# Package 'bdpopt'

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Author Sebastian Jobjörnsson [aut, cre]
Maintainer Sebastian Jobjörnsson <jobjorns@chalmers.se>
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#### create.normal.model Create Normal Emax Model

# Description

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Create a simulation model object for optimisation of the dose and sample size for a (or several, parallel) phase III clinical trial given phase II data. There is one efficacy response and one safety response obtained as sample means for each group of patients given a specific dose. These are both normal given the true populations means. The population means for efficacy and safety are in turn modeled using two independent Emax models.

# Usage

create.normal.model(theta.mu, theta.tau, eta.mu, eta.tau, n.II, d.II, YE.II, YS.II, sigmaE, sigmaS, k.III, path.to.package = NA)

theta.mu	A numeric, atomic vector with four elements that contains the mean parameters for the prior distributions for the efficacy model.
theta.tau	A numeric, atomic vector with four elements that contains the precision param- eters for the prior distributions for the efficacy model.
eta.mu	A numeric, atomic vector with four elements that contains the mean parameters for the prior distributions for the safety model.
eta.tau	A numeric, atomic vector with four elements that contains the precision param- eters for the prior distributions for the safety model.
n.II	A numeric, atomic vector of positive integers containing the group sample sizes corresponding to the phase II efficacy and safety responses.
d.II	A numeric, atomic vector containing the group dose levels corresponding to the phase II efficacy and safety responses.

YE.II	A numeric, atomic vector containing the observed sample means for the efficacy responses in the phase II trial.
YS.II	A numeric, atomic vector containing the observed sample means for the safety responses in the phase II trial.
sigmaE	The population standard deviation for an individual efficacy response. The population standard deviation for a group response is then obtained by dividing by the square root of the group sample size.
sigmaS	The population standard deviation for an individual safety response. The population standard deviation for a group response is then obtained by dividing by the square root of the group sample size.
k.III	A positive integer specifying the number of independent phase III trials, each of which consists of a single group. The sample size and dose is the same for all phase III trials.
path.to.package	2
	The search path to the installation directory of <b>bdpopt</b> . For the default value, the function will attempt to find the path using search.

# Details

Note that n.II, d.II, YE.II and YS.II must all be of the same length. Using the notation of the JAGS manual, the prior distributions for theta and eta are given by theta[i] ~ dnorm(theta.mu[i], theta.tau[i]), eta[i] ~ dnorm(eta.mu[i], eta.tau[i]), for i = 1, 2, and theta[i] ~ dlnorm(theta.mu[i], theta.tau[i]), eta[i] ~ dlnorm(eta.mu[i], eta.tau[i]), for i = 3, 4.

# Value

A simulation model object of class sim.model, created using the data supplied as the arguments and the JAGS model file 'normal\_model\_jags\_model.R'.

## Author(s)

Sebastian Jobjörnsson <jobjorns@chalmers.se>

#### See Also

create.normal.model.from.file

create.normal.model.from.file

Create Normal Emax Model From File

# Description

Create a simulation model object for optimisation of the dose and sample size for a (or several, parallel) phase III clinical trial given phase II data. There is one efficacy response and one safety response obtained as sample means for each group of patients given a specific dose. These are both normal given the true populations means. The population means for efficacy and safety are in turn modeled using two independent Emax models. This function uses the file 'normal\_model\_jags\_data.R' to specify the parameters of the model instead of the user supplying these as arguments (as for create.normal.model).

#### Usage

```
create.normal.model.from.file(path.to.package = NA)
```

#### Arguments

path.to.package

The search path to the installation directory of **bdpopt**. For the default value, the function will attempt to find the path using search.

#### Details

See the argument description of create.normal.model for the objects that have to be specified in 'normal\_model\_jags\_data.R'.

#### Value

A simulation model object of class sim.model, created using the JAGS data file 'normal\_model\_jags\_data.R' and the JAGS model file 'normal\_model\_jags\_model.R'.

#### Author(s)

Sebastian Jobjörnsson <jobjorns@chalmers.se>

#### See Also

create.normal.model

create.utility.function

Create Utility Function For The Normal Model

#### Description

Create a utility function to be used together with a normal simulation model object created using create.normal.model or create.normal.model.from.file.

# Usage

```
create.utility.function(model, n.min, sig.level, safety.max, cE, cS, p,
fixed.cost, cost.per.sample)
```

# Arguments

model	A model object created using create.normal.model or create.normal.model.from.file.
n.min	The minimum group sample size for each phase III group trial required by the regulatory authority in order to consider market approval.
sig.level	The significance level used by the regulatory authority when performing the one-sided hypothesis tests for acceptable efficacy and safety levels in the phase III trial.
safety.max	A parameter defining the maximum safety threshold in the significance test for an acceptable safety level.
cE	A constant defining the utility gain per unit of efficacy.
cS	A constant defining the utility gain per unit of safety. The absolute value of this number defines the utility loss, and hence cS should typically be less than or equal to zero.
p	A number between 0 and 1 which weighs the relative contribution of the ob- served responses and the true population means to the utility upon regulatory approval. A value of 1 corresponds to no contribution made by the population means.
fixed.cost	The fixed cost of performing the phase III trials.
cost.per.samp]	Le
	The cost per observation in the phase III trials

The cost per observation in the phase III trials.

