# Package 'MCDA'

October 12, 2022

000000 12, 2022
Version 0.0.22
<b>Date</b> 2022-09-20
Title Support for the Multicriteria Decision Aiding Process
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Description  Support for the analyst in a Multicriteria Decision Aiding (MCDA) process with algorithms, preference elicitation and data visualisation functions. Sébastien Bigaret, Richard Hodgett, Patrick Meyer,  Tatyana Mironova, Alexandru Olteanu (2017) Supporting the multicriteria decision aiding process:  R and the MCDA package, Euro Journal On Decision Processes, Volume 5, Issue 1 - 4, pages 169 - 194 <doi:10.1007 s40070-017-0064-1="">.</doi:10.1007>
<b>Imports</b> Rglpk, glpkAPI, methods, RColorBrewer, combinat, triangle, plyr, ggplot2
Suggests Rgraphviz, cplexAPI
License EUPL (== 1.1)
Encoding UTF-8
<pre>URL https://github.com/paterijk/MCDA</pre>
NeedsCompilation no
Repository CRAN
<b>Date/Publication</b> 2022-09-20 21:40:05 UTC
R topics documented:
additiveValueFunctionElicitation  AHP

2

Index

LPDMRSortIdentifyIncompatibleAssignments
LPDMRSortIdentifyUsedDictatorProfiles
LPDMRSortIdentifyUsedVetoProfiles
LPDMRSortInferenceApprox
LPDMRSortInferenceExact
MARE
MRSort
MRSortIdentifyIncompatibleAssignments
MRSortIdentifyUsedVetoProfiles
MRSortInferenceApprox
MRSortInferenceExact
MRSortInterval
normalizePerformanceTable
pairwiseConsistencyMeasures
plotAlternativesValuesPreorder
plotMARE 50
plotMRSortSortingProblem
plotPiecewiseLinearValueFunctions
plotRadarPerformanceTable
plotSURE
PROMETHEEI
PROMETHEEII
PROMETHEEOutrankingFlows
PROMETHEEPreferenceIndices
SRMP
SRMPInference         66
SRMPInferenceApprox
SRMPInferenceApproxFixedLexicographicOrder
SRMPInferenceApproxFixedProfilesNumber
SRMPInferenceFixedLexicographicOrder
SRMPInferenceFixedProfilesNumber
SRMPInferenceNoInconsist
SRMPInferenceNoInconsistFixedLexicographicOrder
SRMPInferenceNoInconsistFixedProfilesNumber
SURE
TOPSIS
UTA
UTADIS
UTASTAR
weightedSum
107

additiveValueFunctionElicitation

*Elicitation of a general additive value function.* 

# **Description**

Elicits a general additive value function from a ranking of alternatives.

# Usage

#### **Arguments**

performanceTable

Matrix or data frame containing the performance table. Each row corresponds to an alternative, and each column to a criterion. Rows (resp. columns) must be named according to the IDs of the alternatives (resp. criteria).

criteriaMinMax

Vector containing the preference direction on each of the criteria. "min" (resp. "max") indicates that the criterion has to be minimized (maximized). The elements are named according to the IDs of the criteria.

epsilon

Numeric value containing the minimal difference in value between two consecutive alternatives in the final ranking.

alternativesRanks

Optional vector containing the ranks of the alternatives. The elements are named according to the IDs of the alternatives. If not present, then at least one of alternativesPreferences or alternativesIndifferences should be given.

alternativesPreferences

Optional matrix containing the preference constraints on the alternatives. Each line of the matrix corresponds to a constraint of the type alternative a is strictly preferred to alternative b. If not present, then either alternativesRanks or alternativesIndifferences should be given.

alternativesIndifferences

Optional matrix containing the indifference constraints on the alternatives. Each line of the matrix corresponds to a constraint of the type alternative a is indifferent to alternative b. If not present, then either alternativesRanks or alternativesPreferences should be given.

alternativesIDs

Vector containing IDs of alternatives, according to which the datashould be filtered.

criteriaIDs Vector containing IDs of criteria, according to which the data should be filtered.

#### Value

The function returns a list structured as follows:

optimum The value of the objective function.

valueFunctions A list containing the value functions which have been determined. Each value

function is defined by a matrix of breakpoints, where the first row corresponds to the abscissa (row labelled "x") and where the second row corresponds to the

ordinate (row labelled "y").

overall values A vector containing the overall values of the input alternatives.

ranks A vector containing the ranks of the alternatives obtained via the elicited value

functions. Ties method = "min".

Kendall's tau between the input ranking and the one obtained via the elicited

value functions.

errors The errors (sigma) which have to be added to the overall values of the alterna-

tives in order to respect the input ranking.

#### References

Based on the UTA algorithm (E. Jacquet-Lagreze, J. Siskos, Assessing a set of additive utility functions for multicriteria decision-making, the UTA method, European Journal of Operational Research, Volume 10, Issue 2, 151–164, June 1982) except that the breakpoints of the value functions are the actual performances of the alternatives on the criteria.

```
# ranking some cars (from original article on UTA by Siskos and Lagreze, 1982)
# the separation threshold
epsilon <-0.01
# the performance table
performanceTable <- rbind(</pre>
c(173, 11.4, 10.01, 10, 7.88, 49500),
c(176, 12.3, 10.48, 11, 7.96, 46700),
c(142, 8.2, 7.30, 5, 5.65, 32100),
c(148, 10.5, 9.61, 7, 6.15, 39150),
c(178, 14.5, 11.05, 13, 8.06, 64700),
c(180, 13.6, 10.40, 13, 8.47, 75700),
c(182, 12.7, 12.26, 11, 7.81, 68593),
c(145, 14.3, 12.95, 11, 8.38, 55000),
c(161, 8.6, 8.42, 7, 5.11, 35200),
c(117, 7.2, 6.75, 3, 5.81, 24800)
)
rownames(performanceTable) <- c(</pre>
```

AHP 5

```
"Peugeot 505 GR",
  "Opel Record 2000 LS",
  "Citroen Visa Super E",
 "VW Golf 1300 GLS",
 "Citroen CX 2400 Pallas",
 "Mercedes 230",
 "BMW 520",
 "Volvo 244 DL",
  "Peugeot 104 ZS",
  "Citroen Dyane")
colnames(performanceTable) <- c(</pre>
  "MaximalSpeed",
  {\tt "ConsumptionTown"}
  "Consumption120kmh",
  "HP",
  "Space",
 "Price")
# ranks of the alternatives
alternativesRanks <- c(1,2,3,4,5,6,7,8,9,10)
names(alternativesRanks) <- row.names(performanceTable)</pre>
# criteria to minimize or maximize
criteriaMinMax <- c("max","min","min","max","max","min")</pre>
names(criteriaMinMax) <- colnames(performanceTable)</pre>
x<-additiveValueFunctionElicitation(performanceTable,
                                        criteriaMinMax, epsilon,
                                        alternativesRanks = alternativesRanks)
```

AHP

Analytic Hierarchy Process (AHP) method

# **Description**

AHP is a multi-criteria decision analysis method which was originally developed by Thomas L. Saaty in 1970s.

## Usage

 $AHP (criteria Weights Pairwise Comparisons, \ alternatives Pairwise Comparisons List)\\$ 

6 AHP

## **Arguments**

criteriaWeightsPairwiseComparisons

Matrix or data frame containing the pairwise comparison matrix for the criteria weights. Lines and columns are named according to the IDs of the criteria.

alternativesPairwiseComparisonsList

A list containing a matrix or data frame of pairwise comparisons (comparing alternatives) for each criterion. The elements of the list are named according to the IDs of the criteria. In each matrix, the lines and the columns are named according to the IDs of the alternatives.

#### Value

The function returns a vector containing the AHP score for each alternative.

#### References

The Analytic Hierarchy Process: Planning, Priority Setting (1980), ISBN 0-07-054371-2, McGraw-Hill

```
style <- t(matrix(c(1,0.25,4,1/6,4,1,4,0.25,0.25,0.25,1,0.2,6,4,5,1),
                  nrow=4,ncol=4))
colnames(style) = c("Corsa","Clio","Fiesta","Sandero")
rownames(style) = c("Corsa", "Clio", "Fiesta", "Sandero")
reliability <- t(matrix(c(1,2,5,1,0.5,1,3,2,0.2,1/3,1,0.25,1,0.5,4,1),
                        nrow=4,ncol=4))
colnames(reliability) = c("Corsa","Clio","Fiesta","Sandero")
rownames(reliability) = c("Corsa", "Clio", "Fiesta", "Sandero")
fuel <- t(matrix(c(1,2,4,1,0.5,1,3,2,0.25,1/3,1,0.2,1,0.5,5,1),nrow=4,ncol=4))
colnames(fuel) = c("Corsa", "Clio", "Fiesta", "Sandero")
rownames(fuel) = c("Corsa","Clio","Fiesta","Sandero")
alternativesPairwiseComparisonsList <- list(style=style,</pre>
                                              reliability=reliability,
                                              fuel=fuel)
criteriaWeightsPairwiseComparisons \leftarrow t(matrix(c(1,0.5,3,2,1,4,1/3,0.25,1),
                                                    nrow=3,ncol=3))
colnames(criteriaWeightsPairwiseComparisons) = c("style","reliability","fuel")
rownames(criteriaWeightsPairwiseComparisons) = c("style", "reliability", "fuel")
overall1 <- AHP(criteriaWeightsPairwiseComparisons,</pre>
                  alternativesPairwiseComparisonsList)
```

applyPiecewiseLinearValueFunctionsOnPerformanceTable Applies value functions on a performance table.

# **Description**

Transforms a performance table via given piecewise linear value functions.

## Usage

```
apply \verb|PiecewiseLinearValueFunctionsOnPerformanceTable(valueFunctions, apply \verb|PiecewiseLinearValueFunctions|) apply \verb|PiecewiseLinearValueFunctionsOnPerformanceTable(valueFunctions, apply \verb|PiecewiseLinearValueFunctions|) apply \verb|PiecewiseLinearValueFunctionsOnPerformanceTable(valueFunctions, apply \verb|PiecewiseLinearValueFunctions|) apply \verb|PiecewiseLinearValueFunctionsOnPerformanceTable(valueFunctions, apply \verb|PiecewiseLinearValueFunctions|) apply 
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              performanceTable,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              alternativesIDs = NULL,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              criteriaIDs = NULL)
```

## **Arguments**

valueFunctions A list containing, for each criterion, the piecewise linear value functions defined by the coordinates of the break points. Each value function is defined by a matrix of breakpoints, where the first row corresponds to the abscissa (row labelled "x") and where the second row corresponds to the ordinate (row labelled "y").

performanceTable

Matrix or data frame containing the performance table. Each row corresponds to an alternative, and each column to a criterion. Rows (resp. columns) must be named according to the IDs of the alternatives (resp. criteria).

alternativesIDs

Vector containing IDs of alternatives, according to which the datashould be fil-

criteriaIDs

Vector containing IDs of criteria, according to which the data should be filtered.

#### Value

The function returns a performance table which has been transformed through the given value functions.

```
# the value functions
v<-list(
 Price = array(c(30, 0, 16, 0, 2, 0.0875),
   dim=c(2,3), dimnames = list(c("x", "y"), NULL)),
 Time = array(c(40, 0, 30, 0, 20, 0.025, 10, 0.9),
   dim = c(2, 4), dimnames = list(c("x", "y"), NULL)),
 Comfort = array(c(0, 0, 1, 0, 2, 0.0125, 3, 0.0125),
   dim = c(2, 4), dimnames = list(c("x", "y"), NULL)))
```

 $assign \verb|Alternatives| To Categories By Thresholds$ 

Assign alternatives to categories according to thresholds.

# Description

Assign alternatives to categories according to thresholds representing the lower bounds of the categories.

# Usage

## **Arguments**

alternativesScores

Vector representing the overall scores of the alternatives. The elements are named according to the IDs of the alternatives.

categoriesLowerBounds

Vector containing the lower bounds of the categories. An alternative is assigned to a category if it's score is higher or equal to the lower bound of the category, and strictly lower to the lower bound of the category above.

alternativesIDs

Vector containing IDs of alternatives, according to which the datashould be filtered.

categoriesIDs Vector containing IDs of categories, according to which the data should be filtered.

## Value

The function returns a vector containing the assignments of the alternatives to the categories.

```
# the separation threshold
epsilon <-0.05
# the performance table
performanceTable <- rbind(</pre>
  c(3,10,1),
  c(4,20,2),
  c(2,20,0),
  c(6,40,0),
  c(30,30,3))
rownames(performanceTable) <- c("RER", "METRO1", "METRO2", "BUS", "TAXI")</pre>
colnames(performanceTable) <- c("Price", "Time", "Comfort")</pre>
# ranks of the alternatives
alternativesAssignments <- c("good", "medium", "medium", "bad", "bad")</pre>
names(alternativesAssignments) <- row.names(performanceTable)</pre>
# criteria to minimize or maximize
criteriaMinMax <- c("min", "min", "max")</pre>
names(criteriaMinMax) <- colnames(performanceTable)</pre>
# number of break points for each criterion
criteriaNumberOfBreakPoints <- c(3,4,4)</pre>
names(criteriaNumberOfBreakPoints) <- colnames(performanceTable)</pre>
# ranks of the categories
categoriesRanks <-c(1,2,3)
names(categoriesRanks) <- c("good", "medium", "bad")</pre>
x<-UTADIS(performanceTable, criteriaMinMax, criteriaNumberOfBreakPoints,
             alternativesAssignments, categoriesRanks, 0.1)
npt <- applyPiecewiseLinearValueFunctionsOnPerformanceTable(x$valueFunctions,</pre>
                                                                  performanceTable)
```

10 ELECTREIIIDistillation

```
scores <- weightedSum(npt, c(1,1,1))
# add a lower bound for the "bad" category
lbs <- c(x$categoriesLBs,0)
names(lbs) <- c(names(x$categoriesLBs),"bad")
assignments<-assignAlternativesToCategoriesByThresholds(scores,lbs)</pre>
```

ELECTREIIIDistillation

ELECTRE III ranking

# **Description**

This function computes the two ELECTRE III distillations, or rankings.

# Usage

```
ELECTREIIIDistillation(performanceTable, criteriaWeights, minMaxcriteria, preferenceThresholds, indifferenceThresholds, vetoThresholds)
```

## **Arguments**

performanceTable

Matrix or data frame containing the performance table. Each row corresponds to an alternative, and each column to a criterion. Rows (resp. columns) must be named according to the IDs of the alternatives (resp. criteria).

criteriaWeights

Vector containing the weights of the criteria. The elements are named according to the IDs of the criteria.

minMaxcriteria Vector containing the preference direction on each of the criteria. "min" (resp. "max") indicates that the criterion has to be minimized (maximized). The elements are named according to the IDs of the criteria.

preferenceThresholds

Vector containing preference thresholds for each criterion.

indifferenceThresholds

Vector containing indifferences thresholds for each criterion.

vetoThresholds Vector containing veto thresholds for each criterion.

LPDMRSort 11

#### Value

The function returns two lists, one for each distillation.

# **Examples**

```
performanceTable <- rbind(</pre>
c(10,20,5,10,16),
c(0,5,5,16,10),
c(0,10,0,16,7),
c(20,5,10,10,13),
c(20,10,15,10,13),
c(20,10,20,13,13))
rownames(performanceTable) <-c("P1","P2","P3","P4","P5","P6")</pre>
colnames(performanceTable) <-c("CRIT1","CRIT2","CRIT3","CRIT4","CRIT5")</pre>
## vector indicating the direction of the criteria evaluation .
minMaxcriteria <-c("max","max","max","max","max")</pre>
names(minMaxcriteria) <- colnames(performanceTable)</pre>
## criteriaWeights vector
criteriaWeights \leftarrow c(3,2,3,1,1)
names(criteriaWeights) <- colnames(performanceTable)</pre>
indifferenceThresholds<-c(3,3,3,3,3)</pre>
names(indifferenceThresholds) <- colnames(performanceTable)</pre>
preferenceThresholds<-c(5,5,5,5,5)</pre>
names(preferenceThresholds) <- colnames(performanceTable)</pre>
vetoThresholds<-c(11,11,11,11,11)
names(vetoThresholds) <- colnames(performanceTable)</pre>
ELECTREIIIDistillation(performanceTable,criteriaWeights,minMaxcriteria,
                         preferenceThresholds,indifferenceThresholds,
                         vetoThresholds)
```

**LPDMRSort** 

MRSort that takes into account large performance differences.

# Description

MRSort is a simplified ElectreTRI method that uses the pessimistic assignment rule, without indifference or preference thresholds attached to criteria. LPDMRSort considers both a binary discordance and a binary concordance conditions including several interactions between them.

# Usage

12 **LPDMRSort** 

#### **Arguments**

performanceTable

Matrix or data frame containing the performance table. Each row corresponds to an alternative, and each column to a criterion. Rows (resp. columns) must be named according to the IDs of the alternatives (resp. criteria).

categoriesLowerProfiles

Matrix containing, in each row, the lower profiles of the categories. The columns are named according to the criteria, and the rows are named according to the categories. The index of the row in the matrix corresponds to the rank of the category.

categoriesRanks

A vector containing the ranks of the categories (1 for the best, with higher values for increasingly less preferred categories). The vector needs to be named with the categories names, whereas the ranks need to be a range of values from 1 to the number of categories.

criteriaWeights

Vector containing the weights of the criteria. The elements are named according to the IDs of the criteria.

criteriaMinMax Vector containing the preference direction on each of the criteria. "min" (resp. "max") indicates that the criterion has to be minimized (maximized). The elements are named according to the IDs of the criteria.

majorityThreshold

The cut threshold for the concordance condition. Should be at least half of the sum of the weights.

criteriaVetos

Matrix containing in each row a vector defining the veto values for the lower profile of the category. NA values mean that no veto is defined. A veto threshold for criterion i and category k represents the performance below which an alternative is forbidden to outrank the lower profile of category k, and thus is forbidden to be assigned to the category k. The rows are named according to the categories, whereas the columns are named according to the criteria.

criteriaDictators

Matrix containing in each row a vector defining the dictator values for the lower profile of the category. NA values mean that no veto is defined. A dictator threshold for criterion i and category k represents the performance above which an alternative is guaranteed to outrank the lower profile of category k, and thus may no be assigned below category k. The rows are named according to the categories, whereas the columns are named according to the criteria.

majorityRule

String denoting how the vetoes and dictators are combined in order to form the assignment rule. The values to choose from are "M", "V", "D", "v", "d", "dV", "Dv", "dv". "M" corresponds to using only the majority rule without vetoes or dictators, "V" considers only the vetoes, "D" only the dictators, "v" is like "V" only that a dictator may invalidate a veto, "d" is like "D" only that a veto may invalidate a dictator, "dV" is like "V" only that if there is no veto we may then consider the dictator, "Dv" is like "D" only that when there is no dictator we may consider the vetoes, while finally "dv" is identical to using both dictator and vetoes only that when both are active they invalidate each other, so the majority rule is considered in that case.

LPDMRSort 13

alternativesIDs

Vector containing IDs of alternatives, according to which the datashould be fil-

criteriaIDs Vector containing IDs of criteria, according to which the data should be filtered.

categoriesIDs Vector containing IDs of categories, according to which the data should be fil-

tered.

#### Value

The function returns a vector containing the assignments of the alternatives to the categories.

#### References

Bouyssou, D. and Marchant, T. An axiomatic approach to noncompensatory sorting methods in MCDM, II: more than two categories. European Journal of Operational Research, 178(1): 246–276, 2007.

Meyer, P. and Olteanu, A-L. Integrating large positive and negative performance differences in majority-rule sorting models. European Journal of Operational Research, submitted, 2015.

```
# the performance table
performanceTable <- rbind(c(10,10,9), c(10,9,10), c(9,10,10), c(9,9,10),
                           c(9,10,9), c(10,9,9), c(10,10,7), c(10,7,10),
                           c(7,10,10), c(9,9,17), c(9,17,9), c(17,9,9),
                           c(7,10,17), c(10,17,7), c(17,7,10), c(7,17,10),
                           c(17,10,7), c(10,7,17), c(7,9,17), c(9,17,7),
                           c(17,7,9), c(7,17,9), c(17,9,7), c(9,7,17))
profilesPerformances <- rbind(c(10,10,10),c(0,0,0))
vetoPerformances <- rbind(c(7,7,7),c(0,0,0))
dictatorPerformances <- rbind(c(17,17,17),c(0,0,0))
rownames(performanceTable) <- c("a1", "a2", "a3", "a4", "a5", "a6", "a7",
                                 "a8", "a9", "a10", "a11", "a12", "a13",
                                 "a14", "a15", "a16", "a17", "a18", "a19",
                                 "a20", "a21", "a22", "a23", "a24")
rownames(profilesPerformances) <- c("P", "F")</pre>
rownames(vetoPerformances) <- c("P","F")</pre>
rownames(dictatorPerformances) <- c("P", "F")</pre>
colnames(performanceTable) <- c("c1","c2","c3")</pre>
colnames(profilesPerformances) <- c("c1","c2","c3")</pre>
```

```
colnames(vetoPerformances) <- c("c1","c2","c3")</pre>
colnames(dictatorPerformances) <- c("c1","c2","c3")</pre>
lambda <- 0.5
weights <- c(1/3, 1/3, 1/3)
names(weights) <- c("c1","c2","c3")</pre>
categoriesRanks <-c(1,2)</pre>
names(categoriesRanks) <- c("P","F")</pre>
criteriaMinMax <- c("max", "max", "max")</pre>
names(criteriaMinMax) <- colnames(performanceTable)</pre>
colnames(assignments) <- rownames(performanceTable)</pre>
majorityRules <- c("V","D","v","d","dV","Dv","dv")</pre>
for(i in 1:7)
 ElectreAssignments<-LPDMRSort(performanceTable, profilesPerformances,</pre>
                 categoriesRanks,
                 weights, criteriaMinMax, lambda,
                 criteriaVetos=vetoPerformances,
                 criteriaDictators=dictatorPerformances,
                 majorityRule = majorityRules[i])
 print(all(ElectreAssignments == assignments[i,]))
}
```

LPDMRSortIdentifyIncompatibleAssignments

Identifies all sets of assignment examples which are incompatible with the MRSort sorting method extended to handle large performance differences.

