

# Package ‘MLEce’

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**Type** Package

**Title** Statistical Inference for Asymptotic Efficient Closed-Form Estimators

**Version** 1.0.1

**Description** Estimate asymptotic efficient closed-form estimators and provide goodness of fit, estimates, plot and etc.  
Yue, S. (2001) <[doi:10.1002/hyp.259](https://doi.org/10.1002/hyp.259)>.  
Mosimann, James E. (1962) <[doi:10.1093/biomet/49.1-2.65](https://doi.org/10.1093/biomet/49.1-2.65)>.

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**Author** Yu-Kwang Kim [aut, cre, com],  
Yu-Hyeong Jang [aut],  
Jae Ho Chang [aut],  
Sang Kyu Lee [aut],  
Jun Zhao [aut],  
Hyoung-Moon Kim [aut, ths]

**Maintainer** Yu-Kwang Kim <[lumiere\\_profuse@naver.com](mailto:lumiere_profuse@naver.com)>

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BiGam_CE	<i>Get closed-form estimator for Bivariate gamma</i>
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**Description**

Get closed-form estimator for Bivariate gamma

**Usage**

BiGam\_CE(pars, dat, type = "MLECE", log = TRUE)

**Arguments**

pars	parameters of bivariate gamma (alpha1, alpha2, beta).
dat	data of bivariate gamma
type	output type (MLECE, hessian, score). Default is MLECE
log	log-transformation of data. Default is TRUE

---

BiGam_MME	<i>MME for Bivariate gamma</i>
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**Description**

MME for Bivariate gamma

**Usage**

```
BiGam_MME(dat, scaletype = "first")
```

**Arguments**

dat	data of bivariate gamma
scaletype	scale type for bivariate gamma MME

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BiWei_CE	<i>Get root-n consistent closed-form estimator by correlation method and MLE.</i>
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**Description**

Get root-n consistent closed-form estimator by correlation method and MLE.

**Usage**

```
BiWei_CE(data)
```

**Arguments**

data	data of bivariate weibull
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BiWei_info	<i>Calculating MLEce for Bivariate weibull</i>
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**Description**

Calculating MLEce for Bivariate weibull

**Usage**

```
BiWei_info(par_vec, dat, type)
```

**Arguments**

par_vec	parameters of bivariate weibull (alpha1, beta1, alpha2, beta2, delta).
dat	data of bivariate weibull
type	output type (hessian, MLEce, del, mar)

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BiWei_ML	<i>Get MLE for Bivariate weibull</i>
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**Description**

Get MLE for Bivariate weibull

**Usage**

```
BiWei_ML(data, inits, tol = 1e-07)
```

**Arguments**

data	data of bivariate weibull
inits	initial values of iterative algorithm for MLE
tol	tolerance for difference.

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CD2	<i>CD2 statistics for GCVm gof test</i>
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**Description**

CD2 statistics for GCVm gof test

**Usage**

CD2(dat)

**Arguments**

dat                    data of bivariate weibull

---

coef.MLEce	<i>Extracting estimates. coef extracts estimated parameters.</i>
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---

**Description**

Extracting estimates. coef extracts estimated parameters.

**Usage**

```
## S3 method for class 'MLEce'
coef(object, digits = max(3, getOption("digits") - 3), ...)
```

```
## S3 method for class 'coef.MLEce'
print(x, digits = max(3, getOption("digits") - 3), ...)
```

**Arguments**

object                an object of class "MLEce" made by the function MLEce.  
 digits                a numeric number of significant digits.  
 ...                    not used, but exists because of the compatibility.  
 x                      an object of class "MLEce".

**Value**

estimated parameters are extracted from the "MLEce" class.

---

computeTime	<i>compute MLEce and MLE</i>
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**Description**

computeTime performs a benchmark of MLEce and MLE on a given dataset.

**Usage**

```
computeTime(data, distribution, coef_out = FALSE)
```

**Arguments**

data	a data set.
distribution	a character string of a distribution assuming that data set comes from.
coef_out	if TRUE, estimated parameters are printed. Default is False.

**Value**

a numeric matrix. This matrix include estimated parameters and time.