# Details

The utility function has the form:

RA.decision \* gain - trial.cost

where

```
gain = p * (cE * mean(YE) + cS * mean(YS)) + (1 - p) * (cE * mean(muE) + cS * mean(muS))
```

```
trail.cost = fixed.cost + cost.per.sample * k.III * n.III
```

# Value

An R function to be used together with model when calling eval.on.grid, fit.gpr, fit.loess and optimise.eu.

## Author(s)

Sebastian Jobjörnsson <jobjorns@chalmers.se>

diag.mcmc.list

#### Description

Get the mcmc.list object obtained when running the JAGS model corresponding to model. Diagnostic functions provided by the **coda** package may then be applied in order to check that there is a sufficent amount of adaptation and burn in for the application. This is a generic function for S3 objects.

#### Usage

```
diag.mcmc.list(model, utility.fun, data,
n.iter, n.burn.in, n.adapt = 1000, n.chains = 1, inits = NULL)
```

#### Arguments

model	Simulation model object of class sim.model created using sim.model or create.normal.model.
utility.fun	An R function defining the utility for the decision problem. It must be possible to extract the argument names of the function supplied with formals, and the argument names must constitute a subset of the names used in the JAGS model specification.
data	A named list of R objects which, when combined with the named objects in model\$data, leads to a complete specification of the data for the JAGS model.
n.iter	The number of iterations in the JAGS MCMC simulation.
n.burn.in	The number of burn in iterations prior to the JAGS MCMC simulation.
n.adapt	The number of adaptation iterations prior to the burn in phase and subsequent JAGS MCMC simulation.
n.chains	The number of parallel MCMC chains to run.
inits	The initial values for the chain(s) passed on to the function rjags::jags.model, unless equal to its default value NULL, in which case JAGS chooses default initial values.

# Details

The purpose of this function is to make it possible for the user diagnose the JAGS output (e.g., using the **coda** package) and select appropriate values for n.iter, n.burn.in and n.adapt.

#### Value

An object of type mcmc.list, as produced by rjags::coda.samples.

#### Author(s)

Sebastian Jobjörnsson <jobjorns@chalmers.se>

diag.mcmc.list.sim.model

MCMC List For Diagnostic Evaluation

# Description

diag.mcmc.list method for objects of class sim.model.

# Usage

```
## S3 method for class 'sim.model'
diag.mcmc.list(model, utility.fun, data,
n.iter, n.burn.in, n.adapt = 1000, n.chains = 1, inits = NULL)
```

# Arguments

model	Simulation model object of class sim.model created using sim.model or create.normal.model.
utility.fun	An R function defining the utility for the decision problem. It must be possible to extract the argument names of the function supplied with formals, and the argument names must constitute a subset of the names used in the JAGS model specification.
data	A named list of R objects which, when combined with the named objects in model\$data, leads to a complete specification of the data for the JAGS model.
n.iter	The number of iterations in the JAGS MCMC simulation.
n.burn.in	The number of burn in iterations prior to the JAGS MCMC simulation.
n.adapt	The number of adaptation iterations prior to the burn in phase and subsequent JAGS MCMC simulation.
n.chains	The number of parallel MCMC chains to run.
inits	The initial values for the chain(s) passed on to the function rjags::jags.model, unless equal to its default value NULL, in which case JAGS chooses default initial values.

# Details

See diag.mcmc.list for further documentation.

#### eval.eu

# Description

Simulate an estimate of the expected utility for a specific completion of the JAGS data, i.e., for a specific point in the decision space. This is a generic function for S3 objects.

# Usage

```
eval.eu(model, utility.fun, data,
n.iter, n.burn.in, n.adapt = 1000, inits = NULL, independent.SE = FALSE)
```

#### Arguments

model	Simulation model object of class sim.model created using sim.model or create.normal.model.
utility.fun	An R function defining the utility for the decision problem. It must be possible to extract the argument names of the function supplied with formals, and the argument names must constitute a subset of the names used in the JAGS model specification.
data	A named list of R objects which, when combined with the named objects in model\$data, leads to a complete specification of the data for the JAGS model.
n.iter	The number of iterations in the JAGS MCMC simulation.
n.burn.in	The number of burn iterations prior to the JAGS MCMC simulation.
n.adapt	The number of adaptation iterations prior to the burn in and JAGS MCMC simulation.
inits	The initial values for the chain passed on to the function rjags::jags.model, unless equal to its default value NULL, in which case JAGS chooses default initial values.
independent.SE	If TRUE, then the standard errors of the sample means used to estimate the expected utility will be computed under the assumption of i.i.d. sampling. If FALSE, the standard errors are instead computed using the coda::spectrum0.ar function.

