

Package ‘MultiATSM’

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Type Package

Title Multicountry Term Structure of Interest Rates Models

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Description Estimation routines for several classes of affine term structure of interest rates models. All the models are based on the single-country unspanned macroeconomic risk framework from Joslin, Priebsch, and Singleton (2014) <doi:10.1111/jofi.12131>. Multicountry extensions such as the ones of Jotikasthira, Le, and Lundblad (2015) <doi:10.1016/j.jfineco.2014.09.004> and Candelon and Moura (2021) <<http://hdl.handle.net/2078.1/249985>> are also available.

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A0N_MLEdensity_WOE__jointQ_Bootstrap

Compute the maximum likelihood function (joint Q models) - Bootstrap version

Description

Compute the maximum likelihood function (joint Q models) - Bootstrap version

Usage

```

A0N_MLEdensity_WOE__jointQ_Bootstrap(
  K1XQ,
  r0,
  SSZ,
  K0Z,
  K1Z,
  se,
  Gy.0,
  mat,
  Y,
  Z,
  P,
  Wpca,
  We,
  WpcaFull,
  dt,
  Economies,
  FactorLabels,
  ModelType,
  residBS,
  MaxEigen,
  GVARinputs,
  JLLinputs,
  nargout
)

```

Arguments

| | |
|----------|---|
| K1XQ | risk-neutral feedback matrix (NxN) |
| r0 | long-run interest rate (scalar) |
| SSZ | variance-covariance matrix (KxK) |
| K0Z | intercept from the P-dynamics (Kx1) |
| K1Z | feedback matrix from the P-dynamics (KxK) |
| se | Variance of the portfolio of yields observed with error (scalar) |
| Gy.0 | matrix of contemporaneous terms from the P-dynamics (KxK) |
| mat | vector of maturities (in years) of yields used in estimation (J x 1) |
| Y | matrix of yields used in estimation (J x T) |
| Z | complete set of spanned and unspanned factors (KxT) |
| P | complete set of spanned factors (NxT) |
| Wpca | matrix of weights of the portfolios observed without errors (NxJ) |
| We | matrix of weights of the portfolios observed with errors ((J-N)xJ) |
| WpcaFull | composite matrix of weights the portfolios observed with and without errors |

| | |
|--------------|---|
| dt | time interval unit of the model (scalar). For instance, if data is (i) monthly, dt <- 12; (ii) quarterly, dt <- 4; (iii) yearly, dt <- 1. |
| Economies | a string-vector containing the names of the economies which are part of the economic system |
| FactorLabels | string-list based which contains the labels of all the variables present in the model |
| ModelType | feasible options are (i) "VAR jointQ", (ii) "GVAR jointQ" or (iii) "JLL jointSigma" |
| residBS | index of the re-ordered bootstrap residuals |
| MaxEigen | largest eigenvalue under the P-dynamics |
| GVARinputs | if the model chosen is the "GVAR sepQ", "GVARinputs" should be specified (see "GVAR" function) |
| JLLinputs | if the model chosen is the "JLL jointSigma". "JLLinputs" should be specified (see "JLL" function) |
| nargout | if nargout== 1: provides only the values of the likelihood; if nargout== 2: complete ATSM outputs |

References

This function is modified version of the "A0N_MLEdensity_WOE" function by Le and Singleton (2018).

"A Small Package of Matlab Routines for the Estimation of Some Term Structure Models." (Euro Area Business Cycle Network Training School - Term Structure Modelling). Available at: <https://cepr.org/40029>

A0N_MLEdensity_WOE__jointQ_sepSigma_Bootstrap

Compute the maximum likelihood function ("joint Q" models for separate Sigma estimation) - Bootstrap version

Description

Compute the maximum likelihood function ("joint Q" models for separate Sigma estimation) - Bootstrap version

Usage

```
A0N_MLEdensity_WOE__jointQ_sepSigma_Bootstrap(
    K1XQ,
    r0,
    SSZ,
    K0Z,
    K1Z,
    se,
    Gy.0,
    mat,
```

```

Y,
Z,
P,
Wpca,
We,
WpcaFull,
dt,
Economies,
FactorLabels,
ModelType,
residBS,
MaxEigen,
GVARinputs,
JLLinputs,
nargout
)

```

Arguments

| | |
|--------------|---|
| K1XQ | risk-neutral feedback matrix (NxN) |
| r0 | long-run interest rate (scalar) |
| SSZ | variance-covariance matrix (KxK) |
| K0Z | intercept from the P-dynamics (Kx1) |
| K1Z | feedback matrix from the P-dynamics (KxK) |
| se | Variance of the portfolio of yields observed with error (scalar) |
| Gy.0 | matrix of contemporaneous terms from the P-dynamics (KxK) |
| mat | vector of maturities (in years) of yields used in estimation (J x 1) |
| Y | matrix of yields used in estimation (J x T) |
| Z | complete set of spanned and unspanned factors (KxT) |
| P | complete set of spanned factors (NxT) |
| Wpca | matrix of weights of the portfolios observed without errors (NxJ) |
| We | matrix of weights of the portfolios observed with errors ((J-N)xJ) |
| WpcaFull | composite matrix of weights the portfolios observed with and without errors |
| dt | time interval unit of the model (scalar). For instance, if data is (i) monthly, dt <- 12; (ii) quarterly, dt <- 4; (iii) yearly, dt <- 1. |
| Economies | a string-vector containing the names of the economies which are part of the economic system |
| FactorLabels | string-list based which contains the labels of all the variables present in the model |
| ModelType | feasible options are (i) "JLL original" or (ii) "JLL NoDomUnit" |
| residBS | indexes of the re-ordered bootstrap residuals |
| MaxEigen | largest eigenvalue under the P-dynamics |

| | |
|------------|---|
| GVARinputs | if the model chosen is the "GVAR sepQ", "GVARinputs" must be specified (see "GVAR" function) |
| JLLinputs | if the model chosen is the "JLL jointSigma", "JLLinputs" must be specified (see "JLL" function) |
| nargout | if nargout== 1: provides only the values of the likelihood; if nargout== 2: complete ATSM outputs |

References

This function is modified version of the "A0N_MLEdensity_WOE" function by Le and Singleton (2018).

"A Small Package of Matlab Routines for the Estimation of Some Term Structure Models." (Euro Area Business Cycle Network Training School - Term Structure Modelling). Available at: <https://cepr.org/40029>

A0N_MLEdensity_WOE__sepQ_Bootstrap

Compute the maximum likelihood function ("sep Q" models) - Bootstrap version

Description

Compute the maximum likelihood function ("sep Q" models) - Bootstrap version

Usage

```
A0N_MLEdensity_WOE__sepQ_Bootstrap(
    K1XQ,
    r0,
    SSZ,
    K0Z,
    K1Z,
    se,
    Gy.0,
    mat,
    Y,
    Z,
    P,
    Wpca,
    We,
    WpcaFull,
    dt,
    Economy,
    FactorLabels,
    ModelType,
    residBS,
```



```

    MaxEigen,
    GVARinputs,
    nargout
)

```

Arguments

| | |
|--------------|---|
| K1XQ | risk-neutral feedback matrix (N×N) |
| r0 | long-run interest rate (scalar) |
| SSZ | variance-covariance matrix (K×K) |
| K0Z | intercept from the P-dynamics (K×1) |
| K1Z | feedback matrix from the P-dynamics (K×K) |
| se | Variance of the portfolio of yields observed with error (scalar) |
| Gy.0 | matrix of contemporaneous terms from the P-dynamics (K×K) |
| mat | vector of maturities (in years) of yields used in estimation (J x 1) |
| Y | matrix of yields used in estimation (J x T) |
| Z | complete set of spanned and unspanned factors (K×T) |
| P | complete set of spanned factors (N×T) |
| Wpca | matrix of weights of the portfolios observed without errors (N×J) |
| We | matrix of weights of the portfolios observed with errors ((J-N)×J) |
| WpcaFull | composite matrix of weights the portfolios observed with and without errors |
| dt | time interval unit of the model (scalar). For instance, if data is (i) monthly, dt <- 12; (ii) quarterly, dt <- 4; (iii) yearly, dt <- 1. |
| Economy | Name of the economies under study |
| FactorLabels | string-list based which contains the labels of all the variables present in the model |
| ModelType | Feasible options are: (i) "JPS", (ii) "JPS jointP" or (iii) "GVAR sepQ" |
| residBS | index of the re-ordered bootstrap residuals |
| MaxEigen | largest eigenvalue under the P-dynamics |
| GVARinputs | if the model chosen is the "GVAR sepQ", "GVARinputs" should be specified (see "GVAR" function) |
| nargout | if nargout== 1: provides only the values of the likelihood; if nargout== 2: complete ATSM outputs |

References

This function is modified version of the "A0N_MLEdensity_WOE" function by Le and Singleton (2018).

"A Small Package of Matlab Routines for the Estimation of Some Term Structure Models." (Euro Area Business Cycle Network Training School - Term Structure Modelling). Available at: <https://cepr.org/40029>

A0N__computeBnAn_jointQ

Compute the cross-section loadings of yields of a canonical A0_N model ("joint Q" models)

Description

Compute the cross-section loadings of yields of a canonical A0_N model ("joint Q" models)

Usage

A0N__computeBnAn_jointQ(mat, K1XQ, dx, r0, SSX, Economies)

Arguments

| | |
|-----------|--|
| mat | vector of maturities (J x 1). Maturities are in multiples of the discrete interval used in the model |
| K1XQ | risk neutral feedback matrix (N x N) |
| dx | state loadings for the one-period rate (1xN). Default is a vector of ones |
| r0 | the long run risk neutral mean of the short rate (scalar) |
| SSX | the covariance matrix of the errors (N x N) |
| Economies | Set of economies that are part of the economic system (vector of text) |

Value

List containing:

- Intercept (Jx1)
- slope (JxN)
- the betan (JX1, part of the intercepts unrelated to the long run risk neutral mean r0) coefficients of a canonical A_0(N).

References

This function is an extended version of the "A0N__computeBnAn" function by Le and Singleton (2018).

"A Small Package of Matlab Routines for the Estimation of Some Term Structure Models." (Euro Area Business Cycle Network Training School - Term Structure Modelling). Available at: <https://cepr.org/40029>

A0N__computeBnAn_sepQ *Compute the cross-section loadings of yields of a canonical A0_N model ("sep Q" models)*

Description

Compute the cross-section loadings of yields of a canonical A0_N model ("sep Q" models)

Usage

A0N__computeBnAn_sepQ(mat, K1XQ, dx, r0, SSX)

Arguments

| | |
|------|--|
| mat | vector of maturities (J x 1). Maturities are in multiples of the discrete interval used in the model |
| K1XQ | risk neutral feedback matrix (N x N) |
| dx | state loadings for the one-period rate (1xN). Default is a vector of ones |
| r0 | the long run risk neutral mean of the short rate (scalar) |
| SSX | the covariance matrix of the errors (N x N) |

Value

List containing:

- Intercept (Jx1)
- slope (JxN)
- the betan (JX1, part of the intercepts unrelated to the long run risk neutral mean r0) coefficients of a canonical A_0(N).

References

- This function is based on the "A0N__computeBnAn" function by Le and Singleton (2018). "A Small Package of Matlab Routines for the Estimation of Some Term Structure Models." (Euro Area Business Cycle Network Training School - Term Structure Modelling). Available at: <https://cepr.org/40029>
- Dai and Singleton (2000). "Specification Analysis of Affine Term Structure Models" (The Journal of Finance)

| | |
|----------|---|
| aux2true | <i>Map auxiliary (unconstrained) parameters a to constrained parameters b</i> |
|----------|---|

Description

Map auxiliary (unconstrained) parameters a to constrained parameters b

Usage

```
aux2true(
  a,
  ctype,
  lb,
  ub,
  FactorLabels,
  Economies,
  JLLinputs = NULL,
  GVARinputs = NULL,
  nargout
)
```

Arguments

| | |
|--------------|--|
| a | unconstrained auxiliary parameter |
| ctype | One of the following options: <ul style="list-style-type: none"> • 'Jordan' • 'Jordan; stationary' • 'Jordan MultiCountry' • 'Jordan MultiCountry; stationary' • 'psd'; • 'BlockDiag' • 'bounded' • 'diag' • 'JLLstructure' |
| lb | lower bounds of b (if option 'bounded' is chosen) |
| ub | upper bounds of b (if option 'bounded' is chosen) |
| FactorLabels | string-list based which contains the labels of all the variables present in the model |
| Economies | string-vector containing the names of the economies which are part of the economic system |
| JLLinputs | Inputs used in the estimation of the JLL-based models |
| GVARinputs | Inputs used in the estimation of the GVAR-based models |
| nargout | "nargout <- 1" returns a constrained scalar or matrix "nargout <- 2" returns a list of parameters |

References

This function is a modified version of the "aux2true" function by Le and Singleton (2018).
 "A Small Package of Matlab Routines for the Estimation of Some Term Structure Models."
 (Euro Area Business Cycle Network Training School - Term Structure Modelling). Available at:
<https://cepr.org/40029>

| | |
|-----------|--|
| Bootstrap | <i>Generates the bootstrap-related outputs</i> |
|-----------|--|

Description

Generates the bootstrap-related outputs

Usage

```
Bootstrap(
    ModelType,
    ModelParaPE,
    NumOutPE,
    mat,
    Economies,
    InputsForOutputs,
    FactorLabels,
    DataFrequency,
    vararginPE,
    JLLinputs = NULL,
    GVARinputs = NULL
)
```

Arguments

| | |
|------------------|--|
| ModelType | string-vector containing the label of the model to be estimated |
| ModelParaPE | point estimate from the model parameters (see the outputs of the "Optimization" function) |
| NumOutPE | point estimate from the numerical outputs (see the outputs of the "NumOutputs" function) |
| mat | vector of maturities (in years) used in the estimation |
| Economies | string-vector containing the names of the economies which are part of the economic system |
| InputsForOutputs | list containing the desired inputs for the construction of IRFs, GIRFs, FEVDs, and GFEVDs. |
| FactorLabels | string-list based which contains the labels of all the variables present in the model |

| | |
|---------------|---|
| DataFrequency | character-based vector: "Daily All Days", "Daily Business Days", "Weekly", "Monthly", "Quarterly", "Annually" |
| vararginPE | list containing starting values and constraints (see arguments of the "Optimization" function) |
| JLLinputs | list of necessary inputs for the estimation of JLL-based models (see "JLL" function) |
| GVARinputs | list of necessary inputs for the estimation of GVAR-based models (see "GVAR" function) |

Value

list containing the following elements:

- list of model parameters for one each one the draws;
- list of numerical outputs (IRFs, GIRFs, FEVDs, GFEVDs) for each one of the draws;
- Confidence bands for the chosen level of significance.

References

This function is a modified and extended version of the "VARirbound" function from "A toolbox for VAR analysis" by Ambrogio Cesa-Bianchi (<https://github.com/ambropo/VAR-Toolbox>)

Examples

See examples in the vignette file of this package (Section 4).