**Examples**

```
dat <- rBiWei(n=30, c(4,3,3,4,0.6))
computeTime(dat, "BiWei")
```

---

cor_method	<i>Get root-n consistent estimator by correlation method.</i>
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**Description**

Get root-n consistent estimator by correlation method.

**Usage**

```
cor_method(dat)
```

**Arguments**

dat	data of bivariate weibull
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dBiGam	<i>log-likelihood for Bivariate gamma</i>
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**Description**

log-likelihood for Bivariate gamma

**Usage**

```
dBiGam(pars, dat1, dat2, log = TRUE)
```

**Arguments**

pars	parameters of bivariate gamma (alpha1, alpha2, beta).
dat1	data of marginal column (univariate gamma).
dat2	other data of marginal column (univariate gamma).
log	log-transformation of data. Default is TRUE

---

dBiWei	<i>Evaluating bivariate Weibull distribution of Gumbel-type</i>
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---

**Description**

Evaluating bivariate Weibull distribution of Gumbel-type

**Usage**

```
dBiWei(par_vec, dat, log = TRUE)
```

**Arguments**

par_vec	parameters of bivariate weibull (alpha1, beta1, alpha2, beta2, delta).
dat	data of bivariate weibull
log	log-transformation for data. Default is TRUE.

---

delta\_score\_probit      *Calculating delta score*

---

### Description

Calculating delta score

### Usage

delta\_score\_probit(par\_vec, dat)

### Arguments

par\_vec                  parameters of bivariate weibull (alpha1, beta1, alpha2, beta2, delta).  
 dat                        data of bivariate weibull

---

Diri\_CE                    *Get MLEce for dirichlet*

---

### Description

Get MLEce for dirichlet

### Usage

Diri\_CE(x)

### Arguments

x                          data for estimating MLEce

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Diri\_CE\_bt                *beta tilde: root-n consistent estimator*

---

### Description

beta tilde: root-n consistent estimator

### Usage

Diri\_CE\_bt(x)

### Arguments

x                          data for estimating MLEce



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Diri_MLE	<i>Get MLE for dirichlet</i>
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**Description**

Get MLE for dirichlet

**Usage**

```
Diri_MLE(x, eps = 1e-10, mxit = 1e+05)
```

**Arguments**

x	data for estimating MLE
eps	epsilon for iterative algorithm.
mxit	maximum iteration for MLE. Default is 1e5

---

Diri_MME	<i>Get MME for dirichlet</i>
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**Description**

Get MME for dirichlet

**Usage**

```
Diri_MME(x)
```

**Arguments**

x	data for estimating MME.
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flood

*The flood events data of the Madawaska basin.*

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**Description**

It represents the flood events data of the Madawaska basin from 1911 to 1995. (Yue, 2001).

**Usage**

```
data(flood, package = "MLEce")
```

**Format**

A 2 variables data frame with 77 observations.

**References**

Yue, S. (2001). [doi:10.1002/hyp.259](https://doi.org/10.1002/hyp.259).

---

fossil\_pollen

*The counts data of the frequency of occurrence of different kinds of pollen grains.*

---

**Description**

It represents the counts data of the frequency of occurrence of different kinds of pollen grains. (Mosimann, 1962).

**Usage**

```
data(fossil_pollen, package = "MLEce")
```

**Format**

A 4 variables data frame with 73 observations.

**References**

Mosimann, James E. (1962) [doi:10.1093/biomet/49.1-2.65](https://doi.org/10.1093/biomet/49.1-2.65).

---

gof	<i>test goodness of fit</i>
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---

**Description**

test goodness of fit

**Usage**

```
gof(x, digits = max(3, getOption("digits") - 3), ...)  
  
## S3 method for class 'gof'  
print(x, digits = max(3, getOption("digits") - 3), ...)
```

**Arguments**

x	an object of class "MLEce" made by the function MLEce.
digits	a numeric number of significant digits.
...	not used, but exists because of the compatibility.

**Details**

The null hypothesis of the GCVm test is that "data follows the Bivariate Weibull distribution".

