Package 'bdrc'

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Title Bayesian Discharge Rating Curves

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Maintainer Solvi Rognvaldsson <solviro@gmail.com>

Description Fits a discharge rating curve based on the power-law and the generalized power-law from data on paired stage and discharge measurements in a given river using a Bayesian hierarchical model as described in Hrafnkelsson et al. (2020) <arXiv:2010.04769>.

Depends R (>= 3.5.0)

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LazyData true

RoxygenNote 7.1.1

Imports ggplot2, grid, gridExtra, rlang, scales

Suggests testthat, knitr, rmarkdown, covr, vdiffr

VignetteBuilder knitr

BugReports https://github.com/sor16/bdrc/issues

Encoding UTF-8

NeedsCompilation no

Author Birgir Hrafnkelsson [aut, cph]
(<https://orcid.org/0000-0003-1864-9652>),
Solvi Rognvaldsson [aut, cre] (<https://orcid.org/0000-0002-4376-3361>),
Axel Orn Jansson [aut],
Rafael Vias [aut]

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R topics documented:

`autoplot.plm0` *Autoplot method for discharge rating curves*

Description

Visualize discharge rating curve model objects

Usage

```
## S3 method for class 'plm0'
autoplot(x, type = "rating_curve", param = NULL, transformed = FALSE, ...)

## S3 method for class 'plm'
autoplot(x, type = "rating_curve", param = NULL, transformed = FALSE, ...)

## S3 method for class 'gplm0'
autoplot(x, type = "rating_curve", param = NULL, transformed = FALSE, ...)

## S3 method for class 'gplm'
autoplot(x, type = "rating_curve", param = NULL, transformed = FALSE, ...)
```

Arguments

`x`	an object of class "plm0","plm","gplm0" or "gplm".
`type`	a character denoting what type of plot should be drawn. Defaults to "rating_curve". Possible types are • "rating_curve" to plot the rating curve.

- "rating_curve_mean" to plot the posterior mean of the rating curve.
- "f" to plot the power-law exponent.
- "beta" to plot the random effect in the power-law exponent.
- "sigma_eps" to plot the standard deviation on the data level.
- "residuals" to plot the log residuals.
- "trace" to plot trace plots of parameters given in param.
- "histogram" to plot histograms of parameters given in param.

`param` a character vector with the parameters to plot. Defaults to NULL and is only used if type is "trace" or "histogram". Allowed values are the parameters given in the model summary of x as well as "hyperparameters" or "latent_parameters" for specific groups of parameters.

`transformed` a logical value indicating whether the quantity should be plotted on a transformed scale used during the Bayesian inference. Defaults to FALSE.

`...` further arguments passed to other methods. Currently supports:

- "title" a character denoting the title of the plot
- "xlim" numeric vector of length 2, denoting the limits on the x axis of the plot. Applicable for types "rating_curve","rating_curve_mean","f","beta", "sigma_eps","residuals".
- "ylim" numeric vector of length 2, denoting the limits on the y axis of the plot. Applicable for types "rating_curve","rating_curve_mean","f","beta", "sigma_eps","residuals".

Value

returns an object of class "ggplot2".

Functions

- `autoplot.plm0`: Autoplot method for plm0
- `autoplot.plm`: Autoplot method for plm
- `autoplot.gplm0`: Autoplot method for gplm0
- `autoplot.gplm`: Autoplot method for gplm

See Also

`plm0`, `plm`, `gplm0` and `gplm` for fitting a discharge rating curve and `summary.plm0`, `summary.plm`, `summary.gplm0` and `summary.gplm` for summaries. It is also useful to look at `spread_draws` and `gather_draws` to work directly with the MCMC samples.

Examples

```
library(ggplot2)
data(krokfors)
set.seed(1)
plm0.fit <- plm0(Q~W,krokfors,num_cores=2)
```

```
autoplot(plm0.fit)
autoplot(plm0.fit,transformed=TRUE)
autoplot(plm0.fit,type='histogram',param='c')
autoplot(plm0.fit,type='histogram',param='c',transformed=TRUE)
autoplot(plm0.fit,type='histogram',param='hyperparameters')
autoplot(plm0.fit,type='histogram',param='latent_parameters')
autoplot(plm0.fit,type='residuals')
autoplot(plm0.fit,type='f')
autoplot(plm0.fit,type='sigma_eps')
```

`autoplot.tournament` *Autoplot method for discharge rating curve tournament*

Description

Compare the four discharge rating curves from the tournament object in different ways

Usage

```
## S3 method for class 'tournament'
autoplot(x, type = "deviance", ...)
```

Arguments

`x`	an object of class "tournament"
`type`	a character denoting what type of plot should be drawn. Possible types are • "deviance" to plot the deviance of the four models.
`...`	further arguments passed to other methods.

Value

returns an object of class "ggplot2".

See Also

`tournament` to run a discharge rating curve tournament and `summary.tournament` for summaries.