BootstrapBoundsSet *Builds the confidence bounds and graphs (Bootstrap set)*

Description

Builds the confidence bounds and graphs (Bootstrap set)

Usage

```
BootstrapBoundsSet(
  ModelType,
  ModelBootstrap,
  NumOutPE,
  InputsForOutputs,
  Economies
)
```

Arguments

| | |
|------------------|---|
| ModelType | string-vector containing the label of the model to be estimated |
| ModelBootstrap | list containing the complete set of model parameters after the bootstrap estimation procedure |
| NumOutPE | point estimate from the numerical outputs (see the outputs of the "NumOutputs" function) |
| InputsForOutputs | list containing the desired inputs for the construction of IRFs, GIRFs, FEVDs, and GFEVDs |
| Economies | string-vector containing the names of the economies which are part of the economic system |

| | |
|---------|--|
| bound2x | <i>Transform a number bounded between a lower bound and upper bound to x by:</i> |
|---------|--|

Description

Transform a number bounded between a lower bound and upper bound to x by:

Usage

bound2x(y, lb, ub)

Arguments

| | |
|----|-----------------------------------|
| y | Number to be transformed (scalar) |
| lb | lower bound (scalar) |
| ub | upper bound (scalar) |

References

This function is based on the "bound2x" function by Le and Singleton (2018).
 "A Small Package of Matlab Routines for the Estimation of Some Term Structure Models."
 (Euro Area Business Cycle Network Training School - Term Structure Modelling). Available at:
<https://cepr.org/40029>

| | |
|------------|---|
| BR_jps_out | <i>Replications of the JPS (2014) outputs by Bauer and Rudebusch (2017)</i> |
|------------|---|

Description

Unspanned macro risk model outputs by Bauer and Rudebusch (2017)

Usage

```
data("BR_jps_gro_R3")
```

Format

Unspanned macro risk model outputs by Bauer and Rudebusch (2017)

est.llk summary list of log-likelihood estimations

M.o time series of unspanned factors

pars additional summary list of log-likelihood estimations

W Weight matrix that results from principal components analysis

Y time series of bond yields

N total number of risk factor of the model (spanned and unspanned)

R total number of spanned factor of the model

References

Bauer, M. and Rudebusch, G. "Resolving the Spanning Puzzle in Macro-Finance Term Structure Models"

| | |
|---------------------|---|
| BUnspannedAdapJoint | <i>Transform B_spanned into B_unspanned for jointQ models</i> |
|---------------------|---|

Description

Transform B_spanned into B_unspanned for jointQ models

Usage

```
BUnspannedAdapJoint(G, M, N, C, J, BSpanned)
```


Arguments

| | |
|----------|---|
| G | number of global unspanned factors |
| M | number of domestic unspanned factors |
| N | number of domestic spanned factors |
| C | number of economies of the economic system |
| J | number of country-specific observed bond yields |
| BSpanded | B that accomodates only the map to the spanned factors only |

| | |
|-------------------|---|
| BUnspannedAdapSep | <i>Transform B_spanded into B_unspanned for sepQ models</i> |
|-------------------|---|

Description

Transform B_spanded into B_unspanned for sepQ models

Usage

BUnspannedAdapSep(G, M, ModelPara, Economies, Economy, ModelType)

Arguments

| | |
|-----------|---|
| G | number of global unspanned factors |
| M | number of domestic unspanned factors per country |
| ModelPara | list of model parameter estimates (See the "Optimization" function) |
| Economies | complet set of economies of the economic system |
| Economy | specific economy under study |
| ModelType | a string-vector containing the label of the model to be estimated |

| | |
|----------------------|--|
| BUnspannedAdapSep_BS | <i>Obtain the full form of B unspanned for "sep Q" models within the bootstrap setting</i> |
|----------------------|--|

Description

Obtain the full form of B unspanned for "sep Q" models within the bootstrap setting

Usage

BUnspannedAdapSep_BS(G, M, ModelParaBoot, Economies, Economy, ModelType, tt)

Arguments

| | |
|---------------|--|
| G | number of global unspanned factors |
| M | number of country-specific domestic unspanned factors |
| ModelParaBoot | list of model parameter estimates (see the "Optimization" function) after a bootstrap draw |
| Economies | string-vector containing the names of the economies which are part of the economic system |
| Economy | string-vector containing the names of the economy under study |
| ModelType | string-vector containing the label of the model to be estimated |
| tt | number of the bootstrap draw |

 contain

Check whether one element is a subset of another element

Description

Check whether one element is a subset of another element

Usage

```
contain(s1, s2)
```

Arguments

| | |
|----|----------------|
| s1 | smaller subset |
| s2 | complete set |

References

This function is based on the "contain" function by Le and Singleton (2018).
 "A Small Package of Matlab Routines for the Estimation of Some Term Structure Models."
 (Euro Area Business Cycle Network Training School - Term Structure Modelling). Available at:
<https://cepr.org/40029>

DatabasePrep

Prepare the GVARFactors database

Description

Prepare the GVARFactors database

Usage

```
DatabasePrep(
  t_First,
  t_Last,
  Economies,
  N,
  FactorLabels,
  ModelType,
  Wgvar = NULL,
  DataPathMacro = NULL,
  DataPathYields = NULL
)
```

Arguments

| | |
|----------------|--|
| t_First | sample starting date (yyyy-mm-dd) |
| t_Last | sample last date (yyyy-mm-dd) |
| Economies | string-vector containing the names of the economies which are part of the economic system |
| N | number of country-specific spanned factor (scalar) |
| FactorLabels | list containing the factor labels |
| ModelType | string-vector containing the label of the model to be estimated |
| Wgvar | GVAR transition matrix (Cx C), if GVAR type model is chosen; default is set to NULL. |
| DataPathMacro | path of the Excel file containing the macroeconomic data (if any). The default is linked to the Excel file available in the package. |
| DataPathYields | path of the Excel file containing the yields data (if any). The default is linked to the Excel file available in the package. |

Value

List of the risk factor set used in the estimation of the GVAR model

List containing the risk factor set used in the estimation of the GVAR-based models

Examples

```

DomVar <- c("Eco_Act", "Inflation")
GlobalVar <- c("GBC", "CPI_OECD")
t0 <- "2006-09-01"
tF <- "2019-01-01"
Economies <- c("China", "Brazil", "Mexico", "Uruguay", "Russia")
N <- 3
ModelType <- "JPS jointQ"
FactorLabels <- LabFac(N, DomVar, GlobalVar, Economies, ModelType)

GVARFactors <- DatabasePrep(t0, tF, Economies, N, FactorLabels, ModelType)

```

| | |
|-------------------|---|
| DataForEstimation | <i>Retrieve data from Excel and build the database used in the model estimation</i> |
|-------------------|---|

Description

Retrieve data from Excel and build the database used in the model estimation

Usage

```

DataForEstimation(
  t0,
  tF,
  Economies,
  N,
  FactorLabels,
  ModelType,
  DataFrequency,
  DataPathMacro = NULL,
  DataPathYields = NULL,
  Wgvar = NULL
)

```

Arguments

| | |
|--------------|---|
| t0 | Sample starting date (yyyy-mm-dd) |
| tF | Sample last date (yyyy-mm-dd) |
| Economies | string-vector containing the names of the economies which are part of the economic system |
| N | Number of country-specific spanned factor (scalar) |
| FactorLabels | String-list based which contains the labels of all the variables present in the model |

| | |
|----------------|--|
| ModelType | String-vector containing the label of the model to be estimated |
| DataFrequency | Character-based-vector. Available options are: "Daily All Days", "Daily Business Days", "Weekly", "Monthly", "Quarterly", "Annually" |
| DataPathMacro | Path of the Excel file conating the macroeconomic data (if any). The default is linked to the excel file present in the package. |
| DataPathYields | Path of the Excel file conating the yields data (if any). The default is linked to the excel file present in the package. |
| Wgvar | GVAR transition matrix, if GVAR type model is chosen; default is set to NULL. |

Value

A list containing the

1. time series of the complete set of bond yields (matrix, JxT or CJxT);
2. time series of the complete set risk factors (matrix, KxT);
3. 'GVARFactors': list of all variables that are used in the estimation of the VARX (see e.g. 'CM_Factors_GVAR' file). If the estimated model type is not GVAR-based, then returns NULL.

Examples

```
DomVar <- c("Eco_Act", "Inflation")
GlobalVar <- c("GBC", "CPI_OECD")
t0 <- "2006-09-01"
tF <- "2019-01-01"
Economies <- c("China", "Brazil", "Mexico", "Uruguay", "Russia")
N <- 2
ModelType <- "JPS"
FactorLabels <- LabFac(N, DomVar, GlobalVar, Economies, ModelType)
DataFrequency <- "Monthly"

DataModel <- DataForEstimation(t0, tF, Economies, N, FactorLabels, ModelType, DataFrequency)
```

DataSet_BS

Prepare the factor set for GVAR models (Bootstrap version)

Description

Prepare the factor set for GVAR models (Bootstrap version)

Usage

```
DataSet_BS(ModelType, RiskFactors, Wgvar, Economies, FactorLabels)
```

Arguments

| | |
|--------------|---|
| ModelType | string-vector containing the label of the model to be estimated |
| RiskFactors | Complete set of risk factors (KxT) |
| Wgvar | transition matrix from GVAR models (CxC) |
| Economies | string-vector containing the names of the economies which are part of the economic system |
| FactorLabels | string-list based which contains the labels of all the variables present in the model |

| | |
|--------|--|
| df__dx | <i>Computes numerical first order derivative of f(x)</i> |
|--------|--|

Description

Computes numerical first order derivative of f(x)

Usage

df__dx(f, x)

Arguments

| | |
|---|---|
| f | function which contains vector (J x T) valued function handle |
| x | parameter values |

Value

transformed matrix (MN x JT)

References

This function is based on the "df__dx" function by Le and Singleton (2018).
 "A Small Package of Matlab Routines for the Estimation of Some Term Structure Models."
 (Euro Area Business Cycle Network Training School - Term Structure Modelling). Available at:
<https://cepr.org/40029>

FactorsGVAR

Data: Risk Factors for the GVAR - Candelon and Moura (2021)

Description

Risk factors data used in the GVAR models - Candelon and Moura (2021)

Usage

```
data("CM_Factors_GVAR")
```

Format

list containing the variables used in the GVAR models

References

Candelon, B. and Moura, R. "A Multi-Country Model of the Term Structures of Interest Rates with a GVAR".

FEVDandGFEVDbs_jointQ *Creates the confidence bounds and the graphs of FEVDs and GFEVDs after bootstrap ("joint Q" models)*

Description

Creates the confidence bounds and the graphs of FEVDs and GFEVDs after bootstrap ("joint Q" models)

Usage

```
FEVDandGFEVDbs_jointQ(  
  ModelType,  
  ModelBootstrap,  
  NumOutPE,  
  InputsForOutputs,  
  Economies,  
  PathsGraphs  
)
```

Arguments

| | |
|------------------|---|
| ModelType | string-vector containing the label of the model to be estimated |
| ModelBootstrap | list containing the complete set of model parameters after bootstrap estimation procedure |
| NumOutPE | list of model parameter point estimates |
| InputsForOutputs | list containing the desired inputs for the construction of the outputs of interest |
| Economies | string-vector containing the names of the economies which are part of the economic system |
| PathsGraphs | path of the folder in which the graphs will be saved |

FEVDandGFEVDbs_jointQ_Ortho

Creates the confidence bounds and the graphs of FEVDs and GFEVDs after bootstrap (JLL-based models)

Description

Creates the confidence bounds and the graphs of FEVDs and GFEVDs after bootstrap (JLL-based models)

Usage

```
FEVDandGFEVDbs_jointQ_Ortho(
  ModelType,
  ModelBootstrap,
  NumOutPE,
  InputsForOutputs,
  Economies,
  PathsGraphs
)
```

Arguments

| | |
|------------------|---|
| ModelType | string-vector containing the label of the model to be estimated |
| ModelBootstrap | list containing the complete set of model parameters after bootstrap estimation procedure |
| NumOutPE | list of model parameter point estimates |
| InputsForOutputs | list containing the desired inputs for the construction of the outputs of interest |
| Economies | a string-vector containing the names of the economies which are part of the economic system |
| PathsGraphs | path of the folder in which the graphs will be saved |

| | |
|---------------------|--|
| FEVDandGFEVDbs_sepQ | <i>Creates the confidence bounds and the graphs of FEVDs and GFEVDs after bootstrap ("sep Q" models)</i> |
|---------------------|--|

Description

Creates the confidence bounds and the graphs of FEVDs and GFEVDs after bootstrap ("sep Q" models)

Usage

```
FEVDandGFEVDbs_sepQ(  
  ModelType,  
  ModelBootstrap,  
  NumOutPE,  
  InputsForOutputs,  
  Economies,  
  PathsGraphs  
)
```

Arguments

| | |
|------------------|---|
| ModelType | string-vector containing the label of the model to be estimated |
| ModelBootstrap | list containing the complete set of model parameters after bootstrap estimation procedure |
| NumOutPE | list of model parameter point estimates |
| InputsForOutputs | list containing the desired inputs for the construction of the outputs of interest |
| Economies | string-vector containing the names of the economies which are part of the economic system |
| PathsGraphs | path of the folder in which the graphs will be saved |

| | |
|--------------------|---|
| FEVDgraphsJLLOrtho | <i>FEVDs graphs for orthogonalized risk factors of JLL-based models</i> |
|--------------------|---|

Description

FEVDs graphs for orthogonalized risk factors of JLL-based models

Usage

```
FEVDgraphsJLLOrtho(
  ModelType,
  NumOut,
  WishPdynamicgraphs,
  WishYieldsgraphs,
  FEVDhoriz,
  PathsGraphs
)
```

Arguments

| | |
|--------------------|--|
| ModelType | a string-vector containing the label of the model to be estimated |
| NumOut | list of computed outputs containing the model fit, IRFs, FEVDs, GIRFs, and GFEVDs |
| WishPdynamicgraphs | binary variable: set 1, if the user wishes graphs to be generated; or set 0, otherwise |
| WishYieldsgraphs | binary variable: set 1, if the user wishes graphs to be generated; or set 0, otherwise |
| FEVDhoriz | single numerical vector containing the desired horizon of analysis for the FEVDs |
| PathsGraphs | Path of the folder in which the graphs will be saved |

| | |
|-----------------|--|
| FEVDgraphsJoint | <i>FEVDs graphs for ("joint Q" models)</i> |
|-----------------|--|

Description

FEVDs graphs for ("joint Q" models)

Usage

```
FEVDgraphsJoint(
  ModelType,
  NumOut,
  WishPdynamicgraphs,
  WishYieldsgraphs,
  FEVDhoriz,
  PathsGraphs
)
```

Arguments

| | |
|--------------------|--|
| ModelType | a string-vector containing the label of the model to be estimated |
| NumOut | list of computed outputs containing the model fit, IRFs, FEVDs, GIRFs, and GFEVDs |
| WishPdynamicgraphs | binary variable: set 1, if the user wishes graphs to be generated; or set 0, otherwise |
| WishYieldgraphs | binary variable: set 1, if the user wishes graphs to be generated; or set 0, otherwise |
| FEVDhoriz | single numerical vector containing the desired horizon of analysis for the FEVDs |
| PathsGraphs | Path of the folder in which the graphs will be saved |

| | |
|---------------|--|
| FEVDgraphsSep | <i>FEVDs graphs for ("sep Q" models)</i> |
|---------------|--|

Description

FEVDs graphs for ("sep Q" models)

Usage

```
FEVDgraphsSep(
  ModelType,
  NumOut,
  WishPdynamicgraphs,
  WishYieldgraphs,
  FEVDhoriz,
  PathsGraphs,
  Economies
)
```

Arguments

| | |
|--------------------|---|
| ModelType | a string-vector containing the label of the model to be estimated |
| NumOut | list of computed outputs containing the model fit, IRFs, FEVDs, GIRFs, and GFEVDs |
| WishPdynamicgraphs | binary variable: set 1, if the user wishes graphs to be generated; or set 0, otherwise |
| WishYieldgraphs | binary variable: set 1, if the user wishes graphs to be generated; or set 0, otherwise |
| FEVDhoriz | single numerical vector containing the desired horizon of analysis for the FEVDs |
| PathsGraphs | Path of the folder in which the graphs will be saved |
| Economies | a string-vector containing the names of the economies which are part of the economic system |

| | |
|-----------|-----------------------------------|
| FEVDjoint | <i>FEVDs for "joint Q" models</i> |
|-----------|-----------------------------------|

Description

FEVDs for "joint Q" models

Usage

FEVDjoint(ModelType, ModelPara, FEVDhoriz, FactorLabels, Economies)

Arguments

| | |
|--------------|---|
| ModelType | string-vector containing the label of the model to be estimated |
| ModelPara | list of model parameter estimates (see the "Optimization" function) |
| FEVDhoriz | single numerical vector conataining the desired horizon of analysis for the FEVDs |
| FactorLabels | string-list based which contains all the labels of all the variables present in the model |
| Economies | string-vector containing the names of the economies which are part of the economic system |

Details

Structural shocks are identified via Cholesky decomposition

| | |
|---------------------|--|
| FEVDjointOrthogoJLL | <i>Orthogonalized FEVDs for JLL models</i> |
|---------------------|--|

Description

Orthogonalized FEVDs for JLL models

Usage

FEVDjointOrthogoJLL(ModelType, ModelPara, FEVDhoriz, FactorLabels, Economies)

Arguments

| | |
|--------------|---|
| ModelType | string-vector containing the label of the model to be estimated |
| ModelPara | list of model parameter estimates (see the "Optimization" function) |
| FEVDhoriz | single numerical vector conataining the desired horizon of analysis for the FEVDs |
| FactorLabels | string-list based which contains all the labels of all the variables present in the model |
| Economies | a string-vector containing the names of the economies which are part of the economic system |

Details

Structural shocks are identified via Cholesky decomposition

FEVDjointOrthogoJLL_BS

FEVDs after bootstrap for JLL-based models

Description

FEVDs after bootstrap for JLL-based models

Usage

```
FEVDjointOrthogoJLL_BS(  
  ModelType,  
  ModelParaBoot,  
  FEVDhoriz,  
  FactorLabels,  
  Economies  
)
```

Arguments

| | |
|---------------|--|
| ModelType | string-vector containing the label of the model to be estimated |
| ModelParaBoot | list of model parameter estimates (see the "Optimization" function) after a bootstrap draw |
| FEVDhoriz | single numerical vector containing the desired horizon of analysis for the FEVDs |
| FactorLabels | string-list based which contains all the labels of all the variables present in the model |
| Economies | string-vector containing the names of the economies which are part of the economic system |

FEVDjoint_BS

FEVDs after bootstrap for "joint Q" models

Description

FEVDs after bootstrap for "joint Q" models

Usage

```
FEVDjoint_BS(ModelType, ModelParaBoot, FEVDhoriz, FactorLabels, Economies)
```