**Value**

gof returns the p-value of the GCVm test.

**Examples**

```
datt = rBiGam(100, c(1,4,5))  
res = MLEce(datt, "BiGam", boots = 50)  
gof(res)
```

---

llk	<i>Negative Log likelihood function for dirichlet data</i>
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---

**Description**

Negative Log likelihood function for dirichlet data

**Usage**

```
llk(x, alp)
```

**Arguments**

x	data for loglikelihood
alp	estimated values for the dirichlet parameters

MLEce

*Calculating a value of MLEce according to a distribution***Description**

Provide a function that numerically computes the closed-form estimator which is asymptotically efficient and can be computed faster than the maximum likelihood estimator.

**Usage**

```
MLEce(data, distrib, boots = 1000, CI.alpha = 0.05, ...)

## S3 method for class 'MLEce'
print(x, digits = max(3, getOption("digits") - 3), ...)
```

**Arguments**

data	a numeric vector or matrix.
distrib	a character string "name" naming a distribution for which the corresponding density function dname and the corresponding distribution function pname must be classically defined.
boots	a number of iteration for calculating CI-parametric intervals.
CI.alpha	a significance level of confidence intervals. default is 0.05.
...	not used, but exists because of the compatibility.
x	an object of class "MLEce".
digits	a numeric number of significant digits.

**Details**

The closed-form estimation procedure is based on root n-consistent estimators and a Fisher scoring step or a Newton step on the loglikelihood function. The estimator is obtained by solving the linear equation By E.L. Lehmann. This estimator follows the multivariate normal distribution with mean vector of 0 and variance matrix of inverse of Fisher Information matrix and has the properties of a multivariate normal distribution.

**Value**

an object of class “MLEce”. It is a list with the following components:

estimation	the parameter estimates.
distribution	a character string of a distribution assuming that data set comes from.
stat_summary	a numeric vector with min, 1st quantile, median, 3rd quantile, and max.
CI	a matrix with confidence intervals of Estimates obtained by CI-parametric bootstrapping.
n	a numeric value of data length.
data	the data set.

**Examples**

```
datt = rBiGam(100, c(1,4,5))
res = MLEce(datt, "BiGam", boots = 50)
```

---

MLEce\_est

*Estimate MLEce*


---

**Description**

Estimate MLEce

**Usage**

```
MLEce_est(data, distname, boots, CI.alpha)
```

**Arguments**

data	a numeric vector or matrix.
distname	a character string "name" naming a distribution for which the corresponding density function dname and the corresponding distribution function pname must be classically defined.
boots	a number of iteration for calculating CI-parametric intervals.
CI.alpha	a significance level of confidence intervals. default is 0.05.

---

MLE_est	<i>Statistical inference of MLE</i>
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**Description**

Provide value of maximum likelihood estimator, a result of GOF test, and information on the CI of MLE.

**Usage**

```
MLE_est(data, distname, inits, boots = 1000, CI.alpha = 0.05)
```

**Arguments**

data	a numeric vector or matrix.
distname	a character string of a distribution assuming that data set comes from (Currently, only Biweibull distribution can be input)
inits	a initial vector for MLE.
boots	a number of iteration for parametric bootstrapping compute confidence intervals.
CI.alpha	a significance level of confidence intervals. default is 0.05.

**Value**

MLE\_est returns a list include maximum likelihood estimators and confidence interval of estimated parameters.

---

plot.MLEce	<i>Providing some plots for MLEce</i>
------------	---------------------------------------

---

**Description**

plot method for a class "MLEce".

**Usage**

```
## S3 method for class 'MLEce'
plot(
  x,
  which = c(1, 2, 3, 4),
  ask = prod(par("mfcol")) < length(which) && dev.interactive(),
  ...
)
```

**Arguments**

x	an object of class "MLEce" made by the function MLEce.
which	if a subset of the plots is required, specify a subset of 1:4
ask	logical; if TRUE, the user is asked before each plot.
...	not used, but exists because of the compatibility.