# Details

This function is called by eval.on.grid, but also allows the user to evaluate the expected utility for a specific combination of values for the decision variables of the problem.

#### Value

A list with components

mean	Sample mean of the simulated utilities.
SE	Standard error of the sample mean.

# eval.eu.sim.model

# Author(s)

Sebastian Jobjörnsson <jobjorns@chalmers.se>

# See Also

eval.on.grid

eval.eu.sim.model Evaluate Expected Utility

#### Description

eval.eu method for objects of class sim.model.

# Usage

## S3 method for class 'sim.model'
eval.eu(model, utility.fun, data,
n.iter, n.burn.in, n.adapt = 1000, inits = NULL, independent.SE = FALSE)

# Arguments

model	Simulation model object of class sim.model created using sim.model or create.normal.model.
utility.fun	An R function defining the utility for the decision problem. It must be possible to extract the argument names of the function supplied with formals, and the argument names must constitute a subset of the names used in the JAGS model specification.
data	A named list of R objects which, when combined with the named objects in model\$data, leads to a complete specification of the data for the JAGS model.
n.iter	The number of iterations in the JAGS MCMC simulation.
n.burn.in	The number of burn iterations prior to the JAGS MCMC simulation.
n.adapt	The number of adaptation iterations prior to the burn in and JAGS MCMC simulation.
inits	The initial values for the chain passed on to the function $rjags::jags.model$ , unless equal to its default value NULL, in which case JAGS chooses default initial values.
independent.SE	If TRUE, then the standard errors of the sample means used to estimate the expected utility will be computed under the assumption of i.i.d. sampling. If FALSE, the standard errors are instead computed using the coda::spectrum0.ar function.

# Details

See eval.eu for further documentation.

eval.on.grid

#### Description

Evaluate the expected utility on a grid using MCMC samples from JAGS. The grid is a subset of the space for the decision variables.

#### Usage

```
eval.on.grid(model, utility.fun, grid.spec.list,
n.iter, n.burn.in, n.adapt = 1000, independent.SE = FALSE, parallel = FALSE)
```

# Arguments

model	Simulation model object of class sim.model created using sim.model or create.normal.model.
utility.fun	An R function defining the utility for the decision problem. It must be possible to extract the argument names of the function supplied with formals, and the argument names must constitute a subset of the names used in the JAGS model specification.
grid.spec.list	A nonempty list of array grid specifications. An array grid specification is a list of two componenents. The first component is a dimension vector, giving the di- mensions of the array. The second component is a list of vectors of length equal to the product of the dimension vector. Each such vector has the form c(lower, upper, step). These are passed to the function seq in order to generate a range of values for each component of the array.
n.iter	The number of iterations in the JAGS MCMC simulation for each grid point.
	The number of herations in the trice intention for each grid point
n.burn.in	The number of burn in iterations prior to the JAGS MCMC simulation for each grid point.
n.burn.in n.adapt	The number of burn in iterations prior to the JAGS MCMC simulation for each
n.adapt	The number of burn in iterations prior to the JAGS MCMC simulation for each grid point. The number of adaptation iterations prior to the burn in phase and subsequent

# Value

A new simulation model object constructed from the object given as the first argument and the simulation results. The updated components in the new object are model\$sim.points, model\$sim.means, model\$sim.SEs and model\$grid.spec.list. See sim.model for a description of these components.

# Author(s)

Sebastian Jobjörnsson <jobjorns@chalmers.se>

#### See Also

eval.eu

eval.on.grid.sim.model

Evaluate Expected Utility On A Grid

# Description

eval.on.grid method for objects of class sim.model.

# Usage

## S3 method for class 'sim.model'
eval.on.grid(model, utility.fun, grid.spec.list,
n.iter, n.burn.in, n.adapt = 1000, independent.SE = FALSE, parallel = FALSE)

model	Simulation model object of class sim.model created using sim.model or create.normal.model.
utility.fun	An R function defining the utility for the decision problem. It must be possible to extract the argument names of the function supplied with formals, and the argument names must constitute a subset of the names used in the JAGS model specification.
grid.spec.list	A nonempty list of array grid specifications. An array grid specification is a list of two componenents. The first component is a dimension vector, giving the di- mensions of the array. The second component is a list of vectors of length equal to the product of the dimension vector. Each such vector has the form c(lower, upper, step). These are passed to the function seq in order to generate a range of values for each component of the array.
n.iter	The number of iterations in the JAGS MCMC simulation for each grid point.
n.burn.in	The number of burn in iterations prior to the JAGS MCMC simulation for each grid point.
n.adapt	The number of adaptation iterations prior to the burn in phase and subsequent JAGS MCMC simulation for each grid point.
independent.SE	If TRUE, then the standard errors of the sample means used to estimate the expected utility will be computed under the assumption of i.i.d. sampling. If FALSE, the standard errors are instead computed using the coda::spectrum0.ar function.
parallel	Logical equal to TRUE if the simulation should be done in parallel on a multi-core processor. The default value FALSE leads to single-core evaluation.