Arguments

| | |
|---------------|--|
| ModelType | string-vector containing the label of the model to be estimated |
| ModelParaBoot | list of model parameter estimates (see the "Optimization" function) after a bootstrap draw |
| FEVDhoriz | single numerical vector containing the desired horizon of analysis for the FEVDs |
| FactorLabels | string-list based which contains all the labels of all the variables present in the model |
| Economies | string-vector containing the names of the economies which are part of the economic system |

FEVDsep

FEVDs for "sep Q" models

Description

FEVDs for "sep Q" models

Usage

```
FEVDsep(ModelType, ModelPara, FEVDhoriz, FactorLabels, Economies)
```

Arguments

| | |
|--------------|---|
| ModelType | string-vector containing the label of the model to be estimated |
| ModelPara | list of model parameter estimates (see the "Optimization" function) |
| FEVDhoriz | single numerical vector containing the desired horizon of analysis for the FEVDs |
| FactorLabels | string-list based which contains all the labels of all the variables present in the model |
| Economies | string-vector containing the names of the economies which are part of the economic system |

Details

Structural shocks are identified via Cholesky decomposition

| | |
|------------|---|
| FEVDsep_BS | <i>FEVDs after bootstrap for "sep Q" models</i> |
|------------|---|

Description

FEVDs after bootstrap for "sep Q" models

Usage

```
FEVDsep_BS(ModelType, ModelParaBoot, FEVDhoriz, FactorLabels, Economies)
```

Arguments

| | |
|---------------|--|
| ModelType | string-vector containing the label of the model to be estimated |
| ModelParaBoot | list of model parameter estimates (see the "Optimization" function) after a bootstrap draw |
| FEVDhoriz | single numerical vector containing the desired horizon of analysis for the FEVDs |
| FactorLabels | string-list based which contains all the labels of all the variables present in the model |
| Economies | string-vector containing the names of the economies which are part of the economic system |

| | |
|----------------|--|
| FitgraphsJoint | <i>Model fit graphs for ("joint Q" models)</i> |
|----------------|--|

Description

Model fit graphs for ("joint Q" models)

Usage

```
FitgraphsJoint(
  ModelType,
  WishFitgraphs,
  ModelPara,
  NumOut,
  Economies,
  PathsGraphs
)
```

Arguments

| | |
|---------------|---|
| ModelType | a string-vector containing the label of the model to be estimated |
| WishFitgraphs | binary variable: set 1, if the user wishes graphs to be generated; or set 0, otherwise |
| ModelPara | List of model parameter estimates (See the "Optimization" function) |
| NumOut | list of computed outputs containing the model fit, IRFs, FEVDs, GIRFs, and GFEVDs |
| Economies | a string-vector containing the names of the economies which are part of the economic system |
| PathsGraphs | Path of the folder in which the graphs will be saved |

| | |
|--------------|--|
| FitgraphsSep | <i>Model fit graphs for ("sep Q" models)</i> |
|--------------|--|

Description

Model fit graphs for ("sep Q" models)

Usage

```
FitgraphsSep(
  ModelType,
  WishFitgraphs,
  ModelPara,
  NumOut,
  Economies,
  PathsGraphs
)
```

Arguments

| | |
|---------------|---|
| ModelType | a string-vector containing the label of the model to be estimated |
| WishFitgraphs | binary variable: set 1, if the user wishes graphs to be generated; or set 0, otherwise |
| ModelPara | List of model parameter estimates (See the "Optimization" function) |
| NumOut | list of computed outputs containing the model fit, IRFs, FEVDs, GIRFs, and GFEVDs |
| Economies | a string-vector containing the names of the economies which are part of the economic system |
| PathsGraphs | Path of the folder in which the graphs will be saved |

| | |
|-------------|---------------------------------|
| FMN__Rotate | <i>Performs state rotations</i> |
|-------------|---------------------------------|

Description

Performs state rotations

Usage

FMN__Rotate(y0, U1, U0)

Arguments

| | |
|----|---|
| y0 | list of model parameters as described below |
| U1 | matrix (N x N) |
| U0 | vector (N x 1). Optional. Default: vector of zeros. |

Details

This function performs a rotation from a model with Z as states to one with $S = U0 + U1*Z$ as states.

Specifically, each model is characterized by the following inputs organized in a list of variables:

- (i) K0: intercepts (N x 1);
- (ii) K1: feedback matrix (N x N*p);
- (iii) SS: volatility matrices (N x N*(M+1))

More specifically, the state Z follows the dynamics:

$Z_t = N(K0 + K1 [Z_{t-1}; Z_{t-2}; \dots], SSi[, , 1] + \sum_{i=1}^M SSi[, , i+1])$ where SSi <- array(SS, c(N, N, M+1))

Value

y1 - list of outputs after the transformation, the structure parallels that of y0

References

This function is modified version of the "FMN__Rotate" function by Le and Singleton (2018). "A Small Package of Matlab Routines for the Estimation of Some Term Structure Models." (Euro Area Business Cycle Network Training School - Term Structure Modelling). Available at: <https://cepr.org/40029>

| | |
|----------------|---|
| ForecastYields | <i>Gather bond yields forecasts for all the model types</i> |
|----------------|---|

Description

Gather bond yields forecasts for all the model types

Usage

```
ForecastYields(
  ModelType,
  ModelPara,
  InputsForOutputs,
  FactorLabels,
  Economies,
  DataFrequency,
  JLLinputs,
  GVARinputs
)
```

Arguments

| | |
|------------------|---|
| ModelType | a string-vector containing the label of the model to be estimated |
| ModelPara | List of model parameter estimates (See the "Optimization" function) |
| InputsForOutputs | list containing the desired horizon of analysis for the IRFs, GIRFs, FEVDs, and GFEVDs |
| FactorLabels | a string-list based which contains all the labels of all the variables present in the model |
| Economies | string-vector containing the names of the economies which are part of the economic system |
| DataFrequency | text: "Daily All Days", "Daily Business Days", "Weekly", "Monthly", "Quarterly", "Annually" |
| JLLinputs | list of necessary inputs for the estimation of JLL-based models (see "JLL" function) |
| GVARinputs | list of necessary inputs for the estimation of GVAR-based models (see "GVAR" function) |

Value

List containing the following elements

1. Out-of-sample forecasts of bond yields per forecast horizon
2. Out-of-sample forecast errors of bond yields per forecast horizon
3. Root mean square errors per forecast horizon

Examples

See examples in the vignette file of this package (Section 4).

ForecastYieldsJointQ *Bond yields forecasts ("joint Q" models)*

Description

Bond yields forecasts ("joint Q" models)

Usage

```
ForecastYieldsJointQ(
  ModelType,
  ModelPara,
  InputsForOutputs,
  FactorLabels,
  Economies,
  DataFrequency,
  JLLinputs,
  GVARinputs
)
```

Arguments

| | |
|------------------|---|
| ModelType | a string-vector containing the label of the model to be estimated |
| ModelPara | List of model parameter estimates (See the "Optimization" function) |
| InputsForOutputs | list containing the desired horizon of analysis for the IRFs, GIRFs, FEVDs, and GFEVDs |
| FactorLabels | a string-list based which contains all the labels of all the variables present in the model |
| Economies | string-vector containing the names of the economies which are part of the economic system |
| DataFrequency | character-based vector: "Daily All Days", "Daily Business Days", "Weekly", "Monthly", "Quarterly", "Annually" |
| JLLinputs | list of necessary inputs for the estimation of JLL-based models (see "JLL" function) |
| GVARinputs | list of necessary inputs for the estimation of GVAR-based models (see "GVAR" function) |

ForecastYieldsSepQ *Bond yields forecasts ("sep Q" models)*

Description

Bond yields forecasts ("sep Q" models)

Usage

```
ForecastYieldsSepQ(
  ModelType,
  ModelPara,
  InputsForOutputs,
  FactorLabels,
  Economies,
  DataFrequency,
  JLLinputs,
  GVARinputs
)
```

Arguments

| | |
|------------------|---|
| ModelType | a string-vector containing the label of the model to be estimated |
| ModelPara | List of model parameter estimates (See the "Optimization" function) |
| InputsForOutputs | list containing the desired horizon of analysis for the IRFs, GIRFs, FEVDs, and GFEVDs |
| FactorLabels | a string-list based which contains all the labels of all the variables present in the model |
| Economies | string-vector containing the names of the economies which are part of the economic system |
| DataFrequency | character-based vector: "Daily All Days", "Daily Business Days", "Weekly", "Monthly", "Quarterly", "Annually" |
| JLLinputs | list of necessary inputs for the estimation of JLL-based models (see "JLL" function) |
| GVARinputs | list of necessary inputs for the estimation of GVAR-based models (see "GVAR" function) |

Functionf *Set up the vector-valued objective function (Point estimate)*

Description

Set up the vector-valued objective function (Point estimate)

Usage

```
Functionf(MLEinputs, Economies, mat, DataFrequency, FactorLabels, ModelType)
```

Arguments

| | |
|---------------|---|
| MLEinputs | Set of inputs that are necessary to the log-likelihood function |
| Economies | string-vector containing the names of the economies which are part of the economic system |
| mat | vector of maturities (in years) of yields used in estimation (J x 1) |
| DataFrequency | character-based vector: "Daily All Days", "Daily Business Days", "Weekly", "Monthly", "Quarterly", "Annually" |
| FactorLabels | string-list based which contains the labels of all the variables present in the model |
| ModelType | string-vector containing the label of the model to be estimated |

Value

objective function

Examples

```
# See examples in the vignette file of this package (Section 4).
```

Functionf_Boot *Set up the vector-valued objective function (Bootstrap)*

Description

Set up the vector-valued objective function (Bootstrap)

Usage

```
Functionf_Boot(
  ModelType,
  MLEinputsBS,
  Economies,
  mat,
  dt,
  FactorLabels,
  residBS,
  MaxEigen,
  JLLinputs,
  GVARinputs
)
```

Arguments

| | |
|--------------|---|
| ModelType | string-vector containing the label of the model to be estimated |
| MLEinputsBS | Set of inputs that are necessary to the log-likelihood function |
| Economies | string-vector containing the names of the economies which are part of the economic system |
| mat | vector of maturities (in years) of yields used in estimation (J x 1) |
| dt | adjusted yearly frequency of the data |
| FactorLabels | string-list based which contains the labels of all the variables present in the model |
| residBS | indexes of the re-ordered bootstrap residuals |
| MaxEigen | largest eigenvalue under the P-dynamics |
| JLLinputs | necessary inputs for the estimation of JLL-based models |
| GVARinputs | necessary inputs for the estimation of GVAR-based models |

f_with_vectorized_parameters

Use function f to generate the outputs from a ATSM

Description

Use function f to generate the outputs from a ATSM

Usage

```
f_with_vectorized_parameters(
  x,
  sizex,
  f,
  con,
```

```

    varargin,
    ModelType,
    FactorLabels,
    Economies,
    JLLinputs,
    GVARinputs,
    nargout
)

```

Arguments

| | |
|--------------|--|
| x | vector containing all the vectorized auxiliary parameters |
| sizeX | matrix (6x2) containing the size information of all parameters |
| f | vector-valued objective function (function) |
| con | if con = 'concentration', then set the value of the parameter whose name contains @ to empty |
| varargin | variable inputs used in the optimization (see inputs from "optimization" function) |
| ModelType | string-vector containing the label of the model to be estimated |
| FactorLabels | string-list based which contains the labels of all the variables present in the model |
| Economies | string-vector containing the names of the economies which are part of the economic system |
| JLLinputs | Set of necessary inputs used in the estimation of the JLL-based models (see "JLL" function) |
| GVARinputs | Set of necessary inputs used in the estimation of the GVAR-based models (see "GVAR" function) |
| nargout | if nargout <- 1, returns only the values of the likelihood function. If nargout <- 2, generates the entire set of outputs |

References

This function is modified version of the "f_with_vectorized_parameters" function by Le and Singleton (2018).

"A Small Package of Matlab Routines for the Estimation of Some Term Structure Models."
(Euro Area Business Cycle Network Training School - Term Structure Modelling). Available at:
<https://cepr.org/40029>

GaussianDensity *computes the density function of a gaussian process*

Description

computes the density function of a gaussian process

Usage

GaussianDensity(res, SS, invSS, logabsdetSS)

Arguments

| | |
|-------------|---|
| res | matrix of residuals (N x T) |
| SS | covariance matrice or array of covariance matrices (If $\dim(SS) > 3$, then the model has a stochastic volatility) (N x N) or (N x N x T) |
| invSS | Inverse of SS (N x N) or (N x N x T) - optional input |
| logabsdetSS | $\log(\text{abs}(SS))$ (1 x T) - optional input |

Value

y - vector of density (1 x T)

References

This function is based on the "Gaussian" function by Le and Singleton (2018).
 "A Small Package of Matlab Routines for the Estimation of Some Term Structure Models."
 (Euro Area Business Cycle Network Training School - Term Structure Modelling). Available at:
<https://cepr.org/40029>

getpara *Extract the parameter values from varargin*

Description

Extract the parameter values from varargin

Usage

getpara(varargin)

Arguments

| | |
|----------|------------------------|
| varargin | All parameter features |
|----------|------------------------|

References

This function is modified version of the "getpara" function by Le and Singleton (2018).
 "A Small Package of Matlab Routines for the Estimation of Some Term Structure Models."
 (Euro Area Business Cycle Network Training School - Term Structure Modelling). Available at:
<https://cepr.org/40029>

| | |
|------|---|
| getx | <i>Obtain the auxiliary values corresponding to each parameter, its size and its name</i> |
|------|---|

Description

Obtain the auxiliary values corresponding to each parameter, its size and its name

Usage

```
getx(con, varargin, Economies, FactorLabels, JLLinputs = NULL)
```

Arguments

| | |
|--------------|--|
| con | If con = 'concentration' and a parameter's name contains '@', then its auxiliary value is set to empty |
| varargin | variable inputs used in the optimization (see "optimization" function) |
| Economies | string-vector containing the names of the economies which are part of the economic system |
| FactorLabels | list of necessary inputs for the estimation of JLL-based models (see "JLL" function) |
| JLLinputs | Necessary inputs for the estimation of the JLL-based models |

References

This function is a modified version of the "getx" function by Le and Singleton (2018).
 "A Small Package of Matlab Routines for the Estimation of Some Term Structure Models."
 (Euro Area Business Cycle Network Training School - Term Structure Modelling).

GFEVDgraphsJLLOrtho *GFEVDs graphs for orthogonalized risk factors of JLL-based models*

Description

GFEVDs graphs for orthogonalized risk factors of JLL-based models

Usage

```
GFEVDgraphsJLLOrtho(
  ModelType,
  NumOut,
  WishPdynamicgraphs,
  WishYieldsgraphs,
  GFEVDhoriz,
  PathsGraphs
)
```

Arguments

| | |
|--------------------|--|
| ModelType | a string-vector containing the label of the model to be estimated |
| NumOut | list of computed outputs containing the model fit, IRFs, FEVDs, GIRFs, and GFEVDs |
| WishPdynamicgraphs | binary variable: set 1, if the user wishes graphs to be generated; or set 0, otherwise |
| WishYieldsgraphs | binary variable: set 1, if the user wishes graphs to be generated; or set 0, otherwise |
| GFEVDhoriz | single numerical vector containing the desired horizon of analysis for the GFEVDs |
| PathsGraphs | Path of the folder in which the graphs will be saved |

GFEVDgraphsJoint *GFEVDs graphs for ("joint Q" models)*

Description

GFEVDs graphs for ("joint Q" models)

Usage

```
GFEVDgraphsJoint(
  ModelType,
  NumOut,
  WishPdynamicsgraphs,
  WishYieldsgraphs,
  GFEVDhoriz,
  PathsGraphs
)
```

Arguments

| | |
|---------------------|--|
| ModelType | a string-vector containing the label of the model to be estimated |
| NumOut | list of computed outputs containing the model fit, IRFs, FEVDs, GIRFs, and GFEVDs |
| WishPdynamicsgraphs | binary variable: set 1, if the user wishes graphs to be generated; or set 0, otherwise |
| WishYieldsgraphs | binary variable: set 1, if the user wishes graphs to be generated; or set 0, otherwise |
| GFEVDhoriz | single numerical vector conataining the desired horizon of analysis for the GFEVDs |
| PathsGraphs | Path of the folder in which the graphs will be saved |

| | |
|----------------|---|
| GFEVDgraphsSep | <i>GFEVDs graphs for ("sep Q" models)</i> |
|----------------|---|

Description

GFEVDs graphs for ("sep Q" models)

Usage

```
GFEVDgraphsSep(
  ModelType,
  NumOut,
  WishPdynamicsgraphs,
  WishYieldsgraphs,
  GFEVDhoriz,
  PathsGraphs,
  Economies
)
```

Arguments

| | |
|--------------------|---|
| ModelType | a string-vector containing the label of the model to be estimated |
| NumOut | list of computed outputs containing the model fit, IRFs, FEVDs, GIRFs, and GFEVDs |
| WishPynamicsgraphs | binary variable: set 1, if the user wishes graphs to be generated; or set 0, otherwise |
| WishYieldsgraphs | binary variable: set 1, if the user wishes graphs to be generated; or set 0, otherwise |
| GFEVDhoriz | single numerical vector conataining the desired horizon of analysis for the GFEVDs |
| PathsGraphs | Path of the folder in which the graphs will be saved |
| Economies | a string-vector containing the names of the economies which are part of the economic system |

| | |
|------------|------------------------------------|
| GFEVDjoint | <i>GFEVDs for "joint Q" models</i> |
|------------|------------------------------------|