## **Description**

MRSort is a simplified ElectreTRI method that uses the pessimistic assignment rule, without indifference or preference thresholds attached to criteria. LPDMRSort considers both a binary discordance and a binary concordance conditions including several interactions between them. This function outputs all (or a fixed number of) sets of incompatible assignment examples ranging in size from the minimal size and up to a given threshold. The retrieved sets are also not contained in each other.

# Usage

## **Arguments**

performanceTable

Matrix or data frame containing the performance table. Each row corresponds to an alternative, and each column to a criterion. Rows (resp. columns) must be named according to the IDs of the alternatives (resp. criteria).

assignments

Vector containing the assignments (IDs of the categories) of the alternatives to the categories. The elements are named according to the alternatives.

categoriesRanks

Vector containing the ranks of the categories. The elements are named according to the IDs of the categories.

criteriaMinMax

Vector containing the preference direction on each of the criteria. "min" (resp. "max") indicates that the criterion has to be minimized (maximized). The elements are named according to the IDs of the criteria.

majorityRule

String denoting how the vetoes and dictators are combined in order to form the assignment rule. The values to choose from are "M", "V", "D", "v", "d", "dV", "Dv", "dv". "M" corresponds to using only the majority rule without vetoes

or dictators, "V" considers only the vetoes, "D" only the dictators, "v" is like "V" only that a dictator may invalidate a veto, "d" is like "D" only that a veto may invalidate a dictator, "dV" is like "V" only that if there is no veto we may then consider the dictator, "Dv" is like "D" only that when there is no dictator we may consider the vetoes, while finally "dv" is identical to using both dictator and vetoes only that when both are active they invalidate each other, so the majority rule is considered in that case.

## incompatibleSetsLimit

Pozitive integer denoting the upper limit of the number of sets to be retrieved.

#### largerIncompatibleSetsMargin

Pozitive integer denoting whether sets larger than the minimal size should be retrieved, and by what margin. For example, if this is 0 then only sets of the minimal size will be retrieved, if this is 1 then sets also larger by 1 element will be retrieved.

#### alternativesIDs

Vector containing IDs of alternatives, according to which the datashould be filtered.

criteriaIDs Vector containing IDs of criteria, according to which the data should be filtered.

solver String specifying if the glpk solver (glpk) should be used, or the cplex (cplex)

solver. By default glpk. The cplex solver requires to install the cplex binary and the cplex C API, as well as the cplexAPI R package.

cplexIntegralityTolerance

If the cplex solver is used, allows to fix a tolerance for integrality. By default NULL (which corresponds to the default value of cplex).

cplexThreads If the cplex solver is used, allows to the number of threads for the calculation.

By default NULL (which corresponds to the default value of cplex).

#### Value

The function returns NULL if there is a problem, or a list containing a list of incompatible sets of alternatives as vectors and the status of the execution.

# References

Bouyssou, D. and Marchant, T. An axiomatic approach to noncompen-satory sorting methods in MCDM, II: more than two categories. European Journal of Operational Research, 178(1): 246–276, 2007.

Meyer, P. and Olteanu, A-L. Integrating large positive and negative performance differences in majority-rule sorting models. European Journal of Operational Research, submitted, 2015.

```
# the performance table
```

```
performanceTable <- rbind(c(10,10,9), c(10,9,10), c(9,10,10), c(9,9,10),
c(9,10,9), c(10,9,9), c(10,10,7), c(10,7,10),
c(7,10,10), c(9,9,17), c(9,17,9), c(17,9,9),
c(7,10,17), c(10,17,7), c(17,7,10), c(7,17,10),
```

```
c(17,10,7), c(10,7,17), c(7,9,17), c(9,17,7),
                c(17,7,9), c(7,17,9), c(17,9,7), c(9,7,17),
                c(7,7,7))
rownames(performanceTable) <- c("a1", "a2", "a3", "a4", "a5", "a6", "a7",
                    "a8", "a9", "a10", "a11", "a12", "a13",
                    "a14", "a15", "a16", "a17", "a18", "a19",
                    "a20", "a21", "a22", "a23", "a24", "a25")
colnames(performanceTable) <- c("c1","c2","c3")</pre>
colnames(assignments) <- rownames(performanceTable)</pre>
categoriesRanks <-c(1,2)</pre>
names(categoriesRanks) <- c("P","F")</pre>
criteriaMinMax <- c("max", "max", "max")</pre>
names(criteriaMinMax) <- colnames(performanceTable)</pre>
majorityRules <- c("V","D","v","d","dV","Dv","dv")</pre>
for(i in 1:1)# change to 7 in order to perform all tests
{
 incompatibleAssignmentsSets<-LPDMRSortIdentifyIncompatibleAssignments(</pre>
                    performanceTable, assignments[i,],
                    categoriesRanks, criteriaMinMax,
                    majorityRule = majorityRules[i])
 filteredAlternativesIDs <- setdiff(rownames(performanceTable),</pre>
                       incompatibleAssignmentsSets[[1]][1])
 x<-LPDMRSortInferenceExact(performanceTable, assignments[i,],</pre>
                  categoriesRanks, criteriaMinMax,
                  majorityRule = majorityRules[i],
                  readableWeights = TRUE,
                  readableProfiles = TRUE,
```

LPDMRSortIdentifyUsedDictatorProfiles

Identify dictator profiles evaluations that have an impact on the final assignments of MRSort with large performance differences

# **Description**

MRSort is a simplified ELECTRE-TRI approach which assigns alternatives to a set of ordered categories using delimiting profiles evaluations. In this case, we also take into account large performance differences. This method is used to identify which dictator profiles evaluations have an impact on the final assignment of at least one of the input alternatives.

## Usage

```
LPDMRSortIdentifyUsedDictatorProfiles(performanceTable, assignments, categoriesRanks, criteriaMinMax, majorityThreshold, criteriaWeights, profilesPerformances, dictatorPerformances, vetoPerformances = NULL, majorityRule = "D", alternativesIDs = NULL, criteriaIDs = NULL)
```

## **Arguments**

performanceTable

Matrix or data frame containing the performance table. Each row corresponds to an alternative, and each column to a criterion. Rows (resp. columns) must be named according to the IDs of the alternatives (resp. criteria).

assignments

A vector containing the category to which each alternative is assigned. The vector needs to be named using the alternatives IDs.

#### categoriesRanks

A vector containing the ranks of the categories (1 for the best, with higher values for increasingly less preferred categories). The vector needs to be named with the categories names, whereas the ranks need to be a range of values from 1 to the number of categories.

criteriaMinMax

Vector containing the preference direction on each of the criteria. "min" (resp. "max") indicates that the criterion has to be minimized (maximized). The elements are named according to the IDs of the criteria.

#### majorityThreshold

The majority threshold needed to determine when a coalition of criteria is sufficient in order to validate an outranking relation.

# criteriaWeights

Vector containing the weights of the criteria. The elements are named according to the IDs of the criteria.

# profilesPerformances

Matrix containing, in each row, the lower profiles of the categories. The columns are named according to the criteria, and the rows are named according to the categories. The index of the row in the matrix corresponds to the rank of the category.

#### dictatorPerformances

Matrix containing in each row a vector defining the dictator values for the lower profile of the category. NA values mean that no dictator is defined. A dictator threshold for criterion i and category k represents the performance above which an alternative outranks the lower profile of category k regardless of the size of the coalition of criteria in favor of this statement. The rows are named according to the categories, whereas the columns are named according to the criteria.

# vetoPerformances

Matrix containing in each row a vector defining the veto values for the lower profile of the category. NA values mean that no veto is defined. A veto threshold for criterion i and category k represents the performance below which an alternative is forbidden to outrank the lower profile of category k, and thus is forbidden to be assigned to the category k. The rows are named according to the categories, whereas the columns are named according to the criteria. By default no veto profiles are needed.

majorityRule

String denoting how the vetoes and dictators are combined in order to form the assignment rule. The values to choose from are "D", "v", "d", "dV", "Dv", "dv". "D" considers only the dictators, "v" is like "V" only that a dictator may invalidate a veto, "d" is like "D" only that a veto may invalidate a dictator, "dV" is like "V" only that if there is no veto we may then consider the dictator, "Dv" is like "D" only that when there is no dictator we may consider the vetoes, while finally "dv" is identical to using both dictator and vetoes only that when both are active they invalidate each other, so the majority rule is considered in that case.

#### alternativesIDs

Vector containing IDs of alternatives, according to which the datashould be filtered.

criteriaIDs

Vector containing IDs of criteria, according to which the data should be filtered.

#### Value

The function returns a matrix containing TRUE/FALSE inficators for each evaluation of the veto profiles.

```
# the performance table
performanceTable <- rbind(</pre>
  c(1,27,1),
  c(6,20,1),
  c(2,20,0),
  c(6,40,0),
  c(30,10,3))
rownames(performanceTable) <- c("RER", "METRO1", "METRO2", "BUS", "TAXI")</pre>
colnames(performanceTable) <- c("Price", "Time", "Comfort")</pre>
# lower profiles of the categories (best category in the first position of the list)
categoriesLowerProfiles <- rbind(c(3, 11, 3),c(7, 25, 2),c(NA,NA,NA))</pre>
colnames(categoriesLowerProfiles) <- colnames(performanceTable)</pre>
rownames(categoriesLowerProfiles)<-c("Good", "Medium", "Bad")</pre>
# the order of the categories, 1 being the best
categoriesRanks <-c(1,2,3)</pre>
names(categoriesRanks) <- c("Good", "Medium", "Bad")</pre>
# criteria to minimize or maximize
criteriaMinMax <- c("min", "min", "max")</pre>
names(criteriaMinMax) <- colnames(performanceTable)</pre>
# dictators
criteriaDictators <- rbind(c(1, 1, -1), c(1, 20, 0), c(NA, NA, NA))
colnames(criteriaDictators) <- colnames(performanceTable)</pre>
rownames(criteriaDictators) <- c("Good", "Medium", "Bad")</pre>
# vetos
criteria Vetos <- rbind(c(9, 50, 5), c(50, 50, 5), c(NA, NA, NA))
colnames(criteriaVetos) <- colnames(performanceTable)</pre>
rownames(criteriaVetos) <- c("Good", "Medium", "Bad")</pre>
```

```
# weights
criteriaWeights <- c(1/6,3/6,2/6)
names(criteriaWeights) <- colnames(performanceTable)
# assignments
assignments <- c("Good","Medium","Bad","Bad","Bad")
# LPDMRSortIndetifyUsedVetoProfiles
used<-LPDMRSortIdentifyUsedDictatorProfiles(performanceTable, assignments, categoriesRanks, criteriaMinMax, 0.5, criteriaWeights, categoriesLowerProfiles, criteriaDictators, criteriaDictators, criteriaVetos, "dv")</pre>
```

LPDMRSortIdentifyUsedVetoProfiles

Identify veto profiles evaluations that have an impact on the final assignments of MRSort with large performance differences

# Description

MRSort is a simplified ELECTRE-TRI approach which assigns alternatives to a set of ordered categories using delimiting profiles evaluations. In this case, we also take into account large performance differences. This method is used to identify which veto profiles evaluations have an impact on the final assignment of at least one of the input alternatives.

# Usage

## Arguments

performanceTable

Matrix or data frame containing the performance table. Each row corresponds to an alternative, and each column to a criterion. Rows (resp. columns) must be named according to the IDs of the alternatives (resp. criteria).

assignments

A vector containing the category to which each alternative is assigned. The vector needs to be named using the alternatives IDs.

categoriesRanks

A vector containing the ranks of the categories (1 for the best, with higher values for increasingly less preferred categories). The vector needs to be named with the categories names, whereas the ranks need to be a range of values from 1 to the number of categories.

criteriaMinMax

Vector containing the preference direction on each of the criteria. "min" (resp. "max") indicates that the criterion has to be minimized (maximized). The elements are named according to the IDs of the criteria.

majorityThreshold

The majority threshold needed to determine when a coalition of criteria is sufficient in order to validate an outranking relation.

criteriaWeights

Vector containing the weights of the criteria. The elements are named according to the IDs of the criteria.

profilesPerformances

Matrix containing, in each row, the lower profiles of the categories. The columns are named according to the criteria, and the rows are named according to the categories. The index of the row in the matrix corresponds to the rank of the category.

vetoPerformances

Matrix containing in each row a vector defining the veto values for the lower profile of the category. NA values mean that no veto is defined. A veto threshold for criterion i and category k represents the performance below which an alternative is forbidden to outrank the lower profile of category k, and thus is forbidden to be assigned to the category k. The rows are named according to the categories, whereas the columns are named according to the criteria.

# dictatorPerformances

Matrix containing in each row a vector defining the dictator values for the lower profile of the category. NA values mean that no dictator is defined. A dictator threshold for criterion i and category k represents the performance above which an alternative outranks the lower profile of category k regardless of the size of the coalition of criteria in favor of this statement. The rows are named according to the categories, whereas the columns are named according to the criteria. By default no dictator profiles are needed for this method.

majorityRule

String denoting how the vetoes and dictators are combined in order to form the assignment rule. The values to choose from are "V", "v", "d", "dV", "Dv", "dv". "V" considers only the vetoes, "v" is like "V" only that a dictator may invalidate a veto, "d" is like "D" only that a veto may invalidate a dictator, "dV" is like "V" only that if there is no veto we may then consider the dictator, "Dv" is like

"D" only that when there is no dictator we may consider the vetoes, while finally "dv" is identical to using both dictator and vetoes only that when both are active they invalidate each other, so the majority rule is considered in that case.

alternativesIDs

Vector containing IDs of alternatives, according to which the datashould be filtered.

criteriaIDs

Vector containing IDs of criteria, according to which the data should be filtered.

# Value

The function returns a matrix containing TRUE/FALSE inficators for each evaluation of the veto profiles.

```
# the performance table
performanceTable <- rbind(</pre>
  c(1,27,1),
  c(6,20,1),
  c(2,20,0),
  c(6,40,0).
  c(30,10,3))
rownames(performanceTable) <- c("RER", "METRO1", "METRO2", "BUS", "TAXI")</pre>
colnames(performanceTable) <- c("Price", "Time", "Comfort")</pre>
# lower profiles of the categories (best category in the first position of the list)
categoriesLowerProfiles <- rbind(c(3, 11, 3),c(7, 25, 2),c(NA,NA,NA))</pre>
colnames(categoriesLowerProfiles) <- colnames(performanceTable)</pre>
rownames(categoriesLowerProfiles)<-c("Good", "Medium", "Bad")</pre>
# the order of the categories, 1 being the best
categoriesRanks <-c(1,2,3)</pre>
names(categoriesRanks) <- c("Good", "Medium", "Bad")</pre>
# criteria to minimize or maximize
criteriaMinMax <- c("min", "min", "max")</pre>
names(criteriaMinMax) <- colnames(performanceTable)</pre>
# dictators
criteriaDictators <- rbind(c(1, 1, -1), c(1, 20, 0), c(NA, NA, NA))
```

```
colnames(criteriaDictators) <- colnames(performanceTable)</pre>
rownames(criteriaDictators) <- c("Good", "Medium", "Bad")</pre>
# vetos
criteriaVetos <- rbind(c(9, 50, 5), c(50, 50, 5), c(NA, NA, NA))
colnames(criteriaVetos) <- colnames(performanceTable)</pre>
rownames(criteriaVetos) <- c("Good", "Medium", "Bad")</pre>
# weights
criteriaWeights <- c(1/6,3/6,2/6)
names(criteriaWeights) <- colnames(performanceTable)</pre>
# assignments
assignments <- c("Good", "Medium", "Bad", "Bad", "Bad")</pre>
# LPDMRSortIndetifyUsedVetoProfiles
used<-LPDMRSortIdentifyUsedVetoProfiles(performanceTable, assignments,</pre>
                                            categoriesRanks, criteriaMinMax,
                                           0.5, criteriaWeights,
                                            categoriesLowerProfiles,
                                            criteriaVetos,
                                            criteriaDictators,
                                            "dv")
```

LPDMRSortInferenceApprox

Identification of profiles, weights, majority threshold, veto and dictator thresholds for LPDMRSort using a genetic algorithm.

# **Description**

MRSort is a simplified ElectreTRI method that uses the pessimistic assignment rule, without indifference or preference thresholds attached to criteria. LPDMRSort considers both a binary discordance and a binary concordance conditions including several interactions between them. The identification of the profiles, weights, majority threshold and veto thresholds is done by taking into account assignment examples.

## Usage

#### **Arguments**

performanceTable

Matrix or data frame containing the performance table. Each row corresponds to an alternative, and each column to a criterion. Rows (resp. columns) must be named according to the IDs of the alternatives (resp. criteria).

assignments Vector containing the assignments (IDs of the categories) of the alternatives to

the categories. The elements are named according to the alternatives.

categoriesRanks

Vector containing the ranks of the categories. The elements are named according to the IDs of the categories.

criteriaMinMax Vector containing the preference direction on each of the criteria. "min" (resp.

"max") indicates that the criterion has to be minimized (maximized). The ele-

ments are named according to the IDs of the criteria.

majorityRules A vector containing the different type of majority rules to be considered ("M",

"V", "D", "v", "d", "dV", "Dv", "dv"). "M" corresponds to using only the majority rule without vetoes or dictators, "V" considers only the vetoes, "D" only the dictators, "v" is like "V" only that a dictator may invalidate a veto, "d" is like "D" only that a veto may invalidate a dictator, "dV" is like "V" only that if there is no veto we may then consider the dictator, "Dv" is like "D" only that when there is no dictator we may consider the vetoes, while finally "dv" is identical to using both dictator and vetoes only that when both are active they invalidate each other, so the majority rule is considered in that case.

alternativesIDs

Vector containing IDs of alternatives, according to which the data should be

filtered.

criteriaIDs Vector containing IDs of criteria, according to which the data should be filtered.

timeLimit Allows to fix a time limit of the execution, in seconds (default 60).

populationSize Allows to change the size of the population used by the genetic algorithm (de-

fault 20).

mutationProb Allows to change the mutation probability used by the genetic algorithm (default

0.1).

#### Value

The function returns a list containing:

majorityThreshold

The inferred majority threshold (single numeric value).

criteriaWeights

The inferred criteria weights (a vector named with the criteria IDs).

majorityRule A string corresponding to the inferred majority rule (one of "M", "V", "D", "v", "d", "dV", "Dv", "dv").

profilesPerformances

The inferred category limits (a matrix with the column names given by the criteria IDs and the rownames given by the upper categories each profile delimits).

vetoPerformances

The inferred vetoes (a matrix with the column names given by the criteria IDs and the rownames given by the categories to which each profile applies).

dictatorPerformances

The inferred dictators (a matrix with the column names given by the criteria IDs and the rownames given by the categories to which each profile applies).

fitness

The classification accuracy of the inferred model (from 0 to 1).

#### References

Bouyssou, D. and Marchant, T. An axiomatic approach to noncompen- satory sorting methods in MCDM, II: more than two categories. European Journal of Operational Research, 178(1): 246–276, 2007.

no reference yet for the algorithmic approach; one should become available in 2018

```
performanceTable <- rbind(c(10,10,9), c(10,9,10), c(9,10,10), c(9,9,10), c(9,10,9), c(10,9,9),
                         c(10,10,7),c(10,7,10),c(7,10,10),c(9,9,17),c(9,17,9),c(17,9,9),
                      c(7,10,17),c(10,17,7),c(17,7,10),c(7,17,10),c(17,10,7),c(10,7,17),
                           c(7,9,17),c(9,17,7),c(17,7,9),c(7,17,9),c(17,9,7),c(9,7,17))
rownames(performanceTable) <- c("a1", "a2", "a3", "a4", "a5", "a6", "a7", "a8", "a9", "a10", "a11", "a12", "a13", "a14", "a15", "a16", "a17", "a18", "a19", "a20",
                                 "a21", "a22", "a23", "a24")
colnames(performanceTable) <- c("c1","c2","c3")</pre>
"F", "F", "F", "F")
names(assignments) <- rownames(performanceTable)</pre>
categoriesRanks <- c(1,2)</pre>
names(categoriesRanks) <- c("P","F")</pre>
criteriaMinMax <- c("max","max","max")</pre>
names(criteriaMinMax) <- colnames(performanceTable)</pre>
set.seed(1)
x<-LPDMRSortInferenceApprox(performanceTable, criteriaMinMax, categoriesRanks, assignments,
                             majorityRules = c("dV","Dv","dv"),
                             timeLimit = 180, populationSize = 30,
                             alternativesIDs = c("a1", "a2", "a3", "a4", "a5", "a6", "a7"))
```

#### LPDMRSortInferenceExact

Identification of profiles, weights, majority threshold and veto and dictator thresholds for the MRSort sorting approach extended to handle large performance differences.

# **Description**

MRSort is a simplified ElectreTRI method that uses the pessimistic assignment rule, without indifference or preference thresholds attached to criteria. LPDMRSort considers both a binary discordance and a binary concordance conditions including several interactions between them. The identification of the profiles, weights, majority threshold and veto and dictator thresholds are done by taking into account assignment examples.