#### Details

See eval.on.grid for further documentation.

fit.gpr

#### Fit A Gaussian Process Regression Function

#### Description

Fit a GPR regression function to the estimated expected utility values obtained through simulation via JAGS by calling eval.on.grid. This is a generic function for S3 objects.

## Usage

fit.gpr(model, start, gr = TRUE, method = "L-BFGS-B", lower = 0, upper = Inf, control = list())

#### Arguments

model	A model object obtained as the return value from eval.on.grid.
start	Start value passed on to optim when performing the marginal likelihood optimi- sation to find appropriate values for the hyperparameters for the GPR regression function.
gr	Set to TRUE if gradient information should be passed to optim. If false, optim uses a finite difference approximation of the gradient when performing the optimisation of the hyperparameters.
method	The optimisation method to be used by optim. One of "Nelder-Mead", "BFGS", "CG", "L-BFGS-B", "SANN" or "Brent".
lower	A numeric, atomic vector containing the lower limits for the hyperparameters. The first entry is for the standard deviation parameter and the remaining entries are for the length parameters. If supplied, all elements must be $\geq 0$ .
upper	A numeric, atomic vector containing the upper limits for the hyperparameters. The first entry is for the standard deviation parameter and the remaining entries are for the length parameters.
control	A list of control parameters passed on to optim.

#### **Details**

The fitting operation consists of maximising the marginal likelihood of the hyperparameters for a GPR model based on a squared-exponential covariance model. This is done by minimising a function proportional to the negative marginal likelihood. The number of hyperparameters for this model equals 1 + the number of decision variables of the decision model. The first hyperparameter is a standard deviation and the rest consists of a length parameter for each decision dimension.

The optimisation strategy depends on the value of method. If "L-BFGS-B" is used, then the arguments lower and upper are passed on as specified to optim as the lower and upper limits for the optimisation of the hyperparameters. If any other value is provided for method, then optim will be

# fit.gpr.sim.model

used to minimise a function defined to be equal to the objective function when the hyperparameter argument x satisfies  $x \ge 1$  ower,  $x \le 1$  upper and equal to Inf otherwise. The actual lower and upper limits passed to optim in this latter case are -Inf and Inf, respectively.

# Value

A new simulation model object constructed from the object given as the first argument and the GPR regression results. The updated components in the new object are model\$regression.fun and model\$gpr.hyper.params. See sim.model for a description of these components.

# Author(s)

Sebastian Jobjörnsson <jobjorns@chalmers.se>

# See Also

fit.loess

fit.gpr.sim.model Fit A Gaussian Process Regression Function

## Description

fit.gpr method for objects of class sim.model.

#### Usage

```
## S3 method for class 'sim.model'
fit.gpr(model, start, gr = TRUE, method = "L-BFGS-B",
lower = 0, upper = Inf, control = list())
```

model	A model object obtained as the return value from eval.on.grid.
start	Start value passed on to optim when performing the marginal likelihood optimi- sation to find appropriate values for the hyperparameters for the GPR regression function.
gr	Set to TRUE if gradient information should be passed to optim. If false, optim uses a finite difference approximation of the gradient when performing the optimisation of the hyperparameters.
method	The optimisation method to be used by optim. One of "Nelder-Mead", "BFGS", "CG", "L-BFGS-B", "SANN" or "Brent".
lower	A numeric, atomic vector containing the lower limits for the hyperparameters. The first entry is for the standard deviation parameter and the remaining entries are for the length parameters. If supplied, all elements must be $\geq 0$ .

upper	A numeric, atomic vector containing the upper limits for the hyperparameters.
	The first entry is for the standard deviation parameter and the remaining entries
	are for the length parameters.
control	A list of control parameters passed on to optim.

# Details

See fit.gpr for further documentation.

fit.loess

Fit A Local Polynomial Regression Function

# Description

Fit a local polynomial regression function to the estimated expected utility values obtained through simulation via JAGS by calling eval.on.grid. This is a generic function for S3 objects.

#### Usage

fit.loess(model, span = 0.75, degree = 2)

#### Arguments

model	A model object obtained as the return value from eval.on.grid.
span	A parameter which controls the degree of smoothing.
degree	The degree of the polynomials to be used, normally 1 or 2.