Description

GFEVDs for "joint Q" models

Usage

```
GFEVDjoint(ModelType, ModelPara, GFEVDhoriz, FactorLabels, Economies)
```

Arguments

| | |
|--------------|---|
| ModelType | string-vector containing the label of the model to be estimated |
| ModelPara | list of model parameter estimates (see the "Optimization" function) |
| GFEVDhoriz | single numerical vector conataining the desired horizon of analysis for the GFEVDs |
| FactorLabels | string-list based which contains all the labels of all the variables present in the model |
| Economies | string-vector containing the names of the economies which are part of the economic system |

References

- This function is a modified and extended version of the "fevd" function from Smith, L.V. and A. Galesi (2014). GVAR Toolbox 2.0, available at <https://sites.google.com/site/gvarmodelling/gvar-toolbox>.
- Pesaran and Shin, 1998. "Generalized impulse response analysis in linear multivariate models" (Economics Letters)

GFEVDjointOrthoJLL *Orthogonalized GFEVDs for JLL models*

Description

Orthogonalized GFEVDs for JLL models

Usage

GFEVDjointOrthoJLL(ModelType, ModelPara, GFEVDhoriz, FactorLabels, Economies)

Arguments

| | |
|--------------|---|
| ModelType | a string-vector containing the label of the model to be estimated |
| ModelPara | List of model parameter estimates (See the "Optimization" function) |
| GFEVDhoriz | single numerical vector conataining the desired horizon of analysis for the GFEVDs |
| FactorLabels | a string-list based which contains all the labels of all the variables present in the model |
| Economies | a string-vector containing the names of the economies which are part of the economic system |

References

- This function is a modified and extended version of the "fevd" function from Smith, L.V. and A. Galesi (2014). GVAR Toolbox 2.0, available at <https://sites.google.com/site/gvarmodelling/gvar-toolbox>.
- Pesaran and Shin, 1998. "Generalized impulse response analysis in linear multivariate models" (Economics Letters)

GFEVDjointOrthoJLL_BS *GFEVDs after bootstrap for JLL-based models*

Description

GFEVDs after bootstrap for JLL-based models

Usage

```
GFEVDjointOrthoJLL_BS(
  ModelType,
  ModelParaBoot,
  GFEVDhoriz,
  FactorLabels,
  Economies
)
```

Arguments

| | |
|---------------|--|
| ModelType | string-vector containing the label of the model to be estimated |
| ModelParaBoot | list of model parameter estimates (see the "Optimization" function) after a bootstrap draw |
| GFEVDhoriz | single numerical vector containing the desired horizon of analysis for the GFEVDs |
| FactorLabels | string-list based which contains all the labels of all the variables present in the model |
| Economies | string-vector containing the names of the economies which are part of the economic system |

References

- This function is a modified and extended version of the "fevd" function from Smith, L.V. and A. Galesi (2014). GVAR Toolbox 2.0, available at <https://sites.google.com/site/gvarmodelling/gvar-toolbox>.
- Pesaran and Shin, 1998. "Generalized impulse response analysis in linear multivariate models" (Economics Letters)

GFEVDjoint_BS

GFEVDs after bootstrap for "joint Q" models

Description

GFEVDs after bootstrap for "joint Q" models

Usage

GFEVDjoint_BS(ModelType, ModelParaBoot, GFEVDhoriz, FactorLabels, Economies)

Arguments

| | |
|---------------|--|
| ModelType | string-vector containing the label of the model to be estimated |
| ModelParaBoot | List of model parameter estimates (See the "Optimization" function) after a bootstrap draw |
| GFEVDhoriz | single numerical vector containing the desired horizon of analysis for the GFEVDs |
| FactorLabels | string-list based which contains all the labels of all the variables present in the model |
| Economies | string-vector containing the names of the economies which are part of the economic system |

References

- This function is a modified and extended version of the "fevd" function from Smith, L.V. and A. Galesi (2014). GVAR Toolbox 2.0, available at <https://sites.google.com/site/gvarmodelling/gvar-toolbox>.
- Pesaran and Shin, 1998. "Generalized impulse response analysis in linear multivariate models" (Economics Letters)

GFEVDsep

GFEVDs for "sep Q" models

Description

GFEVDs for "sep Q" models

Usage

GFEVDsep(ModelType, ModelPara, GFEVDhoriz, FactorLabels, Economies)

Arguments

| | |
|--------------|---|
| ModelType | string-vector containing the label of the model to be estimated |
| ModelPara | list of model parameter estimates (see the "Optimization" function) |
| GFEVDhoriz | single numerical vector containing the desired horizon of analysis for the GFEVDs |
| FactorLabels | string-list based which contains all the labels of all the variables present in the model |
| Economies | string-vector containing the names of the economies which are part of the economic system |

References

- This function is a modified and extended version of the "fevd" function from Smith, L.V. and A. Galesi (2014). GVAR Toolbox 2.0, available at <https://sites.google.com/site/gvarmodelling/gvar-toolbox>.
- Pesaran and Shin, 1998. "Generalized impulse response analysis in linear multivariate models" (Economics Letters)

GFEVDsep_BS *GFEVDs after bootstrap for "sep Q" models*

Description

GFEVDs after bootstrap for "sep Q" models

Usage

GFEVDsep_BS(ModelType, ModelParaBoot, GFEVDhoriz, FactorLabels, Economies)

Arguments

| | |
|---------------|--|
| ModelType | string-vector containing the label of the model to be estimated |
| ModelParaBoot | list of model parameter estimates (see the "Optimization" function) after a bootstrap draw |
| GFEVDhoriz | single numerical vector containing the desired horizon of analysis for the GFEVDs |
| FactorLabels | string-list based which contains all the labels of all the variables present in the model |
| Economies | string-vector containing the names of the economies which are part of the economic system |

References

- This function is a modified and extended version of the "fevd" function from Smith, L.V. and A. Galesi (2014). GVAR Toolbox 2.0, available at <https://sites.google.com/site/gvarmodelling/gvar-toolbox>.
- Pesaran and Shin, 1998. "Generalized impulse response analysis in linear multivariate models" (Economics Letters)

GIRFgraphsJLLOrtho *GIRFs graphs for orthogonalized risk factors of JLL-based models*

Description

GIRFs graphs for orthogonalized risk factors of JLL-based models

Usage

```
GIRFgraphsJLLOrtho(
  ModelType,
  NumOut,
  WishPdynamicsgraphs,
  WishYieldsgraphs,
  GIRFhoriz,
  PathsGraphs
)
```


Arguments

| | |
|--------------------|--|
| ModelType | a string-vector containing the label of the model to be estimated |
| NumOut | list of computed outputs containing the model fit, IRFs, FEVDs, GIRFs, and GFEVDs |
| WishPynamicsgraphs | binary variable: set 1, if the user wishes graphs to be generated; or set 0, otherwise |
| WishYieldsgraphs | binary variable: set 1, if the user wishes graphs to be generated; or set 0, otherwise |
| GIRFhoriz | single numerical vector conataining the desired horizon of analysis for the GIRFs |
| PathsGraphs | Path of the folder in which the graphs will be saved |

| | |
|-----------------|--|
| GIRFgraphsJoint | <i>GIRFs graphs for ("joint Q" models)</i> |
|-----------------|--|

Description

GIRFs graphs for ("joint Q" models)

Usage

```
GIRFgraphsJoint(
  ModelType,
  NumOut,
  WishPynamicsgraphs,
  WishYieldsgraphs,
  GIRFhoriz,
  PathsGraphs
)
```

Arguments

| | |
|--------------------|--|
| ModelType | a string-vector containing the label of the model to be estimated |
| NumOut | list of computed outputs containing the model fit, IRFs, FEVDs, GIRFs, and GFEVDs |
| WishPynamicsgraphs | binary variable: set 1, if the user wishes graphs to be generated; or set 0, otherwise |
| WishYieldsgraphs | binary variable: set 1, if the user wishes graphs to be generated; or set 0, otherwise |
| GIRFhoriz | single numerical vector conataining the desired horizon of analysis for the GIRFs |
| PathsGraphs | Path of the folder in which the graphs will be saved |

GIRFgraphsSep *GIRFs graphs for ("sep Q" models)*

Description

GIRFs graphs for ("sep Q" models)

Usage

```
GIRFgraphsSep(
  ModelType,
  NumOut,
  WishPdynamicsgraphs,
  WishYieldsgraphs,
  GIRFhoriz,
  PathsGraphs,
  Economies
)
```

Arguments

| | |
|---------------------|---|
| ModelType | a string-vector containing the label of the model to be estimated |
| NumOut | list of computed outputs containing the model fit, IRFs, FEVDs, GIRFs, and GFEVDs |
| WishPdynamicsgraphs | binary variable: set 1, if the user wishes graphs to be generated; or set 0, otherwise |
| WishYieldsgraphs | binary variable: set 1, if the user wishes graphs to be generated; or set 0, otherwise |
| GIRFhoriz | single numerical vector conataining the desired horizon of analysis for the GIRFs |
| PathsGraphs | Path of the folder in which the graphs will be saved |
| Economies | a string-vector containing the names of the economies which are part of the economic system |

GIRFjoint *GIRFs for "joint Q" models*

Description

GIRFs for "joint Q" models

Usage

```
GIRFjoint(ModelType, ModelPara, GIRFhoriz, FactorLabels, Economies)
```

Arguments

| | |
|--------------|---|
| ModelType | a string-vector containing the label of the model to be estimated |
| ModelPara | List of model parameter estimates (See the "Optimization" function) |
| GIRFhoriz | single numerical vector conataining the desired horizon of analysis for the GIRFs |
| FactorLabels | a string-list based which contains all the labels of all the variables present in the model |
| Economies | a string-vector containing the names of the economies which are part of the economic system |

References

- This function is a modified and extended version of the "irf" function from Smith, L.V. and A. Galesi (2014). GVAR Toolbox 2.0, available at <https://sites.google.com/site/gvarmodelling/gvar-toolbox>.
- Pesaran and Shin, 1998. "Generalized impulse response analysis in linear multivariate models" (Economics Letters)

GIRFjointOrthoJLL *Orthogonalized GIRFs for JLL models*

Description

Orthogonalized GIRFs for JLL models

Usage

GIRFjointOrthoJLL(ModelType, ModelPara, GIRFhoriz, FactorLabels, Economies)

Arguments

| | |
|--------------|---|
| ModelType | a string-vector containing the label of the model to be estimated |
| ModelPara | List of model parameter estimates (See the "Optimization" function) |
| GIRFhoriz | single numerical vector conataining the desired horizon of analysis for the GIRFs |
| FactorLabels | a string-list based which contains all the labels of all the variables present in the model |
| Economies | a string-vector containing the names of the economies which are part of the economic system |

References

- This function is a modified and extended version of the "irf" function from Smith, L.V. and A. Galesi (2014). GVAR Toolbox 2.0, available at <https://sites.google.com/site/gvarmodelling/gvar-toolbox>.
- Pesaran and Shin, 1998. "Generalized impulse response analysis in linear multivariate models" (Economics Letters)

GIRFjointOrthoJLL_BS *GIRFs after bootstrap for JLL-based models*

Description

GIRFs after bootstrap for JLL-based models

Usage

```
GIRFjointOrthoJLL_BS(
  ModelType,
  ModelParaBoot,
  GIRFhoriz,
  FactorLabels,
  Economies
)
```

Arguments

| | |
|---------------|--|
| ModelType | string-vector containing the label of the model to be estimated |
| ModelParaBoot | list of model parameter estimates (see the "Optimization" function) after a bootstrap draw |
| GIRFhoriz | single numerical vector containing the desired horizon of analysis for the GIRFs |
| FactorLabels | string-list based which contains the labels of all the variables present in the model |
| Economies | string-vector containing the names of the economies which are part of the economic system |

References

- This function is a modified and extended version of the "irf" function from Smith, L.V. and A. Galesi (2014). GVAR Toolbox 2.0, available at <https://sites.google.com/site/gvarmodelling/gvar-toolbox>.
- Pesaran and Shin, 1998. "Generalized impulse response analysis in linear multivariate models" (Economics Letters)

GIRFjoint_BS *GIRFs after bootstrap for "joint Q" models*

Description

GIRFs after bootstrap for "joint Q" models

Usage

GIRFjoint_BS(ModelType, ModelParaBoot, GIRFhoriz, FactorLabels, Economies)

Arguments

| | |
|---------------|--|
| ModelType | string-vector containing the label of the model to be estimated |
| ModelParaBoot | list of model parameter estimates (see the "Optimization" function) after a bootstrap draw |
| GIRFhoriz | single numerical vector containing the desired horizon of analysis for the GIRFs |
| FactorLabels | string-list based which contains all the labels of all the variables present in the model |
| Economies | string-vector containing the names of the economies which are part of the economic system |

References

- This function is a modified and extended version of the "irf" function from Smith, L.V. and A. Galesi (2014). GVAR Toolbox 2.0, available at <https://sites.google.com/site/gvarmodelling/gvar-toolbox>.
- Pesaran and Shin, 1998. "Generalized impulse response analysis in linear multivariate models" (Economics Letters)

GIRFSep *GIRFs for "sep Q" models*

Description

GIRFs for "sep Q" models

Usage

GIRFSep(ModelType, ModelPara, GIRFhoriz, FactorLabels, Economies)

Arguments

| | |
|--------------|---|
| ModelType | string-vector containing the label of the model to be estimated |
| ModelPara | list of model parameter estimates (see the "Optimization" function) |
| GIRFhoriz | single numerical vector conataining the desired horizon of analysis for the GIRFs |
| FactorLabels | string-list based which contains all the labels of all the variables present in the model |
| Economies | string-vector containing the names of the economies which are part of the economic system |

References

- This function is a modified and extended version of the "irf" function from Smith, L.V. and A. Galesi (2014). GVAR Toolbox 2.0, available at <https://sites.google.com/site/gvarmodelling/gvar-toolbox>.
- Pesaran and Shin, 1998. "Generalized impulse response analysis in linear multivariate models" (Economics Letters)

GIRFSep_BS

GIRFs after bootstrap for "sep Q" models

Description

GIRFs after bootstrap for "sep Q" models

Usage

GIRFSep_BS(ModelType, ModelParaBoot, GIRFhoriz, FactorLabels, Economies)

Arguments

| | |
|---------------|--|
| ModelType | string-vector containing the label of the model to be estimated |
| ModelParaBoot | list of model parameter estimates (see the "Optimization" function) after a bootstrap draw |
| GIRFhoriz | single numerical vector conataining the desired horizon of analysis for the GIRFs |
| FactorLabels | string-list based which contains all the labels of all the variables present in the model |
| Economies | string-vector containing the names of the economies which are part of the economic system |

References

- This function is a modified and extended version of the "irf" function from Smith, L.V. and A. Galesi (2014). GVAR Toolbox 2.0, available at <https://sites.google.com/site/gvarmodelling/gvar-toolbox>.
- Pesaran and Shin, 1998. "Generalized impulse response analysis in linear multivariate models" (Economics Letters)

| | |
|------------------|--|
| GraphicalOutputs | <i>Generate the graphical outputs for the selected models (Point estimate)</i> |
|------------------|--|

Description

Generate the graphical outputs for the selected models (Point estimate)

Usage

```
GraphicalOutputs(
  ModelType,
  ModelPara,
  NumOut,
  InputsForOutputs,
  Economies,
  FactorLabels
)
```

Arguments

| | |
|------------------|---|
| ModelType | a string-vector containing the label of the model to be estimated |
| ModelPara | List of model parameter estimates (See the "Optimization" function) |
| NumOut | list of computed outputs containing the model fit, IRFs, FEVDs, GIRFs, and GFEVDs |
| InputsForOutputs | list containing the desired inputs for the construction of the desired output |
| Economies | string-vector containing the names of the economies which are part of the economic system |
| FactorLabels | string-list based which contains the labels of all the variables present in the model |

| | |
|------|---|
| GVAR | <i>Estimate a GVAR(1) and a VARX(1,1,1)</i> |
|------|---|

Description

Estimate a GVAR(1) and a VARX(1,1,1)

Usage

```
GVAR(GVARinputs, N)
```

Arguments

- GVARinputs List containing the following necessary inputs for the estimation of the GVAR:
1. Economies: string-vector containing the names of the economies which are part of the economic system
 2. 'GVARFactors': list of all variables that are used in the estimation of the VARX
(see e.g. 'CM_Factors_GVAR' file);
 3. 'VARXtype': character-vector containing two possibilities:
 - 'unconstrained': model is estimated without any constrained (each equation is estimated individually by OLS);
 - 'constrained: Spanned Factors': model is estimated taking into account the fact that foreign-pricing-factors do NOT impinge on (i) domestic economic variables and (ii) domestic pricing factors. (equations are estimated by restricted least squares)
 - 'constrained: ' extended by the name of the risk factor: model is estimated taking into account the fact that the restricted factor is only affected by its own lagged values and the lagged values of its own star variables. (equations are estimated by restricted least squares)
 4. 'Wgvar': GVAR transition matrix (C x C) - see the output from 'Transition_Matrix' function
- N number of country-specific spanned factors (scalar)