# Usage

#### **Arguments**

performanceTable

Matrix or data frame containing the performance table. Each row corresponds to an alternative, and each column to a criterion. Rows (resp. columns) must be named according to the IDs of the alternatives (resp. criteria).

assignments

Vector containing the assignments (IDs of the categories) of the alternatives to the categories. The elements are named according to the alternatives.

categoriesRanks

Vector containing the ranks of the categories. The elements are named according to the IDs of the categories.

criteriaMinMax

Vector containing the preference direction on each of the criteria. "min" (resp. "max") indicates that the criterion has to be minimized (maximized). The elements are named according to the IDs of the criteria.

majorityRule

String denoting how the vetoes and dictators are combined in order to form the assignment rule. The values to choose from are "M", "V", "D", "v", "d", "dV", "Dv", "dv". "M" corresponds to using only the majority rule without vetoes or dictators, "V" considers only the vetoes, "D" only the dictators, "v" is like "V" only that a dictator may invalidate a veto, "d" is like "D" only that a veto may invalidate a dictator, "dV" is like "V" only that if there is no veto we may then consider the dictator, "Dv" is like "D" only that when there is no dictator we may consider the vetoes, while finally "dv" is identical to using both dictator and

vetoes only that when both are active they invalidate each other, so the majority rule is considered in that case.

readableWeights

Boolean parameter indicating whether the weights are to be spaced more evenly or not.

readableProfiles

Boolean parameter indicating whether the profiles are to be spaced more evenly or not.

minmaxLPD Boolean parameter indicating whether the veto thresholds are to be minimized

(or maximized if lower criteria values are preferred) while the dictator thresholds are to be maximized (or minimized if lower criteria values are preferred).

alternativesIDs

Vector containing IDs of alternatives, according to which the data should be filtered.

criteriaIDs Vector containing IDs of criteria, according to which the data should be filtered.

solver String specifying if the glpk solver (glpk) should be used, or the cplex (cplex) solver. By default glpk. The cplex solver requires to install the cplex binary and

the cplex C API, as well as the cplex API R package.

cplexTimeLimit If the cplex solver is used, allows to fix a time limit of the execution, in seconds.

By default NULL (which corresponds to the default value of cplex).

cplexIntegralityTolerance

If the cplex solver is used, allows to fix a tolerance for integrality. By default NULL (which corresponds to the default value of cplex).

(Which corresponds to the default value of opicity).

cplexThreads If the cplex solver is used, allows to the number of threads for the calculation.

By default NULL (which corresponds to the default value of cplex).

# Value

The function returns a list structured as follows:

lambda The majority threshold.

weights A vector containing the weights of the criteria. The elements are named accord-

ing to the criteria IDs.

profilesPerformances

A matrix containing the lower profiles of the categories. The columns are named according to the criteria, whereas the rows are named according to the categories. The lower profile of the lower category can be considered as a dummy

profile.

vetoPerformances

A matrix containing the veto profiles of the categories. The columns are named according to the criteria, whereas the rows are named according to the categories. The veto profile of the lower category can be considered as a dummy

profile.

solverStatus The solver status as given by glpk or cplex.

#### References

Bouyssou, D. and Marchant, T. An axiomatic approach to noncompen- satory sorting methods in MCDM, II: more than two categories. European Journal of Operational Research, 178(1): 246–276, 2007.

Meyer, P. and Olteanu, A-L. Integrating large positive and negative performance differences in majority-rule sorting models. European Journal of Operational Research, submitted, 2015.

```
# the performance table
performanceTable <- rbind(c(10,10,9), c(10,9,10), c(9,10,10), c(9,9,10),
               c(9,10,9), c(10,9,9), c(10,10,7), c(10,7,10),
               c(7,10,10), c(9,9,17), c(9,17,9), c(17,9,9),
               c(7,10,17), c(10,17,7), c(17,7,10), c(7,17,10),
               c(17,10,7), c(10,7,17), c(7,9,17), c(9,17,7),
               c(17,7,9), c(7,17,9), c(17,9,7), c(9,7,17))
rownames(performanceTable) <- c("a1", "a2", "a3", "a4", "a5", "a6", "a7",
                  "a8", "a9", "a10", "a11", "a12", "a13",
                  "a14", "a15", "a16", "a17", "a18", "a19", 
"a20", "a21", "a22", "a23", "a24")
colnames(performanceTable) <- c("c1","c2","c3")</pre>
categoriesRanks <-c(1,2)
names(categoriesRanks) <- c("P", "F")</pre>
criteriaMinMax <- c("max", "max", "max")</pre>
names(criteriaMinMax) <- colnames(performanceTable)</pre>
colnames(assignments) <- rownames(performanceTable)</pre>
majorityRules <- c("V","D","v","d","dV","Dv","dv")</pre>
```

30 MARE

```
for(i in 1:1)# change to 7 in order to perform all tests
 x<-LPDMRSortInferenceExact(performanceTable, assignments[i,],</pre>
                              categoriesRanks, criteriaMinMax,
                              majorityRule = majorityRules[i],
                              readableWeights = TRUE,
                              readableProfiles = TRUE,
                             minmaxLPD = TRUE)
 ElectreAssignments<-LPDMRSort(performanceTable, x$profilesPerformances,</pre>
                                 categoriesRanks,
                                 x$weights, criteriaMinMax, x$lambda,
                                 criteriaVetos=x$vetoPerformances,
                                 criteriaDictators=x$dictatorPerformances,
                                 majorityRule = majorityRules[i])
 print(x)
 print(all(ElectreAssignments == assignments[i,]))
}
```

MARE

Multi-Attribute Range Evaluations (MARE)

# **Description**

MARE is a multi-criteria decision analysis method which was originally developed by Hodgett et al. in 2014.

# Usage

# **Arguments**

performanceTableMin

Matrix or data frame containing the minimum performance table. Each column corresponds to an alternative, and each row to a criterion. Columns (resp. rows) must be named according to the IDs of the alternatives (resp. criteria).

performanceTable

Matrix or data frame containing the most likely performance table. Each column corresponds to an alternative, and each row to a criterion. Columns (resp. rows) must be named according to the IDs of the alternatives (resp. criteria).

MARE 31

performanceTableMax

Matrix or data frame containing the maximum performance table. Each column corresponds to an alternative, and each row to a criterion. Columns (resp. rows) must be named according to the IDs of the alternatives (resp. criteria).

criteriaWeights

Vector containing the weights of the criteria. The elements are named according to the IDs of the criteria.

criteriaMinMax Vector containing the preference direction on each of the criteria. "min" (resp. "max") indicates that the criterion has to be minimized (maximized). The elements are named according to the IDs of the criteria.

alternativesIDs

Vector containing IDs of alternatives, according to which the data should be filtered.

criteriaIDs Vector containing IDs of criteria, according to which the data should be filtered.

#### Value

The function returns an element of type mare which contains the MARE scores for each alternative.

#### References

Richard E. Hodgett, Elaine B. Martin, Gary Montague, Mark Talford (2014). Handling uncertain decisions in whole process design. Production Planning & Control, Volume 25, Issue 12, 1028-1038

```
performanceTableMin \leftarrow t(matrix(c(78,87,79,19,8,68,74,8,90,89,74.5,9,20,81,30),
                   nrow=3,ncol=5, byrow=TRUE))
performanceTable <- t(matrix(c(80,87,86,19,8,70,74,10,90,89,75,9,33,82,30),
                                nrow=3,ncol=5, byrow=TRUE))
performanceTableMax <- t(matrix(c(81,87,95,19,8,72,74,15,90,89,75.5,9,36,84,30))
                                   nrow=3,ncol=5, byrow=TRUE))
row.names(performanceTable) <- c("Yield", "Toxicity", "Cost", "Separation", "Odour")
colnames(performanceTable) <- c("Route One","Route Two","Route Three")</pre>
row.names(performanceTableMin) <- row.names(performanceTable)</pre>
colnames(performanceTableMin) <- colnames(performanceTable)</pre>
row.names(performanceTableMax) <- row.names(performanceTable)</pre>
colnames(performanceTableMax) <- colnames(performanceTable)</pre>
weights < c(0.339,0.077,0.434,0.127,0.023)
names(weights) <- row.names(performanceTable)</pre>
criteriaMinMax <- c("max", "max", "max", "max", "max")</pre>
names(criteriaMinMax) <- row.names(performanceTable)</pre>
overall1 <- MARE(performanceTableMin,</pre>
                    performanceTable,
                    performanceTableMax,
```

32 MRSort

MRSort

Electre TRI-like sorting method axiomatized by Bouyssou and Marchant.

# Description

This simplification of the Electre TRI method uses the pessimistic assignment rule, without indifference or preference thresholds attached to criteria. Only a binary discordance condition is considered, i.e. a veto forbids an outranking in any possible concordance situation, or not.

# Usage

#### **Arguments**

performanceTable

Matrix or data frame containing the performance table. Each row corresponds to an alternative, and each column to a criterion. Rows (resp. columns) must be named according to the IDs of the alternatives (resp. criteria).

categoriesLowerProfiles

Matrix containing, in each row, the lower profiles of the categories. The columns are named according to the criteria, and the rows are named according to the categories. The index of the row in the matrix corresponds to the rank of the category.

categoriesRanks

A vector containing the ranks of the categories (1 for the best, with higher values for increasingly less preferred categories). The vector needs to be named with the categories names, whereas the ranks need to be a range of values from 1 to the number of categories.

criteriaWeights

Vector containing the weights of the criteria. The elements are named according to the IDs of the criteria.

MRSort 33

criteriaMinMax Vector containing the preference direction on each of the criteria. "min" (resp.

"max") indicates that the criterion has to be minimized (maximized). The elements are named according to the IDs of the criteria.

majorityThreshold

The cut threshold for the concordance condition. Should be at least half of the sum of the weights.

criteriaVetos Matrix containing in each row a vector defining the veto values for the lower

profile of the category. NA values mean that no veto is defined. A veto threshold for criterion i and category k represents the performance below which an alternative is forbidden to outrank the lower profile of category k, and thus is forbidden to be assigned to the category k. The rows are named according to the

categories, whereas the columns are named according to the criteria.

alternativesIDs

Vector containing IDs of alternatives, according to which the datashould be fil-

tered.

criteriaIDs Vector containing IDs of criteria, according to which the data should be filtered.

categoriesIDs Vector containing IDs of categories, according to which the data should be fil-

tered.

#### Value

The function returns a vector containing the assignments of the alternatives to the categories.

## References

Bouyssou, D. and Marchant, T. An axiomatic approach to noncompen- satory sorting methods in MCDM, II: more than two categories. European Journal of Operational Research, 178(1): 246–276, 2007.

```
# the performance table

performanceTable <- rbind(
    c(1,10,1),
    c(4,20,2),
    c(2,20,0),
    c(6,40,0),
    c(30,30,3))

rownames(performanceTable) <- c("RER","METRO1","METRO2","BUS","TAXI")

colnames(performanceTable) <- c("Price","Time","Comfort")

# lower profiles of the categories
# (best category in the first position of the list)

categoriesLowerProfiles <- rbind(c(3, 11, 3),c(7, 25, 2),c(NA,NA,NA))</pre>
```

MRSort MRSort

```
colnames(categoriesLowerProfiles) <- colnames(performanceTable)</pre>
rownames(categoriesLowerProfiles)<-c("Good", "Medium", "Bad")</pre>
# the order of the categories, 1 being the best
categoriesRanks <-c(1,2,3)</pre>
names(categoriesRanks) <- c("Good", "Medium", "Bad")</pre>
# criteria to minimize or maximize
criteriaMinMax <- c("min", "min", "max")</pre>
names(criteriaMinMax) <- colnames(performanceTable)</pre>
# vetos
criteriaVetos <- rbind(c(10, NA, NA),c(NA, NA, 1),c(NA,NA,NA))</pre>
colnames(criteriaVetos) <- colnames(performanceTable)</pre>
rownames(criteriaVetos) <- c("Good", "Medium", "Bad")</pre>
# weights
criteriaWeights <- c(1,3,2)</pre>
names(criteriaWeights) <- colnames(performanceTable)</pre>
# MRSort
assignments<-MRSort(performanceTable, categoriesLowerProfiles,
                     categoriesRanks, criteriaWeights,
                     criteriaMinMax, 3,
                     criteriaVetos = criteriaVetos)
print(assignments)
# un peu de filtrage
assignments<-MRSort(performanceTable, categoriesLowerProfiles,</pre>
                     categoriesRanks, criteriaWeights,
                     criteriaMinMax, 2,
                     categoriesIDs = c("Medium", "Bad"),
                     criteriaIDs = c("Price", "Time"),
                     alternativesIDs = c("RER", "BUS"))
print(assignments)
```

MRSortIdentifyIncompatibleAssignments

Identifies all sets of assignment examples which are incompatible with the MRSort method.

# **Description**

This MRSort method, which is a simplification of the Electre TRI method, uses the pessimistic assignment rule, without indifference or preference thresholds attached to criteria. Only a binary discordance condition is considered, i.e. a veto forbids an outranking in any possible concordance situation, or not. This function outputs for all (or a fixed number of) sets of incompatible assignment examples ranging in size from the minimal size and up to a given threshold. The retrieved sets are also not contained in each other.

#### Usage

```
MRSortIdentifyIncompatibleAssignments(performanceTable,
                                       assignments,
                                       categoriesRanks,
                                       criteriaMinMax, veto = FALSE,
                                       incompatibleSetsLimit = 100,
                                       largerIncompatibleSetsMargin = 0,
                                       alternativesIDs = NULL,
                                       criteriaIDs = NULL,
                                       solver="glpk",
                                       cplexIntegralityTolerance = NULL,
                                       cplexThreads = NULL)
```

# **Arguments**

performanceTable

Matrix or data frame containing the performance table. Each row corresponds to an alternative, and each column to a criterion. Rows (resp. columns) must be named according to the IDs of the alternatives (resp. criteria).

assignments

Vector containing the assignments (IDs of the categories) of the alternatives to the categories. The elements are named according to the alternatives.

categoriesRanks

Vector containing the ranks of the categories. The elements are named according to the IDs of the categories.

criteriaMinMax Vector containing the preference direction on each of the criteria. "min" (resp. "max") indicates that the criterion has to be minimized (maximized). The elements are named according to the IDs of the criteria.

veto

Boolean parameter indicating whether veto profiles are being used by the model or not.

incompatibleSetsLimit

Pozitive integer denoting the upper limit of the number of sets to be retrieved.

largerIncompatibleSetsMargin

Pozitive integer denoting whether sets larger than the minimal size should be retrieved, and by what margin. For example, if this is 0 then only sets of the minimal size will be retrieved, if this is 1 then sets also larger by 1 element will be retrieved.

alternativesIDs

Vector containing IDs of alternatives, according to which the datashould be filtered.

criteriaIDs Vector containing IDs of criteria, according to which the data should be filtered.

solver String specifying if the glpk solver (glpk) should be used, or the cplex (cplex)

solver. By default glpk. The cplex solver requires to install the cplex binary and the cplex C API, as well as the cplexAPI R package.

cplexIntegralityTolerance

If the cplex solver is used, allows to fix a tolerance for integrality. By default

NULL (which corresponds to the default value of cplex).

cplexThreads If the cplex solver is used, allows to the number of threads for the calculation.

By default NULL (which corresponds to the default value of cplex).

#### Value

The function returns NULL if there is a problem, or a list containing a list of incompatible sets of alternatives as vectors and the status of the execution.

#### References

Bouyssou, D. and Marchant, T. An axiomatic approach to noncompen- satory sorting methods in MCDM, II: more than two categories. European Journal of Operational Research, 178(1): 246–276, 2007.

```
names(assignments) <- rownames(performanceTable)</pre>
categoriesRanks <-c(1,2)</pre>
names(categoriesRanks) <- c("P","F")</pre>
criteriaMinMax <- c("max", "max", "max")</pre>
names(criteriaMinMax) <- colnames(performanceTable)</pre>
incompatibleAssignmentsSets<-MRSortIdentifyIncompatibleAssignments(</pre>
                                performanceTable, assignments,
                                 categoriesRanks, criteriaMinMax,
                                 veto = TRUE,
                                 alternativesIDs = c("a1", "a2", "a3", "a4",
                                 "a5","a6","a7","a8","a9","a10"))
print(incompatibleAssignmentsSets)
filteredAlternativesIDs <- setdiff(c("a1","a2","a3","a4","a5","a6","a7","a8","a9"),
                                     incompatibleAssignmentsSets[[1]][1])
print(filteredAlternativesIDs)
x<-MRSortInferenceExact(performanceTable, assignments, categoriesRanks,
                         criteriaMinMax, veto = TRUE,
                         readableWeights = TRUE, readableProfiles = TRUE,
                         alternativesIDs = filteredAlternativesIDs)
ElectreAssignments<-MRSort(performanceTable, x$profilesPerformances,</pre>
                            categoriesRanks, x$weights,
                            criteriaMinMax, x$lambda,
                            criteriaVetos=x$vetoPerformances,
                            alternativesIDs = filteredAlternativesIDs)
```

 ${\tt MRSortIdentifyUsedVetoProfiles}$ 

Identify veto profiles evaluations that have an impact on the final assignments of MRSort

# **Description**

MRSort is a simplified ELECTRE-TRI approach which assigns alternatives to a set of ordered categories using delimiting profiles evaluations. In addition, veto profiles may also be used in order to circumvent a sufficient majority coalition in favor of an alternative being assigned to a certain category. This method is used to identify which veto profiles evaluations have an impact on the final assignment of at least one of the input alternatives.

### Usage

MRSortIdentifyUsedVetoProfiles(performanceTable, assignments,

categoriesRanks, criteriaMinMax,
majorityThreshold,
criteriaWeights,
profilesPerformances,
vetoPerformances,
alternativesIDs = NULL,
criteriaIDs = NULL)

#### Arguments

#### performanceTable

Matrix or data frame containing the performance table. Each row corresponds to an alternative, and each column to a criterion. Rows (resp. columns) must be named according to the IDs of the alternatives (resp. criteria).

assignments

A vector containing the category to which each alternative is assigned. The vector needs to be named using the alternatives IDs.

#### categoriesRanks

A vector containing the ranks of the categories (1 for the best, with higher values for increasingly less preferred categories). The vector needs to be named with the categories names, whereas the ranks need to be a range of values from 1 to the number of categories.

criteriaMinMax

Vector containing the preference direction on each of the criteria. "min" (resp. "max") indicates that the criterion has to be minimized (maximized). The elements are named according to the IDs of the criteria.

#### majorityThreshold

The majority threshold needed to determine when a coalition of criteria is sufficient in order to validate an outranking relation.

### criteriaWeights

Vector containing the weights of the criteria. The elements are named according to the IDs of the criteria.

#### profilesPerformances

Matrix containing, in each row, the lower profiles of the categories. The columns are named according to the criteria, and the rows are named according to the categories. The index of the row in the matrix corresponds to the rank of the category.

# vetoPerformances

Matrix containing in each row a vector defining the veto values for the lower profile of the category. NA values mean that no veto is defined. A veto threshold for criterion i and category k represents the performance below which an alternative is forbidden to outrank the lower profile of category k, and thus is forbidden to be assigned to the category k. The rows are named according to the categories, whereas the columns are named according to the criteria.

#### alternativesIDs

Vector containing IDs of alternatives, according to which the datashould be filtered.

criteriaIDs Vector containing IDs of criteria, according to which the data should be filtered.

### Value

The function returns a matrix containing TRUE/FALSE inficators for each evaluation of the veto profiles.

```
# the performance table
performanceTable <- rbind(</pre>
  c(1,10,1),
  c(4,20,2),
  c(2,20,0),
  c(6,40,0),
  c(30,10,3))
rownames(performanceTable) <- c("RER", "METRO1", "METRO2", "BUS", "TAXI")</pre>
colnames(performanceTable) <- c("Price", "Time", "Comfort")</pre>
# lower profiles of the categories (best category in the first position of the list)
categoriesLowerProfiles <- rbind(c(3, 11, 3),c(7, 25, 2),c(NA,NA,NA))</pre>
colnames(categoriesLowerProfiles) <- colnames(performanceTable)</pre>
rownames(categoriesLowerProfiles)<-c("Good", "Medium", "Bad")</pre>
# the order of the categories, 1 being the best
categoriesRanks <-c(1,2,3)</pre>
names(categoriesRanks) <- c("Good", "Medium", "Bad")</pre>
# criteria to minimize or maximize
criteriaMinMax <- c("min", "min", "max")</pre>
names(criteriaMinMax) <- colnames(performanceTable)</pre>
# vetos
criteriaVetos <- rbind(c(9, 50, -1),c(50, 50, 0),c(NA,NA,NA))
colnames(criteriaVetos) <- colnames(performanceTable)</pre>
rownames(criteriaVetos) <- c("Good", "Medium", "Bad")</pre>
# weights
criteriaWeights <- c(1/6,3/6,2/6)
```

```
names(criteriaWeights) <- colnames(performanceTable)</pre>
# assignments
assignments <- c("Good", "Medium", "Bad", "Bad", "Bad")</pre>
# MRSortIndetifyUsedVetoProfiles
used<-MRSortIdentifyUsedVetoProfiles(performanceTable, assignments,</pre>
                                        categoriesRanks, criteriaMinMax,
                                        0.5, criteriaWeights,
                                        categoriesLowerProfiles,
                                        criteriaVetos)
```

MRSortInferenceApprox Identification of profiles, weights, majority threshold and veto thresholds for MRSort using a genetic algorithm.

# **Description**

MRSort is a simplification of the Electre TRI method that uses the pessimistic assignment rule, without indifference or preference thresholds attached to criteria. Only a binary discordance condition is considered, i.e. a veto forbids an outranking in any possible concordance situation, or not. The identification of the profiles, weights, majority threshold and veto thresholds are done by taking into account assignment examples.

# Usage

```
MRSortInferenceApprox(performanceTable, assignments, categoriesRanks, criteriaMinMax,
                      veto = FALSE, alternativesIDs = NULL, criteriaIDs = NULL,
                      timeLimit = 60, populationSize = 20, mutationProb = 0.1)
```

#### **Arguments**

performanceTable

Matrix or data frame containing the performance table. Each row corresponds to an alternative, and each column to a criterion. Rows (resp. columns) must be named according to the IDs of the alternatives (resp. criteria).

assignments

Vector containing the assignments (IDs of the categories) of the alternatives to the categories. The elements are named according to the alternatives.

categoriesRanks

Vector containing the ranks of the categories. The elements are named according to the IDs of the categories.

criteriaMinMax Vector containing the preference direction on each of the criteria. "min" (resp. "max") indicates that the criterion has to be minimized (maximized). The elements are named according to the IDs of the criteria.

veto

Boolean parameter indicating whether veto profiles are to be used or not.

alternativesIDs

Vector containing IDs of alternatives, according to which the data should be

filtered.

criteriaIDs Vector containing IDs of criteria, according to which the data should be filtered.

timeLimit Allows to fix a time limit of the execution, in seconds (default 60).

populationSize Allows to change the size of the population used by the genetic algorithm (de-

fault 20).

mutationProb Allows to change the mutation probability used by the genetic algorithm (default

0.1).

