1000, na.action = na.fail, ...)

## S3 method for class 'ics'
rank.ictest(X, index = NULL, na.action = na.fail, ...)
```

Arguments

X   a numeric data frame or matrix or an ics object.

mu	a vector indicating the hypothesized value of the location. NULL represents the origin.
scores	options are 'rank' for the signed rank test, 'sign' for the sign test and 'normal' for the normal score test.
method	defines the method used for the computation of the p-value. The possibilites are "approximation" (default), "simulation" or "permutation". Details below.
n.simu	if 'method=simulation' or 'method=permutation' this specifies the number of replications used in the simulation or permutation procedure.
index	an integer vector that gives the columns to choose from invariant coordinates form the 'ics' object. The default uses all columns.
na.action	a function which indicates what should happen when the data contain 'NA's. Default is to fail.
...	further arguments to be passed to or from methods.

Details

The test is normally used to test for location in the symmetric independent component model.

By default the limiting distribution is used to compute the p-values. However for moderate sample sizes (N=50) was observed in Nordhausen et al. (2009) that the normal score test can be sometimes slightly biased. Therefore the argument method can be used to get p-values based on simulations from a multivariate normal under the null or by permuting the signs of the centered observations.

Value

A list with class 'htest' containing the following components:

statistic	the value of the Q-statistic.
parameter	the degrees of freedom for the Q-statistic.
p.value	the p-value for the test.
null.value	the specified hypothesized value of the location.
alternative	a character string with the value 'two.sided'.
method	a character string indicating what type of test was performed.
data.name	a character string giving the name of the data.

Author(s)

Klaus Nordhausen

References

Nordhausen, K., Oja, H. and Paindaveine, D. (2009), Signed-rank tests for location in the symmetric independent component model, Journal of Multivariate Analysis, **100**, *821–834.*

Examples

```
set.seed(555)
X <- cbind(rt(30,8), rnorm(30,0.5), runif(30,-3,3))
mix.matrix <- matrix(c(3,2,1,2,4,-0.5,1,-0.5,2), ncol=3)
X.mixed <- X %*% t(mix.matrix)
ica.X <- ics(X, covOrigin, cov4, S2args = list(location = "Origin"))
rank.ictest(ica.X)
rank.ictest(ica.X, scores = "normal", method = "simu")
rank.ictest(ics.components(ica.X), scores = "normal", method = "perm")
rm(.Random.seed)
```

---

spatial.median   *Spatial Median*

Description

iterative algorithm to compute the spatial median.

Usage

```
spatial.median(X, init = NULL, maxiter = 500, eps = 1e-06,
                print.it = FALSE, na.action = na.fail)
```

Arguments

X	a numeric data frame or data matrix.
init	Starting value for the alogrihtm, if 'NULL', the vector of marginal medians is used.
maxiter	maximum number of iterations.
eps	convergence tolerance.
print.it	logical. If TRUE prints the number of iterations, otherwise not.
na.action	a function which indicates what should happen when the data contain 'NA's. Default is to fail.

Details

Follows the algorithm of Vardi and Zhang.

Value

vector of the spatial median.

Author(s)

Klaus Nordhausen and Seija Sirkiä

References

Vardi, Y. and Zhang, C.-H. (1999), The multivariate L1-median and associated data depth, PNAS, **97**, *1423–1426.*

Examples

```
set.seed(654321)
cov.matrix <- matrix(c(3,2,1,2,4,-0.5,1,-0.5,2), ncol=3)
X <- rmvnorm(100, c(0,0,0), cov.matrix)
spatial.median(X)
rm(.Random.seed)
```

---

spatial.sign   *Spatial Signs*

Description

Function to obtain the spatial signs of a multivariate dataset. The function can compute the spatial signs also with respect to a given or estimated loacation and scale. If both location and scale have to be estimated the HR.Mest function is used, if only one has to be estimated the, estimation is done using spatial.median or tyler.shape.

Usage