Value

A list containing

1. parameters of the country-specific VARX(1,1,1)
 - intercept (M+Nx1);
 - phi_1 (M+N x M+N);
 - phi_1^star (M+N x M+N);
 - phi_g (M+N x M+N);
 - Sigma (M+N x G)
2. parameters of the GVAR.
 - F0 (F X 1);
 - F1 (F x F);
 - Sigma_y (F x F)

References

Chudik and Pesaran, (2016). "Theory and Practice of GVAR modelling" (Journal of Economic Surveys)

Examples

```

data(CM_Factors_GVAR)

N <- 3

GVARinputs <- list()
GVARinputs$Economies <- c("China", "Brazil", "Mexico", "Uruguay")
GVARinputs$GVARFactors <- FactorsGVAR
GVARinputs$VARXtype <- "unconstrained"
GVARinputs$Wgvar <- matrix( c(0, 0.83, 0.86, 0.38,
                             0.65, 0, 0.13, 0.55,
                             0.32, 0.12, 0, 0.07,
                             0.03, 0.05, 0.01, 0), nrow = 4, ncol = 4)

GVAR(GVARinputs, N)

```

| | |
|---------------|--|
| IdxAllSpanned | <i>Find the indexes of the spanned factors</i> |
|---------------|--|

Description

Find the indexes of the spanned factors

Usage

```
IdxAllSpanned(ModelType, FactorLabels, Economies)
```

Arguments

| | |
|--------------|---|
| ModelType | string-vector containing the label of the model to be estimated |
| FactorLabels | string-list based which contains the labels of all the variables present in the model |
| Economies | string-vector containing the names of the economies which are part of the economic system |

| | |
|------------|---|
| IdxSpanned | <i>Extract the indexes related to the spanned factors in the variance-covariance matrix</i> |
|------------|---|

Description

Extract the indexes related to the spanned factors in the variance-covariance matrix

Usage

```
IdxSpanned(G, M, N, C)
```

Arguments

| | |
|---|---|
| G | number of global unspanned factors (scalar) |
| M | number of domestic unspanned factors per country (scalar) |
| N | number of domestic spanned factors per country (scalar) |
| C | number of countries of the economic system (scalar) |

| | |
|---------------------|---|
| InputsForMLEdensity | <i>Generates several inputs that are necessary to build the likelihood function</i> |
|---------------------|---|

Description

Generates several inputs that are necessary to build the likelihood function

Usage

```
InputsForMLEdensity(
  ModelType,
  Yields,
  PdynamicsFactors,
  FactorLabels,
  mat,
  Economies,
  DataFrequency,
  JLLinputs = NULL,
  GVARinputs = NULL
)
```

Arguments

| | |
|------------------|--|
| ModelType | string-vector containing the label of the model to be estimated |
| Yields | time series of yields (JxT or CJ x T) |
| PdynamicsFactors | time series of the risk factors (K x T) |
| FactorLabels | string-list based which contains the labels of all the variables present in the model |
| mat | vector of maturities (in years) used in the estimation |
| Economies | string-vector containing the names of the economies of the system. If the ModelType selected is "JPS", "JPS jointP", "GVAR sepQ", then only one economy can be selected. For the other models, more than one economy must be selected. |
| DataFrequency | character-based-vector. Available options are: "Daily All Days", "Daily Business Days", "Weekly", "Monthly", "Quarterly", "Annually" |

| | |
|------------|--|
| JLLinputs | list of necessary inputs for the estimation of JLL-based models (see "JLL" function) |
| GVARinputs | list of necessary inputs for the estimation of GVAR-based models (see "GVAR" function) |

Details

To ensure that the risk factors matrix is correctly built for the model "JPS", the global factors should be allocated on the first G rows of this matrix.

Value

List of necessary inputs for constructing the model's log-likelihood function

Examples

```
# Example 1:
data(CM_Factors)
data(CM_Yields)

ModelType <- "JPS"
Economies <- "Mexico"
Factors <- RiskFactors
N <- 3
GlobalVar <- c("GBC", "CPI_OECD") # Global Variables
DomVar <- c("Eco_Act", "Inflation") # Domestic Variables
FactorLabels <- LabFac(N, DomVar, GlobalVar, Economies, ModelType)

mat <- c(0.25, 0.5, 1, 3, 5, 10)
DataFrequency <- "Monthly"

i <- length(Economies)
ATSMInputs <- InputsForMLEdensity(ModelType, Yields, Factors, FactorLabels, mat,
                                   Economies, DataFrequency)

# Example 2:
data(CM_Factors)
data(CM_Yields)
data(CM_Factors_GVAR)

ModelType <- "GVAR jointQ"
Economies <- c("China", "Brazil", "Mexico", "Uruguay")
mat <- c(0.25, 0.5, 1, 3, 5, 10)
DataFrequency <- "Monthly"
Factors <- RiskFactors
N <- 3
GlobalVar <- c("GBC", "CPI_OECD") # Global Variables
DomVar <- c("Eco_Act", "Inflation") # Domestic Variables
FactorLabels <- LabFac(N, DomVar, GlobalVar, Economies, ModelType)

GVARinputs <- list()
GVARinputs$Economies <- Economies
```

```

GVARinputs$GVARFactors <- FactorsGVAR
GVARinputs$VARXtype <- "unconstrained"
GVARinputs$Wgvar <- matrix( c(0, 0.83, 0.86, 0.38,
                             0.65, 0, 0.13, 0.55,
                             0.32, 0.12, 0, 0.07,
                             0.03, 0.05, 0.01, 0), nrow = 4, ncol = 4)
ATSMinputs <- InputsForMLEdensity(ModelType, Yields, Factors, FactorLabels, mat, Economies,
                                  DataFrequency, JLLinputs= NULL , GVARinputs)

# Example 3:
if (requireNamespace('neldermead', quietly = TRUE)) {

data(CM_Factors)
data(CM_Yields)
ModelType <- "JLL jointSigma"
GlobalVar <- c("GBC", "CPI_OECD") # Global Variables
DomVar <- c("Eco_Act", "Inflation") # Domestic Variables
N <- 3
Economies <- c( "China", "Brazil", "Mexico", "Uruguay")
FactorLabels <- LabFac(N, DomVar, GlobalVar, Economies, ModelType)

Factors <- RiskFactors
mat <- c(0.25, 0.5, 1, 3, 5, 10)
DataFrequency <- "Monthly"
JLLinputs <- list()
JLLinputs$Economies <- Economies
JLLinputs$DomUnit <- "China"
JLLinputs$WishSigmas <- 1
JLLinputs$SigmaNonOrtho <- NULL
JLLinputs$JLLModelType <- ModelType

ATSMinputs <- InputsForMLEdensity(ModelType, Yields, Factors, FactorLabels, mat, Economies,
                                  DataFrequency, JLLinputs)
} else {
  message("skipping functionality due to missing Suggested dependency")
}

```

InputsForMLEdensity_BS

Generates several inputs that are necessary to build the likelihood function - Bootstrap version

Description

Generates several inputs that are necessary to build the likelihood function - Bootstrap version

Usage

```

InputsForMLEdensity_BS(
  ModelType,
  Y_artificial,
  Z_artificial,
  FactorLabels,
  mat,
  Economies,
  DataFrequency,
  JLLinputs = NULL,
  GVARinputs = NULL
)

```

Arguments

| | |
|---------------|--|
| ModelType | string-vector containing the label of the model to be estimated |
| Y_artificial | time series of yields (CJ x T or JxT) |
| Z_artificial | time series of the risk factors (F x T) |
| FactorLabels | string-list based which contains the labels of all the variables present in the model |
| mat | vector of maturities (in years) used in the estimation |
| Economies | string-vector containing the names of the economies of the system. If the ModelType selected is "JPS", "JPS jointP", "GVAR sepQ", then only one economy can be selected. For the other models, more than one economy must be selected. |
| DataFrequency | character-based-vector. Available options are: "Daily All Days", "Daily Business Days", "Weekly", "Monthly", "Quarterly", "Annually" |
| JLLinputs | list of necessary inputs for the estimation of JLL-based models (see "JLL" function) |
| GVARinputs | list of necessary inputs for the estimation of GVAR-based models (see "GVAR" function) |

| | |
|------------------|--|
| InputsForOutputs | <i>Collect the inputs that are used to construct the numerical and the graphical outputs</i> |
|------------------|--|

Description

Collect the inputs that are used to construct the numerical and the graphical outputs

Usage

```

InputsForOutputs(
  ModelType,
  Horiz,
  ListOutputWished,
  OutputLabel,
  WishStationarityQ,
  WishGraphYields = 0,
  WishGraphRiskFactors = 0,
  WishOrthoJLLgraphs = 0,
  WishBootstrap = 0,
  ListBoot = NULL,
  WishForecast = 0,
  ListForecast = NULL
)

```

Arguments

| | |
|----------------------|--|
| ModelType | String-vector containing the label of the model to be estimated |
| Horiz | Single numerical vector containing the desired horizon of analysis for the outputs |
| ListOutputWished | List of desired graphical outputs. Available options are: "Fit", "IRF", "FEVD", "GIRF", "GFEVD". |
| OutputLabel | Name of the output label to be stored |
| WishStationarityQ | User must set 1 if she wishes to impose the largest eigenvalue under the Q to be strictly smaller than 1, otherwise set 0. |
| WishGraphYields | Binary variable: set 1, if the user wishes graphs to be generated; or set 0, otherwise. Default is set as "0". |
| WishGraphRiskFactors | Binary variable: set 1, if the user wishes graphs to be generated; or set 0, otherwise. Default is set as "0". |
| WishOrthoJLLgraphs | Binary variable: set 1, if the user wishes orthogonalized JLL-based graphs to be generated; or set 0, otherwise. Default is set as "0" |
| WishBootstrap | Binary variable: set 1, if the user wishes graphs to be generated; or set 0, otherwise. Default is set as "0". |
| ListBoot | List containing the four following elements: <ol style="list-style-type: none"> 1. "methodBS": Desired bootstrap method among (a) 'bs' (standard residual bootstrap), (b) 'wild' (wild bootstrap), (c) 'block' (block bootstrap); 2. "BlockLength": if block bootstrap is chosen, then the user has to specify the length of the block (single numerical vector); 3. "ndraws": number of draws; |

- 4. "pctg": level of confidence (single numerical vector expressed in basis points)
- WishForecast Binary variable: set 1, if the user wishes graphs to be generated; or set 0, otherwise. Default is set as "0".
- ListForecast list containing the three following elements:
- 1. "ForHoriz": forecast horizon;
 - 2. "t0Sample": index of the first variable of the information set;
 - 3. "t0Forecast": index of the first forecast cut-off date.

Value

List of necessary inputs to generate the graphs of the outputs of the desired model

Examples

```

ModelType <- "JPS"
Horiz <- 100
DesiredOutputGraphs <- c("Fit", "GIRF", "GFEVD")
OutputLabel <- "Test"
WishStationarityQ <- 1
WishGraphRiskFac <- 0
WishGraphYields <- 1

```

```

InputsList <- InputsForOutputs(ModelType, Horiz, DesiredOutputGraphs, OutputLabel,
                               WishStationarityQ, WishGraphYields, WishGraphRiskFac)

```

IRFandGIRFbs_jointQ *Creates the confidence bounds and the graphs of IRFs and GIRFs after bootstrap ("joint Q" models)*

Description

Creates the confidence bounds and the graphs of IRFs and GIRFs after bootstrap ("joint Q" models)

Usage

```

IRFandGIRFbs_jointQ(
  ModelType,
  ModelBootstrap,
  NumOutPE,
  InputsForOutputs,
  Economies,
  PathsGraphs
)

```

Arguments

| | |
|------------------|---|
| ModelType | string-vector containing the label of the model to be estimated |
| ModelBootstrap | list containing the complete set of model parameters after bootstrap estimation procedure |
| NumOutPE | list of model parameter point estimates |
| InputsForOutputs | list conataining the desired inputs for the construction of the outputs of interest |
| Economies | string-vector containing the names of the economies which are part of the economic system |
| PathsGraphs | path of the folder in which the graphs will be saved |

IRFandGIRFbs_jointQ_Ortho

Creates the confidence bounds and the graphs of IRFs and GIRFs after bootstrap (JLL-based models)

Description

Creates the confidence bounds and the graphs of IRFs and GIRFs after bootstrap (JLL-based models)

Usage

```
IRFandGIRFbs_jointQ_Ortho(
  ModelType,
  ModelBootstrap,
  NumOutPE,
  InputsForOutputs,
  Economies,
  PathsGraphs
)
```

Arguments

| | |
|------------------|---|
| ModelType | string-vector containing the label of the model to be estimated |
| ModelBootstrap | list containing the complete set of model parameters after bootstrap estimation procedure |
| NumOutPE | list of model parameter point estimates |
| InputsForOutputs | list conataining the desired inputs for the construction of the outputs of interest |
| Economies | string-vector containing the names of the economies which are part of the economic system |
| PathsGraphs | path of the folder in which the graphs will be saved |

| | |
|-------------------|--|
| IRFandGIRFbs_sepQ | <i>Creates the confidence bounds and the graphs of IRFs and GIRFs after bootstrap ("sep Q" models)</i> |
|-------------------|--|

Description

Creates the confidence bounds and the graphs of IRFs and GIRFs after bootstrap ("sep Q" models)

Usage

```
IRFandGIRFbs_sepQ(  
  ModelType,  
  ModelBootstrap,  
  NumOutPE,  
  InputsForOutputs,  
  Economies,  
  PathsGraphs  
)
```

Arguments

| | |
|------------------|---|
| ModelType | string-vector containing the label of the model to be estimated |
| ModelBootstrap | list containing the complete set of model parameters after bootstrap estimation procedure |
| NumOutPE | list of model parameter point estimates |
| InputsForOutputs | list containing the desired inputs for the construction of the outputs of interest |
| Economies | string-vector containing the names of the economies which are part of the economic system |
| PathsGraphs | path of the folder in which the graphs will be saved |

| | |
|-------------------|--|
| IRFgraphsJLLOrtho | <i>IRFs graphs for orthogonalized risk factors of JLL-based models</i> |
|-------------------|--|

Description

IRFs graphs for orthogonalized risk factors of JLL-based models

Usage

```
IRFgraphsJLLOrtho(
  ModelType,
  NumOut,
  WishPdynamicgraphs,
  WishYieldsgraphs,
  IRFhoriz,
  PathsGraphs
)
```

Arguments

| | |
|--------------------|--|
| ModelType | a string-vector containing the label of the model to be estimated |
| NumOut | list of computed outputs containing the model fit, IRFs, FEVDs, GIRFs, and GFEVDs |
| WishPdynamicgraphs | binary variable: set 1, if the user wishes graphs to be generated; or set 0, otherwise |
| WishYieldsgraphs | binary variable: set 1, if the user wishes graphs to be generated; or set 0, otherwise |
| IRFhoriz | single numerical vector containing the desired horizon of analysis for the IRFs |
| PathsGraphs | Path of the folder in which the graphs will be saved |

| | |
|----------------|---|
| IRFgraphsJoint | <i>IRFs graphs for ("joint Q" models)</i> |
|----------------|---|

Description

IRFs graphs for ("joint Q" models)

Usage

```
IRFgraphsJoint(
  ModelType,
  NumOut,
  WishPdynamicgraphs,
  WishYieldsgraphs,
  IRFhoriz,
  PathsGraphs
)
```

Arguments

| | |
|--------------------|--|
| ModelType | a string-vector containing the label of the model to be estimated |
| NumOut | list of computed outputs containing the model fit, IRFs, FEVDs, GIRFs, and GFEVDs |
| WishPynamicsgraphs | binary variable: set 1, if the user wishes graphs to be generated; or set 0, otherwise |
| WishYieldsgraphs | binary variable: set 1, if the user wishes graphs to be generated; or set 0, otherwise |
| IRFhoriz | single numerical vector conataining the desired horizon of analysis for the IRFs |
| PathsGraphs | Path of the folder in which the graphs will be saved |

| | |
|--------------|---|
| IRFgraphsSep | <i>IRFs graphs for ("sep Q" models)</i> |
|--------------|---|

Description

IRFs graphs for ("sep Q" models)

Usage

```
IRFgraphsSep(
  ModelType,
  NumOut,
  WishPynamicsgraphs,
  WishYieldsgraphs,
  IRFhoriz,
  PathsGraphs,
  Economies
)
```