#### Value

The function returns a list containing:

majorityThreshold

The inferred majority threshold (single numeric value).

criteriaWeights

The inferred criteria weights (a vector named with the criteria IDs).

profilesPerformances

The inferred category limits (a matrix with the column names given by the criteria IDs and the rownames given by the upper categories each profile delimits).

vetoPerformances

The inferred vetoes (a matrix with the column names given by the criteria IDs and the rownames given by the categories to which each profile applies).

fitness The classification accuracy of the inferred model (from 0 to 1).

### References

Bouyssou, D. and Marchant, T. An axiomatic approach to noncompen- satory sorting methods in MCDM, II: more than two categories. European Journal of Operational Research, 178(1): 246–276, 2007.

no reference yet for the algorithmic approach; one should become available in 2018

42 MRSortInferenceExact

 ${\tt MRSortInferenceExact}$ 

Identification of profiles, weights and majority threshold for the MR-Sort sorting method using an exact approach.

# **Description**

The MRSort method, a simplification of the Electre TRI method, uses the pessimistic assignment rule, without indifference or preference thresholds attached to criteria. Only a binary discordance condition is considered, i.e. a veto forbids an outranking in any possible concordance situation, or not. The identification of the profiles, weights and majority threshold are done by taking into account assignment examples.

#### **Usage**

### Arguments

performanceTable

Matrix or data frame containing the performance table. Each row corresponds to an alternative, and each column to a criterion. Rows (resp. columns) must be named according to the IDs of the alternatives (resp. criteria).

assignments

Vector containing the assignments (IDs of the categories) of the alternatives to the categories. The elements are named according to the alternatives.

MRSortInferenceExact 43

categoriesRanks

Vector containing the ranks of the categories. The elements are named according

to the IDs of the categories.

criteriaMinMax Vector containing the preference direction on each of the criteria. "min" (resp.

"max") indicates that the criterion has to be minimized (maximized). The ele-

ments are named according to the IDs of the criteria.

veto Boolean parameter indicating whether veto profiles are being used or not.

readableWeights

Boolean parameter indicating whether the weights are to be spaced more evenly

or not.

readableProfiles

Boolean parameter indicating whether the profiles are to be spaced more evenly

or not.

alternativesIDs

Vector containing IDs of alternatives, according to which the data should be

filtered.

criteriaIDs Vector containing IDs of criteria, according to which the data should be filtered.

solver String specifying if the glpk solver (glpk) should be used, or the cplex (cplex)

solver. By default glpk. The cplex solver requires to install the cplex binary and

the cplex C API, as well as the cplexAPI R package.

cplexTimeLimit If the cplex solver is used, allows to fix a time limit of the execution, in seconds.

By default NULL (which corresponds to the default value of cplex).

cplexIntegralityTolerance

If the cplex solver is used, allows to fix a tolerance for integrality. By default

NULL (which corresponds to the default value of cplex).

cplexThreads If the cplex solver is used, allows to the number of threads for the calculation.

By default NULL (which corresponds to the default value of cplex).

### Value

The function returns a list structured as follows:

lambda The majority threshold.

weights A vector containing the weights of the criteria. The elements are named accord-

ing to the criteria IDs.

profilesPerformances

A matrix containing the lower profiles of the categories. The columns are named according to the criteria, whereas the rows are named according to the categories. The lower profile of the lower category can be considered as a dummy

profile.

vetoPerformances

A matrix containing the veto profiles of the categories. The columns are named according to the criteria, whereas the rows are named according to the categories. The veto profile of the lower category can be considered as a dummy

profile.

solverStatus The solver status as given by glpk or cplex.

44 MRSortInterval

### References

Bouyssou, D. and Marchant, T. An axiomatic approach to noncompen-satory sorting methods in MCDM, II: more than two categories. European Journal of Operational Research, 178(1): 246–276, 2007.

```
performanceTable <- rbind(c(10,10,9), c(10,9,10), c(9,10,10), c(9,9,10),
                        c(9,10,9), c(10,9,9), c(10,10,7), c(10,7,10),
                        c(7,10,10), c(9,9,17), c(9,17,9), c(17,9,9),
                        c(7,10,17), c(10,17,7), c(17,7,10), c(7,17,10),
                        c(17,10,7), c(10,7,17), c(7,9,17), c(9,17,7),
                        c(17,7,9), c(7,17,9), c(17,9,7), c(9,7,17))
rownames(performanceTable) <- c("a1", "a2", "a3", "a4", "a5", "a6", "a7",
                              "a8", "a9", "a10", "a11", "a12", "a13",
                              "a14", "a15", "a16", "a17", "a18", "a19",
                              "a20", "a21", "a22", "a23", "a24")
colnames(performanceTable) <- c("c1","c2","c3")</pre>
names(assignments) <- rownames(performanceTable)</pre>
categoriesRanks <-c(1,2)</pre>
names(categoriesRanks) <- c("P","F")</pre>
criteriaMinMax <- c("max", "max", "max")</pre>
names(criteriaMinMax) <- colnames(performanceTable)</pre>
x<-MRSortInferenceExact(performanceTable, assignments, categoriesRanks,
                        criteriaMinMax, veto = TRUE, readableWeights = TRUE,
                        readableProfiles = TRUE,
                       alternativesIDs = c("a1", "a2", "a3", "a4", "a5", "a6", "a7"))
ElectreAssignments<-MRSort(performanceTable, x$profilesPerformances,</pre>
                         categoriesRanks,
                         x$weights, criteriaMinMax, x$lambda,
                         criteriaVetos=x$vetoPerformances,
                         alternativesIDs = c("a1", "a2", "a3", "a4", "a5", "a6", "a7"))
```

MRSortInterval 45

# **Description**

This method is an extension of the classical MRSort, that allows the handling of problems where the decision alternatives contain imprecise or even missing evaluations. Unlike MRSort, where an alternative is assigned to one category, MRSortInterval offers the possibility of assigning an alternative to one or more neighboring categories.

# Usage

### **Arguments**

performanceTable

Two-dimmensionnal list containing the performance table. Each row corresponds to an alternative, and each column to a criterion. Rows (resp. columns) must be named according to the IDs of the alternatives (resp. criteria). This list may contain imprecise performances of alternatives on the criteria, represented by interval evaluations, as well as missing performances.

 ${\it categories Lower Profiles}$ 

Matrix containing, in each row, the lower profiles of the categories. The columns are named according to the criteria, and the rows are named according to the categories except of the last one.

categoriesRanks

A vector containing the ranks of the categories (1 for the best, with higher values for increasingly less preferred categories). The vector needs to be named with the categories names, whereas the ranks need to be a range of values from 1 to the number of categories.

criteriaWeights

Vector containing the weights of the criteria. The elements are named according to the IDs of the criteria.

criteriaMinMax Vector containing the preference direction on each of the criteria. "min" (resp. "max") indicates that the criterion has to be minimized (maximized).

majorityThresholdPes

The cut threshold for the pessimistic concordance relation.

majorityThresholdOpt

The cut threshold for the optimistic concordance relation.

#### Value

The function returns a list containing the assignments of the alternatives to all possibles categories.

```
# the performance table
performanceTable <- as.list(numeric(6*5))</pre>
```

46 MRSortInterval

```
dim(performanceTable)=c(6,5)
performanceTable[[1,1]]<-0</pre>
performanceTable[[1,2]]<-0</pre>
performanceTable[[1,3]]<-0</pre>
performanceTable[[1,4]]<-0</pre>
performanceTable[[1,5]]<-0</pre>
performanceTable[[2,1]]<-0</pre>
performanceTable[[2,2]]<-0</pre>
performanceTable[[2,3]]<-1</pre>
performanceTable[[2,4]]<-0</pre>
performanceTable[[2,5]]<-0</pre>
performanceTable[[3,1]]<-0</pre>
performanceTable[[3,2]]<-0</pre>
performanceTable[[3,3]]<-2</pre>
performanceTable[[3,4]]<-0</pre>
performanceTable[[3,5]]<-0</pre>
performanceTable[[4,1]]<-0</pre>
performanceTable[[4,2]]<-0</pre>
performanceTable[[4,3]]<-0:1</pre>
performanceTable[[4,4]]<-0</pre>
performanceTable[[4,5]]<-0</pre>
performanceTable[[5,1]]<-0</pre>
performanceTable[[5,2]]<-0</pre>
performanceTable[[5,3]]<-NA</pre>
performanceTable[[5,4]]<-0</pre>
performanceTable[[5,5]]<-0</pre>
performanceTable[[6,1]]<-0</pre>
performanceTable[[6,2]]<-0</pre>
performanceTable[[6,3]]<-0</pre>
performanceTable[[6,4]]<-0</pre>
performanceTable[[6,5]]<-NA</pre>
rownames(performanceTable)<-c("a1","a2","a3","a4","a5","a6")
colnames(performanceTable)<-c("c1","c2","c3","c4","c5")</pre>
# lower profiles of the categories (best category in the first position of the list)
categoriesLowerProfiles <- rbind(c(1,1,1,1,1),c(0,0,0,2,2))
colnames(categoriesLowerProfiles) <- colnames(performanceTable)</pre>
rownames(categoriesLowerProfiles)<-c("Medium", "Good")</pre>
categoriesRanks <-c(1,2,3)</pre>
names(categoriesRanks) <- c("Good", "Medium", "Bad")</pre>
# weights
criteriaWeights <- c(1/5, 1/5, 1/5, 1/5, 1/5)
names(criteriaWeights) <- colnames(performanceTable)</pre>
#pessimistic and optimistic majority thresholds
majorityThresholdPes=majorityThresholdOpt=3/5
```

normalizePerformanceTable

Function to normalize (or rescale) the columns (or criteria) of a performance table.

# Description

Standardizes the range of the criteria according to a few methods: percentage of max, scale between 0 and 1, scale to 0 mean and 1 standard deviation, scale to euclidian unit length.

# Usage

# **Arguments**

performanceTable

A matrix containing the performance table to be plotted. The columns are labelled according to the criteria IDs, and the rows according to the alternatives IDs.

normalizationTypes

Vector indicating the type of normalization that should be applied to each of the criteria. Possible values: "percentageOfMax", "rescaling" (minimum becomes 0, maximum becomes 1), "standardization" (rescale to a mean of 0 and a standard deviation of 1), "scaleToUnitLength" (scale the criteria values such that the column has euclidian length 1). Any other value (like "none") will result in no data transformation. The elements are named according to the IDs of the criteria

alternativesIDs

Vector containing IDs of alternatives, according to which the data should be filtered.

criteriaIDs Vector containing IDs of criteria, according to which the data should be filtered.

# **Examples**

pairwiseConsistencyMeasures

Consistency Measures for Pairwise Comparison Matrices

# **Description**

This function calculates four pairwise consistency checks: Consistency Ratio (CR) from Saaty (1980), Koczkodaj's Measure from Koczkodaj (1993) and Congruence / Dissonance Measures from Siraj et al. (2015).

### Usage

```
pairwiseConsistencyMeasures(matrix)
```

### **Arguments**

matrix

A reciprocal matrix containing pairwise judgements

### Value

The function returns a list of outputs for the four pairwise consistency checks

### References

Thomas Saaty (1980). The Analytic Hierarchy Process: Planning, Priority Setting, ISBN 0-07-054371-2, McGraw-Hill.

W.W. Koczkodaj (1993). A new definition of consistency of pairwise comparisons. Mathematical and Computer Modelling. 18 (7).

Sajid Siraj, Ludmil Mikhailov & John A. Keane (2015). Contribution of individual judgments toward inconsistency in pairwise comparisons. European Journal of Operational Research. 242(2).

# **Examples**

```
examplematrix < t(matrix(c(1,0.25,4,1/6,4,1,4,0.25,0.25,0.25,1,0.2,6,4,5,1),nrow=4,ncol=4)) pairwiseConsistencyMeasures(examplematrix)
```

plotAlternativesValuesPreorder

Function to plot a preorder of alternatives, based on some score or ranking.

# Description

Plots a preorder of alternatives as a graph, representing the ranking of the alternatives, w.r.t. some scores or ranks. A decreasing order or increasing order can be specified, w.r.t. to these scores or ranks.

## Usage

### **Arguments**

alternativesValues

A vector containing some values related to alternatives, as scores or ranks. The elements of the vector are named according to the IDs of the alternatives.

decreasing

A boolean to indicate if the alternatives are to be sorted increasingly (FALSE) or decreasingly (TRUE) w.r.t. the alternatives Values.

alternativesIDs

Vector containing IDs of alternatives, according to which the data should be filtered.

50 plotMARE

plotMARE

Plot Multi-Attribute Range Evaluations (MARE)

## **Description**

Plots the output of function MARE()

### Usage

plotMARE(x)

## **Arguments**

Х

Output from function MARE()

```
performanceTableMin \leftarrow t(matrix(c(78,87,79,19,8,68,74,8,90,89,74.5,9,20,81,30),
                                    nrow=3,ncol=5, byrow=TRUE))
performanceTable \leftarrow t(matrix(c(80,87,86,19,8,70,74,10,90,89,75,9,33,82,30),
                                  nrow=3,ncol=5, byrow=TRUE))
performanceTableMax <- t(matrix(c(81,87,95,19,8,72,74,15,90,89,75.5,9,36,84,30),</pre>
                                     nrow=3,ncol=5, byrow=TRUE))
row.names(performanceTable) <- c("Yield","Toxicity","Cost","Separation","Odour")</pre>
colnames(performanceTable) <- c("Route One", "Route Two", "Route Three")</pre>
row.names(performanceTableMin) <- row.names(performanceTable)</pre>
colnames(performanceTableMin) <- colnames(performanceTable)</pre>
row.names(performanceTableMax) <- row.names(performanceTable)</pre>
colnames(performanceTableMax) <- colnames(performanceTable)</pre>
weights < c(0.339,0.077,0.434,0.127,0.023)
names(weights) <- row.names(performanceTable)</pre>
criteriaMinMax <- c("max", "max", "max", "max", "max")</pre>
names(criteriaMinMax) <- row.names(performanceTable)</pre>
overall1 <- MARE(performanceTableMin, performanceTable, performanceTableMax,
                             weights, criteriaMinMax)
plotMARE(overall1)
overall2 <- MARE(performanceTableMin,</pre>
                     performanceTable,
                     performanceTableMax,
                     weights,
                     criteriaMinMax,
                     alternativesIDs = c("Route Two", "Route Three"),
                     criteriaIDs = c("Yield", "Toxicity", "Cost", "Separation"))
plotMARE(overall2)
```

plotMRSortSortingProblem

Plot the categories and assignments of an Electre TRI-like sorting problem (via separation profiles).

### **Description**

The profiles shown are the separation profiles between the classes. They are stored as the lower profiles of the categories.

## Usage

```
plotMRSortSortingProblem(performanceTable, categoriesLowerProfiles,
                         categoriesRanks, assignments, criteriaMinMax,
                         criteriaUBs, criteriaLBs,
                         categoriesDictators = NULL, categoriesVetoes = NULL,
                         majorityRule = NULL, criteriaWeights = NULL,
                         majorityThreshold = NULL, alternativesIDs = NULL,
                         criteriaIDs = NULL, legendRatio = 0.2)
```

### **Arguments**

performanceTable

Matrix or data frame containing the performance table. Each row corresponds to an alternative, and each column to a criterion. Rows (resp. columns) must be named according to the IDs of the alternatives (resp. criteria).

categoriesLowerProfiles

Matrix containing, in each row, the lower profiles of the categories (the separation profiles in fact). The columns are named according to the criteria, and the rows are named according to the categories. The index of the row in the matrix corresponds to the rank of the category.

categoriesRanks

A vector containing the ranks of the categories (1 for the best, with higher values for increasingly less preferred categories). The vector needs to be named with the categories names, whereas the ranks need to be a range of values from 1 to the number of categories.

assignments Vector containing the assignments (IDs of the categories) of the alternatives to the categories. The elements are named according to the alternatives.

criteriaMinMax Vector containing the preference direction on each of the criteria. "min" (resp. "max") indicates that the criterion has to be minimized (maximized). The ele-

ments are named according to the IDs of the criteria.

criteriaLBs Vector containing the lower bounds of the criteria to be considered for the plotting. The elements are named according to the IDs of the criteria.

criteriaUBs Vector containing the upper bounds of the criteria to be considered for the plotting. The elements are named according to the IDs of the criteria.

categoriesDictators

Matrix containing, in each row, the lower dictator profiles of the categories. The columns are named according to the criteria, and the rows are named according to the categories. The index of the row in the matrix corresponds to the rank of the category.

### categoriesVetoes

Matrix containing, in each row, the lower veto profiles of the categories. The columns are named according to the criteria, and the rows are named according to the categories. The index of the row in the matrix corresponds to the rank of the category.

majorityRule

A string containing one of the following values: 'V', 'D', 'v', 'd', 'dV', 'Dv', 'dv'. This indicates the type of majority rule that will be used by the MRSort model. 'V' stands for MRSort with vetoes, 'D' stands for MRSort with dictators, 'v' stands for MRSort with vetoes weakened by dictators, 'd' stands for MRSort with dictators weakened by vetoes, 'dV' stands for MRSort with vetoes dominating dictators, 'Dv' stands for MRSort with dictators dominating vetoes, while 'dv' stands for MRSort with conflicting vetoes and dictators.

### criteriaWeights

Vector containing the criteria weights. The elements are named according to the IDs of the criteria.

majorityThreshold

A value corresponding to the majority threshold. Along with the criteria weights, this value is used to determine when a coalition of criteria is sufficient in order to assert that an alternative is at least as good as a category profile.

alternativesIDs

Vector containing IDs of alternatives, according to which the datashould be filtered.

criteriaIDs

Vector containing IDs of criteria, according to which the data should be filtered.

legendRatio

The ratio between the legend and plot heights. By defaut 0.2.

```
# the performance table

performanceTable <- rbind(
    c(1,10,1),
    c(4,20,2),
    c(2,20,0),
    c(6,40,0),
    c(30,30,3))

rownames(performanceTable) <- c("RER","METRO1","METRO2","BUS","TAXI")

colnames(performanceTable) <- c("Price","Time","Comfort")

# lower profiles of the categories
# (best category in the first position of the list)

categoriesLowerProfiles <- rbind(c(3, 11, 3),c(7, 25, 2),c(30,30,0))</pre>
```

```
colnames(categoriesLowerProfiles) <- colnames(performanceTable)</pre>
rownames(categoriesLowerProfiles)<-c("Good", "Medium", "Bad")</pre>
categoriesRanks <-c(1,2,3)</pre>
names(categoriesRanks) <- c("Good", "Medium", "Bad")</pre>
# criteria to minimize or maximize
criteriaMinMax <- c("min", "min", "max")</pre>
names(criteriaMinMax) <- colnames(performanceTable)</pre>
# lower bounds of the criteria for the determination of value functions
criteriaLBs=c(0,5,0)
names(criteriaLBs) <- colnames(performanceTable)</pre>
# upper bounds of the criteria for the determination of value functions
criteriaUBs=c(50,50,4)
names(criteriaUBs) <- colnames(performanceTable)</pre>
# weights
criteriaWeights <- c(1,3,2)</pre>
names(criteriaWeights) <- colnames(performanceTable)</pre>
assignments <- assignments<-MRSort(performanceTable,</pre>
                                      categoriesLowerProfiles,
                                      categoriesRanks,
                                      criteriaWeights,
                                      criteriaMinMax, 3)
names(assignments) <- rownames(performanceTable)</pre>
plotMRSortSortingProblem(performanceTable, categoriesLowerProfiles,
                           categoriesRanks, assignments, criteriaMinMax,
                           criteriaUBs, criteriaLBs)
```

plotPiecewiseLinearValueFunctions

Function to plot piecewise linear value functions.

### **Description**

Plots piecewise linear value function.

### Usage

# **Arguments**

valueFunctions A list containing, for each criterion, the piecewise linear value functions defined

by the coordinates of the break points. Each value function is defined by a matrix of breakpoints, where the first row corresponds to the abscissa (row labelled "x") and where the second row corresponds to the ordinate (row labelled "y").

criteriaIDs Vector containing IDs of criteria, according to which the data should be filtered.

# **Examples**

```
v<-list(
    Price = array(c(30, 0, 16, 0, 2, 0.0875),
        dim=c(2,3), dimnames = list(c("x", "y"), NULL)),
    Time = array(c(40, 0, 30, 0, 20, 0.025, 10, 0.9),
        dim = c(2, 4), dimnames = list(c("x", "y"), NULL)),
    Comfort = array(c(0, 0, 1, 0, 2, 0.0125, 3, 0.0125),
        dim = c(2, 4), dimnames = list(c("x", "y"), NULL)))
# plot the value functions

plotPiecewiseLinearValueFunctions(v)</pre>
```

plotRadarPerformanceTable

Function to plot radar plots of alternatives of a performance table.

### **Description**

Plots radar plots of alternatives contained in a performance table, either in one radar plot, or on multiple radar plots. For a given alternative, the plot shows how far above/below average (the thick black line) each of the criteria performances values are (average taken w.r.t. to the filtered performance table).

