

# Package ‘aum’

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**Type** Package

**Title** Area Under Minimum of False Positives and Negatives

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**Description** Standard template library sort is  
used to implement an efficient  
algorithm <[arXiv:2107.01285](https://arxiv.org/abs/2107.01285)> for computing Area Under Minimum and  
directional derivatives.

**License** GPL-3

**LinkingTo** Rcpp

**URL** <https://github.com/tdhock/aum>

**BugReports** <https://github.com/tdhock/aum/issues>

**Imports** Rcpp, data.table

**Suggests** testthat, ggplot2, WeightedROC, penaltyLearning, knitr,  
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**VignetteBuilder** knitr

**NeedsCompilation** yes

**Repository** CRAN

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## R topics documented:

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**aum***aum*

## Description

Compute the Area Under Minimum of False Positives and False Negatives, and its directional derivatives.

## Usage

```
aum(error.diff.df, pred.vec)
```

## Arguments

- `error.diff.df` data frame of error differences, typically computed via [aum\\_diffs\\_binary](#) or [aum\\_diffs\\_penalty](#). There should be one row for each change in error functions. "example" column indicates example ID (int from 1 to N), "pred" column indicates predicted value where there is a change in the error function(s), "fp\_diff" and "fn\_diff" columns indicate differences in false positives and false negatives at that predicted value. Note that this representation assumes that each error function has fp=0 at pred=-Inf and fn=0 at pred=Inf.
- `pred.vec` numeric vector of N predicted values.

## Value

Named list of two items: `aum` is numeric scalar loss value, `derivative_mat` is N x 2 matrix of directional derivatives (first column is derivative from left, second column is derivative from right). If

## Author(s)

Toby Dylan Hocking

## Examples

```
(bin.diffs <- aum::aum_diffs_binary(c(0,1)))
aum::aum(bin.diffs, c(-10,10))
aum::aum(bin.diffs, c(0,0))
aum::aum(bin.diffs, c(10,-10))
```

---

|                        |                  |
|------------------------|------------------|
| <code>aum_diffs</code> | <i>aum diffs</i> |
|------------------------|------------------|

---

## Description

Create error differences data table which can be used as input to `aum` function. Typical users should not use this function directly, and instead use `aum_diffs_binary` for binary classification, and `aum_diffs_penalty` for error defined as a function of non-negative penalty.

## Usage

```
aum_diffs(example, pred,
          fp_diff, fn_diff,
          pred.name.vec)
```

## Arguments

|                            |   |
|----------------------------|---|
| <code>example</code>       | Integer or character vector identifying different examples.     |
| <code>pred</code>          | Numeric vector of predicted values at which the error changes.  |
| <code>fp_diff</code>       | Numeric vector of difference in fp at <code>pred</code> .       |
| <code>fn_diff</code>       | Numeric vector of difference in fn at <code>pred</code> .       |
| <code>pred.name.vec</code> | Character vector of <code>example</code> names for predictions. |

## Value

data table of class "aum\_diffs" in which each rows represents a breakpoint in an error function. Columns are interpreted as follows: there is a change of "fp\_diff", "fn\_diff" at predicted value "pred" for example/observation "example". This can be used for computing Area Under Minimum via `aum` function, and plotted via `plot.aum_diffs`.

## Author(s)

Toby Dylan Hocking

## Examples

```
aum::aum_diffs_binary(c(0,1))
aum::aum_diffs(c("positive", "negative"), 0, c(0,1), c(-1,1), c("negative", "positive"))
rbind(aum::aum_diffs(0L, 0, 1, 0), aum_diffs(1L, 0, 0, -1))
```

**aum\_diffs\_binary**      *aum diffs binary*

## Description

Convert binary labels to error differences.

## Usage

```
aum_diffs_binary(label.vec,
  pred.name.vec, denominator = "count")
```

## Arguments

|               |  |
|---------------|--|
| label.vec     | Numeric vector representing binary labels (either all 0,1 or all -1,1). If named, names are used to identify each example. |
| pred.name.vec | Character vector of prediction example names, used to convert names of label.vec to integers.                              |
| denominator   | Type of diffs, either "count" or "rate".   |

## Value

data table of class "aum\_diffs" in which each rows represents a breakpoint in an error function. Columns are interpreted as follows: there is a change of "fp\_diff", "fn\_diff" at predicted value "pred" for example/observation "example". This can be used for computing Area Under Minimum via [aum](#) function, and plotted via [plot.aum\\_diffs](#).

## Author(s)

Toby Dylan Hocking

## Examples

```
aum_diffs_binary(c(0,1))
aum_diffs_binary(c(-1,1))
aum_diffs_binary(c(a=0,b=1,c=0), pred.name.vec=c("c","b"))
aum_diffs_binary(c(0,0,1,1,1), denominator="rate")
```

---

|                   |                          |
|-------------------|--------------------------|
| aum_diffs_penalty | <i>aum diffs penalty</i> |
|-------------------|--------------------------|

---

## Description

Convert penalized errors to error differences. A typical use case is for penalized optimal change-point models, for which small penalty values result in large fp/fn, and large penalty values result in small fp/fn.