```
spatial.sign(X, center = TRUE, shape = TRUE,
             na.action = na.fail, ...)
```

Arguments

X	a numeric data frame or matrix.
center	either a logical value or a numeric vector of length equal to the number of columns of 'X'. See below for more information.
shape	either a logical value or a square numeric matrix with number of columns equal to the number of columns of 'X'. See below for more information.
na.action	a function which indicates what should happen when the data contain 'NA's. Default is to fail.
...	arguments that can be passed on to functions used for the estimation of location and shape.

Details

The spatial signs U of X with location μ and shape V are given by

$$u_i = \frac{(x_i - \mu)V^{-\frac{1}{2}}}{\|(x_i - \mu)V^{-\frac{1}{2}}\|}.$$

If a numeric value is given as 'center' and/or 'shape' these are used as μ and/or V in the above formula. If 'center' and/or 'shape' are 'TRUE' the values for μ and/or V are estimated, if 'FALSE' the origin is used as the value of μ and/or the identity matrix as the value of V.

In the special case of univariate data the univariate signs of the data (centered if requested) are returned and the shape parameter is redundant.

Value

a matrix with the spatial signs of the data as rows or the univariate signs as a px1 matrix. The centering vector and scaling matrix used are returned as attributes 'center' and 'shape'.

Author(s)

Klaus Nordhausen and Seija Sirkiä

See Also

[HR.Mest](#)

Examples

```
set.seed(654321)
cov.matrix <- matrix(c(3,2,1,2,4,-0.5,1,-0.5,2), ncol=3)
X <- rmvnorm(15, c(1,0,-1), cov.matrix)
spatial.sign(X)
spatial.sign(X, center=FALSE, shape=FALSE)
spatial.sign(X, center=colMeans(X), shape=cov(X))
rm(.Random.seed)
```

---

symm.huber   *Symmetrized Huber Scatter Matrix*

Description

Iterative algorithm to estimate the symmetrized Huber scatter matrix.

Usage

```
symm.huber(X, qg = 0.9, init = NULL, eps = 1e-06, maxiter = 100,
           na.action = na.fail)
```

Arguments

X	numeric data frame or matrix.
qg	tuning parameter. Should be between 0 and 1. The default is 0.9.
init	an optional matrix giving the starting value for the iteration.
eps	convergence tolerance.
maxiter	maximum number of iterations.
na.action	a function which indicates what should happen when the data contain 'NA's. Default is to fail.

Details

The symmetrized Huber scatter matrix is the regular Huber scatter matrix for the pairwise differences of the observations taken wrt to the origin.

Note that this function might be memory comsuming and slow for large data sets since the matrix is based on all pairwise difference of the observations.

The function symmhuber in the package **SpatialNP** offers also a k-step option. The **SpatialNP** package contains also the function mvhuberM for the regular multivariate Huber location and scatter estimatior.

Value

a matrix.

Author(s)

Klaus Nordhausen and Jari Miettinen

References

Sirkiä, S., Taskinen, S. and Oja, H. (2007), Symmetrised M-estimators of scatter. Journal of Multivariate Analysis, **98**, *1611–1629.*

See Also

[symm.huber.wt](), symmhuber, mvhuberM

Examples

```
set.seed(654321)
cov.matrix <- matrix(c(3,2,1,2,4,-0.5,1,-0.5,2), ncol=3)
X <- rmvnorm(100, c(0,0,0), cov.matrix)
symm.huber(X)
rm(.Random.seed)
```

---

symm.huber.wt   *Weighted Symmetrized Huber Scatter Matrix*

Description

Iterative algorithm to estimate the weighted symmetrized Huber scatter matrix.

Usage

```
symm.huber.wt(X, wt = rep(1, nrow(X)), qg = 0.9, init = NULL,
              eps = 1e-06, maxiter = 100, na.action = na.fail)
```

Arguments

X	numeric data frame or matrix.
wt	vector of weights. Should be nonnegative and at least one larger than zero.
qg	tuning parameter. Should be between 0 and 1. The default is 0.9.
init	an optional matrix giving the starting value for the iteration.
eps	convergence tolerance.
maxiter	maximum number of iterations.
na.action	a function which indicates what should happen when the data contain 'NA's. Default is to fail.

Details

The weighted symmetrized Huber scatter matrix is the regular Huber scatter matrix for the weighted pairwise differences of the observations taken wrt to the origin.

Note that this function is memory comsuming and slow for large data sets since the matrix is based on all pairwise difference of the observations.

Value

a matrix.

Author(s)

Klaus Nordhausen

References

Sirkiä, S., Taskinen, S. and Oja, H. (2007), Symmetrised M-estimators of scatter. Journal of Multivariate Analysis, **98**, *1611–1629.*

See Also

symm.huber

Examples