Arguments

| | |
|--------------------|---|
| ModelType | a string-vector containing the label of the model to be estimated |
| NumOut | list of computed outputs containing the model fit, IRFs, FEVDs, GIRFs, and GFEVDs |
| WishPynamicsgraphs | binary variable: set 1, if the user wishes graphs to be generated; or set 0, otherwise |
| WishYieldsgraphs | binary variable: set 1, if the user wishes graphs to be generated; or set 0, otherwise |
| IRFhoriz | single numerical vector conataining the desired horizon of analysis for the IRFs |
| PathsGraphs | Path of the folder in which the graphs will be saved |
| Economies | a string-vector containing the names of the economies which are part of the economic system |

| | |
|----------|----------------------------------|
| IRFjoint | <i>IRFs for "joint Q" models</i> |
|----------|----------------------------------|

Description

IRFs for "joint Q" models

Usage

IRFjoint(ModelType, ModelPara, IRFhoriz, FactorLabels, Economies)

Arguments

| | |
|--------------|---|
| ModelType | string-vector containing the label of the model to be estimated |
| ModelPara | list of model parameter estimates (see the "Optimization" function) |
| IRFhoriz | single numerical vector conataining the desired horizon of analysis for the IRFs |
| FactorLabels | string-list based which contains all the labels of all the variables present in the model |
| Economies | string-vector containing the names of the economies which are part of the economic system |

Details

Structural shocks are identified via Cholesky decomposition

| | |
|------------------|---|
| IRFjointOrthoJLL | <i>Orthogonalized IRFs for JLL models</i> |
|------------------|---|

Description

Orthogonalized IRFs for JLL models

Usage

IRFjointOrthoJLL(ModelType, ModelPara, IRFhoriz, FactorLabels, Economies)

Arguments

| | |
|--------------|---|
| ModelType | string-vector containing the label of the model to be estimated |
| ModelPara | list of model parameter estimates (see the "Optimization" function) |
| IRFhoriz | single numerical vector conataining the desired horizon of analysis for the IRFs |
| FactorLabels | string-list based which contains all the labels of all the variables present in the model |
| Economies | string-vector containing the names of the economies which are part of the economic system |

Details

Structural shocks are identified via Cholesky decomposition

IRFjointOrthoJLL_BS *IRFs after bootstrap for JLL-based models*

Description

IRFs after bootstrap for JLL-based models

Usage

```
IRFjointOrthoJLL_BS(  
  ModelType,  
  ModelParaBoot,  
  IRFhoriz,  
  FactorLabels,  
  Economies  
)
```

Arguments

| | |
|---------------|--|
| ModelType | string-vector containing the label of the model to be estimated |
| ModelParaBoot | list of model parameter estimates (see the "Optimization" function) after a bootstrap draw |
| IRFhoriz | single numerical vector containing the desired horizon of analysis for the IRFs |
| FactorLabels | string-list based which contains all the labels of all the variables present in the model |
| Economies | string-vector containing the names of the economies which are part of the economic system |

IRFjoint_BS *IRFs after bootstrap for "joint Q" models*

Description

IRFs after bootstrap for "joint Q" models

Usage

```
IRFjoint_BS(ModelType, ModelParaBoot, IRFhoriz, FactorLabels, Economies)
```

Arguments

| | |
|---------------|---|
| ModelType | string-vector containing the label of the model to be estimated |
| ModelParaBoot | list of model parameter estimates (see the "Optimization" function) after a bootstrap draw |
| IRFhoriz | single numerical vector containing the desired horizon of analysis for the IRFs |
| FactorLabels | a string-list based which contains all the labels of all the variables present in the model |
| Economies | a string-vector containing the names of the economies which are part of the economic system |

| | |
|--------|--------------------------------|
| IRFsep | <i>IRFs for "sep Q" models</i> |
|--------|--------------------------------|

Description

IRFs for "sep Q" models

Usage

IRFsep(ModelType, ModelPara, IRFhoriz, FactorLabels, Economies)

Arguments

| | |
|--------------|---|
| ModelType | string-vector containing the label of the model to be estimated |
| ModelPara | list of model parameter estimates (See the "Optimization" function) |
| IRFhoriz | single numerical vector containing the desired horizon of analysis for the IRFs |
| FactorLabels | string-list based which contains the labels of all the variables present in the model |
| Economies | string-vector containing the names of the economies which are part of the economic system |

Details

Structural shocks are identified via Cholesky decomposition

| | |
|-----------|--|
| IRFsep_BS | <i>IRFs after bootstrap for "sep Q" models</i> |
|-----------|--|

Description

IRFs after bootstrap for "sep Q" models

Usage

IRFsep_BS(ModelType, ModelParaBoot, IRFhoriz, FactorLabels, Economies)

Arguments

| | |
|---------------|--|
| ModelType | string-vector containing the label of the model to be estimated |
| ModelParaBoot | list of model parameter estimates (see the "Optimization" function) after a bootstrap draw |
| IRFhoriz | single numerical vector containing the desired horizon of analysis for the IRFs |
| FactorLabels | string-list based which contains all the labels of all the variables present in the model |
| Economies | string-vector containing the names of the economies which are part of the economic system |

| | |
|-----|--|
| JLL | <i>Set of inputs present at JLL's P-dynamics</i> |
|-----|--|

Description

Set of inputs present at JLL's P-dynamics

Usage

JLL(NonOrthoFactors, N, JLLinputs)

Arguments

| | |
|-----------------|---|
| NonOrthoFactors | Risk factors before the orthogonalization (FxT) |
| N | Number of country-specific spanned factors |
| JLLinputs | List of necessary inputs to estimate JLL outputs: <ol style="list-style-type: none"> 1. Economies: set of economies that are part of the economic system (string-vector) 2. "DomUnit": name of the economy which is assigned as the dominant unit. If no dominant unit is assigned, then this variable is defined as "None" |

3. WishSigmas: equal to "1" if one wishes the variance-covariance matrices and the Cholesky factorizations (can take long if they need to be estimated). Set "0", otherwise.
4. SigmaNonOrtho: NULL or some $K \times K$ matrix from the non-orthogonalized dynamics
5. JLLModelType: available options are "JLL original", "JLL jointSigma" or "JLL NoDomUnit"

Details

For the models 'JLL original' or "JLL jointSigma" the name of one dominant economy must assigned.

For the model 'JLL NoDomUnit', the name of one dominant economy must be set as "None".

Value

List of model parameters from both the orthogonalized and non-orthogonalized versions of the JLL's based models

References

Jotiskhatira, Le and Lundblad (2015). "Why do interest rates in different currencies co-move?" (Journal of Financial Economics)

Examples

```
if (requireNamespace('neldermead', quietly = TRUE)) {

data(CM_Factors)
ZZ <- RiskFactors
N <- 3

JLLinputs <- list()
JLLinputs$Economies <- c("China", "Brazil", "Mexico", "Uruguay")
JLLinputs$DomUnit <- "China"
JLLinputs$WishSigmas <- 1
JLLinputs$SigmaNonOrtho <- NULL
JLLinputs$JLLModelType <- "JLL original"
JLL(ZZ, N, JLLinputs)

#} else {
  message("skipping functionality due to missing Suggested dependency")
}
```

| | |
|----------------|--|
| K1XQStationary | <i>Impose stationarity under the Q-measure</i> |
|----------------|--|

Description

Impose stationarity under the Q-measure

Usage

```
K1XQStationary(StationaryEigenvalues)
```

Arguments

StationaryEigenvalues

Binary variable: set "1" if the user whises the largest eigenvalue to be strictly smaller than 1. Set "0", otherwise

Value

list

Examples

```
stat <- 1 # Takes values 1 and 0  
K1XQStationary(stat)
```

| | |
|-------|-------------------------|
| killa | <i>Eliminates the @</i> |
|-------|-------------------------|

Description

Eliminates the @

Usage

```
killa(s)
```

Arguments

s text vector containing the feature of the variable

References

This function is a modified version of the "kill" function by Le and Singleton (2018). "A Small Package of Matlab Routines for the Estimation of Some Term Structure Models." (Euro Area Business Cycle Network Training School - Term Structure Modelling).

| | |
|---------------|---|
| LabelsSpanned | <i>Generate the labels of the spanned factors</i> |
|---------------|---|

Description

Generate the labels of the spanned factors

Usage

LabelsSpanned(N)

Arguments

| | |
|---|---------------------------|
| N | number of spanned factors |
|---|---------------------------|

| | |
|------------|--|
| LabelsStar | <i>Generate the labels of the star variables</i> |
|------------|--|

Description

Generate the labels of the star variables

Usage

LabelsStar(FactorLabels)

Arguments

| | |
|--------------|---------------|
| FactorLabels | Factor labels |
|--------------|---------------|

| | |
|--------|-------------------------------------|
| LabFac | <i>Generates the labels factors</i> |
|--------|-------------------------------------|

Description

Generates the labels factors

Usage

LabFac(N, DomVar, GlobalVar, Economies, ModelType)

Arguments

| | |
|-----------|---|
| N | number of spanned factors per country (scalar) |
| DomVar | character-vector containing the names of the domestic variables |
| GlobalVar | character-vector containing the names of the global variables |
| Economies | string-vector containing the names of the economies which are part of the economic system |
| ModelType | string-vector containing the label of the model to be estimated |

Value

List containing the country-specific risk factor labels

Examples

```
N <- 2
DomVar <- c("inflation", "Economic growth")
GlobalVar <- "Commodity Prices"
Economies <- c("U.S.", "Canada", "Germany", "Japan")
ModelType <- "JPS"

VarLabels <- LabFac(N, DomVar, GlobalVar, Economies, ModelType)
```

Maturities

Create a vector of numerical maturities in years

Description

Create a vector of numerical maturities in years

Usage

```
Maturities(DataYields, Economies, UnitYields)
```

Arguments

| | |
|------------|---|
| DataYields | matrix containing all yields of the system (JxT,if the model is single-country-based or CJxT if the model is multy-country-based) |
| Economies | vector containing names of all the economies of the system |
| UnitYields | (i) "Month": if maturity of yields are expressed in months or (ii) "Year": if maturity of yields are expressed in years |

Value

Vector containing all observed maturities expressed in years

Examples

```
data('CM_Yields')
Economies <- c("China", "Brazil", "Mexico", "Uruguay")
Maturities(Yields, Economies, "Month")
```

MLEdensity_jointQ *Compute the maximum likelihood function ("joint Q" models)*

Description

Compute the maximum likelihood function ("joint Q" models)

Usage

```
MLEdensity_jointQ(
  K1XQ,
  r0,
  SSZ,
  K0Z,
  K1Z,
  se,
  Gy.0,
  mat,
  Y,
  Z,
  P,
  Wpca,
  We,
  WpcaFull,
  dt,
  Economies,
  FactorLabels,
  ModelType,
  GVARinputs,
  JLLinputs,
  nargout
)
```

Arguments

| | |
|------|---|
| K1XQ | risk-neutral feedback matrix (N×N) |
| r0 | long-run interest rate (scalar) |
| SSZ | variance-covariance matrix (K×K) |
| K0Z | intercept from the P-dynamics (K×1) |
| K1Z | feedback matrix from the P-dynamics (K×K) |

| | |
|--------------|---|
| se | Variance of the portfolio of yields observed with error (scalar) |
| Gy.0 | matrix of contemporaneous terms from the P-dynamics (KxK) |
| mat | vector of maturities (in years) of yields used in estimation (J x 1) |
| Y | matrix of yields used in estimation (J x T) |
| Z | complete set of spanned and unspanned factors (KxT) |
| P | complete set of spanned factors (NxT) |
| Wpca | matrix of weights of the portfolios observed without errors (NxJ) |
| We | matrix of weights of the portfolios observed with errors ((J-N)xJ) |
| WpcaFull | composite matrix of weights the portfolios observed with and without errors |
| dt | time interval unit of the model (scalar). For instance, if data is (i) monthly, dt <- 12; (ii) quarterly, dt <- 4; (iii) yearly, dt <- 1. |
| Economies | set of economies that are part of the economic system (vector of text) |
| FactorLabels | string-list based which contains the labels of all the variables present in the model |
| ModelType | feasible options are (i) "VAR jointQ", (ii) "GVAR jointQ" or (iii) "JLL jointSigma" |
| GVARinputs | if the model chosen is the "GVAR sepQ", the "GVARinputs" should be specified (see "GVAR" function) |
| JLLinputs | if the model chosen is the "JLL jointSigma". "JLLinputs" should contain (i) DomUnit, (ii) WishSigmas, (iii) SigmaNonOrtho, (iv) JLLModelType (See JLL function) |
| nargout | if nargout== 1: provides only the values of the likelihood; if nargout== 2: complete ATSM outputs |

References

This function is an extended version of the "AON_MLEdensity_WOE" function by Le and Singleton (2018).
 "A Small Package of Matlab Routines for the Estimation of Some Term Structure Models."
 (Euro Area Business Cycle Network Training School - Term Structure Modelling). Available at:
<https://cepr.org/40029>

MLEdensity_jointQ_sepSigma

Compute the maximum likelihood function ("joint Q" models for separate Sigma estimation)

Description

Compute the maximum likelihood function ("joint Q" models for separate Sigma estimation)

Usage

```
MLEdensity_jointQ_sepSigma(
  K1XQ,
  r0,
  SSZ,
  K0Z,
  K1Z,
  se,
  Gy.0,
  mat,
  Y,
  Z,
  P,
  Wpca,
  We,
  WpcaFull,
  dt,
  Economies,
  FactorLabels,
  ModelType,
  JLLinputs,
  nargout
)
```

Arguments

| | |
|-----------|---|
| K1XQ | risk-neutral feedback matrix (NxN) |
| r0 | long-run interest rate (scalar) |
| SSZ | variance-covariance matrix (KxK) |
| K0Z | intercept from the P-dynamics (Kx1) |
| K1Z | feedback matrix from the P-dynamics (KxK) |
| se | Variance of the portfolio of yields observed with error (scalar) |
| Gy.0 | matrix of contemporaneous terms from the P-dynamics (KxK) |
| mat | vector of maturities (in years) of yields used in estimation (J x 1) |
| Y | matrix of yields used in estimation (J x T) |
| Z | complete set of spanned and unspanned factors (KxT) |
| P | complete set of spanned factors (NxT) |
| Wpca | matrix of weights of the portfolios observed without errors (NxJ) |
| We | matrix of weights of the portfolios observed with errors ((J-N)xJ) |
| WpcaFull | composite matrix of weights the portfolios observed with and without errors |
| dt | time interval unit of the model (scalar). For instance, if data is (i) monthly, dt <- 12; (ii) quarterly, dt <- 4; (iii) yearly, dt <- 1. |
| Economies | Set of economies that are part of the economic system (vector of text) |

| | |
|--------------|---|
| FactorLabels | string-list based which contains the labels of all the variables present in the model |
| ModelType | feasible options are (i) "JLL original" or (ii) "JLL NoDomUnit" |
| JLLinputs | if the model chosen is the "JLL jointSigma", "JLLinputs" should be specified (see "JLL" function) |
| nargout | if nargout== 1: provides only the values of the likelihood; if nargout== 2: complete ATSM outputs |

References

This function is an extended version of the "AON_MLEdensity_WOE" function by Le and Singleton (2018).

"A Small Package of Matlab Routines for the Estimation of Some Term Structure Models."

(Euro Area Business Cycle Network Training School - Term Structure Modelling). Available at: <https://cepr.org/40029>

| | |
|-----------------|---|
| MLEdensity_sepQ | <i>Compute the maximum likelihood function ("sep Q" models)</i> |
|-----------------|---|

Description

Compute the maximum likelihood function ("sep Q" models)

Usage

```
MLEdensity_sepQ(
    K1XQ,
    r0,
    SSZ,
    K0Z,
    K1Z,
    se,
    Gy.0,
    mat,
    Y,
    Z,
    P,
    Wpca,
    We,
    WpcaFull,
    dt,
    Economy,
    FactorLabels,
    ModelType,
    GVARinputs = NULL,
    nargout
)
```

Arguments

| | |
|--------------|---|
| K1XQ | risk-neutral feedback matrix (N×N) |
| r0 | long-run interest rate (scalar) |
| SSZ | variance-covariance matrix (K×K) |
| K0Z | intercept from the P-dynamics (K×1) |
| K1Z | feedback matrix from the P-dynamics (K×K) |
| se | Variance of the portfolio of yields observed with error (scalar) |
| Gy.0 | matrix of contemporaneous terms from the P-dynamics (K×K) |
| mat | vector of maturities (in years) of yields used in estimation (J x 1) |
| Y | matrix of yields used in estimation (J x T) |
| Z | complete set of spanned and unspanned factors (K×T) |
| P | complete set of spanned factors (N×T) |
| Wpca | matrix of weights of the portfolios observed without errors (N×J) |
| We | matrix of weights of the portfolios observed with errors ((J-N)×J) |
| WpcaFull | composite matrix of weights the portfolios observed with and without errors |
| dt | time interval unit of the model (scalar). For instance, if data is (i) monthly, dt <- 12; (ii) quarterly, dt <- 4; (iii) yearly, dt <- 1. |
| Economy | name of the economy under study |
| FactorLabels | string-list based which contains the labels of all the variables present in the model |
| ModelType | Feasible options are: (i) "JPS", (ii) "JPS jointP" or (iii) "GVAR sepQ" |
| GVARinputs | if the model chosen is the "GVAR sepQ", the "GVARinputs" should be specified (see "GVAR" function) |
| nargout | if nargout== 1: provides only the values of the likelihood; if nargout== 2: complete ATSM outputs |

References

This function is modified version of the "A0N_MLEdensity_WOE" function by Le and Singleton (2018).