**Details**

The first figure is a boxplot for given data. The second figure is a contour line drawn by the probability density function of the estimated parameter based on MLEce. the x-axis is the first column of data and the y-axis is the second column of data. The third figure is a marginally fitted probability density plot for the first column of input data. It provides a fitted line for each of CME, MLE and MLEce. The fourth figure is a marginally fitted probability density plot for the second column of input data. It can also provide a fitted line for each of CME, MLE and MLEce.

**Value**

returns plots for MLEce which describe "details".

**Examples**

```
datt = rBiGam(100, c(1,4,5))
res = MLEce(datt, "BiGam", boots = 50)
plot(res, c(1))
```

---

rBiGam	<i>random generation for the Bivariate Gamma distribution with (shape1, shape2, scale).</i>
--------	---

---

**Description**

random generation for the Bivariate Gamma distribution with (shape1, shape2, scale).

**Usage**

```
rBiGam(n, pars)
```

**Arguments**

n	number of observations.
pars	parameters of BiWeibull (shape1, shape2, scale).

**Details**

These functions implement formulas given in Hyoung-Moon Kim. et al. (2020). (will be revised.)

**Value**

rBiGam generates random deviates.

**Examples**

```
datt = rBiGam(n=50, c(4,3,3))
```

---

rBiWei	<i>Generating random number for the bivariate Weibull distribution with (alpha1, beta1, alpha2, beta2, delta).</i>
--------	--

---

**Description**

Generating random number for the bivariate Weibull distribution with (alpha1, beta1, alpha2, beta2, delta).

**Usage**

```
rBiWei(n, par_vec)
```

**Arguments**

n	number of observations.
par_vec	parameters of BiWeibull (alpha1, beta1, alpha2, beta2, delta).

**Details**

rBiWei generates random number data for bivariate weibull distribution.

**Value**

rBiWei generates random deviates.

**Examples**

```
datt = rBiWei(n=50, c(4,3,3,4,0.6))
```



---

RNCE_est	<i>Statistical inference of root-n consistent estimator</i>
----------	---

---

**Description**

Provide value of root-n consistent estimator

**Usage**

```
RNCE_est(data, distname)
```

**Arguments**

data	a numeric vector or matrix.
distname	a character string of a distribution assuming that data set

**Value**

a numeric vector of estimated parameters.

---

Rosen	<i>Rosen's transformation for GCVm gof test</i>
-------	---

---

**Description**

Rosen's transformation for GCVm gof test

**Usage**

```
Rosen(dat, pars)
```

**Arguments**

dat	data of bivariate weibull
pars	parameters of bivariate weibull (alpha1, beta1, alpha2, beta2, delta).

---

SD2fun.diri	<i>SD2 statistics for GCVM gof test</i>
-------------	---

---

**Description**

SD2 statistics for GCVM gof test

**Usage**

SD2fun.diri(Data, EST)

**Arguments**

Data	data for gof test
EST	estimates for gof test

---

SD2fun.gam	<i>SD2 statistics for GCVM gof test</i>
------------	---

---

**Description**

SD2 statistics for GCVM gof test

**Usage**

SD2fun.gam(Data, EST)

**Arguments**

Data	data for gof test
EST	estimates for gof test

---

stbz	<i>stabilization</i>
------	----------------------

---

**Description**

stabilization

**Usage**

stbz(x, eps = 1e-10)

**Arguments**

x	data for stabilization.
eps	epsilon for stabilization. It is very small number to extremely small data points

---

summary.MLEce	<i>Summarizing MLEce function</i>
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---

**Description**

summary method for a class "MLEce".

**Usage**

```
## S3 method for class 'MLEce'  
summary(object, ...)  
  
## S3 method for class 'summary.MLEce'  
print(x, digits = max(3, getOption("digits") - 3), ...)
```

**Arguments**

object	an object of class "MLEce" made by the function MLEce.
...	not used, but exists because of the compatibility.
x	an object of class "MLEce".
digits	a numeric number of significant digits.

**Value**

summary describes information about MLEce. (quantile statistics, correlation, estimates)

**Examples**

```
datt = rBiGam(100, c(1,4,5))  
res = MLEce(datt, "BiGam", boots = 50)  
summary(res)
```

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