### Usage

```
overlay=FALSE,
bw=FALSE,
1wd=2)
```

### **Arguments**

performanceTable

A matrix containing the performance table to be plotted. The columns are labelled according to the criteria IDs, and the rows according to the alternatives

criteriaMinMax Vector indicating whether criteria should be minimized or maximized. If it is given, a "higher" value in the radar plot corresponds to a more preferred value according to the decision maker. "min" (resp. "max") indicates that the criterion has to be minimized (maximized). The elements are named according to the IDs of the criteria.

alternativesIDs

Vector containing IDs of alternatives, according to which the data should be

criteriaIDs Vector containing IDs of criteria, according to which the data should be filtered.

overlay Boolean value indicating if the plots should be overlayed on one plot (TRUE),

or not (FALSE)

Boolean value indicating if the plots should be in black/white (TRUE) or color hw

(FALSE)

lwd Value indicating the line width of the plot.

```
library(MCDA)
performanceTable <- matrix(runif(6*9), ncol=6)</pre>
row.names(performanceTable) <- c("x1","x2","x3","x4","x5","x6","x7","x8","x9")
colnames(performanceTable) <- c("g1", "g2", "g3", "g4", "g5", "g6")</pre>
criteriaMinMax <- c("min", "max", "min", "max", "min", "max")</pre>
names(criteriaMinMax) <- c("g1","g2","g3","g4","g5","g6")</pre>
# plotRadarPerformanceTable(performanceTable, criteriaMinMax, overlay=TRUE)
plotRadarPerformanceTable(performanceTable, criteriaMinMax,
                            alternativesIDs = c("x1","x2","x3","x4"),
                            criteriaIDs = c("g1","g3","g4","g5","g6"),
                            overlay=FALSE, bw=FALSE)
# plotRadarPerformanceTable(performanceTable, criteriaMinMax,
                            alternativesIDs = c("x1", "x2"),
#
                             criteriaIDs = c("g1", "g3", "g4", "g5", "g6"),
```

56 plotSURE

# overlay=FALSE)

plotSURE

Plot SURE kernel density plots.

# Description

Plots the output of function SURE()

## Usage

```
plotSURE(SURE,
          greyScale = FALSE,
          separate = FALSE)
```

# **Arguments**

SURE Output from function SURE().

greyScale TRUE/FALSE indicating if you want the plot to be in greyscale.

separate TRUE/FALSE indicating if you want the density plots to be separated.

```
performanceTableMin \leftarrow t(matrix(c(78,87,79,19,8,68,74,8,90,89,74.5,9,20,81,30),
                   nrow=3,ncol=5, byrow=TRUE))
performanceTable \leftarrow t(matrix(c(80,87,86,19,8,70,74,10,90,89,75,9,33,82,30),
                                nrow=3,ncol=5, byrow=TRUE))
performanceTableMax <- t(matrix(c(81,87,95,19,8,72,74,15,90,89,75.5,9,36,84,30),
                                   nrow=3,ncol=5, byrow=TRUE))
row.names(performanceTable) <- c("Yield", "Toxicity", "Cost", "Separation", "Odour")
colnames(performanceTable) <- c("Route One", "Route Two", "Route Three")</pre>
row.names(performanceTableMin) <- row.names(performanceTable)</pre>
colnames(performanceTableMin) <- colnames(performanceTable)</pre>
row.names(performanceTableMax) <- row.names(performanceTable)</pre>
colnames(performanceTableMax) <- colnames(performanceTable)</pre>
criteriaWeights < c(0.339,0.077,0.434,0.127,0.023)
names(criteriaWeights) <- row.names(performanceTable)</pre>
criteriaMinMax <- c("max", "max", "max", "max", "max")</pre>
names(criteriaMinMax) <- row.names(performanceTable)</pre>
test1 <- SURE(performanceTableMin,</pre>
                  performanceTable,
                  performanceTableMax,
                  criteriaWeights,
                  criteriaMinMax,
```

PROMETHEEI 57

```
NoOfSimulations = 101)
```

```
summary(test1)
plotSURE(test1)
plotSURE(test1, greyScale = TRUE, separate = TRUE)
```

**PROMETHEEI** 

PROMETHEE I

# **Description**

The PROMETHEE I constructs preference indices from the criteria evaluations of alternatives and outputs three preference relations (P - preference, I - indifference, R - incomparability) based on the outranking flows between the alternatives.

# Usage

```
PROMETHEEI(performanceTable, preferenceFunction,preferenceThreshold, indifferenceThreshold,gaussParameter, criteriaWeights,criteriaMinMax)
```

## **Arguments**

performanceTable

Matrix containing the evaluation table. Each row corresponds to an alternative, and each column to a criterion. Rows (resp. columns) must be named according to the IDs of the alternatives (resp. criteria).

preferenceFunction

A vector with preference functions.preferenceFunction should be equal to Usual,Ushape,V-shape,Level,V-shape-Indiff or Gaussian. The elements are named according to the IDs of the criteria.

preferenceThreshold

A vector containing threshold of strict preference. The elements are named according to the IDs of the criteria.

indifferenceThreshold

A vector containing threshold of indifference. The elements are named according to the IDs of the criteria.

gaussParameter A vector containing parameter of the Gaussian preference function. The elements are named according to the IDs of the criteria.

criteriaWeights

Vector containing the weights of the criteria. The elements are named according to the IDs of the criteria.

criteriaMinMax Vector containing the preference direction on each of the criteria. "min" (resp. "max") indicates that the criterion has to be minimized (maximized). The elements are named according to the IDs of the criteria.

58 PROMETHEEII

#### Value

The function returns three matrices: The first one contains the preference relations between the alternatives, the second one contains the indifference relations between the alternatives and the third one contains the incomparability relations between the alternatives.

```
# The evaluation table
performanceTable <- rbind(</pre>
  c(1,10,1),
  c(4,20,2),
  c(2,20,0),
  c(6,40,0),
  c(30,30,3))
rownames(performanceTable) <- c("RER", "METRO1", "METRO2", "BUS", "TAXI")</pre>
colnames(performanceTable) <- c("Price","Time","Comfort")</pre>
# The preference functions
preferenceFunction<-c("Gaussian", "Level", "V-shape-Indiff")</pre>
#Preference threshold
preferenceThreshold<-c(5,15,3)</pre>
names(preferenceThreshold)<-colnames(performanceTable)</pre>
#Indifference threshold
indifferenceThreshold<-c(3,11,1)</pre>
names(indifferenceThreshold)<-colnames(performanceTable)</pre>
#Parameter of the Gaussian preference function
gaussParameter<-c(4,0,0)</pre>
names(gaussParameter)<-colnames(performanceTable)</pre>
#weights
criteriaWeights < -c(0.2, 0.3, 0.5)
names(criteriaWeights)<-colnames(performanceTable)</pre>
# criteria to minimize or maximize
criteriaMinMax<-c("min","min","max")</pre>
names(criteriaMinMax)<-colnames(performanceTable)</pre>
PROMETHEEI(performanceTable, preferenceFunction,preferenceThreshold,
           indifferenceThreshold,gaussParameter,criteriaWeights,criteriaMinMax)
```

**PROMETHEEII** 59

# **Description**

The PROMETHEE II constructs preference indices from the criteria evaluations of alternatives and outputs a pre-order based on the outranking flows between the alternatives.

# **Usage**

```
PROMETHEEII(performanceTable, preferenceFunction,
            preferenceThreshold,indifferenceThreshold,gaussParameter,
            criteriaWeights,criteriaMinMax)
```

#### **Arguments**

performanceTable

Matrix containing the evaluation table. Each row corresponds to an alternative, and each column to a criterion. Rows (resp. columns) must be named according to the IDs of the alternatives (resp. criteria).

preferenceFunction

A vector with preference functions.preferenceFunction should be equal to Usual,Ushape, V-shape, Level, V-shape-Indiff or Gaussian. The elements are named according to the IDs of the criteria.

preferenceThreshold

A vector containing threshold of strict preference. The elements are named according to the IDs of the criteria.

indifferenceThreshold

A vector containing threshold of indifference. The elements are named according to the IDs of the criteria.

gaussParameter A vector containing parameter of the Gaussian preference function. The elements are named according to the IDs of the criteria.

criteriaWeights

Vector containing the weights of the criteria. The elements are named according to the IDs of the criteria.

criteriaMinMax Vector containing the preference direction on each of the criteria. "min" (resp. "max") indicates that the criterion has to be minimized (maximized). The elements are named according to the IDs of the criteria.

### Value

The function returns a list containing the alternatives IDs in decreasing order of preference. Each elements of the list can be a vector of alternatives IDs.

```
# The evaluation table
performanceTable <- rbind(</pre>
  c(1,10,1),
  c(4,20,2),
  c(2,20,0),
```

```
c(6,40,0),
  c(30,30,3))
rownames(performanceTable) <- c("RER", "METRO1", "METRO2", "BUS", "TAXI")</pre>
colnames(performanceTable) <- c("Price", "Time", "Comfort")</pre>
# The preference functions
preferenceFunction<-c("Gaussian", "Level", "V-shape-Indiff")</pre>
#Preference threshold
preferenceThreshold<-c(5,15,3)</pre>
names(preferenceThreshold)<-colnames(performanceTable)</pre>
#Indifference threshold
indifferenceThreshold<-c(3,11,1)</pre>
names(indifferenceThreshold)<-colnames(performanceTable)</pre>
#Parameter of the Gaussian preference function
gaussParameter<-c(4,0,0)
names(gaussParameter)<-colnames(performanceTable)</pre>
#weights
criteriaWeights<-c(0.2,0.3,0.5)</pre>
names(criteriaWeights)<-colnames(performanceTable)</pre>
# criteria to minimize or maximize
criteriaMinMax<-c("min", "min", "max")</pre>
names(criteriaMinMax)<-colnames(performanceTable)</pre>
PROMETHEEII(performanceTable, preferenceFunction,preferenceThreshold,
             indifferenceThreshold,gaussParameter,criteriaWeights,
             criteriaMinMax)
```

PROMETHEEOutrankingFlows

Outranking flows for the PROMETHEE methods

# **Description**

This function computes the positive and negative outranking flows for the PROMETHEE methods. It takes as input a performance table and converts the evaluations to preference indices based on the given function types and parameters for each criterion.

### Usage

```
PROMETHEEOutrankingFlows(performanceTable, preferenceFunction, preferenceThreshold,indifferenceThreshold, gaussParameter,criteriaWeights,criteriaMinMax)
```

#### **Arguments**

### performanceTable

Matrix containing the evaluation table. Each row corresponds to an alternative, and each column to a criterion. Rows (resp. columns) must be named according to the IDs of the alternatives (resp. criteria).

#### preferenceFunction

A vector with preference functions.preferenceFunction should be equal to Usual,Ushape, V-shape, Level, V-shape-Indiff or Gaussian. The elements are named according to the IDs of the criteria.

#### preferenceThreshold

A vector containing threshold of strict preference. The elements are named according to the IDs of the criteria.

### indifferenceThreshold

A vector containing threshold of indifference. The elements are named according to the IDs of the criteria.

gaussParameter A vector containing parameter of the Gaussian preference function. The elements are named according to the IDs of the criteria.

criteriaWeights

Vector containing the weights of the criteria. The elements are named according to the IDs of the criteria.

criteriaMinMax Vector containing the preference direction on each of the criteria. "min" (resp. "max") indicates that the criterion has to be minimized (maximized). The elements are named according to the IDs of the criteria.

#### Value

The function returns two vectors: The first one contains the positive outranking flows and the second one contains the negative outranking flows.

```
# The evaluation table
performanceTable <- rbind(</pre>
  c(1,10,1),
  c(4,20,2),
  c(2,20,0),
  c(6,40,0),
  c(30,30,3))
rownames(performanceTable) <- c("RER", "METRO1", "METRO2", "BUS", "TAXI")</pre>
colnames(performanceTable) <- c("Price", "Time", "Comfort")</pre>
# The preference functions
preferenceFunction<-c("Gaussian","Level","V-shape-Indiff")</pre>
#Preference threshold
preferenceThreshold<-c(5,15,3)</pre>
names(preferenceThreshold)<-colnames(performanceTable)</pre>
```

```
#Indifference threshold
indifferenceThreshold<-c(3,11,1)</pre>
names(indifferenceThreshold)<-colnames(performanceTable)</pre>
#Parameter of the Gaussian preference function
gaussParameter<-c(4,0,0)</pre>
names(gaussParameter)<-colnames(performanceTable)</pre>
#weights
criteriaWeights < -c(0.2, 0.3, 0.5)
names(criteriaWeights)<-colnames(performanceTable)</pre>
# criteria to minimize or maximize
criteriaMinMax<-c("min","min","max")</pre>
names(criteriaMinMax)<-colnames(performanceTable)</pre>
# Outranking flows
outranking Flows <- PROMETHEE Outranking Flows (performance Table, preference Function, and the preference function), and the preference function of the p
                                                                                                                                                                                {\tt preferenceThreshold, indifferenceThreshold,}
                                                                                                                                                                                 gaussParameter,criteriaWeights,
                                                                                                                                                                                 criteriaMinMax)
```

PROMETHEEPreferenceIndices

Preference indices for the PROMETHEE methods

# Description

This function computes the preference indices from a performance table based on the given function types and parameters for each criterion.

## Usage

```
PROMETHEEPreferenceIndices(performanceTable, preferenceFunction, preferenceThreshold,indifferenceThreshold, gaussParameter,criteriaWeights,criteriaMinMax)
```

# Arguments

performanceTable

Matrix containing the performance table. Each row corresponds to an alternative, and each column to a criterion. Rows (resp. columns) must be named according to the IDs of the alternatives (resp. criteria).

#### preferenceFunction

A vector containing the names of the preference functions to be used. preferenceFunction should be equal to Usual, U-shape, V-shape, Level, V-shape-Indiff or Gaussian. The elements of the vector are named according to the IDs of the criteria.

## preferenceThreshold

A vector containing thresholds of strict preference. The elements are named according to the IDs of the criteria.

#### indifferenceThreshold

A vector containing thresholds of indifference. The elements are named according to the IDs of the criteria.

gaussParameter A vector containing parameters of the Gaussian preference function. The elements are named according to the IDs of the criteria.

criteriaWeights

Vector containing the weights of the criteria. The elements are named according to the IDs of the criteria.

criteriaMinMax Vector containing the preference direction on each of the criteria. "min" (resp. "max") indicates that the criterion has to be minimized (maximized). The elements are named according to the IDs of the criteria.

#### Value

The function returns a matrix containing all the aggregated preference indices.

```
# The evaluation table
performanceTable <- rbind(</pre>
  c(1,10,1),
  c(4,20,2),
  c(2,20,0),
  c(6,40,0),
  c(30,30,3))
rownames(performanceTable) <- c("RER", "METRO1", "METRO2", "BUS", "TAXI")</pre>
colnames(performanceTable) <- c("Price", "Time", "Comfort")</pre>
# The preference functions
preferenceFunction<-c("Gaussian","Level","V-shape-Indiff")</pre>
#Preference threshold
preferenceThreshold<-c(5,15,3)</pre>
names(preferenceThreshold)<-colnames(performanceTable)</pre>
#Indifference threshold
indifferenceThreshold<-c(3,11,1)</pre>
names(indifferenceThreshold)<-colnames(performanceTable)</pre>
#Parameter of the Gaussian preference function
gaussParameter<-c(4,0,0)</pre>
```

64 SRMP

```
names(gaussParameter)<-colnames(performanceTable)

#weights

criteriaWeights<-c(0.2,0.3,0.5)
names(criteriaWeights)<-colnames(performanceTable)

# criteria to minimize or maximize

criteriaMinMax<-c("min","min","max")
names(criteriaMinMax)<-colnames(performanceTable)

#Preference indices

preferenceTable<-PROMETHEEPreferenceIndices(performanceTable, preferenceFunction, preferenceThreshold, indifferenceThreshold, gaussParameter, criteriaWeights, criteriaMinMax)</pre>
```

**SRMP** 

SRMP: a simple ranking method using reference profiles

# Description

SRMP is a ranking method that uses dominating reference profiles, in a given lexicographic ordering, in order to output a total preorder of a set of alternatives.

# Usage

#### **Arguments**

performanceTable

Matrix or data frame containing the performance table. Each row corresponds to an alternative, and each column to a criterion. Rows (resp. columns) must be named according to the IDs of the alternatives (resp. criteria).

referenceProfiles

Matrix containing, in each row, the reference profiles. The columns are named according to the criteria.

lexicographicOrder

A vector containing the indexes of the reference profiles in a given order. This vetor needs to be of the same length as the number of rows in referenceProfiles and it has to contain a permutation of the indices of these rows.

SRMP 65

criteriaWeights

Vector containing the weights of the criteria. The elements are named according to the IDs of the criteria.

criteriaMinMax

Vector containing the preference direction on each of the criteria. "min" (resp. "max") indicates that the criterion has to be minimized (maximized). The elements are named according to the IDs of the criteria.

alternativesIDs

Vector containing IDs of alternatives, according to which the datashould be fil-

criteriaIDs Vector containing IDs of criteria, according to which the data should be filtered.

#### Value

The function returns a vector containing the ranks of the alternatives (the higher the better).

#### References

A. Rolland. Procédures d'agrégation ordinale de préférences avec points de référence pour l'aide a la décision. PhD thesis, Université Paris VI, 2008.

```
# the performance table
performanceTable < rbind(c(10,10,9),c(10,9,10),c(9,10,10),c(9,9,10),c(9,10,9),c(10,9,9),
                          c(10,10,7),c(10,7,10),c(7,10,10),c(9,9,17),c(9,17,9),c(17,9,9),
                       c(7,10,17),c(10,17,7),c(17,7,10),c(7,17,10),c(17,10,7),c(10,7,17),
                           c(7,9,17),c(9,17,7),c(17,7,9),c(7,17,9),c(17,9,7),c(9,7,17))
referenceProfiles <- rbind(c(5,5,5),c(10,10,10),c(15,15,15))
lexicographicOrder \leftarrow c(2,1,3)
weights <- c(0.2, 0.44, 0.36)
criteriaMinMax <- c("max", "max", "max")</pre>
rownames(performanceTable) <- c("a1","a2","a3","a4","a5","a6","a7","a8","a9","a10","a11","a12",
                             "a13", "a14", "a15", "a16", "a17", "a18", "a19", "a20", "a21", "a22",
                                  "a23", "a24")
colnames(performanceTable) <- c("c1", "c2", "c3")</pre>
colnames(referenceProfiles) <- c("c1","c2","c3")</pre>
names(weights) <- c("c1","c2","c3")</pre>
names(criteriaMinMax) <- colnames(performanceTable)</pre>
expectedpreorder <- list('a16','a13',c('a3','a9'),'a14','a17',c('a1','a7'),'a18','a15',
                          c('a2','a8'),c('a11','a20','a22'),'a5',c('a10','a19','a24'),
```

66 SRMPInference

```
'a4',c('a12','a21','a23'),'a6')
```

preorder<-SRMP(performanceTable, referenceProfiles, lexicographicOrder, weights, criteriaMinMax)</pre>

SRMPInference

Exact inference of an SRMP model given a maximum number of reference profiles

## **Description**

Exact inference approach from pairwise comparisons of alternatives for the SRMP ranking model. This method outputs an SRMP model that is as consistent as possible with the provided pairwise comparisons (i.e. the model - the number of profiles and their lexicographic order - that maximizes the number of fulfilled pairwise comparisons). The method will search for a model with the minimum possible number of profiles up to a given maximum value.

### Usage

## Arguments

performanceTable

Matrix or data frame containing the performance table. Each row corresponds to an alternative, and each column to a criterion. Rows (resp. columns) must be named according to the IDs of the alternatives (resp. criteria).

criteriaMinMax

Vector containing the preference direction on each of the criteria. "min" (resp. "max") indicates that the criterion has to be minimized (maximized). The elements are named according to the IDs of the criteria.

maxProfilesNumber

A strictly pozitive numerical value which gives the highest number of reference profiles the sought SRMP model should have.

preferencePairs

A two column matrix containing on each row a pair of alternative names where the first alternative is considered to be strictly preferred to the second.

indifferencePairs

A two column matrix containing on each row a pair of alternative names the two alternatives are considered to indifferent with respect to each other.

alternativesIDs

Vector containing IDs of alternatives, according to which the datashould be filtered.

criteriaIDs Vector containing IDs of criteria, according to which the data should be filtered.

SRMPInference 67

solver String specifying if the glpk solver (glpk) should be used, or the cplex (cplex)

solver. By default glpk. The cplex solver requires to install the cplex binary and

the cplex C API, as well as the cplexAPI R package.

timeLimit Allows to fix a time limit of the execution, in seconds. By default NULL (which

corresponds to no time limit).

cplexIntegralityTolerance

If the cplex solver is used, allows to fix a tolerance for integrality. By default

NULL (which corresponds to the default value of cplex).

cplexThreads If the cplex solver is used, allows to the number of threads for the calculation.

By default NULL (which corresponds to the default value of cplex).

#### Value

The function returns a list containing:

criteriaWeights

The inferred criteria weights.

referenceProfilesNumber

The inferred reference profiles number.

referenceProfiles

The inferred reference profiles.

lexicographicOrder

The inferred lexicographic order of the profiles.

fitness The percentage (0 to 1) of fulfilled pair-wise relations.

solverStatus The solver status as given by glpk or cplex.

humanReadableStatus

A description of the solver status.

### References

A-L. OLTEANU, V. MOUSSEAU, W. OUERDANE, A. ROLLAND, Y. ZHENG, Preference Elicitation for a Ranking Method based on Multiple Reference Profiles, forthcoming 2018.

SRMPInferenceApprox

Approximative inference of an SRMP model

## **Description**

Approximative inference approach from pairwise comparisons of alternatives for the SRMP ranking model. This method outputs an SRMP model that fulfils as many pairwise comparisons as possible. Neither the number of reference profiles, nor the lexicographic order are fixed beforehand, however a maximum value for the number of reference profiles needs to be provided.

#### Usage

#### **Arguments**

performanceTable

Matrix or data frame containing the performance table. Each row corresponds to an alternative, and each column to a criterion. Rows (resp. columns) must be named according to the IDs of the alternatives (resp. criteria).

criteriaMinMax

Vector containing the preference direction on each of the criteria. "min" (resp. "max") indicates that the criterion has to be minimized (maximized). The elements are named according to the IDs of the criteria.

maxProfilesNumber

The maximum number of reference profiles of the SRMP model.

preferencePairs

A two column matrix containing on each row a pair of alternative names where the first alternative is considered to be strictly preferred to the second.

indifferencePairs

A two column matrix containing on each row a pair of alternative names the two alternatives are considered to indifferent with respect to each other.

alternativesIDs

Vector containing IDs of alternatives, according to which the datashould be fil-

tered.

criteriaIDs Vector containing IDs of criteria, according to which the data should be filtered.

timeLimit Allows to fix a time limit of the execution, in seconds (default 60).

populationSize Allows to change the size of the population used by the genetic algorithm (de-

fault 20).

mutationProb Allows to change the mutation probability used by the genetic algorithm (default

0.1).