```
set.seed(1)
cov.matrix.1 <- matrix(c(3,2,1,2,4,-0.5,1,-0.5,2), ncol = 3)
X.1 <- rmvnorm(100, c(0,0,0), cov.matrix.1)
cov.matrix.2 <- diag(1,3)
X.2 <- rmvnorm(50, c(1,1,1), cov.matrix.2)
X <- rbind(X.1, X.2)

D1 <-  symm.huber.wt(X, rep(c(0,1), c(100,50)))
D2 <-  symm.huber.wt(X, rep(c(1,0), c(100,50)))

D1
D2

rm(.Random.seed)
```

---

tyler.shape   *Tyler's Shape Matrix*

Description

Iterative algorithm to estimate Tyler's shape matrix.

Usage

```
tyler.shape(X, location = NULL, init = NULL, steps = Inf, eps = 1e-06,
            maxiter = 100, in.R = FALSE, print.it = FALSE,
            na.action = na.fail)
```

Arguments

X	numeric data matrix or dataframe.
location	if NULL the sample mean is used, otherwise a vector with the location can be specified.
init	an optional matrix giving the starting value for the iteration
steps	a fixed number of iteration steps to take. See details.
eps	convergence tolerance.
maxiter	maximum number of iterations.
in.R	logical. If TRUE R-code (and not C) is used in the iteration
print.it	logical. If TRUE prints the number of iterations, otherwise not.
na.action	a function which indicates what should happen when the data contain 'NA's. Default is to fail.

Details

The most robust M-estimator of shape. It is proportional to the regular covariance matrix for elliptical contoured distributions. The estimate is in such a way standardized, that its determinate is 1.

The algorithm requires an estimate of location, if none is provided, the sample mean is used. Observations which are equal to the location estimate are removed form the data.

The algorithm also allows for a k-step version where the iteration is run for a fixed number of steps instead of until convergence. If steps is finite that number of steps is taken and maxiter is ignored.

A different implementation is available in the package fastM as the function TYLERshape.

Value

A matrix.

Author(s)

Klaus Nordhausen, and Seija Sirkiä

References

Tyler, D.E. (1987), A distribution-free M-estimator of scatter, Annals of Statistics, **15**, 234–251.

See Also

[duembgen.shape,](duembgen.shape) HR.Mest

Examples

```
set.seed(654321)
cov.matrix <- matrix(c(3,2,1,2,4,-0.5,1,-0.5,2), ncol=3)
X <- rmvnorm(100, c(0,0,0), cov.matrix)
tyler.shape(X)
tyler.shape(X, location=0)
cov.matrix/det(cov.matrix)^(1/3)
rm(.Random.seed)
```

---

vdw.loc   *Van der Waerden Estimator of Location*

Description

Iterative algorithm to compute the location estimator based on van der Waerden scores (sometimes also referred to as normal scores).

Usage

```
vdw.loc(x, int.diff = 10, maxiter = 1000, na.action = na.fail)
```

Arguments

x	a numeric vector.
int.diff	number of observations in internal interval when the estimate is searched.
maxiter	maximum number of iterations.
na.action	a function which indicates what should happen when the data contain 'NA's. Default is to fail.

Details

The algorithm searches among the observations and all Walsh averages for the two points nearest around the root of the van der Waerden score criterion. Since the criterion function is monotone first the int.diff of the sorted data points are searched that contain the root. After then determining there the two points of question a linear interpolation is used as an estimate.

Value

the van der Waerden score estimator of location.

Author(s)

Klaus Nordhausen

References

Hettmansperger, T.P. and McKean, J.W. (1998), Robust Nonparametric Statistical Methods, *London, Arnold.*

Examples

```
set.seed(1)
x <- rt(100, df = 3)
vdw.loc(x)
rm(.Random.seed)
```

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