## Details

This function calls loess in package **stats** to perform a regression. Note that the number of decision variables must be between 1 and 4, since this is the range supported by loess.

The formula passed as formula to loess has the form " $y \sim x1 + x2$ " (for two decision variables, and correspondingly for any other number between 1 and 4). The span and degree arguments are passed on to loess as given. Further, surface = "direct" is used as a loess control value in order to allow for extrapolation for the fitted function. For the remaining arguments of loess, the default values are used.

#### Value

A new simulation model object constructed from the object given as the first argument and the local polynomial regression results. The updated components in the new object are model\$regression.fun and model\$gpr.hyper.params (set to NA). See sim.model for a description of these components.

#### Author(s)

Sebastian Jobjörnsson <jobjorns@chalmers.se>

### fit.loess.sim.model

#### See Also

fit.gpr

fit.loess.sim.model Fit A Local Polynomial Regression Function

# Description

fit.loess method for objects of class sim.model.

#### Usage

```
## S3 method for class 'sim.model'
fit.loess(model, span = 0.75, degree = 2)
```

#### Arguments

model	A model object obtained as the return value from eval.on.grid.
span	A parameter which controls the degree of smoothing.
degree	The degree of the polynomials to be used, normally 1 or 2.

#### Details

See fit.loess for further documentation.

n.opt

**Optimise A Simple Normal Model** 

#### Description

Find an approximation of the optimal sample size and corresponding expected utility for a simple phase III clinical trial model with a single, normally distributed response and a utility function of a fixed form.

### Usage

```
n.opt(nu = 0, tau = 1, sigma = 1, alpha = 0.025,
gain.constant = 1, gain.function = function(X, mu) 0,
fixed.cost = 0, sample.cost = 0.005,
k = 1, n.min = 1, n.max = 50, n.step = 1,
n.iter = 10000, n.burn.in = 1000, n.adapt = 1000,
regression.type = "loess",
plot.results = TRUE, independent.SE = FALSE,
parallel = FALSE, path.to.package = NA)
```

nu	The mean of the conjugate normal prior distribution for the unknown population mean.
tau	The standard deviation of the conjugate normal prior distribution for the un- known population mean.
sigma	The known population standard deviation for each individual response in the trial.
alpha	The significance level in the one-sided test used by the regulatory authority to decide upon marketing approval for the new treatment.
gain.constant	A constant utility gain received upon treatment approval. The total gain consists of the sum of gain.constant and gain.function.
gain.function	A variable utility gain obtained in addition to the constant utility gain upon treat- ment approval.
fixed.cost	The fixed cost of performing the trial.
sample.cost	The marginal cost per observation for the trial.
k	The number independent, parallel trials. Must be an integer greater than zero.
n.min	Lower limit for the one-dimensional grid for the sample size.
n.max	Upper limit for the one-dimensional grid for the sample size.
n.step	The step size of the grid for the sample size.
n.iter	The number of iterations in the JAGS MCMC simulation.
n.burn.in	The number of burn iterations prior to the JAGS MCMC simulation.
n.adapt	The number of adaptation iterations prior to the burn in and JAGS MCMC simulation.
regression.typ	
	If set to "loess", the default value, then local polynomial regression will be used (via a call to fit.loess) to fit the grid simulation results. If set to "gpr", GPR regression will be used instead. For any other value, no regression is per- formed and the optimisation done will consist of a maximisation over the values corresponding to the grid points.
plot.results	Set to TRUE if a plot of the results of the simulation over the grid is to be con- structed.
independent.SE	If TRUE, then the standard errors of the sample means used to estimate the expected utility will be computed under the assumption of i.i.d. sampling. If FALSE, the standard errors are instead computed using the coda::spectrum0.ar function.
parallel	Set to TRUE if the simulations over the grid should be done in parallel on a multi- core processor. The default value FALSE leads to single-core computations.
path.to.package	
	The search path to the installation directory of <b>bdpopt</b> . For the default value, the function will attempt to find the path using search.

# optimise.eu

# Value

A list with components

ns	A numeric, atomic vector containing the sample size grid points.
eus	A numeric, atomic vector containing the sample means of the simulated expected utilities corresponding to the sample size grid points.
opt.arg	The optimal sample size found by maximising the estimated expected utility.
opt.eu	The estimated optimal utility corresponding to the optimal sample size found.

# Author(s)

Sebastian Jobjörnsson <jobjorns@chalmers.se>

# See Also

optimise.eu

optimise.eu

**Optimise Expected Utility** 

# Description

Optimisation of expected utility, either directly over the results of a grid evaluation performed by eval.on.grid or by optimisation of the regression function constructed by fit.gpr or fit.loess. This is a generic function for an S3 object.