## Usage

```
aum_diffs_penalty(errors.df,
                   pred.name.vec, denominator = "count")
```

## Arguments

|                            |  |
|----------------------------|--|
| <code>errors.df</code>     | data.frame which describes error as a function of penalty/lambda, with at least columns <code>example</code> , <code>min.lambda</code> , <code>fp</code> , <code>fn</code> . Interpreted as follows: fp/fn occur from all penalties from <code>min.lambda</code> to the next value of <code>min.lambda</code> within the current value of <code>example</code> . |
| <code>pred.name.vec</code> | Character vector of prediction example names, used to convert names of <code>label.vec</code> to integers.   |
| <code>denominator</code>   | Type of diffs, either "count" or "rate".   |

## Value

data table of class "aum\_diffs" in which each rows represents a breakpoint in an error function. Columns are interpreted as follows: there is a change of "fp\_diff", "fn\_diff" at predicted value "pred" for example/observation "example". This can be used for computing Area Under Minimum via [aum](#) function, and plotted via [plot.aum\\_diffs](#).

## Author(s)

Toby Dylan Hocking

## Examples

```
## Simple synthetic example with two changes in error function.
simple.df <- data.frame(
  example=1L,
  min.lambda=c(0, exp(1), exp(2), exp(3)),
  fp=c(6,2,2,0),
  fn=c(0,1,1,5))
(simple.diffs <- aum::aum_diffs_penalty(simple.df))
if(requireNamespace("ggplot2"))plot(simple.diffs)
(simple.rates <- aum::aum_diffs_penalty(simple.df, denominator="rate"))
if(requireNamespace("ggplot2"))plot(simple.rates)
```

```

## Simple real data with four example, one has non-monotonic fn.
if(requireNamespace("penaltyLearning")){
  data(neuroblastomaProcessed, package="penaltyLearning", envir=environment())
  ## assume min.lambda, max.lambda columns only? use names?
  nb.err <- with(neuroblastomaProcessed$errors, data.frame(
    example=paste0(profile.id, ".", chromosome),
    min.lambda,
    max.lambda,
    fp, fn))
  (nb.diffs <- aum::aum_diffs_penalty(nb.err, c("1.2", "1.1", "4.1", "4.2")))
  if(requireNamespace("ggplot2"))plot(nb.diffs)
}

## More complex real data example
data(fn.not.zero, package="aum", envir=environment())
pred.names <- unique(fn.not.zero$example)
(fn.not.zero.diffs <- aum::aum_diffs_penalty(fn.not.zero, pred.names))
if(requireNamespace("ggplot2"))plot(fn.not.zero.diffs)

if(require("ggplot2")){
  name2id <- structure(seq(0, length(pred.names)-1L), names=pred.names)
  fn.not.zero.wide <- fn.not.zero[, .(example=name2id[example], min.lambda, max.lambda, fp, fn)]
  fn.not.zero.tall <- data.table::melt(fn.not.zero.wide, measure=c("fp", "fn"))
  ggplot()+
    geom_segment(aes(
      -log(min.lambda), value,
      xend=-log(max.lambda), yend=value,
      color=variable, size=variable),
      data=fn.not.zero.tall)+
    geom_point(aes(
      -log(min.lambda), value,
      fill=variable),
      color="black",
      shape=21,
      data=fn.not.zero.tall)+
    geom_vline(aes(
      xintercept=pred),
      data=fn.not.zero.diffs)+
    scale_size_manual(values=c(fp=2, fn=1))+
    facet_grid(example ~ ., labeller=label_both)
}

```

---

aum\_errors*aum errors*

---

## Description

Convert diffs to canonical errors, used internally in [plot.aum\\_diffs](#).

**Usage**

```
aum_errors(diffs.df)
```

**Arguments**

`diffs.df` data.table of `diffs` from [aum\\_diffs](#).

**Value**

data.table suitable for plotting piecewise constant error functions, with columns `example`, `min.pred`, `max.pred`, `fp`, `fn`.

**Author(s)**

Toby Dylan Hocking

**Examples**

```
(bin.diffs <- aum::aum_diffs_binary(c(0,1)))
if(requireNamespace("ggplot2"))plot(bin.diffs)
aum::aum_errors(bin.diffs)
```

`fn.not.zero`

*Penalized models with non-zero fn at penalty=0*

**Description**

Usually we assume that `fn` must be zero at `penalty=0`, but this is not always the case in real data/labels. For example in the PeakSegDisk model with `penalty=0`, there are peaks almost everywhere but if a positive label is too small or misplaced with respect to the detected peaks, then there can be false negatives.

**Usage**

```
data("fn.not.zero")
```

**Format**

A data frame with 156 observations on the following 5 variables.

|                         |                    |
|-------------------------|--------------------|
| <code>example</code>    | a character vector |
| <code>min.lambda</code> | a numeric vector   |
| <code>max.lambda</code> | a numeric vector   |
| <code>fp</code>         | a numeric vector   |
| <code>fn</code>         | a numeric vector   |

**Source**

<https://github.com/tdhock/feature-learning-benchmark>

---

`plot.aum_diffs`      *plot aum diffs*

---

**Description**

Plot method for `aum_diffs` which shows piecewise constant error functions. Uses `aum_errors` internally to compute error functions which are plotted. Not recommended for large number of examples (>20).

**Usage**

```
## S3 method for class 'aum_diffs'  
plot(x, ...)
```

**Arguments**

|                  |                                    |
|------------------|------------------------------------|
| <code>x</code>   | data table with class "aum_diffs". |
| <code>...</code> | ignored.                           |

**Value**

ggplot of error functions, each example in a different panel.

**Author(s)**

Toby Dylan Hocking

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