"A Small Package of Matlab Routines for the Estimation of Some Term Structure Models." (Euro Area Business Cycle Network Training School - Term Structure Modelling). Available at: <https://cepr.org/40029>

ModelPara

Replications of the JPS (2014) outputs by the MultiATSM package

Description

Unspanned macro risk model outputs by the MultiATSM package

Usage

```
data("JPSrep")
```

Format

list of inputs and outputs

inputs general model inputs

ests model parameters estimates (JPS form)

llk log-likelihood of the observations

rot model parameters estimates (rotation form)

MultiATSM

ATSM Package

Description

Estimation of several classes of affine term structure of interest rates models.

Author(s)

Rubens Moura <rubens.gtmoura@gmail.com>

| | |
|------------|--|
| NumOutputs | <i>Construct the model numerical outputs (model fit, IRFs, GIRFs, FEVDs, and GFEVDs)</i> |
|------------|--|

Description

Construct the model numerical outputs (model fit, IRFs, GIRFs, FEVDs, and GFEVDs)

Usage

```
NumOutputs(ModelType, ModelPara, InputsForOutputs, FactorLabels, Economies)
```

Arguments

| | |
|------------------|--|
| ModelType | a string-vector containing the label of the model to be estimated |
| ModelPara | List of model parameter estimates (See the "Optimization" function) |
| InputsForOutputs | list conataining the desired horizon of analysis for the model fit, IRFs, GIRFs, FEVDs, and GFEVDs |
| FactorLabels | a string-list based which contains all the labels of all the variables present in the model |
| Economies | a string-vector containing the names of the economies which are part of the economic system |

Value

List of the model numerical outputs, namely

1. Model fit of bond yields
2. IRFs
3. FEVDs
4. GIRFs
5. GFEVDs

Examples

```
# See examples in the vignette file of this package (Section 4).
```

NumOutputs_Bootstrap *Numerical outputs (IRFs, GIRFs, FEVD, and GFEVD) for bootstrap*

Description

Numerical outputs (IRFs, GIRFs, FEVD, and GFEVD) for bootstrap

Usage

```
NumOutputs_Bootstrap(  
  ModelType,  
  ModelParaBoot,  
  InputsForOutputs,  
  FactorLabels,  
  Economies  
)
```

Arguments

| | |
|------------------|--|
| ModelType | string-vector containing the label of the model to be estimated |
| ModelParaBoot | list of model parameter estimates (see the "Optimization" function) after a bootstrap draw |
| InputsForOutputs | list containing the desired inputs for the construction of the model fit, IRFs, GIRFs, FEVDs, and GFEVDs |
| FactorLabels | string-list based which contains all the labels of all the variables present in the model |
| Economies | string-vector containing the names of the economies which are part of the economic system |

Optimization *Perform the minimization of mean(f)*

Description

Perform the minimization of mean(f)

Usage

```
Optimization(  
  f,  
  tol,  
  varargin,  
  FactorLabels,
```

```

Economies,
ModelType,
JLLinputs = NULL,
GVARinputs = NULL
)

```

Arguments

| | |
|---------------------------|---|
| <code>f</code> | vector-valued objective function (function) |
| <code>tol</code> | convergence tolerance (scalar). For ML estimation, a reasonable value is <code>tol <- 1e-4</code> |
| <code>varargin</code> | list containing starting values and constraints: for each input argument <code>K</code> (of <code>f</code>), we need four inputs that look like: <ol style="list-style-type: none"> a starting value: <code>K0</code> a variable label (<code>'K0'</code>) followed by a <code>':'</code> followed by a type of constraint. The constraint can be: <ul style="list-style-type: none"> <code>'bounded'</code>: bounded matrix; <code>'Jordan'</code> or <code>'Jordan MultiCountry'</code>: a matrix of Jordan type; <code>'psd'</code>: psd matrix; <code>'stationary'</code>: largest eigenvalue of the risk-neutral feedback matrix is strictly smaller than 1; <code>'diag'</code> or <code>'BlockDiag'</code>: a diagonal or block diagonal matrix. <code>'JLLstructure'</code>: to impose the zero-restrictions on the variance-covariance matrix along the lines of the JLL models a lower bound <code>lb</code> (<code>lb <- NULL</code> -> no lower bound) an upper bound <code>ub</code> (<code>ub <- NULL</code> -> no upper bound) Specification of the optimization settings: <ul style="list-style-type: none"> <code>'iter off'</code>: hide the printouts of the numerical optimization routines; <code>'fminunc only'</code>: only uses <code>fminunc</code> for the optimization; <code>'fminsearch only'</code>: only uses <code>fminsearch</code> for the optimization. |
| <code>FactorLabels</code> | string-list based which contains the labels of all the variables present in the model |
| <code>Economies</code> | string-vector containing the names of the economies which are part of the economic system |
| <code>ModelType</code> | string-vector containing the label of the model to be estimated |
| <code>JLLinputs</code> | inputs used in the estimation of the JLL-based models; Default is set to <code>NULL</code> |
| <code>GVARinputs</code> | inputs used in the estimation of the GVAR-based models; Default is set to <code>NULL</code> |

Details

If a variable name starts with a `'@'`, it means that that parameter will be analytically concentrated out in the specification of `f`. In this case, no starting value is needed for this particular parameter (an empty matrix can be provided as a starting value).

Value

- (i) out: list of second output produced by f (the first output of f must be the objective value to be minimized).
- (ii) x: list containing parameter estimates

References

This function is based on the "LS__opt" function by Le and Singleton (2018).
 "A Small Package of Matlab Routines for the Estimation of Some Term Structure Models."
 (Euro Area Business Cycle Network Training School - Term Structure Modelling). Available at:
<https://cepr.org/40029>

Examples

#' # See examples in the vignette file of this package (Section 4).

| | |
|-------------------|--|
| Optimization_Boot | <i>Perform the minimization of mean(f) (adapted for the bootstrap setting)</i> |
|-------------------|--|

Description

Perform the minimization of mean(f) (adapted for the bootstrap setting)

Usage

```
Optimization_Boot(
  f,
  tol,
  varargin,
  FactorLabels,
  Economies,
  ModelType,
  JLLinputs = NULL,
  GVARinputs = NULL
)
```

Arguments

- | | |
|----------|--|
| f | vector-valued objective function (function) |
| tol | convergence tolerance (scalar). For ML estimation, a reasonable value is $\text{tol} < 1e-4$ |
| varargin | list containing starting values and constraints: for each input argument K (of f), we need four inputs that look like: <ol style="list-style-type: none"> 1. a starting value: K0 |

2. a variable label ('K0') followed by a ':' followed by a type of constraint. The constraint can be:
 - 'bounded': bounded matrix;
 - 'Jordan' or 'Jordan MultiCountry': a matrix of Jordan type;
 - 'psd': psd matrix;
 - 'stationary': largest eigenvalue of the risk-neutral feedback matrix is strictly smaller than 1;
 - 'diag' or 'BlockDiag': a diagonal or block diagonal matrix.
 - 'JLLstructure': to impose the zero-restrictions on the variance-covariance matrix along the lines of the JLL models
3. a lower bound lb (lb <- NULL -> no lower bound)
4. an upper bound ub (ub <- NULL -> no upper bound)
5. Specification of the optimization settings:
 - 'iter off': hide the printouts of the numerical optimization routines;
 - 'fminunc only': only uses fminunc for the optimization;
 - 'fminsearch only': only uses fminsearch for the optimization.

| | |
|--------------|---|
| FactorLabels | string-list based which contains the labels of all the variables present in the model |
| Economies | string-vector containing the names of the economies which are part of the economic system |
| ModelType | string-vector containing the label of the model to be estimated |
| JLLinputs | inputs used in the estimation of the JLL-based models; Default is set to NULL |
| GVARinputs | inputs used in the estimation of the GVAR-based models; Default is set to NULL |

Details

If a variable name starts with a '@', it means that that parameter will be analytically concentrated out in the specification of f . In this case, no starting value is needed for this particular parameter. An empty matrix can be provided as a starting value

Value

- (i) out: list of second output produced by f (the first output of f must be the objective value to be minimized)
- (ii) x: list containing parameter estimates

References

This function is based on the "LS__opt" function by Le and Singleton (2018).
 "A Small Package of Matlab Routines for the Estimation of Some Term Structure Models."
 (Euro Area Business Cycle Network Training School - Term Structure Modelling). Available at:
<https://cepr.org/40029>

OutputConstructionJoint

Numerical outputs (variance explained, model fit, IRFs, GIRFs, FEVDs, and GFEVDs) for "joint Q" models

Description

Numerical outputs (variance explained, model fit, IRFs, GIRFs, FEVDs, and GFEVDs) for "joint Q" models

Usage

```
OutputConstructionJoint(
  ModelType,
  ModelPara,
  InputsForOutputs,
  FactorLabels,
  Economies
)
```

Arguments

| | |
|------------------|---|
| ModelType | string-vector containing the label of the model to be estimated |
| ModelPara | list of model parameter estimates (see the "Optimization" function) |
| InputsForOutputs | list containing the desired horizon of analysis for the model fit, IRFs, GIRFs, FEVDs, and GFEVDs |
| FactorLabels | string-list based which contains all the labels of all the variables present in the model |
| Economies | string-vector containing the names of the economies which are part of the economic system |

OutputConstructionJoint_BS

Gathers all the model numerical outputs after bootstrap for "joint Q" models

Description

Gathers all the model numerical outputs after bootstrap for "joint Q" models

Usage

```
OutputConstructionJoint_BS(
  ModelType,
  ModelParaBoot,
  InputsForOutputs,
  FactorLabels,
  Economies
)
```

Arguments

| | |
|------------------|--|
| ModelType | string-vector containing the label of the model to be estimated |
| ModelParaBoot | list of model parameter estimates (see the "Optimization" function) after a bootstrap draw |
| InputsForOutputs | list containing the desired inputs for the construction of IRFs, GIRFs, FEVDs, and GFEVDs |
| FactorLabels | string-list based which contains all the labels of all the variables present in the model |
| Economies | string-vector containing the names of the economies which are part of the economic system |

OutputConstructionSep *Numerical outputs (variance explained, model fit, IRFs, GIRFs, FEVDs, and GFEVDs) for "sep Q" models*

Description

Numerical outputs (variance explained, model fit, IRFs, GIRFs, FEVDs, and GFEVDs) for "sep Q" models

Usage

```
OutputConstructionSep(
  ModelType,
  ModelPara,
  InputsForOutputs,
  FactorLabels,
  Economies
)
```


Arguments

| | |
|------------------|--|
| ModelType | string-vector containing the label of the model to be estimated |
| ModelPara | list of model parameter estimates (See the "Optimization" function) |
| InputsForOutputs | list conataining the desired horizon of analysis for the model fit, IRFs, GIRFs, FEVDs, and GFEVDs |
| FactorLabels | string-list based which contains all the labels of all the variables present in the model |
| Economies | string-vector containing the names of the economies which are part of the economic system |

OutputConstructionSep_BS

Gathers all the model numerical ouputs after bootstrap for "sep Q" models

Description

Gathers all the model numerical ouputs after bootstrap for "sep Q" models

Usage

```
OutputConstructionSep_BS(  
  ModelType,  
  ModelParaBoot,  
  InputsForOutputs,  
  FactorLabels,  
  Economies  
)
```

Arguments

| | |
|------------------|---|
| ModelType | string-vector containing the label of the model to be estimated |
| ModelParaBoot | list of model parameter estimates (see the "Optimization" function) after a bootstrap draw |
| InputsForOutputs | list conataining the desired inputs for the cunstruction of the model fit, IRFs, GIRFs, FEVDs, and GFEVDs |
| FactorLabels | string-list based which contains all the labels of all the variables present in the model |
| Economies | string-vector containing the names of the economies which are part of the economic system |

| | |
|------------|--|
| ParaLabels | <i>Create the variable labels used in the estimation</i> |
|------------|--|

Description

Create the variable labels used in the estimation

Usage

```
ParaLabels(ModelType, WishStationarityQ)
```

Arguments

| | |
|-------------------|---|
| ModelType | a string-vector containing the label of the model to be estimated |
| WishStationarityQ | User must set "1" if she wishes to impose the largest eigenvalue under the Q to be strictly smaller than 1. Otherwise set "0" |

Value

list containing the features of the parameters that will be used in the estimation

Examples

```
ModelType <- "GVAR jointQ"
WishStationarityQ <- 1
ParaLabels(ModelType, WishStationarityQ)
```

| | |
|-------------------------|---|
| pca_weights_one_country | <i>Weight matrix from principal components (matrix of eigenvectors)</i> |
|-------------------------|---|

Description

Weight matrix from principal components (matrix of eigenvectors)

Usage

```
pca_weights_one_country(Y, Economy)
```

Arguments

| | |
|---------|---|
| Y | matrix dimension (J x T), where J - the number of maturities and T - time series length |
| Economy | string-vector containing the name of one economy |

Value

matrix (J x J)

Examples

```
data("CM_Yields")
pca_weights_one_country(Yields, Economy= "Brazil")
```

| | |
|-----------------|--|
| PdynamicsSet_BS | <i>Compute some key parameters from the P-dynamics (Bootstrap set)</i> |
|-----------------|--|

Description

Compute some key parameters from the P-dynamics (Bootstrap set)

Usage

```
PdynamicsSet_BS(  
  ModelType,  
  AllFactorsUnderP,  
  FactorLabels,  
  Economies,  
  JLLinputs = NULL,  
  GVARinputs = NULL  
)
```

Arguments

| | |
|------------------|---|
| ModelType | string-vector containing the label of the model to be estimated |
| AllFactorsUnderP | complete set of factors that may be used in the estimation of P (KxT) |
| FactorLabels | string-list based which contains the labels of all the variables present in the model (see "LabFac" function) |
| Economies | string-vector containing the names of the economies which are part of the economic system |
| JLLinputs | List containing the necessary inputs for the estimation of the JLL-based models (see "JLL" function). Default is set to NULL. |
| GVARinputs | List containing the necessary inputs for the estimation of the GVAR-based models (see "GVAR" function). Default is set to NULL. |

 pos2x

Transform a positive number y to back to x by:

Description

Transform a positive number y to back to x by:

Usage

pos2x(y)

Arguments

y scalar

References

This function is based on the "pos2x" function by Le and Singleton (2018).
 "A Small Package of Matlab Routines for the Estimation of Some Term Structure Models."
 (Euro Area Business Cycle Network Training School - Term Structure Modelling). Available at:
<https://cepr.org/40029>

 Reg_K1Q

Estimate the risk-neutral feedback matrix K1Q using linear regressions

Description

Estimate the risk-neutral feedback matrix K1Q using linear regressions

Usage

Reg_K1Q(Y, mat, Z, dt, type)

Arguments

Y matrix of yields used in estimation (J x T)
 mat vector of maturities (in years) of yields used in estimation (J x 1)
 Z pricing factors (can be yields-based or non-yields/macro variables) (N x T)
 dt time unit of the model (scalar). For instance, if data is (i) monthly, dt <- 12; (ii) quarterly, dt <- 4; (iii) yearly, dt <- 1.
 type 'Jordan' -> K1Q will be of the Jordan type

Value

Risk neutral feedback matrix K1Q.