Examples

```
library(ggplot2)
data(krokfors)
set.seed(1)
t_obj <- tournament(formula=Q~W,data=krokfors,num_cores=2)
autoplot(t_obj)
```

gather_draws *Gather MCMC chain draws to data.frame on a long format*

Description

Useful to convert MCMC chain draws of particular parameters or output from the model object to a long format for further data wrangling

Usage

```
gather_draws(mod, ..., transformed = F)
```

Arguments

mod	an object of class "plm0","plm","gplm0" or "gplm".
...	any number of character vectors containing valid names of parameters in the model or "rating_curve" and "rating_curve_mean". Also accepts "latent_parameters" and "hyperparameters".
transformed	boolean value determining whether the parameter is to be represented on the transformed scale used for sampling in the MCMC chain or the original scale. Defaults to FALSE.

Value

Data frame with columns `chain` `iter` `param` `value`

References

B. Hrafnkelsson, H. Sigurdarson, S.M. Gardarsson, 2020, Generalization of the power-law rating curve using hydrodynamic theory and Bayesian hierarchical modeling. arXiv preprint 2010.04769

See Also

`plm0`, `plm`, `gplm0`, `gplm` for further information on parameters

Examples

```
data(krokfors)
set.seed(1)
plm0.fit <- plm0(formula=Q~W,data=krokfors,num_cores=2)
hyp_samples <- gather_draws(plm0.fit,'hyperparameters')
head(hyp_samples)
rating_curve_samples <- gather_draws(plm0.fit,'rating_curve','rating_curve_mean')
head(rating_curve_samples)
```

get_report *Report for a discharge rating curve or tournament*

Description

Save a pdf file with a report of a discharge rating curve object or tournament.

Usage

```
get_report(x, path = NULL, type = 1, ...)

## S3 method for class 'plm0'
get_report(x, path = NULL, type = 1, ...)

## S3 method for class 'plm'
get_report(x, path = NULL, type = 1, ...)

## S3 method for class 'gplm0'
get_report(x, path = NULL, type = 1, ...)

## S3 method for class 'gplm'
get_report(x, path = NULL, type = 1, ...)

## S3 method for class 'tournament'
get_report(x, path = NULL, type = 1, ...)
```

Arguments

x	an object of class "tournament", "plm0", "plm", "gplm0" or "gplm".
path	file path to which the pdf file of the report is saved. If NULL, the current working directory is used.
type	an integer denoting what type of report is to be produced. Defaults to type 1. Only type 1 is permissible for an object of class "plm0", "plm", "gplm0" or "gplm". Possible types are • 1 - produces a report displaying the results of the model (winning model if a tournament provided). The first page contains a panel of four plots and a summary of the posterior distributions of the parameters. On the second page a tabular prediction of discharge on an equally spaced grid of stages is displayed. This prediction table can span multiple pages. • 2 - produces a ten page report and is only permissible for objects of class "tournament". The first four pages contain a panel of four plots and a summary of the posterior distributions of the parameters for each of the four models in the tournament, the fifth page shows model comparison plots and tables, the sixth page convergence diagnostics plots, and the final four pages shows the histograms of the parameters in each of the four models.
...	further arguments passed to other methods (currently unused).

Details

This function can only be used in an interactive R session as it asks permission from the user to write to their file system.

Value

No return value, called for side effects

Methods (by class)

- `plm0`: Get report for plm0 model object
- `plm`: Get report for plm model object
- `gplm0`: Get report for gplm0 model object
- `gplm`: Get report for gplm
- `tournament`: Get report for discharge rating curve tournament

See Also

`get_report` for generating and saving a report.

Examples

```
data(krokfors)
set.seed(1)
plm0.fit <- plm0(formula=Q~W,data=krokfors,num_cores=2)

## Not run:
get_report(plm0.fit)

## End(Not run)
```

---

get_report_pages *Report pages for a discharge rating curve or tournament*

Description

Get a list of the pages of a report on a discharge rating curve model or tournament

Usage

```
get_report_pages(x, type = 1, ...)

## S3 method for class 'plm0'
get_report_pages(x, type = 1, ...)

## S3 method for class 'plm'
```

```
get_report_pages(x, type = 1, ...)

## S3 method for class 'gplm0'
get_report_pages(x, type = 1, ...)

## S3 method for class 'gplm'
get_report_pages(x, type = 1, ...)

## S3 method for class 'tournament'
get_report_pages(x, type = 1, ...)
```

Arguments

x	an object of class "tournament", "plm0", "plm", "gplm0" or "gplm".
type	an integer denoting what type of report is to be produced. Defaults to type 1. Possible types are • 1 - produces a report displaying the results of the model (winning model if a tournament provided). The first page contains a panel of four plots and a summary of the posterior distributions of the parameters. On the second page a tabular prediction of discharge on an equally spaced grid of stages is displayed. This prediction table can span multiple pages. • 2 - produces a ten page report and is only permissible for objects of class "tournament". The first four pages contain a panel of four plots and a summary of the posterior distributions of the parameters for each of the four models in the tournament, the fifth page shows model comparison plots and tables, the sixth page convergence diagnostics plots, and the final four pages shows the histograms of the parameters in each of the four models.
...	further arguments passed to other methods (currently unused).