# Usage

optimise.eu(model, start, method = "L-BFGS-B", lower = -Inf, upper = Inf, control = list())

model	A simulation model object returned by eval.on.grid, fit.gpr or fit.loess. Specifying any method other than "Grid" requires that the object has been ob- tained from fit.gpr or fit.loess.
start	The start value when performing the search for a maximum. Passed on to optim.
method	The optimisation method to be used. Must be one of "Nelder-Mead", "BFGS", "CG", "L-BFGS-B", "SANN", "Brent" or "Grid".
lower	A numeric, atomic vector giving the lower limits for the decision variables when performing the maximisation.
upper	A numeric, atomic vector giving the upper limits for the decision variables when performing the maximisation.
control	A list of control parameters passed on to optim.

# Details

The optimisation strategy depends on the value of method. All arguments except model are ignored if the method "Grid" is used. If "L-BFGS-B" is used, then the arguments lower and upper are passed on as specified to optim as the lower and upper limits for the optimisation of the decision variables. If any other value is provided for method, then optim will be used to maximise a function defined to be equal to the objective function when the decision variable argument x satisfies  $x \ge$ lower,  $x \le$ upper and equal to -Inf otherwise. The actual lower and upper limits passed to optim in this last case are -Inf and Inf, respectively.

#### Value

A list with components

opt.arg	A named vector containing the optimal values for the decision variables.
opt.eu	An estimate of the optimal expected utility.

# Author(s)

Sebastian Jobjörnsson <jobjorns@chalmers.se>

optimise.eu.sim.model Optimise Expected Utility

# Description

optimise.eu method for objects of class sim.model.

## Usage

```
## S3 method for class 'sim.model'
optimise.eu(model, start, method = "L-BFGS-B",
lower = -Inf, upper = Inf, control = list())
```

#### Arguments

model	A simulation model object returned by eval.on.grid, fit.gpr or fit.loess. Specifying any method other than "Grid" requires that the object has been ob- tained from fit.gpr or fit.loess.
start	The start value when performing the search for a maximum. Passed on to optim.
method	The optimisation method to be used. Must be one of "Nelder-Mead", "BFGS", "CG", "L-BFGS-B", "SANN", "Brent" or "Grid".
lower	A numeric, atomic vector giving the lower limits for the decision variables when performing the maximisation.
upper	A numeric, atomic vector giving the upper limits for the decision variables when performing the maximisation.
control	A list of control parameters passed on to optim.

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#### Details

See optimise.eu for further documentation.

optimise.sequential.eu

**Optimise Sequential Expected Utility** 

# Description

Optimise the expected utility for a sequential decision problem. The optimisation proceeds by backward induction, computing the optimal decision and corresponding expected utility at each stage over a grid for the current state summarising the posterior distribution of the unknown parameter.

#### Usage

```
optimise.sequential.eu(dp, mins, maxs, steps, n.sims, state.start = NA)
```

#### Arguments

dp	A decision problem object constructed by calling sequential.dp.
mins	A numeric, atomic vector specifying the lower boundary of the grid points for each dimension of the state vector.
maxs	A numeric, atomic vector specifying the upper boundary of the grid points for each dimension of the state vector.
steps	A numeric, atomic vector specifying the step size between grid points for each dimension of the state vector.
n.sims	A numeric, atomic vector of length equal to dp\$n.stages specifying the number of simulation draws to perform at each stage.
state.start	An optional start value for the state. If provided, this value effectively deter- mines a fixed prior for the parameter of the decision problem (before the first stage). The first stage computations will then only be performed for this partic- ular value. If the default value NA is used, computations for the first stage will be performed for all grid points, as for the subsequent stages.

#### Value

If state.start equals NA, then the value returned is a list with components

opt.decision Function taking a stage and a state into the optimal decision corresponding to the closest grid point at that stage.opt.utility Function taking a stage and a state into the optimal expected utility corresponding to the closest grid point at that stage.

If an explicit value for state.start is provided, the value returned is a list with components

opt.stage1.deci	sion
	Optimal stage 1 decision.
opt.stage1.utility	
	Optimal stage 1 utility.
opt.decision	Function taking a stage (greater than 1) and a state into the optimal decision corresponding to the closest grid point at that stage.
opt.utility	Function taking a stage (greater than 1) and a state into the optimal expected utility corresponding to the closest grid point at that stage.

# Author(s)

Sebastian Jobjörnsson <jobjorns@chalmers.se>

#### See Also

optimise.sequential.normal.eu

optimise.sequential.normal.eu

**Optimise A Sequential Normal Decision Problem** 

# Description

Optimise a sequential normal decision problem constructed by a call to the function sequential.normal.dp.

# Usage

optimise.sequential.normal.eu(dp, range, step.size, prior.mean = 0, n.sims = 1000, plot.results = TRUE)

dp	A sequential normal decision problem created by a call to sequential.normal.dp.
range	The range of the one-dimensional grid for the state. All grid points will lie in the interval c(prior.mean - range / 2, prior.mean + range / 2).
step.size	The step size between the grid points for the state.
prior.mean	Defines the mid-point of the grid for the state.
n.sims	The number of random draws for simulations used to estimate the expected util- ity for a decision at each stage.
plot.results	If TRUE, construct a plot of the optimal policy.