### Value

The function returns a list containing:

criteriaWeights

The inferred criteria weights.

referenceProfilesNumber

The number of inferred reference profiles.

referenceProfiles

The inferred reference profiles.

lexicographicOrder

The inferred lexicographic order of the reference profiles.

fitness The percentage of fulfilled pair-wise relations.

#### References

A-L. OLTEANU, V. MOUSSEAU, W. OUERDANE, A. ROLLAND, Y. ZHENG, Preference Elicitation for a Ranking Method based on Multiple Reference Profiles, forthcoming 2018.

SRMPInferenceApproxFixedLexicographicOrder

Approximative inference of an SRMP model given the lexicographic order of the profiles

### Description

Approximative inference approach from pairwise comparisons of alternatives for the SRMP ranking model. This method outputs an SRMP model that fulfils as many pairwise comparisons as possible. The number of reference profiles and their lexicographic order is fixed beforehand.

# Usage

#### **Arguments**

performanceTable

Matrix or data frame containing the performance table. Each row corresponds to an alternative, and each column to a criterion. Rows (resp. columns) must be named according to the IDs of the alternatives (resp. criteria).

criteriaMinMax Vector containing the preference direction on each of the criteria. "min" (resp. "max") indicates that the criterion has to be minimized (maximized). The elements are named according to the IDs of the criteria.

lexicographicOrder

A vector containing the indexes of the reference profiles in a given order. The number of reference profiles to be used is derrived implicitly from the size of this vector. The elements of this vector need to be a permutation of the indices from 1 to its size.

preferencePairs

A two column matrix containing on each row a pair of alternative names where the first alternative is considered to be strictly preferred to the second.

indifferencePairs

A two column matrix containing on each row a pair of alternative names the two alternatives are considered to indifferent with respect to each other.

alternativesIDs

Vector containing IDs of alternatives, according to which the datashould be fil-

criteriaIDs Vector containing IDs of criteria, according to which the data should be filtered.

timeLimit Allows to fix a time limit of the execution, in seconds (default 60).

populationSize Allows to change the size of the population used by the genetic algorithm (de-

fault 20).

mutationProb Allows to change the mutation probability used by the genetic algorithm (default

0.1).

#### Value

The function returns a list containing:

criteriaWeights

The inferred criteria weights.

referenceProfiles

The inferred reference profiles.

lexicographicOrder

The lexicographic order of the reference profiles, in this case the one that was originally given as input.

fitness The percentage of fulfilled pair-wise relations.

#### References

A-L. OLTEANU, V. MOUSSEAU, W. OUERDANE, A. ROLLAND, Y. ZHENG, Preference Elicitation for a Ranking Method based on Multiple Reference Profiles, forthcoming 2018.

### **Examples**

lexicographicOrder <- c(1,2,3)

```
criteriaMinMax <- c("max", "max", "max")</pre>
rownames(performanceTable) <- c("a1","a2","a3","a4","a5","a6","a7","a8","a9","a10","a11",
                                  "a12", "a13", "a14", "a15", "a16", "a17", "a18", "a19", "a20",
                                  "a21", "a22", "a23", "a24")
colnames(performanceTable) <- c("c1","c2","c3")</pre>
names(criteriaMinMax) <- colnames(performanceTable)</pre>
# expected result for the tests below
expectedpreorder <- list("a16","a13",c("a3","a9"),"a14","a17",c("a1","a7"),"a18","a15")
# test - preferences and indifferences
preferencePairs <- matrix(c("a16","a13","a3","a14","a17","a1","a18","a15","a2","a11",
                              "a5", "a10", "a4", "a12", "a13", "a3", "a14", "a17", "a1", "a18",
                             "a15", "a2", "a11", "a5", "a10", "a4", "a12", "a6"), 14, 2)
indifferencePairs <- matrix(c("a3","a1","a2","a11","a11","a20","a10","a10","a19","a12",
                                "a12","a21","a9","a7","a8","a20","a22","a22","a19","a24",
                                "a24","a21","a23","a23"),12,2)
set.seed(1)
result<-SRMPInferenceApproxFixedLexicographicOrder(performanceTable, criteriaMinMax,
                                                      lexicographicOrder, preferencePairs,
                                                      indifferencePairs, alternativesIDs =
                                                      c("a1","a3","a7","a9","a13","a14",
                                                      "a15", "a16", "a17", "a18"))
```

 ${\tt SRMPInference ApproxFixed Profiles Number}$ 

Approximative inference of an SRMP model given the number of reference profiles

### **Description**

Approximative inference approach from pairwise comparisons of alternatives for the SRMP ranking model. This method outputs an SRMP model that fulfils as many pairwise comparisons as possible. The number of reference profiles is fixed beforehand, however the algorithm will explore any lexicographic order between them.

### Usage

```
alternativesIDs = NULL, criteriaIDs = NULL,
  timeLimit = 60,
  populationSize = 20, mutationProb = 0.1)
```

# **Arguments**

performanceTable

Matrix or data frame containing the performance table. Each row corresponds to an alternative, and each column to a criterion. Rows (resp. columns) must be named according to the IDs of the alternatives (resp. criteria).

criteriaMinMax Vector containing the preference direction on each of the criteria. "min" (resp. "max") indicates that the criterion has to be minimized (maximized). The elements are named according to the IDs of the criteria.

profilesNumber The number of reference profiles of the SRMP model.

preferencePairs

A two column matrix containing on each row a pair of alternative names where the first alternative is considered to be strictly preferred to the second.

indifferencePairs

A two column matrix containing on each row a pair of alternative names the two alternatives are considered to indifferent with respect to each other.

alternativesIDs

Vector containing IDs of alternatives, according to which the datashould be filtered.

Vector containing IDs of criteria, according to which the data should be filtered. criteriaIDs

timel imit Allows to fix a time limit of the execution, in seconds (default 60).

populationSize Allows to change the size of the population used by the genetic algorithm (de-

fault 20).

Allows to change the mutation probability used by the genetic algorithm (default mutationProb

0.1).

### Value

The function returns a list containing:

criteriaWeights

The inferred criteria weights.

referenceProfiles

The inferred reference profiles.

lexicographicOrder

The inferred lexicographic order of the reference profiles.

The percentage of fulfilled pair-wise relations. fitness

# References

A-L. OLTEANU, V. MOUSSEAU, W. OUERDANE, A. ROLLAND, Y. ZHENG, Preference Elicitation for a Ranking Method based on Multiple Reference Profiles, forthcoming 2018.

# **Examples**

```
# the performance table
performanceTable \leftarrow rbind(c(10,10,9),c(10,9,10),c(9,10,10),c(9,9,10),c(9,10,9),c(10,9,9),
                          c(10,10,7),c(10,7,10),c(7,10,10),c(9,9,17),c(9,17,9),c(17,9,9),
                       c(7,10,17),c(10,17,7),c(17,7,10),c(7,17,10),c(17,10,7),c(10,7,17),
                            c(7,9,17),c(9,17,7),c(17,7,9),c(7,17,9),c(17,9,7),c(9,7,17))
criteriaMinMax <- c("max", "max", "max")</pre>
rownames(performanceTable) <- c("a1", "a2", "a3", "a4", "a5", "a6", "a7", "a8", "a9", "a10", "a11",
                                  "a12", "a13", "a14", "a15", "a16", "a17", "a18", "a19", "a20",
                                  "a21", "a22", "a23", "a24")
colnames(performanceTable) <- c("c1","c2","c3")</pre>
names(criteriaMinMax) <- colnames(performanceTable)</pre>
# expected result for the tests below
expectedpreorder <- list("a16", "a13", c("a3", "a9"), "a14", c("a1", "a7"), "a15")
# test - preferences and indifferences
preferencePairs <- matrix(c("a16","a13","a3","a14","a17","a1","a18","a18","a2","a11",</pre>
                              "a5", "a10", "a4", "a12", "a13", "a3", "a14", "a17", "a1", "a18",
                              "a15", "a2", "a11", "a5", "a10", "a4", "a12", "a6"), 14, 2)
indifferencePairs <- matrix(c("a3","a1","a2","a11","a11","a20","a10","a10","a19","a12",
                                "a12", "a21", "a9", "a7", "a8", "a20", "a22", "a22", "a19", "a24",
                                "a24", "a21", "a23", "a23"), 12, 2)
set.seed(1)
result<-SRMPInferenceApproxFixedProfilesNumber(performanceTable, criteriaMinMax, 3,
                                                  preferencePairs, indifferencePairs,
                                                   alternativesIDs = c("a1","a3","a7","a9",
                                                   "a13", "a14", "a15", "a16"))
```

SRMPInferenceFixedLexicographicOrder

Exact inference of an SRMP model given the lexicographic order of the profiles

### **Description**

Exact inference approach from pairwise comparisons of alternatives for the SRMP ranking model. This method outputs an SRMP model that maximizes the number of fulfilled pairwise comparisons. The number of reference profiles and their lexicographic order is fixed.

# Usage

```
SRMPInferenceFixedLexicographicOrder(performanceTable, criteriaMinMax, lexicographicOrder,
                                     preferencePairs, indifferencePairs = NULL,
                                    alternativesIDs = NULL, criteriaIDs = NULL,
                                     solver="glpk", timeLimit = NULL,
                                     cplexIntegralityTolerance = NULL,
                                     cplexThreads = NULL)
```

#### Arguments

### performanceTable

Matrix or data frame containing the performance table. Each row corresponds to an alternative, and each column to a criterion. Rows (resp. columns) must be named according to the IDs of the alternatives (resp. criteria).

criteriaMinMax Vector containing the preference direction on each of the criteria. "min" (resp. "max") indicates that the criterion has to be minimized (maximized). The elements are named according to the IDs of the criteria.

### lexicographicOrder

A vector containing the indexes of the reference profiles in a given order. The number of reference profiles to be used is derrived implicitly from the size of this vector. The elements of this vector need to be a permutation of the indices from 1 to its size.

### preferencePairs

A two column matrix containing on each row a pair of alternative names where the first alternative is considered to be strictly preferred to the second.

### indifferencePairs

A two column matrix containing on each row a pair of alternative names the two alternatives are considered to indifferent with respect to each other.

### alternativesIDs

Vector containing IDs of alternatives, according to which the datashould be fil-

# criteriaIDs

Vector containing IDs of criteria, according to which the data should be filtered.

# solver

String specifying if the glpk solver (glpk) should be used, or the cplex (cplex) solver. By default glpk. The cplex solver requires to install the cplex binary and the cplex C API, as well as the cplexAPI R package.

### timeLimit

Allows to fix a time limit of the execution, in seconds. By default NULL (which corresponds to no time limit).

### cplexIntegralityTolerance

If the cplex solver is used, allows to fix a tolerance for integrality. By default NULL (which corresponds to the default value of cplex).

### cplexThreads

If the cplex solver is used, allows to set the number of threads for the calculation. By default NULL (which corresponds to the default value of cplex - 1).

### Value

The function returns a list containing:

```
criteriaWeights
```

The inferred criteria weights.

referenceProfiles

The inferred reference profiles.

fitness The percentage (0 to 1) of fulfilled pair-wise relations.

solverStatus The solver status as given by glpk or cplex.

humanReadableStatus

A description of the solver status.

### References

A-L. OLTEANU, V. MOUSSEAU, W. OUERDANE, A. ROLLAND, Y. ZHENG, Preference Elicitation for a Ranking Method based on Multiple Reference Profiles, forthcoming 2018.

```
# the performance table
performanceTable \leftarrow rbind(c(10,10,9),c(10,9,10),c(9,10,10),c(9,9,10),c(9,10,9),c(10,9,9),
                          c(10,10,7),c(10,7,10),c(7,10,10),c(9,9,17),c(9,17,9),c(17,9,9),
                       c(7,10,17),c(10,17,7),c(17,7,10),c(7,17,10),c(17,10,7),c(10,7,17),
                            c(7,9,17),c(9,17,7),c(17,7,9),c(7,17,9),c(17,9,7),c(9,7,17))
lexicographicOrder <- c(2,1,3)</pre>
criteriaMinMax <- c("max", "max", "max")</pre>
rownames(performanceTable) <- c("a1","a2","a3","a4","a5","a6","a7","a8","a9","a10","a11","a12",
                              "a13", "a14", "a15", "a16", "a17", "a18", "a19", "a20", "a21", "a22",
                                  "a23", "a24")
colnames(performanceTable) <- c("c1","c2","c3")</pre>
names(criteriaMinMax) <- colnames(performanceTable)</pre>
preferencePairs <- matrix(c("a16","a13","a3","a14","a17","a17","a18","a15","a2","a11","a5",
                            "a10", "a4", "a12", "a13", "a3", "a14", "a17", "a1", "a18", "a15", "a2",
                              "a11", "a5", "a10", "a4", "a12", "a6"), 14, 2)
indifferencePairs <- matrix(c("a3","a1","a2","a11","a11","a20","a10","a10","a10","a19","a12",
                           "a21", "a9", "a7", "a8", "a20", "a22", "a22", "a19", "a24", "a24", "a21",
                                "a23", "a23"), 12, 2)
result<-SRMPInferenceFixedLexicographicOrder(performanceTable, criteriaMinMax,
                                                lexicographicOrder, preferencePairs,
                                                indifferencePairs, alternativesIDs =
                                            c("a1", "a3", "a7", "a9", "a13", "a14", "a16", "a17"))
```

SRMPInferenceFixedProfilesNumber

Exact inference of an SRMP model given the number of reference profiles

### **Description**

Exact inference approach from pairwise comparisons of alternatives for the SRMP ranking model. This method outputs an SRMP model that is as consistent as possible with the provided pairwise comparisons (i.e. the model - and the lexicographic order of the reference profiles - that maximizes the number of fulfilled pairwise comparisons). The number of reference profiles is fixed and needs to be provided.

### Usage

```
SRMPInferenceFixedProfilesNumber(performanceTable, criteriaMinMax, profilesNumber,
                                 preferencePairs, indifferencePairs = NULL,
                                 alternativesIDs = NULL, criteriaIDs = NULL,
                                 solver="glpk", timeLimit = NULL,
                                 cplexIntegralityTolerance = NULL,
                                 cplexThreads = NULL)
```

### **Arguments**

performanceTable

Matrix or data frame containing the performance table. Each row corresponds to an alternative, and each column to a criterion. Rows (resp. columns) must be named according to the IDs of the alternatives (resp. criteria).

criteriaMinMax

Vector containing the preference direction on each of the criteria. "min" (resp. "max") indicates that the criterion has to be minimized (maximized). The elements are named according to the IDs of the criteria.

profilesNumber A strictly pozitive numerical value which gives the number of reference profiles in the sought SRMP model.

preferencePairs

A two column matrix containing on each row a pair of alternative names where the first alternative is considered to be strictly preferred to the second.

indifferencePairs

A two column matrix containing on each row a pair of alternative names the two alternatives are considered to indifferent with respect to each other.

alternativesIDs

Vector containing IDs of alternatives, according to which the datashould be fil-

criteriaIDs

Vector containing IDs of criteria, according to which the data should be filtered. String specifying if the glpk solver (glpk) should be used, or the cplex (cplex) solver. By default glpk. The cplex solver requires to install the cplex binary and the cplex C API, as well as the cplex API R package.

solver

timeLimit Allows to fix a time limit of the execution, in seconds. By default NULL (which

corresponds to no time limit).

 ${\tt cplexIntegralityTolerance}$ 

If the cplex solver is used, allows to fix a tolerance for integrality. By default

NULL (which corresponds to the default value of cplex).

cplexThreads If the cplex solver is used, allows to the number of threads for the calculation.

By default NULL (which corresponds to the default value of cplex).

### Value

The function returns a list containing:

criteriaWeights

The inferred criteria weights.

referenceProfiles

The inferred reference profiles.

lexicographicOrder

The inferred lexicographic order of the profiles.

fitness The percentage (0 to 1) of fulfilled pair-wise relations.

solverStatus The solver status as given by glpk or cplex.

humanReadableStatus

A description of the solver status.

### References

A-L. OLTEANU, V. MOUSSEAU, W. OUERDANE, A. ROLLAND, Y. ZHENG, Preference Elicitation for a Ranking Method based on Multiple Reference Profiles, forthcoming 2018.

```
"a21", "a9", "a7", "a8", "a20", "a22", "a22", "a19", "a24", "a24", "a21",
      "a23", "a23"), 12, 2)
```

```
result<-SRMPInferenceFixedProfilesNumber(performanceTable, criteriaMinMax, 3, preferencePairs,
                                        indifferencePairs, alternativesIDs = c("a1", "a3",
                                           "a7", "a9", "a13", "a14", "a15", "a16", "a17", "a18"))
```

SRMPInferenceNoInconsist

Exact inference of an SRMP model given a maximum number of reference profiles - no inconsistencies

### **Description**

Exact inference approach from pairwise comparisons of alternatives for the SRMP ranking model. This method only outputs a result when an SRMP model consistent with the provided pairwise comparisons exists. The method will search for a model with the minimum possible number of profiles up to a given maximum value. If such a model exists, this method is significantly faster than the one which handles inconsistencies.

### Usage

```
SRMPInferenceNoInconsist(performanceTable, criteriaMinMax, maxProfilesNumber,
                        preferencePairs, indifferencePairs = NULL,
                        alternativesIDs = NULL, criteriaIDs = NULL,
                        solver="glpk", timeLimit = NULL,
                        cplexIntegralityTolerance = NULL,
                        cplexThreads = NULL)
```

### **Arguments**

performanceTable

Matrix or data frame containing the performance table. Each row corresponds to an alternative, and each column to a criterion. Rows (resp. columns) must be named according to the IDs of the alternatives (resp. criteria).

criteriaMinMax Vector containing the preference direction on each of the criteria. "min" (resp. "max") indicates that the criterion has to be minimized (maximized). The elements are named according to the IDs of the criteria.

maxProfilesNumber

A strictly pozitive numerical value which gives the highest number of reference profiles the sought SRMP model should have.

preferencePairs

A two column matrix containing on each row a pair of alternative names where the first alternative is considered to be strictly preferred to the second.

indifferencePairs

A two column matrix containing on each row a pair of alternative names the two alternatives are considered to indifferent with respect to each other.

alternativesIDs

Vector containing IDs of alternatives, according to which the datashould be fil-

tered.

criteriaIDs Vector containing IDs of criteria, according to which the data should be filtered.

solver String specifying if the glpk solver (glpk) should be used, or the cplex (cplex)

solver. By default glpk. The cplex solver requires to install the cplex binary and

the cplex C API, as well as the cplexAPI R package.

timeLimit Allows to fix a time limit of the execution, in seconds. By default NULL (which

corresponds to no time limit).

cplexIntegralityTolerance

If the cplex solver is used, allows to fix a tolerance for integrality. By default

NULL (which corresponds to the default value of cplex).

cplexThreads If the cplex solver is used, allows to the number of threads for the calculation.

By default NULL (which corresponds to the default value of cplex).

### Value

The function returns a list containing:

criteriaWeights

The inferred criteria weights.

referenceProfilesNumber

The inferred reference profiles number.

referenceProfiles

The inferred reference profiles.

lexicographicOrder

The inferred lexicographic order of the profiles.

solverStatus The solver status as given by glpk or cplex.

humanReadableStatus

A description of the solver status.

# References

A-L. OLTEANU, V. MOUSSEAU, W. OUERDANE, A. ROLLAND, Y. ZHENG, Preference Elicitation for a Ranking Method based on Multiple Reference Profiles, forthcoming 2018.

 ${\tt SRMPInferenceNoInconsistFixedLexicographicOrder}$ 

Exact inference of an SRMP model given the lexicographic order of the profiles - no inconsistencies

### **Description**

Exact inference approach from pairwise comparisons of alternatives for the SRMP ranking model. This method only outputs a result when an SRMP model consistent with the provided pairwise comparisons exists. The number of reference profiles and their lexicographic order is fixed. If such a model exists, this method is significantly faster than the one which handles inconsistencies.

# Usage

### **Arguments**

performanceTable

Matrix or data frame containing the performance table. Each row corresponds to an alternative, and each column to a criterion. Rows (resp. columns) must be named according to the IDs of the alternatives (resp. criteria).

criteriaMinMax Vector containing the preference direction on each of the criteria. "min" (resp. "max") indicates that the criterion has to be minimized (maximized). The ele-

ments are named according to the IDs of the criteria.

lexicographicOrder

A vector containing the indexes of the reference profiles in a given order. The number of reference profiles to be used is derrived implicitly from the size of this vector. The elements of this vector need to be a permutation of the indices from 1 to its size.

preferencePairs

A two column matrix containing on each row a pair of alternative names where the first alternative is considered to be strictly preferred to the second.

indifferencePairs

A two column matrix containing on each row a pair of alternative names the two alternatives are considered to indifferent with respect to each other.

alternativesIDs

Vector containing IDs of alternatives, according to which the datashould be fil-

tered.

criteriaIDs Vector containing IDs of criteria, according to which the data should be filtered.

solver String specifying if the glpk solver (glpk) should be used, or the cplex (cplex)

solver. By default glpk. The cplex solver requires to install the cplex binary and

the cplex C API, as well as the cplexAPI R package.

timeLimit Allows to fix a time limit of the execution, in seconds. By default NULL (which

corresponds to no time limit).

cplexIntegralityTolerance

If the cplex solver is used, allows to fix a tolerance for integrality. By default

NULL (which corresponds to the default value of cplex).

cplexThreads If the cplex solver is used, allows to the number of threads for the calculation.

By default NULL (which corresponds to the default value of cplex).

### Value

The function returns a list containing:

criteriaWeights

The inferred criteria weights.

referenceProfiles

The inferred reference profiles.

solverStatus The solver status as given by glpk or cplex.

humanReadableStatus

A description of the solver status.

### References

A-L. OLTEANU, V. MOUSSEAU, W. OUERDANE, A. ROLLAND, Y. ZHENG, Preference Elicitation for a Ranking Method based on Multiple Reference Profiles, forthcoming 2018.