References

This function is based on the "Reg_K1Q" function by Le and Singleton (2018).
 "A Small Package of Matlab Routines for the Estimation of Some Term Structure Models."
 (Euro Area Business Cycle Network Training School - Term Structure Modelling). Available at:
<https://cepr.org/40029>

Examples

```
data(CM_Yields)

Y_China <- Yields[1:6,]
Z_China <- Spanned_Factors(Y_China, Economies ="China", N=3)
mat <-c(0.25 , 0.5 , 1, 3, 5, 10)
dt <- 1/12
type <- 'Jordan'
Reg_K1Q(Y_China, mat, Z_China, dt, type)
```

Reg_OLSconstrained *Restricted OLS regression*

Description

Restricted OLS regression

Usage

```
Reg_OLSconstrained(Y, X, Bcon, G)
```

Arguments

| | |
|------|--|
| Y | left hand side variables (M x T) |
| X | regressors (i.e. N-1 variables + the intercept) (N x T) |
| Bcon | constraints matrix (M x N). If Bcon(i,j) = nan -> B(i,j) is a free parameter |
| G | weighting matrix (psd) - (M x M). Default is set to be identity |

Details

Estimate of B is obtained by minimizing the objective:
 $\sum_t (Y_t - B X_t)' G^{-1} (Y_t - B X_t)$
 subject to the constraint that $B = Bcon$ for all non-nan entries of Bcon

Value

matrix of coefficient (M x N)

References

This function is based on the "Reg__OLSconstrained" function by Le and Singleton (2018).
 "A Small Package of Matlab Routines for the Estimation of Some Term Structure Models."
 (Euro Area Business Cycle Network Training School - Term Structure Modelling). Available at:
<https://cepr.org/40029>

| | |
|----------|--|
| RemoveNA | <i>Exclude series that contain NAs</i> |
|----------|--|

Description

Exclude series that contain NAs

Usage

RemoveNA(YieldsData, MacroData, Economies)

Arguments

| | |
|------------|---|
| YieldsData | List of country-specific bond yields |
| MacroData | List of country-specific and global economic variables |
| Economies | string-vector containing the names of the economies which are part of the economic system |

Value

return the time series data that were not initially composed by NAs.

| | |
|-------------|---|
| RiskFactors | <i>Data: Risk Factors - Candelon and Moura (2021)</i> |
|-------------|---|

Description

Risk factors data used in Candelon and Moura (2021)

Usage

data("CM_Factors")

Format

matrix containing the risk factors of the models

References

Candelon, B. and Moura, R. "A Multi-Country Model of the Term Structures of Interest Rates with a GVAR".

| | |
|-------------------|---|
| RiskFactorsGraphs | <i>Spanned and unspanned factors plot</i> |
|-------------------|---|

Description

Spanned and unspanned factors plot

Usage

```
RiskFactorsGraphs(ModelType, ModelOutputs, Economies, FactorLabels)
```

Arguments

| | |
|--------------|---|
| ModelType | string-vector containing the label of the model to be estimated |
| ModelOutputs | list of model parameter estimates (see the "Optimization" function) |
| Economies | string-vector containing the names of the economies which are part of the economic system |
| FactorLabels | string-list based which contains the labels of all the variables present in the model |

| | |
|-----------------|---|
| RiskFactorsPrep | <i>Builds the complete set of time series of the risk factors (spanned and unspanned)</i> |
|-----------------|---|

Description

Builds the complete set of time series of the risk factors (spanned and unspanned)

Usage

```
RiskFactorsPrep(
  FactorSet,
  Economies,
  FactorLabels,
  Initial_Date,
  Final_Date,
  DataFrequency
)
```

Arguments

| | |
|---------------|---|
| FactorSet | Factor set list (see e.g. "CM_Factors_GVAR" data file) |
| Economies | string-vector containing the names of the economies which are part of the economic system |
| FactorLabels | string-list based which contains the labels of all the variables present in the model |
| Initial_Date | Sample starting date (yyyy-mm-dd) |
| Final_Date | Sample last date (yyyy-mm-dd) |
| DataFrequency | character-based vector: "Daily All Days", "Daily Business Days", "Weekly", "Monthly", "Quarterly", "Annually" |

Value

Risk factors used in the estimation of the desired ATSM

| | |
|-----------|--|
| RMSEjoint | <i>Compute the root mean square error ("joint Q" models)</i> |
|-----------|--|

Description

Compute the root mean square error ("joint Q" models)

Usage

RMSEjoint(ForecastOutputs)

Arguments

| | |
|-----------------|--|
| ForecastOutputs | List of country-specific forecasts (see "ForecastYieldsjointQ" function) |
|-----------------|--|

| | |
|---------|--|
| RMSEsep | <i>Compute the root mean square error ("sep Q" models)</i> |
|---------|--|

Description

Compute the root mean square error ("sep Q" models)

Usage

RMSEsep(ForecastOutputs)

Arguments

| | |
|-----------------|--|
| ForecastOutputs | List of country-specific forecasts (see "ForecastYieldsSepQ" function) |
|-----------------|--|

SpannedFactorsjointQ *Gather all spanned factors ("joint Q" models)*

Description

Gather all spanned factors ("joint Q" models)

Usage

SpannedFactorsjointQ(ModelType, ModelPara, Economies, t0Sample, tlastObserved)

Arguments

| | |
|---------------|---|
| ModelType | string-vector containing the label of the model to be estimated |
| ModelPara | set of model parameters |
| Economies | string-vector containing the names of the economies which are part of the economic system |
| t0Sample | index for the initial sample date |
| tlastObserved | index for the last observation of the information set |

SpannedFactorsSepQ *Gather all spanned factors ("sep Q" models)*

Description

Gather all spanned factors ("sep Q" models)

Usage

SpannedFactorsSepQ(ModelType, ModelPara, Economies, t0Sample, tlastObserved)

Arguments

| | |
|---------------|---|
| ModelType | string-vector containing the label of the model to be estimated |
| ModelPara | set of model parameters |
| Economies | string-vector containing the names of the economies which are part of the economic system |
| t0Sample | index for the initial sample date |
| tlastObserved | index for the last observation of the information set |

Spanned_Factors *Compute the country-specific spanned factors*

Description

Compute the country-specific spanned factors

Usage

```
Spanned_Factors(Yields, Economies, N)
```

Arguments

Yields matrix (J x T), where J - the number of maturities and T - time series length
Economies C-dimensional string-vector containing the names of the economies which are part of the economic system
N scalar: desired number of spanned factors (maximum number allowed is N= J)

Value

Matrix containing the N spanned for all the countries of the system (CJ xT)

Examples

```
data(CM_Yields)
Economies <- c("China", "Brazil", "Mexico", "Uruguay")
N <- 3
Spanned_Factors(Yields, Economies, N)
```

sqrtm_robust *Compute the square root of a matrix*

Description

Compute the square root of a matrix

Usage

```
sqrtm_robust(m)
```

Arguments

m squared matrix (KxK)

Value

squared matrix x ($K \times K$) such that x

References

#' This function is a modified version of the "sqrtm_robust" function by Le and Singleton (2018).
 "A Small Package of Matlab Routines for the Estimation of Some Term Structure Models."
 (Euro Area Business Cycle Network Training School - Term Structure Modelling). Available at:
<https://cepr.org/40029>

 StarFactors

Generates the star variables necessary for the GVAR estimation

Description

Generates the star variables necessary for the GVAR estimation

Usage

```
StarFactors(RiskFactors, Economies, W)
```

Arguments

| | |
|-------------|---|
| RiskFactors | time series of the risk factors ($F \times T$) |
| Economies | string-vector containing the names of the economies which are part of the economic system |
| W | GVAR transition matrix ($C \times C$) |

Value

List containing the star factors of each country of the economic system

Examples

```
data(CM_Factors)
Economies <- c("China", "Brazil", "Mexico", "Uruguay")
Wgvar <- matrix( c(0, 0.83, 0.86, 0.38, 0.65, 0, 0.13, 0.55,
                  0.32, 0.12, 0, 0.07, 0.03, 0.05, 0.01, 0), nrow = 4, ncol = 4)
rownames(Wgvar) <- Economies
colnames(Wgvar) <- Economies
StarFactors(RiskFactors, Economies, Wgvar)
```

| | |
|------------|--|
| TradeFlows | <i>Data: Trade Flows - Candelon and Moura (2021)</i> |
|------------|--|

Description

Trade Flows data used in Candelon and Moura (2021)

Usage

```
data("CM_Trade")
```

Format

list containing the bilateral trade flows

References

Candelon, B. and Moura, R. "A Multi-Country Model of the Term Structures of Interest Rates with a GVAR".

| | |
|-------------------|---|
| Transition_Matrix | <i>Compute the transition matrix required in the estimation of the GVAR model</i> |
|-------------------|---|

Description

Compute the transition matrix required in the estimation of the GVAR model

Usage

```
Transition_Matrix(  
  t_First,  
  t_Last,  
  Economies,  
  type,  
  DataPath = NULL,  
  Data = NULL  
)
```

Arguments

| | |
|-----------|--|
| t_First | Sample starting date (year) |
| t_Last | Sample last date (year) |
| Economies | Vector containing the names of all the economies of the system. |
| type | Three possibilities: <ul style="list-style-type: none"> • "Full Sample": if one wishes ALL weight matrices of each year from which data is available (it may extrapolate the sample period); • "Sample Mean": if one wishes a SINGLE weight matrix containing the average of weights over of the entire sample period; • Some year in particular (e.g. "1998", "2005" ...). |
| DataPath | path of the Excel file containing the data (if any). The default is linked to the Excel file available in the package. |
| Data | Data for computing the transition matrix. Default is set to NULL. |

Details

NOTE: if there is missing data for any country of the system for that particularly year, then the transition matrix will include only NAs.

Value

matrix or list of matrices

Examples

```
data(CM_Trade)

t_First <- "2006"
t_Last <- "2019"
Economies <- c("China", "Brazil", "Mexico", "Uruguay")
type <- "Sample Mean"
Transition_Matrix(t_First, t_Last, Economies, type, DataPath = NULL, Data = TradeFlows)
```

true2aux *Map constrained parameters b to unconstrained auxiliary parameters a.*

Description

Map constrained parameters b to unconstrained auxiliary parameters a.

Usage

```
true2aux(b, ctype, lb, ub, Economies, FactorLabels, JLLinputs = NULL)
```

Arguments

| | |
|--------------|--|
| b | Constrained parameter |
| ctype | character-based vector that describes the constraints. Constraints are: <ul style="list-style-type: none"> • 'Jordan'; • 'Jordan; stationary' • 'Jordan MultiCountry' • 'Jordan MultiCountry; stationary' • 'stationary' • 'psd' • 'BlockDiag' • 'bounded' • 'diag' • 'JLLstructure' |
| lb | lower bounds of b (for the bounded case). Accomodates a scalar or a matrix. |
| ub | upper bounds of b (for the bounded case). Accomodates a scalar or a matrix. |
| Economies | string-vector containing the names of the economies which are part of the economic system |
| FactorLabels | string-list based which contains the labels of all the variables present in the model |
| JLLinputs | list of necessary inputs for the estimation of JLL-based models (see "JLL" function) |

Value

unconstrained auxiliary matrix.

References

This function is a modified and extended version of the "true2aux" function by Le and Singleton (2018).

"A Small Package of Matlab Routines for the Estimation of Some Term Structure Models." (Euro Area Business Cycle Network Training School - Term Structure Modelling). Available at: <https://cepr.org/40029>

| | |
|-------------|--|
| update_para | <i>converts the vectorized auxiliary parameter vector x to the parameters that go directly into the likelihood function.</i> |
|-------------|--|

Description

converts the vectorized auxiliary parameter vector x to the parameters that go directly into the likelihood function.

Usage

```

update_para(
    x,
    sizex,
    ii,
    con,
    FactorLabels,
    Economies,
    JLLinputs = NULL,
    GVARinputs = NULL,
    varargin
)

```

Arguments

| | |
|--------------|--|
| x | vector containing all the vectorized auxiliary parameters |
| sizex | matrix (6x2) containing the size information of all parameters |
| ii | if empty: converts all the parameters; otherwise converts some specific parameters |
| con | if con = 'concentration', then set the value of the parameter whose name contains @ to empty |
| FactorLabels | string-list based which contains the labels of all the variables present in the model |
| Economies | string-vector containing the names of the economies which are part of the economic system |
| JLLinputs | Set of necessary inputs used in the estimation of the JLL-based models |
| GVARinputs | Set of necessary inputs used in the estimation of the GVAR-based models |
| varargin | variable inputs used in the optimization (see "Optimization" function) |

Value

same form as varargin, except now the parameters are updated with the values provided by the auxiliary x. Importantly, by construction, all the constraints on the underlying parameters are satisfied.

References

This function is a modified version of the "update_para" function by Le and Singleton (2018). "A Small Package of Matlab Routines for the Estimation of Some Term Structure Models." (Euro Area Business Cycle Network Training School - Term Structure Modelling). Available at: <https://cepr.org/40029>

VAR *Estimates a VAR(1)*

Description

Estimates a VAR(1)

Usage

```
VAR(RiskFactors, VARtype, Bcon = NULL)
```

Arguments

| | |
|-------------|--|
| RiskFactors | matrix containing all the risk factors (K x T) |
| VARtype | string-vector which accommodates two possibilities: 'unconstrained' or 'constrained' |
| Bcon | constraints matrix (K+1 x N) - should contain an intercept. If Bcon(i,j) = nan -> B(i,j) is a free parameter. Default is set to NULL. |

Value

intercept, feedback matrix and the variance-covariance matrix of a VAR(1)

Examples

```
data("CM_Factors")
#Example 1
VAR(RiskFactors, VARtype= 'unconstrained')
#Example 2
K <- nrow(RiskFactors)
Bcon <-matrix(0, nrow = K, ncol = K+1)
Bcon[,1:3] <- NaN
VAR(RiskFactors, VARtype= 'constrained', Bcon)
```

VarianceExplainedJoint

Percentage explained by the spanned factors of the variations in the set of observed yields for "joint Q" models

Description

Percentage explained by the spanned factors of the variations in the set of observed yields for "joint Q" models

Usage

VarianceExplainedJoint(ModelType, ModelPara, FactorLabels, Economies)

Arguments

| | |
|--------------|---|
| ModelType | string-vector containing the label of the model to be estimated |
| ModelPara | list of model parameter estimates (see the "Optimization" function) |
| FactorLabels | string-list based which contains all the labels of all the variables present in the model |
| Economies | string-vector containing the names of the economies which are part of the economic system |

VarianceExplainedSep *Percentage explained by the spanned factors of the variations in the set of observed yields for "sep Q" models*

Description

Percentage explained by the spanned factors of the variations in the set of observed yields for "sep Q" models

Usage

VarianceExplainedSep(ModelType, ModelPara, FactorLabels, Economies)

Arguments

| | |
|--------------|---|
| ModelType | string-vector containing the label of the model to be estimated |
| ModelPara | List of model parameter estimates (see the "Optimization" function) |
| FactorLabels | string-list based which contains all the labels of all the variables present in the model |
| Economies | string-vector containing the names of the economies which are part of the economic system |

| | |
|---------|--|
| x2bound | <i>Transform x to a number bounded btw lb and ub by:</i> |
|---------|--|

Description

Transform x to a number bounded btw lb and ub by:

Usage

x2bound(x, lb, ub, nargout)

Arguments

| | |
|---------|-----------------------------------|
| x | number to be transformed (scalar) |
| lb | lower bound (scalar) |
| ub | upper bound (scalar) |
| nargout | "1" or "2" (scalar) |

References

This function is based on the "x2bound" function by Le and Singleton (2018).
 "A Small Package of Matlab Routines for the Estimation of Some Term Structure Models."
 (Euro Area Business Cycle Network Training School - Term Structure Modelling). Available at:
<https://cepr.org/40029>

| | |
|-------|--|
| x2pos | <i>Transform x to a positive number by: $y = \log(e^x + 1)$</i> |
|-------|--|

Description

Transform x to a positive number by: $y = \log(e^x + 1)$

Usage

x2pos(x, nargout)

Arguments

| | |
|---------|------------------|
| x | scalar or vector |
| nargout | 1 or 2 |

References

This function is based on the "x2pos" function by Le and Singleton (2018).
 "A Small Package of Matlab Routines for the Estimation of Some Term Structure Models."
 (Euro Area Business Cycle Network Training School - Term Structure Modelling) Available at:
<https://cepr.org/40029>

| | |
|--------|---|
| Yields | <i>Data: Yields - Candelon and Moura (2021)</i> |
|--------|---|

Description

Yields data used in Candelon and Moura (2021)

Usage

```
data("CM_Yields")
```

Format

matrix containing the Yields of the models

References

Candelon, B. and Moura, R. "A Multi-Country Model of the Term Structures of Interest Rates with a GVAR".

| | |
|----------------|---|
| YieldsFitJoint | <i>Computes two measures of model fit for bond yields</i> |
|----------------|---|

Description

Computes two measures of model fit for bond yields

Usage

```
YieldsFitJoint(ModelType, ModelPara, FactorLabels, Economies)
```

Arguments

| | |
|--------------|---|
| ModelType | string-vector containing the label of the model to be estimated |
| ModelPara | list of model parameter estimates (see the "Optimization" function) |
| FactorLabels | string-list based which contains all the labels of all the variables present in the model |
| Economies | string-vector containing the names of the economies which are part of the economic system |

Details

"Model-implied yields" is the measure of fit based exclusively on the risk-neutral parameters, whereas the "Model-Fit" takes into account both the risk-neutral and the physical parameters.

References

See, for instance, Jotiskhatira, Le and Lundblad (2015). "Why do interest rates in different currencies co-move?" (Journal of Financial Economics)

| | |
|--------------|---|
| YieldsFitsep | <i>Computes two measures of model fit for bond yields</i> |
|--------------|---|

Description

Computes two measures of model fit for bond yields

Usage

YieldsFitsep(ModelType, ModelPara, FactorLabels, Economies)

Arguments

| | |
|--------------|---|
| ModelType | a string-vector containing the label of the model to be estimated |
| ModelPara | List of model parameter estimates (See the "Optimization" function) |
| FactorLabels | a string-list based which contains the labels of all the variables present in the model |
| Economies | a string-vector containing the names of the economies which are part of the economic system |

Details

"Model-implied yields" is the measure of fit based exclusively on the risk-neutral parameters, whereas the "Model-Fit" takes into account both the risk-neutral and the physical parameters.

References

See, for instance, Jotiskhatira, Le and Lundblad (2015). "Why do interest rates in different currencies co-move?" (Journal of Financial Economics)

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