#### plot.sim.model

#### Details

The plot has the stage number on the x-axis. The y-axis levels of the points (one for each stage) shows the cutoff levels for when it is optimal to continue (for all but the last stage) or finalise (for the last stage). It will be optimal to continue or finalise if the posterior mean of the parameter at a given stage is above the level of the point at that stage.

If no cutoff point can be established in the interior of the region defined by the interval I = c(prior.mean - range / 2, prior.mean + range / 2), then a cross will be used instead of a circle to indicate the level of the stage. If the cross is located at prior.mean + range / 2, it is optimal to continue for no state in I. If the cross is located at prior.mean - range / 2, it is optimal to continue for all states in I.

# Value

A list with components

opt.decision	Function taking a stage and a state into the optimal decision corresponding to the closest grid point at that stage.
opt.utility	Function taking a stage and a state into the optimal expected utility correspond- ing to the closest grid point at that stage.

# Author(s)

Sebastian Jobjörnsson <jobjorns@chalmers.se>

#### See Also

optimise.sequential.eu

plot.sim.model Plot The Results Contained In Simulation Model Object

#### Description

Plot method for an object of class sim.model.

#### Usage

```
## S3 method for class 'sim.model'
plot(x, main.var.name = NULL, main.var.min = -Inf,
    main.var.max = Inf, fixed = list(), no.legends = FALSE,
no.reg = FALSE, reg.steps = 100, ...)
```

#### Arguments

х	A simulation model object obtained as output from eval.on.grid, fit.gpr or fit.loess.
main.var.name	A name for the main variable to be used when plotting. This defines the variable that varies along the x-axis of the plot. The full name of the variable must be given as a string, i.e., the name must include array brackets and array indices.
main.var.min	The minimum value for the main variable.
main.var.max	The maximum value for the main variable.
fixed	A list of vectors with named entries. Each such vector defines a set of fixed values for the remaining decision variables. The number of curves in the plot will be equal to the length of fixed. Note that the names of the entries must be written in full array notation, including explicit brackets and indices.
no.legends	By default, legends are included with numbers corresponding to the entries of fixed. Set no.legends to TRUE to remove it.
no.reg	Set to TRUE in order so suppress plotting of the regression curves.
reg.steps	The number of steps to use when plotting the regression curves.
	Not used.

#### Details

The simulation grid points included in the plot are selected as follows:

- 1. All points for which the value of the decision variable defined by main.var.name is not within the region defined by main.var.min and main.var.max are excluded from the total set of grid points.
- 2. For the points remaining, any point which does not correspond to a value listed in fixed is excluded.

In the special case when there is only one decision variable, only the model x needs to be specified. In the special case when there are only two decision variables, fixed may also be given as a vector. It then specifies the values of the secondary variable and one curve will be drawn for each value.

The default behaviour is to also plot the fitted regression function if it is available, with one curve corresponding to each of the point sets defined by the entries of fixed.

#### Value

Returns NULL.

# Author(s)

Sebastian Jobjörnsson <jobjorns@chalmers.se>

print.sim.model Print Status Of Simulation Model Object

#### Description

Print method for an object of class sim.model. Outputs some very concise information about the given model object.

## Usage

## S3 method for class 'sim.model'
print(x, ...)

#### Arguments

х	The simulation model object.
	Not used.

#### Details

Prints the JAGS model used. If a simulation over a grid has been performed, prints the number of simulation points. Prints a message stating whether or not regression has been performed. Prints the hyperparameters of a GPR regression if available.

# Value

Returns NULL.

#### Author(s)

Sebastian Jobjörnsson <jobjorns@chalmers.se>

sequential.dp Construct A Sequential Decision Problem

# Description

Construct a sequential decision problem. The object constructed is just a list with components named as the arguments to the function.

#### Usage

sequential.dp(n.stages, post.sample, pred.sample, update.state, term.decisions, term.obs.decisions, cont.decisions, term.utility.fun, term.obs.utility.fun, cont.utility.fun)