# **Examples**

```
# the performance table
performanceTable < rbind(c(10,10,9),c(10,9,10),c(9,10,10),c(9,9,10),c(9,10,9),c(10,9,9),
                           c(10,10,7),c(10,7,10),c(7,10,10),c(9,9,17),c(9,17,9),c(17,9,9),
                       c(7,10,17),c(10,17,7),c(17,7,10),c(7,17,10),c(17,10,7),c(10,7,17),
                            c(7,9,17),c(9,17,7),c(17,7,9),c(7,17,9),c(17,9,7),c(9,7,17))
lexicographicOrder <- c(2,1,3)</pre>
criteriaMinMax <- c("max", "max", "max")</pre>
rownames(performanceTable) <- c("a1", "a2", "a3", "a4", "a5", "a6", "a7", "a8", "a9", "a10", "a11", "a12",
                              "a13", "a14", "a15", "a16", "a17", "a18", "a19", "a20", "a21", "a22",
                                   "a23", "a24")
colnames(performanceTable) <- c("c1","c2","c3")</pre>
names(criteriaMinMax) <- colnames(performanceTable)</pre>
preferencePairs <- matrix(c("a16","a13","a3","a14","a17","a1","a18","a18","a15","a2","a11","a5",</pre>
                            "a10", "a4", "a12", "a13", "a3", "a14", "a17", "a1", "a18", "a15", "a2",
                              "a11", "a5", "a10", "a4", "a12", "a6"), 14, 2)
indifferencePairs <- matrix(c("a3","a1","a2","a11","a11","a20","a10","a10","a19","a19","a12",
                           "a21", "a9", "a7", "a8", "a20", "a22", "a22", "a19", "a24", "a24", "a21",
                                 "a23", "a23"), 12, 2)
result<-SRMPInferenceNoInconsistFixedLexicographicOrder(performanceTable, criteriaMinMax,
                                                         lexicographicOrder, preferencePairs,
                                                         indifferencePairs, alternativesIDs =
                                                       c("a1", "a2", "a3", "a4", "a5", "a6", "a7",
                                                          "a8", "a10", "a11", "a12", "a14", "a16"
                                                         "a17", "a18", "a19", "a20", "a21", "a23",
                                                             "a24"))
```

 ${\tt SRMPInferenceNoInconsistFixedProfilesNumber}$ 

Exact inference of an SRMP model given the number of reference profiles - no inconsistencies

# Description

Exact inference approach from pairwise comparisons of alternatives for the SRMP ranking model. This method only outputs a result when an SRMP model consistent with the provided pairwise comparisons exists. The number of reference profiles is fixed and need to be provided. If such a model exists, this method is significantly faster than the one which handles inconsistencies.

### Usage

# **Arguments**

performanceTable

Matrix or data frame containing the performance table. Each row corresponds to an alternative, and each column to a criterion. Rows (resp. columns) must be named according to the IDs of the alternatives (resp. criteria).

criteriaMinMax Vector containing the preference direction on each of the criteria. "min" (resp.

"max") indicates that the criterion has to be minimized (maximized). The elements are named according to the IDs of the criteria.

profilesNumber A strictly pozitive numerical value which gives the number of reference profiles

in the sought SRMP model.

preferencePairs

A two column matrix containing on each row a pair of alternative names where the first alternative is considered to be strictly preferred to the second.

indifferencePairs

A two column matrix containing on each row a pair of alternative names the two alternatives are considered to indifferent with respect to each other.

alternativesIDs

Vector containing IDs of alternatives, according to which the datashould be fil-

tered.

criteriaIDs Vector containing IDs of criteria, according to which the data should be filtered.

solver String specifying if the glpk solver (glpk) should be used, or the cplex (cplex) solver. By default glpk. The cplex solver requires to install the cplex binary and

the cplex C API, as well as the cplex API R package.

timeLimit Allows to fix a time limit of the execution, in seconds. By default NULL (which

corresponds to no time limit).

cplexIntegralityTolerance

If the cplex solver is used, allows to fix a tolerance for integrality. By default

NULL (which corresponds to the default value of cplex).

cplexThreads If the cplex solver is used, allows to the number of threads for the calculation.

By default NULL (which corresponds to the default value of cplex).

### Value

The function returns a list containing:

criteriaWeights

The inferred criteria weights.

SURE 85

referenceProfiles

The inferred reference profiles.

lexicographicOrder

The inferred lexicographic order of the profiles.

solverStatus The solver status as given by glpk or cplex.

humanReadableStatus

A description of the solver status.

### References

A-L. OLTEANU, V. MOUSSEAU, W. OUERDANE, A. ROLLAND, Y. ZHENG, Preference Elicitation for a Ranking Method based on Multiple Reference Profiles, forthcoming 2018.

```
performanceTable <- rbind(c(10,10,9),c(10,9,10),c(9,10,10),c(9,9,10),c(9,10,9),c(10,9,9),
                          c(10,10,7),c(10,7,10),c(7,10,10),c(9,9,17),c(9,17,9),c(17,9,9),
                       c(7,10,17),c(10,17,7),c(17,7,10),c(7,17,10),c(17,10,7),c(10,7,17),
                            c(7,9,17),c(9,17,7),c(17,7,9),c(7,17,9),c(17,9,7),c(9,7,17))
criteriaMinMax <- c("max", "max", "max")</pre>
rownames(performanceTable) <- c("a1","a2","a3","a4","a5","a6","a7","a8","a9","a10","a11","a12",
                              "a13", "a14", "a15", "a16", "a17", "a18", "a19", "a20", "a21", "a22",
                                  "a23", "a24")
colnames(performanceTable) <- c("c1","c2","c3")</pre>
names(criteriaMinMax) <- colnames(performanceTable)</pre>
preferencePairs <- matrix(c("a16", "a13", "a3", "a14", "a17", "a1", "a18", "a15", "a2", "a11", "a5",
                            "a10", "a4", "a12", "a13", "a3", "a14", "a17", "a1", "a18", "a15", "a2",
                              "a11", "a5", "a10", "a4", "a12", "a6"), 14, 2)
indifferencePairs <- matrix(c("a3","a1","a2","a11","a11","a20","a10","a10","a19","a19","a12",
                           "a21", "a9", "a7", "a8", "a20", "a22", "a22", "a19", "a24", "a24", "a21",
                                "a23", "a23"), 12, 2)
result<-SRMPInferenceNoInconsistFixedProfilesNumber(performanceTable, criteriaMinMax, 3,
                                                        preferencePairs, indifferencePairs,
                                                    alternativesIDs = c("a1", "a2", "a3", "a4",
                                                      "a5", "a6", "a7", "a8", "a10", "a11", "a12",
                                                  "a14", "a16", "a17", "a18", "a19", "a20", "a21",
                                                        "a23","a24"))
```

**SURE** 86

### **Description**

SURE is a multi-criteria decision analysis method which was developed by Richard Hodgett and Sajid Siraj. More details on the method are available in https://doi.org/10.1016/j.eswa.2018.08.048

### Usage

```
SURE(performanceTableMin,
     performanceTable,
     performanceTableMax,
     criteriaWeights,
     criteriaMinMax,
     alternativesIDs = NULL,
     criteriaIDs = NULL,
 NoOfSimulations = 100000)
```

# Arguments

performanceTableMin

Matrix or data frame containing the minimum performance table. Each column corresponds to an alternative, and each row to a criterion. Columns (resp. rows) must be named according to the IDs of the alternatives (resp. criteria).

performanceTable

Matrix or data frame containing the most likely performance table. Each column corresponds to an alternative, and each row to a criterion. Columns (resp. rows) must be named according to the IDs of the alternatives (resp. criteria).

performanceTableMax

Matrix or data frame containing the maximum performance table. Each column corresponds to an alternative, and each row to a criterion. Columns (resp. rows) must be named according to the IDs of the alternatives (resp. criteria).

criteriaWeights

Vector containing the weights of the criteria. The elements are named according to the IDs of the criteria.

criteriaMinMax Vector containing the preference direction on each of the criteria. "min" (resp. "max") indicates that the criterion has to be minimized (maximized). The elements are named according to the IDs of the criteria.

alternativesIDs

Vector containing IDs of alternatives, according to which the data should be filtered.

criteriaIDs

Vector containing IDs of criteria, according to which the data should be filtered.

**NoOfSimulations** 

Integer stating the number of Simulations to use.

# Value

The function returns an element of type SURE which contains the SURE simulated scores for each alternative.

SURE 87

#### References

Richard E. Hodgett, Sajid Siraj (2019). SURE: A method for decision-making under uncertainty. Expert Systems with Applications, Volume 115, 684-694.

```
performanceTableMin <- t(matrix(c(78,87,79,19,8,68,74,8,90,89,74.5,9,20,81,30),</pre>
                   nrow=3,ncol=5, byrow=TRUE))
performanceTable <- t(\text{matrix}(c(80,87,86,19,8,70,74,10,90,89,75,9,33,82,30)),
                                nrow=3,ncol=5, byrow=TRUE))
performanceTableMax <- t(matrix(c(81,87,95,19,8,72,74,15,90,89,75.5,9,36,84,30),
                                   nrow=3,ncol=5, byrow=TRUE))
row.names(performanceTable) <- c("Yield","Toxicity","Cost","Separation","Odour")</pre>
colnames(performanceTable) <- c("Route One", "Route Two", "Route Three")</pre>
row.names(performanceTableMin) <- row.names(performanceTable)</pre>
colnames(performanceTableMin) <- colnames(performanceTable)</pre>
row.names(performanceTableMax) <- row.names(performanceTable)</pre>
colnames(performanceTableMax) <- colnames(performanceTable)</pre>
criteriaWeights < c(0.339,0.077,0.434,0.127,0.023)
names(criteriaWeights) <- row.names(performanceTable)</pre>
criteriaMinMax <- c("max", "max", "max", "max", "max")</pre>
names(criteriaMinMax) <- row.names(performanceTable)</pre>
test1 <- SURE(performanceTableMin,</pre>
                  performanceTable,
                  performanceTableMax,
                  criteriaWeights,
                  criteriaMinMax, NoOfSimulations = 101)
summary(test1)
plotSURE(test1)
plotSURE(test1, greyScale = TRUE, separate = TRUE)
test2 <- SURE(performanceTableMin,</pre>
              performanceTable,
              performanceTableMax,
               criteriaWeights,
              criteriaMinMax,
              alternativesIDs = c("Route Two", "Route Three"),
               criteriaIDs = c("Yield", "Toxicity", "Separation"),
              NoOfSimulations = 101)
summary(test2)
plotSURE(test2)
plotSURE(test2, greyScale = TRUE, separate = TRUE)
```

88 **TOPSIS** 

TOPSIS

Technique for Order of Preference by Similarity to Ideal Solution (TOPSIS) method

# **Description**

TOPSIS is a multi-criteria decision analysis method which was originally developed by Hwang and Yoon in 1981.

### **Usage**

```
TOPSIS(performanceTable,
         criteriaWeights,
         criteriaMinMax,
         positiveIdealSolutions = NULL,
         negativeIdealSolutions = NULL,
         alternativesIDs = NULL,
         criteriaIDs = NULL)
```

### **Arguments**

performanceTable

Matrix or data frame containing the performance table. Each row corresponds to an alternative, and each column to a criterion. Rows (resp. columns) must be named according to the IDs of the alternatives (resp. criteria).

criteriaWeights

Vector containing the weights of the criteria. The elements are named according to the IDs of the criteria.

criteriaMinMax Vector containing the preference direction on each of the criteria. "min" (resp. "max") indicates that the criterion has to be minimized (maximized). The elements are named according to the IDs of the criteria.

positiveIdealSolutions

Vector containing the positive ideal solutions for each criteria. The elements are named according to the IDs of the criteria.

negativeIdealSolutions

Vector containing the negative ideal solutions for each criteria. The elements are named according to the IDs of the criteria.

alternativesIDs

Vector containing IDs of alternatives, according to which the data should be filtered.

criteriaIDs

Vector containing IDs of criteria, according to which the data should be filtered.

### Value

The function returns a vector containing the TOPSIS score for each alternative.

TOPSIS 89

### References

Hwang, C.L.; Yoon, K. (1981). Multiple Attribute Decision Making: Methods and Applications. New York: Springer-Verlag. http://hodgett.co.uk/topsis-in-excel/

```
performanceTable <- matrix(c(5490,51.4,8.5,285,6500,70.6,7,</pre>
                                288,6489,54.3,7.5,290),
                                nrow=3.
                                ncol=4,
                                byrow=TRUE)
row.names(performanceTable) <- c("Corsa", "Clio", "Fiesta")</pre>
colnames(performanceTable) <- c("Purchase Price", "Economy",</pre>
                                      "Aesthetics", "Boot Capacity")
weights <-c(0.35, 0.25, 0.25, 0.15)
criteriaMinMax <- c("min", "max", "max", "max")</pre>
positiveIdealSolutions <- c(0.179573776, 0.171636015, 0.159499658, 0.087302767)
negativeIdealSolutions <- c(0.212610118, 0.124958799, 0.131352659, 0.085797547)
names(weights) <- colnames(performanceTable)</pre>
names(criteriaMinMax) <- colnames(performanceTable)</pre>
names(positiveIdealSolutions) <- colnames(performanceTable)</pre>
names(negativeIdealSolutions) <- colnames(performanceTable)</pre>
overall1 <- TOPSIS(performanceTable, weights, criteriaMinMax)</pre>
overall2 <- TOPSIS(performanceTable,</pre>
                         weights,
                         criteriaMinMax,
                         positiveIdealSolutions,
                        negativeIdealSolutions)
overall3 <- TOPSIS(performanceTable,</pre>
                       weights,
                        criteriaMinMax,
                        alternativesIDs = c("Corsa", "Clio"),
                        criteriaIDs = c("Purchase Price", "Economy", "Aesthetics"))
overall4 <- TOPSIS(performanceTable,</pre>
                     weights,
                     criteriaMinMax,
                      positiveIdealSolutions,
                     negativeIdealSolutions,
                      alternativesIDs = c("Corsa", "Clio"),
                     criteriaIDs = c("Purchase Price", "Economy", "Aesthetics"))
```

UTA

UTA method to elicit value functions.

### **Description**

Elicits value functions from a ranking of alternatives, according to the UTA method.

# Usage

```
UTA(performanceTable, criteriaMinMax,
    criteriaNumberOfBreakPoints, epsilon,
    alternativesRanks = NULL,
    alternativesPreferences = NULL,
    alternativesIndifferences = NULL,
    criteriaLBs=NULL, criteriaUBs=NULL,
    alternativesIDs = NULL, criteriaIDs = NULL,
    kPostOptimality = NULL)
```

# **Arguments**

performanceTable

Matrix or data frame containing the performance table. Each row corresponds to an alternative, and each column to a criterion. Rows (resp. columns) must be named according to the IDs of the alternatives (resp. criteria).

criteriaMinMax

Vector containing the preference direction on each of the criteria. "min" (resp. "max") indicates that the criterion has to be minimized (maximized). The elements are named according to the IDs of the criteria.

criteriaNumberOfBreakPoints

Vector containing the number of breakpoints of the piecewise linear value functions to be determined. Minimum 2. The elements are named according to the IDs of the criteria.

epsilon

Numeric value containing the minimal difference in value between two consecutive alternatives in the final ranking.

alternativesRanks

Optional vector containing the ranks of the alternatives. The elements are named according to the IDs of the alternatives. If not present, then at least one of alternativesPreferences or alternativesIndifferences should be given.

alternativesPreferences

Optional matrix containing the preference constraints on the alternatives. Each line of the matrix corresponds to a constraint of the type alternative a is strictly preferred to alternative b. If not present, then either alternativesRanks or alternativesIndifferences should be given.

alternativesIndifferences

Optional matrix containing the indifference constraints on the alternatives. Each line of the matrix corresponds to a constraint of the type alternative a is indifferent to alternative b. If not present, then either alternativesRanks or alternativesPreferences should be given.

criteriaLBs Vector containing the lower bounds of the criteria to be considered for the elic-

itation of the value functions. If not specified, the lower bounds present in the

performance table are taken.

criteriaUBs Vector containing the upper bounds of the criteria to be considered for the elic-

itation of the value functions. If not specified, the upper bounds present in the

performance table are taken.

alternativesIDs

Vector containing IDs of alternatives, according to which the datashould be fil-

tered.

criteriaIDs Vector containing IDs of criteria, according to which the data should be filtered.

kPostOptimality

A small positive threshold used during the postoptimality analysis (see article on UTA by Siskos and Lagreze in EJOR, 1982). If not specified, no postoptimality

analysis is performed.

### Value

The function returns a list structured as follows:

optimum The value of the objective function.

valueFunctions A list containing the value functions which have been determined. Each value

function is defined by a matrix of breakpoints, where the first row corresponds to the abscissa (row labelled "x") and where the second row corresponds to the

ordinate (row labelled "y").

overallValues A vector of the overall values of the input alternatives.

ranks A vector of the ranks of the alternatives obtained via the elicited value functions.

Ties method = "min".

Kendall's tau between the input ranking and the one obtained via the elicited

value functions. NULL if no input ranking is given but alternativesPreferences

or alternativesIndifferences.

errors A vector of the errors (sigma) which have to be added to the overall values of

the alternatives in order to respect the input ranking.

minimumWeightsP0

In case a post-optimality analysis is performed, the minimal weight of each

criterion, else NULL.

maximumWeightsP0

In case a post-optimality analysis is performed, the maximal weight of each

criterion, else NULL.

averageValueFunctionsP0

In case a post-optimality analysis is performed, average value functions respect-

ing the input ranking, else NULL.

### References

E. Jacquet-Lagreze, J. Siskos, Assessing a set of additive utility functions for multicriteria decision-making, the UTA method, European Journal of Operational Research, Volume 10, Issue 2, 151–164, June 1982.

```
# the separation threshold
epsilon <-0.05
# the performance table
performanceTable <- rbind(</pre>
   c(3,10,1),
c(4,20,2),
c(2,20,0),
c(6,40,0),
c(30,30,3))
rownames(performanceTable) <- c("RER","METRO1","METRO2","BUS","TAXI")</pre>
colnames(performanceTable) <- c("Price", "Time", "Comfort")</pre>
# ranks of the alternatives
alternativesRanks \leftarrow c(1,2,2,3,4)
names(alternativesRanks) <- row.names(performanceTable)</pre>
# criteria to minimize or maximize
criteriaMinMax <- c("min", "min", "max")</pre>
names(criteriaMinMax) <- colnames(performanceTable)</pre>
# number of break points for each criterion
criteriaNumberOfBreakPoints <- c(3,4,4)</pre>
names(criteriaNumberOfBreakPoints) <- colnames(performanceTable)</pre>
x<-UTA(performanceTable, criteriaMinMax,
        criteriaNumberOfBreakPoints, epsilon,
        alternativesRanks = alternativesRanks)
# plot the value functions obtained
plotPiecewiseLinearValueFunctions(x$valueFunctions)
# apply the value functions on the original performance table
transformedPerformanceTable <- applyPiecewiseLinearValueFunctionsOnPerformanceTable(</pre>
  x$valueFunctions,
  performanceTable)
# calculate the overall score of each alternative
```

```
weightedSum(transformedPerformanceTable, c(1,1,1))
# ranking some cars (from original article on UTA by Siskos and Lagreze, 1982)
# the separation threshold
epsilon <-0.01
# the performance table
performanceTable <- rbind(</pre>
c(173, 11.4, 10.01, 10, 7.88, 49500),
c(176, 12.3, 10.48, 11, 7.96, 46700),
c(142, 8.2, 7.30, 5, 5.65, 32100),
c(148, 10.5, 9.61, 7, 6.15, 39150),
c(178, 14.5, 11.05, 13, 8.06, 64700),
c(180, 13.6, 10.40, 13, 8.47, 75700),
c(182, 12.7, 12.26, 11, 7.81, 68593),
c(145, 14.3, 12.95, 11, 8.38, 55000),
c(161, 8.6, 8.42, 7, 5.11, 35200),
c(117, 7.2, 6.75, 3, 5.81, 24800)
rownames(performanceTable) <- c(</pre>
  "Peugeot 505 GR",
  "Opel Record 2000 LS"
  "Citroen Visa Super E",
  "VW Golf 1300 GLS",
  "Citroen CX 2400 Pallas",
  "Mercedes 230",
  "BMW 520",
  "Volvo 244 DL",
  "Peugeot 104 ZS",
  "Citroen Dyane")
colnames(performanceTable) <- c(</pre>
  "MaximalSpeed",
  "ConsumptionTown"
  "Consumption120kmh",
  "HP",
  "Space"
  "Price")
# ranks of the alternatives
alternativesRanks <- c(1,2,3,4,5,6,7,8,9,10)
names(alternativesRanks) <- row.names(performanceTable)</pre>
# criteria to minimize or maximize
criteriaMinMax <- c("max", "min", "min", "max", "max", "min")</pre>
```

```
names(criteriaMinMax) <- colnames(performanceTable)</pre>
# number of break points for each criterion
criteriaNumberOfBreakPoints <- c(5,4,4,5,4,5)</pre>
names(criteriaNumberOfBreakPoints) <- colnames(performanceTable)</pre>
# lower bounds of the criteria for the determination of value functions
criteriaLBs=c(110,7,6,3,5,20000)
names(criteriaLBs) <- colnames(performanceTable)</pre>
# upper bounds of the criteria for the determination of value functions
criteriaUBs=c(190,15,13,13,9,80000)
names(criteriaUBs) <- colnames(performanceTable)</pre>
x<-UTA(performanceTable, criteriaMinMax,
        criteriaNumberOfBreakPoints, epsilon,
        alternativesRanks = alternativesRanks,
        criteriaLBs = criteriaLBs, criteriaUBs = criteriaUBs)
# plot the value functions obtained
plotPiecewiseLinearValueFunctions(x$valueFunctions)
# apply the value functions on the original performance table
transformedPerformanceTable <- applyPiecewiseLinearValueFunctionsOnPerformanceTable(</pre>
      x$valueFunctions,
      performanceTable)
# calculate the overall score of each alternative
weights <-c(1,1,1,1,1,1)
names(weights)<-colnames(performanceTable)</pre>
weightedSum(transformedPerformanceTable, c(1,1,1,1,1,1))
# the same analysis with less extreme value functions
# from the post-optimality analysis
x<-UTA(performanceTable, criteriaMinMax,
        criteriaNumberOfBreakPoints, epsilon,
        alternativesRanks = alternativesRanks,
        criteriaLBs = criteriaLBs,
        criteriaUBs = criteriaUBs,
```

```
kPostOptimality = 0.01)
# plot the value functions obtained
plotPiecewiseLinearValueFunctions(x$averageValueFunctionsP0)
# apply the value functions on the original performance table
transformed Performance Table <- apply Piecewise Linear Value Functions On Performance Table (- apply Piecewise Linear Value Functions Control Performance Table (- apply Piecewise Linear Value Functions Control Performance Table (- apply Piecewise Linear Value Functions Control Performance Table (- apply Piecewise Linear Value Functions Control Performance Table (- apply Piecewise Linear Value Functions Control Performance Table (- apply Piecewise Linear Value Functions Control Performance Table (- apply Piecewise Linear Value Functions Control Performance Table (- apply Piecewise Linear Value Functions Control Performance Table (- apply Piecewise Linear Value Functions Control Performance Table (- apply Piecewise Linear Value Functions Control Performance Table (- apply Piecewise Linear Value Functions Control Performance Table (- apply Piecewise Linear Value Functions Control Performance Table (- apply Piecewise Linear Value Functions Control Performance Table (- apply Piecewise Linear Value Functions Control Performance Table (- apply Piecewise Linear Value Functions Control Performance Table (- apply Piecewise Linear Value Functions Control Performance Table (- apply Piecewise Linear Value Functions Control Performance Table (- apply Piecewise Table Control Performance Table (- apply Piecewise Table Control Performance Table Control Performance Table (- apply Piecewise Table Control Performance Table Control Performance Table (- apply Piecewise Table Control Performance Table Control Performance Table (- apply Piecewise Table Control Performance Table Control Performance Table (- apply Piecewise Table Control Performance Table Control Performance Table (- apply Piecewise Table Control Performance Table Control Performance Table (- apply Piecewise Table Control Performance Table Control Performance Table (- apply Piecewise Table Control Performance Table Control Performance Table Control Performance Table (- apply Piecewise Table Control Performance Table Control Performance Table (- apply Piecewise Table 
              x$averageValueFunctionsPO,
              performanceTable)
# calculate the overall score of each alternative
weights <-c(1,1,1,1,1,1)
names(weights)<-colnames(performanceTable)</pre>
weightedSum(transformedPerformanceTable,c(1,1,1,1,1,1))
# Let us consider only 2 criteria : Price and MaximalSpeed. What happens ?
# x<-UTA(performanceTable, criteriaMinMax,</pre>
                        criteriaNumberOfBreakPoints, epsilon,
                        alternativesRanks = alternativesRanks,
                        criteriaLBs = criteriaLBs, criteriaUBs = criteriaUBs,
                        criteriaIDs = c("MaximalSpeed","Price"))
# plot the value functions obtained
# plotPiecewiseLinearValueFunctions(x$valueFunctions,
                                                                                         criteriaIDs = c("MaximalSpeed","Price"))
# apply the value functions on the original performance table
# transformedPerformanceTable <- applyPiecewiseLinearValueFunctionsOnPerformanceTable(</pre>
       x$valueFunctions,
         performanceTable,
         criteriaIDs = c("MaximalSpeed","Price")
# calculate the overall score of each alternative
# weights < -c(1,1,1,1,1,1)
# names(weights)<-colnames(performanceTable)</pre>
# weightedSum(transformedPerformanceTable,
                          weights, criteriaIDs = c("MaximalSpeed","Price"))
```