# Arguments

n.stages	The number of stages in the sequential decision problem.
post.sample	A function taking a stage, a state and the simulation iteration count into a random sample from the posterior distribution of the model parameter given the value of the state when being at the given stage.
pred.sample	A function taking a stage, a list of parameter values and a decision into a list of random samples from the conditional distributions of the observable variable at the given stage. The i:th value in the list returned should be a sample from the predictive distribution conditioned on the i:th entry in the list of parameter values.
update.state	A function that takes a stage, a state, a decision d and a list of observations into a list of updated states. The updated values should be the ones obtained when combining the observations in order with the original state, given d.
term.decisions	A list the length of which must be equal to n.stages. The i:th element of the list specifies the terminal decisions available at stage i.
term.obs.decis	
	A list the length of which must be equal to n.stages. The i:th element of the list specifies the terminal observation decisions available at stage i.
cont.decisions	A list the length of which must be equal to n.stages. The ith element of the list specifies the continuation decisions available at stage i.
term.utility.f	un
	A list of terminal utility functions of length equal to n.stages. Each element of the list should be a function mapping a pair (d, theta) into to a numeric value, where d is a decision and theta is a parameter value.
term.obs.utili	•
	A list of terminal utility functions of length equal to n.stages. Each element of the list should be a function mapping a triple (d, X, theta) into to a numeric value, where d is a decision, X is an observation and theta is a parameter value.
cont.utility.fun	
	A list of terminal utility functions of length equal to $n.stages$ . Each element of the list should be a function mapping a pair (d, X) into to a numeric value, where d is a decision and X is an observation.

# Details

For any stage i, at least one of the elements of the decision lists must be nonempty, i.e., the sum of length(term.decisions[[i]]), length(term.obs.decisions[[i]]) and length(cont.decisions[[i]]) must be greater than or equal to 1.

For the last stage, all decisions must be terminal decisions, i.e., length(cont.decisions[[n.stages]]) must equal 0 and the sum of length(term.decisions[[n.stages]]) and length(term.obs.decisions[[n.stages]]) must be greater than or equal to 1.

#### Value

A list for which the components have the same names and are in the same order as the arguments to the function.

#### sequential.normal.dp

#### Author(s)

Sebastian Jobjörnsson <jobjorns@chalmers.se>

#### See Also

sequential.normal.dp

sequential.normal.dp Create A Sequential Normal Decision Problem

#### Description

Create an object representing a sequential normal decision problem. A single observation with a normal distribution is made at each stage. The parameter is a true population mean with a conjugate normal prior. Under the assumption of a known population standard deviation, the variance of the posterior distribution for the parameter does not depend on the observations as is known at each stage. This implies that the state is one-dimensional and equals the mean of the posterior distribution for the parameter at each stage.

# Usage

```
sequential.normal.dp(n.stages, group.size, tau, sigma,
stage.cost, final.cost, final.gain)
```

## Arguments

n.stages	The number of stages of the sequential decision problem.
group.size	The sample size at each stage. The individal samples are combined into a group mean, which is the single observation at each stage.
tau	The standard deviation of the prior for the unknown population mean before the first stage.
sigma	The population standard deviation for a single individual. The standard devia- tion for the group response is this value divided by the square root of group.size.
stage.cost	The cost of proceeding to the next stage.
final.cost	The cost payed at the final stage if a finalisation decision is taken (if a stopping decision is taken, this cost is not payed).
final.gain	A constant which is multiplied with the true population mean in order to obtain the utility gain at the final stage, if a finalisation decision is taken (if a stopping decision is taken, this gain is not included in the total utility).

#### Details

In all stages but the last, the two decisions available are to either continue and pay the stage cost or to stop and abort (which costs nothing). At the final stage, the two decisions available are to either finalise the process and obtain the final gain and pay the final cost or to stop and abort (whith no gain and no cost).

# Value

A list representing a sequential decision problem object. See sequential.dp for further description of the components.

# Author(s)

Sebastian Jobjörnsson <jobjorns@chalmers.se>

# See Also

sequential.dp

sim.model Construct A Simulation Model Object

# Description

Construct a simulation model object from a JAGS model file and a JAGS data file or a named list of data objects.

# Usage

```
sim.model(model.file, data)
```

# Arguments

model.file	Name of the file defining the JAGS model. This must be an atomic character
	vector of a single element.
data	Name of the file defining the JAGS data or a named list of R objects. If a file
	name, it must be an atomic character vector of a single element.

# Value

An S3 object of class sim.model with components

model.file	The name of the JAGS model file used to create the object.
data	A named list of data objects extracted from the JAGS data file or directly supplied as an argument.
grid.spec.list	The grid specification list after grid evaluation. Initially set to NA when the object is created.
sim.points	A matrix with with columns holding the positions of the grid points after grid evaluation. Initially set to NA when the object is created.
sim.means	A vector holding the sample means after grid evaluation. Initially set to NA when the object is created.
sim.SEs	A vector holding the standard errors corresponding to the sample means after grid evaluation. Initially set to NA when the object is created.

#### sim.model

regression.fun The approximate, smoothed function after regression has been performed. Initially set to NA when the object is created.

# gpr.hyper.params

The hyperparameters selected in the GPR regression after it has been performed. Initially set to NA when the object is created.

# Author(s)

Sebastian Jobjörnsson <jobjorns@chalmers.se>

# See Also

create.normal.model

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