96 UTADIS

UTADIS

UTADIS method to elicit value functions in view of sorting alternatives in ordered categories

# Description

Elicits value functions from assignment examples, according to the UTADIS method.

### **Usage**

### **Arguments**

performanceTable

Matrix or data frame containing the performance table. Each row corresponds to an alternative, and each column to a criterion. Rows (resp. columns) must be named according to the IDs of the alternatives (resp. criteria).

criteriaMinMax

Vector containing the preference direction on each of the criteria. "min" (resp. "max") indicates that the criterion has to be minimized (maximized). The elements are named according to the IDs of the criteria.

criteriaNumberOfBreakPoints

Vector containing the number of breakpoints of the piecewise linear value functions to be determined. Minimum 2. The elements are named according to the IDs of the criteria.

UTADIS 97

alternativesAssignments

Vector containing the assignments of the alternatives to categories. Minimum 2 categories. The elements of the vector are named according to the IDs of the alternatives.

categoriesRanks

Vector containing the ranks of the categories. Minimum 2 categories. The elements of the vector are named according to the IDs of the categories.

epsilon Numeric value containing the minimal difference in value between the upper

bound of a category and an alternative of that category.

criteriaLBs Vector containing the lower bounds of the criteria to be considered for the elic-

itation of the value functions. If not specified, the lower bounds present in the

performance table are taken.

criteriaUBs Vector containing the upper bounds of the criteria to be considered for the elic-

itation of the value functions. If not specified, the upper bounds present in the

performance table are taken.

alternativesIDs

Vector containing IDs of alternatives, according to which the datashould be fil-

tered.

criteriaIDs Vector containing IDs of criteria, according to which the data should be filtered.

categoriesIDs Vector containing IDs of categories, according to which the data should be fil-

tered.

# Value

The function returns a list structured as follows:

optimum The value of the objective function.

valueFunctions A list containing the value functions which have been determined. Each value

function is defined by a matrix of breakpoints, where the first row corresponds to the abscissa (row labelled "x") and where the second row corresponds to the

ordinate (row labelled "y").

overall Values A vector of the overall values of the input alternatives.

categoriesLBs A vector containing the lower bounds of the considered categories.

errors A list containing the errors (sigmaPlus and sigmaMinus) which have to be sub-

stracted and added to the overall values of the alternatives in order to respect the

input ranking.

### References

J.M. Devaud, G. Groussaud, and E. Jacquet-Lagrèze, UTADIS: Une méthode de construction de fonctions d'utilité additives rendant compte de jugements globaux, European Working Group on Multicriteria Decision Aid, Bochum, 1980.

98 UTADIS

```
# the separation threshold
epsilon <-0.05
# the performance table
performanceTable <- rbind(</pre>
 c(3,10,1),
 c(4,20,2),
 c(2,20,0),
 c(6,40,0),
 c(30,30,3))
rownames(performanceTable) <- c("RER", "METRO1", "METRO2", "BUS", "TAXI")</pre>
colnames(performanceTable) <- c("Price", "Time", "Comfort")</pre>
# ranks of the alternatives
alternativesAssignments <- c("good", "medium", "medium", "bad", "bad")</pre>
names(alternativesAssignments) <- row.names(performanceTable)</pre>
# criteria to minimize or maximize
criteriaMinMax <- c("min", "min", "max")</pre>
names(criteriaMinMax) <- colnames(performanceTable)</pre>
# number of break points for each criterion
criteriaNumberOfBreakPoints <- c(3,4,4)</pre>
names(criteriaNumberOfBreakPoints) <- colnames(performanceTable)</pre>
# ranks of the categories
categoriesRanks \leftarrow c(1,2,3)
names(categoriesRanks) <- c("good", "medium", "bad")</pre>
x<-UTADIS(performanceTable, criteriaMinMax, criteriaNumberOfBreakPoints,
           alternativesAssignments, categoriesRanks,0.1)
# filtering out category "good" and assigment examples "RER" and "TAXI"
y<-UTADIS(performanceTable, criteriaMinMax, criteriaNumberOfBreakPoints,
           alternativesAssignments, categoriesRanks, 0.1,
           categoriesIDs=c("medium","bad"),
           alternativesIDs=c("METR01", "METR02", "BUS"))
```

UTASTAR

UTASTAR method to elicit value functions.

# **Description**

Elicits value functions from a ranking of alternatives, according to the UTASTAR method.

# Usage

```
UTASTAR(performanceTable, criteriaMinMax,
    criteriaNumberOfBreakPoints, epsilon,
    alternativesRanks = NULL,
    alternativesPreferences = NULL,
    alternativesIndifferences = NULL,
    criteriaLBs=NULL, criteriaUBs=NULL,
    alternativesIDs = NULL, criteriaIDs = NULL,
    kPostOptimality = NULL)
```

### Arguments

performanceTable

Matrix or data frame containing the performance table. Each row corresponds to an alternative, and each column to a criterion. Rows (resp. columns) must be named according to the IDs of the alternatives (resp. criteria).

criteriaMinMax

Vector containing the preference direction on each of the criteria. "min" (resp. "max") indicates that the criterion has to be minimized (maximized). The elements are named according to the IDs of the criteria.

criteriaNumberOfBreakPoints

Vector containing the number of breakpoints of the piecewise linear value functions to be determined. Minimum 2. The elements are named according to the IDs of the criteria.

epsilon

Numeric value containing the minimal difference in value between two consecutive alternatives in the final ranking.

alternativesRanks

Optional vector containing the ranks of the alternatives. The elements are named according to the IDs of the alternatives. If not present, then at least one of alternativesPreferences or alternativesIndifferences should be given.

alternativesPreferences

Optional matrix containing the preference constraints on the alternatives. Each line of the matrix corresponds to a constraint of the type alternative a is strictly preferred to alternative b. If not present, then either alternativesRanks or alternativesIndifferences should be given.

alternativesIndifferences

Optional matrix containing the indifference constraints on the alternatives. Each line of the matrix corresponds to a constraint of the type alternative a is indifferent to alternative b. If not present, then either alternativesRanks or alternativesPreferences should be given.

tivesPreferences should be given.

criteriaLBs Vector containing the lower bounds of the criteria to be considered for the elic-

itation of the value functions. If not specified, the lower bounds present in the

performance table are taken.

criteriaUBs Vector containing the upper bounds of the criteria to be considered for the elic-

itation of the value functions. If not specified, the upper bounds present in the

performance table are taken.

alternativesIDs

Vector containing IDs of alternatives, according to which the datashould be fil-

tered

 $\label{lem:criterialDs} \textbf{Vector containing IDs of criteria}, according to which the data should be filtered.}$ 

kPostOptimality

A small positive threshold used during the postoptimality analysis (see article on UTA by Siskos and Lagreze in EJOR, 1982). If not specified, no postoptimality analysis is performed.

### Value

The function returns a list structured as follows:

optimum The value of the objective function.

valueFunctions A list containing the value functions which have been determined. Each value

function is defined by a matrix of breakpoints, where the first row corresponds to the abscissa (row labelled "x") and where the second row corresponds to the

ordinate (row labelled "y").

overall values A vector of the overall values of the input alternatives.

ranks A vector of the ranks of the alternatives obtained via the elicited value functions.

Ties method = "min".

Kendall's tau between the input ranking and the one obtained via the elicited

value functions.

errors A list containing the errors (sigmaPlus and sigmaMinus) which have to be sub-

stracted and added to the overall values of the alternatives in order to respect the

input ranking.

 $\verb|minimumWeightsPO||$ 

In case a post-optimality analysis is performed, the minimal weight of each

criterion, else NULL.

maximumWeightsP0

In case a post-optimality analysis is performed, the maximal weight of each

criterion, else NULL.

averageValueFunctionsPO

In case a post-optimality analysis is performed, average value functions respect-

ing the input ranking, else NULL.

### References

Siskos, Y. and D. Yannacopoulos, UTASTAR: An ordinal regression method for building additive value functions, Investigação Operacional, 5 (1), 39–53, 1985.

```
# the separation threshold
epsilon <-0.05
# the performance table
performanceTable <- rbind(</pre>
   c(3,10,1),
c(4,20,2),
c(2,20,0),
c(6,40,0),
c(30,30,3))
rownames(performanceTable) <- c("RER", "METRO1", "METRO2", "BUS", "TAXI")</pre>
colnames(performanceTable) <- c("Price", "Time", "Comfort")</pre>
# ranks of the alternatives
alternativesRanks \leftarrow c(1,2,2,3,4)
names(alternativesRanks) <- row.names(performanceTable)</pre>
# criteria to minimize or maximize
criteriaMinMax <- c("min", "min", "max")</pre>
names(criteriaMinMax) <- colnames(performanceTable)</pre>
# number of break points for each criterion
criteriaNumberOfBreakPoints <- c(3,4,4)</pre>
names(criteriaNumberOfBreakPoints) <- colnames(performanceTable)</pre>
x<-UTASTAR(performanceTable, criteriaMinMax,
        criteriaNumberOfBreakPoints, epsilon,
        alternativesRanks = alternativesRanks)
# plot the value functions obtained
plotPiecewiseLinearValueFunctions(x$valueFunctions)
# apply the value functions on the original performance table
transformedPerformanceTable <- applyPiecewiseLinearValueFunctionsOnPerformanceTable(</pre>
```

```
x$valueFunctions,
  performanceTable)
# calculate the overall score of each alternative
weightedSum(transformedPerformanceTable,c(1,1,1))
# ranking some cars (from original article on UTA by Siskos and Lagreze, 1982)
# the separation threshold
epsilon <-0.01
# the performance table
performanceTable <- rbind(</pre>
c(173, 11.4, 10.01, 10, 7.88, 49500),
c(176, 12.3, 10.48, 11, 7.96, 46700),
c(142, 8.2, 7.30, 5, 5.65, 32100),
c(148, 10.5, 9.61, 7, 6.15, 39150),
c(178, 14.5, 11.05, 13, 8.06, 64700),
c(180, 13.6, 10.40, 13, 8.47, 75700),
c(182, 12.7, 12.26, 11, 7.81, 68593),
c(145, 14.3, 12.95, 11, 8.38, 55000),
c(161, 8.6, 8.42, 7, 5.11, 35200),
c(117, 7.2, 6.75, 3, 5.81, 24800)
rownames(performanceTable) <- c(</pre>
  "Peugeot 505 GR",
  "Opel Record 2000 LS",
  "Citroen Visa Super E",
  "VW Golf 1300 GLS",
  "Citroen CX 2400 Pallas",
  "Mercedes 230",
  "BMW 520",
  "Volvo 244 DL",
  "Peugeot 104 ZS",
  "Citroen Dyane")
colnames(performanceTable) <- c(</pre>
  "MaximalSpeed",
  "ConsumptionTown"
  "Consumption120kmh",
  "HP",
  "Space",
  "Price")
# ranks of the alternatives
alternativesRanks <-c(1,2,3,4,5,6,7,8,9,10)
```

```
names(alternativesRanks) <- row.names(performanceTable)</pre>
# criteria to minimize or maximize
criteriaMinMax <- c("max", "min", "min", "max", "max", "min")</pre>
names(criteriaMinMax) <- colnames(performanceTable)</pre>
# number of break points for each criterion
criteriaNumberOfBreakPoints <- c(5,4,4,5,4,5)</pre>
names(criteriaNumberOfBreakPoints) <- colnames(performanceTable)</pre>
# lower bounds of the criteria for the determination of value functions
criteriaLBs=c(110,7,6,3,5,20000)
names(criteriaLBs) <- colnames(performanceTable)</pre>
# upper bounds of the criteria for the determination of value functions
criteriaUBs=c(190,15,13,13,9,80000)
names(criteriaUBs) <- colnames(performanceTable)</pre>
x<-UTASTAR(performanceTable, criteriaMinMax,
        criteriaNumberOfBreakPoints, epsilon,
        alternativesRanks = alternativesRanks,
        criteriaLBs = criteriaLBs, criteriaUBs = criteriaUBs)
# plot the value functions obtained
plotPiecewiseLinearValueFunctions(x$valueFunctions)
# apply the value functions on the original performance table
transformedPerformanceTable <- applyPiecewiseLinearValueFunctionsOnPerformanceTable(</pre>
      x$valueFunctions,
      performanceTable)
# calculate the overall score of each alternative
weights <-c(1,1,1,1,1,1)
names(weights)<-colnames(performanceTable)</pre>
weightedSum(transformedPerformanceTable, c(1,1,1,1,1,1))
# the same analysis with less extreme value functions
# from the post-optimality analysis
```

```
x<-UTASTAR(performanceTable, criteriaMinMax,
        criteriaNumberOfBreakPoints, epsilon,
        alternativesRanks = alternativesRanks,
        criteriaLBs = criteriaLBs,
        criteriaUBs = criteriaUBs,
        kPostOptimality = 0.01)
# plot the value functions obtained
plotPiecewiseLinearValueFunctions(x$averageValueFunctionsP0)
# apply the value functions on the original performance table
transformedPerformanceTable <- applyPiecewiseLinearValueFunctionsOnPerformanceTable(</pre>
      x$averageValueFunctionsPO,
      performanceTable)
# calculate the overall score of each alternative
weights <-c(1,1,1,1,1,1)
names(weights)<-colnames(performanceTable)</pre>
weightedSum(transformedPerformanceTable,c(1,1,1,1,1,1))
# Let us consider only 2 criteria : Price and MaximalSpeed. What happens ?
x<-UTASTAR(performanceTable, criteriaMinMax,
        criteriaNumberOfBreakPoints, epsilon,
        alternativesRanks = alternativesRanks,
        criteriaLBs = criteriaLBs, criteriaUBs = criteriaUBs,
        criteriaIDs = c("MaximalSpeed", "Price"))
# plot the value functions obtained
plotPiecewiseLinearValueFunctions(x$valueFunctions,
                                  criteriaIDs = c("MaximalSpeed", "Price"))
# apply the value functions on the original performance table
transformedPerformanceTable <- applyPiecewiseLinearValueFunctionsOnPerformanceTable(</pre>
 x$valueFunctions,
 performanceTable,
 criteriaIDs = c("MaximalSpeed", "Price")
# calculate the overall score of each alternative
weights <-c(1,1,1,1,1,1)
```

weightedSum 105

weightedSum

Weighted sum of evaluations of alternatives.

### **Description**

Computes the weighted sum of the evaluations of alternatives, stored in a performance table, with respect to a vector of criteria weights.

### Usage

# Arguments

performanceTable

Matrix or data frame containing the performance table. Each row corresponds to an alternative, and each column to a criterion. Rows (resp. columns) must be named according to the IDs of the alternatives (resp. criteria).

criteriaWeights

Vector containing the weights of the criteria. The elements are named according to the IDs of the criteria.

alternativesIDs

Vector containing IDs of alternatives, according to which the performance table should be filtered.

criteriaIDs

Vector containing IDs of criteria, according to which the performance table should be filtered.

106 weightedSum

# Value

The function returns a vector containing the weighted sum of the alternatives with respect to the criteria weights.

# **Index**

```
* methods
                                                    SRMPInferenceNoInconsist. 79
    additiveValueFunctionElicitation,
                                                    SRMPInferenceNoInconsistFixedLexicographicOrder,
    apply Piecewise Linear Value Functions On Performan \textbf{SeMB} \textbf{bit} \textbf{e} \texttt{prenceNoInconsistFixedProfilesNumber},
                                                         83
                                                    UTA, 90
    assignAlternativesToCategoriesByThresholds,
                                                    UTADIS, 96
                                                    UTASTAR, 99
    LPDMRSort, 11
                                                    weightedSum, 105
    LPDMRSortIdentifyIncompatibleAssignments,
                                                additiveValueFunctionElicitation, 3
    LPDMRSortIdentifyUsedDictatorProfiles,
                                                AHP, 5
                                                applyPiecewiseLinearValueFunctionsOnPerformanceTable,
    LPDMRSortIdentifyUsedVetoProfiles,
                                                assignAlternativesToCategoriesByThresholds,
    LPDMRSortInferenceApprox, 24
    LPDMRSortInferenceExact, 27
    MRSort, 32
                                                ELECTREIIIDistillation, 10
    MRSortIdentifyIncompatibleAssignments,
                                                LPDMRSort, 11
    MRSortIdentifyUsedVetoProfiles, 37
                                                LPDMRSortIdentifyIncompatibleAssignments,
    MRSortInferenceApprox, 40
                                                LPDMRSortIdentifyUsedDictatorProfiles,
    MRSortInferenceExact, 42
    normalizePerformanceTable, 47
                                                LPDMRSortIdentifyUsedVetoProfiles, 21
    plotAlternativesValuesPreorder, 49
                                                LPDMRSortInferenceApprox, 24
    plotMRSortSortingProblem, 51
                                                LPDMRSortInferenceExact, 27
    plotPiecewiseLinearValueFunctions,
                                                MARE, 30
    plotRadarPerformanceTable, 54
                                                MRSort, 32
    SRMP, 64
                                                MRSortIdentifyIncompatibleAssignments,
    SRMPInference, 66
                                                         35
    SRMPInferenceApprox, 68
    SRMPInferenceApproxFixedLexicographicOrder MRSortInferenceApprox, 40
                                                MRSortIdentifyUsedVetoProfiles, 37
                                                MRSortInferenceExact, 42
    SRMPInferenceApproxFixedProfilesNumber,
                                                MRSortInterval, 44
    SRMPInferenceFixedLexicographicOrder,
                                                normalizePerformanceTable, 47
    SRMPInferenceFixedProfilesNumber,
                                                pairwiseConsistencyMeasures, 48
        77
                                                plotAlternativesValuesPreorder, 49
```

INDEX

```
plotMARE, 50
{\tt plotMRSortSortingProblem}, {\tt 51}
plotPiecewiseLinearValueFunctions, 53
plotRadarPerformanceTable, 54
plotSURE, 56
PROMETHEEI, 57
PROMETHEEII, 58
PROMETHEEOutrankingFlows, 60
PROMETHEEPreferenceIndices, 62
SRMP, 64
SRMPInference, 66
SRMPInferenceApprox, 68
{\tt SRMPInferenceApproxFixedLexicographicOrder},
        70
SRMPInferenceApproxFixedProfilesNumber,
{\tt SRMPInferenceFixedLexicographicOrder},
        74
SRMPInferenceFixedProfilesNumber, 77
SRMPInferenceNoInconsist, 79
{\tt SRMPInferenceNoInconsistFixedLexicographicOrder},
{\tt SRMPInferenceNoInconsistFixedProfilesNumber},
SURE, 85
TOPSIS, 88
UTA, 90
UTADIS, 96
UTASTAR, 99
weightedSum, 105
```