Value

A list of objects of type "grob" that correspond to the pages in a rating curve report.

Methods (by class)

- `plm0`: Get report pages for plm0 model object
- `plm`: Get report pages for plm model object
- `gplm0`: Get report pages for gplm0 model object
- `gplm`: Get report pages for gplm model object
- `tournament`: Get report pages for discharge rating curve tournament model object

See Also

`tournament` for running a tournament,`summary.tournament` for summaries and `get_report` for generating and saving a report of a tournament object.

Examples

```
data(krokfors)
set.seed(1)
plm0.fit <- plm0(formula=Q~W,data=krokfors,num_cores=2)
plm0_pages <- get_report_pages(plm0.fit)
```

---

gplm *Generalized power-law model with variance that varies with stage.*

Description

gplm is used to fit a discharge rating curve for paired measurements of stage and discharge using a generalized power-law model with variance that varies with stage as described in Hrafnkelsson et al. (2020). See "Details" for a more elaborate description of the model.

Usage

```
gplm(
  formula,
  data,
  c_param = NULL,
  h_max = NULL,
  parallel = TRUE,
  num_cores = NULL,
  forcepoint = rep(FALSE, nrow(data))
)
```

Arguments

formula	an object of class "formula", with discharge column name as response and stage column name as a covariate, i.e. of the form y~x where y is discharge in m^3/s and x is stage in m (it is very important that the data is in the correct units).
data	data.frame containing the variables specified in formula.
c_param	stage for which there is zero discharge. If NULL, it is treated as unknown in the model and inferred from the data.
h_max	maximum stage to which the rating curve should extrapolate to. If NULL, the maximum stage value in the data is selected as an upper bound.
parallel	logical value indicating whether to run the MCMC in parallel or not. Defaults to TRUE.
num_cores	integer between 1 and 4 (number of MCMC chains) indicating how many cores to use. Only used if parallel=TRUE. If NULL, the number of cores available on the device is detected automatically.

`forcepoint` logical vector of the same length as the number of rows in data. If an element at index i is TRUE it indicates that the rating curve should be forced through the i-th measurement. Use with care, as this will strongly influence the resulting rating curve.

Details

The generalized power-law model is of the form

$$Q = a(h - c)^{f(h)}$$

where Q is discharge, h is stage, a and c are unknown constants and f is a function of h, referred to as the generalized power-law exponent.

The generalized power-law model is here inferred by using a Bayesian hierarchical model. The function f is modeled at the latent level as a fixed constant b plus a continuous stochastic process, $\beta(h)$, which is assumed to be twice differentiable. The model is on a logarithmic scale

$$\log(Q_i) = \log(a) + (b + \beta(h_i)) \log(h_i - c) + \varepsilon_i, i = 1, ..., n$$

where ε_i follows a normal distribution with mean zero and variance $\sigma_\varepsilon(h_i)^2$ that varies with stage. The stochastic process $\beta(h)$ is assumed a priori to be a Gaussian process governed by a Matern covariance function with smoothness parameter $\nu = 2.5$. The error variance, $\sigma_\varepsilon^2(h)$, of the log-discharge data is modeled as an exponential of a B-spline curve, that is, a linear combination of six B-spline basis functions that are defined over the range of the stage observations. An efficient posterior simulation is achieved by sampling from the joint posterior density of the hyperparameters of the model, and then sampling from the density of the latent parameters conditional on the hyperparameters.

Bayesian inference is based on the posterior density and summary statistics such as the posterior mean and 95% posterior intervals are based on the posterior density. Analytical formulas for these summary statistics are intractable in most cases and thus they are computed by generating samples from the posterior density using a Markov chain Monte Carlo simulation.

Value

gplm returns an object of class "gplm". An object of class "gplm" is a list containing the following components:

`rating_curve` a data frame with 2.5%, 50% and 97.5% percentiles of the posterior predictive distribution of the rating curve.

`rating_curve_mean` a data frame with 2.5%, 50% and 97.5% percentiles of the posterior distribution of the mean of the rating curve.

`param_summary` a data frame with 2.5%, 50% and 97.5% percentiles of the posterior distribution of latent- and hyperparameters. Additionally contains columns with r_hat and the effective number of samples for each parameter as defined in Gelman et al. (2013).

`f_summary` a data frame with 2.5%, 50% and 97.5% percentiles of the posterior distribution of $f(h)$.

`beta_summary` a data frame with 2.5%, 50% and 97.5% percentiles of the posterior distribution of $\beta(h)$.

`sigma_eps_summary`
a data frame with 2.5%, 50% and 97.5% percentiles of the posterior distribution of $\sigma_\varepsilon(h)$.

`Deviance_summary`
a data frame with 2.5%, 50% and 97.5% percentiles of the posterior distribution of the deviance.

`rating_curve_posterior`
a matrix containing the full thinned posterior samples of the posterior predictive distribution of the rating curve excluding burn-in samples.

`rating_curve_mean_posterior`
a matrix containing the full thinned posterior samples of the posterior distribution of the mean of the rating curve excluding burn-in samples.

`a_posterior` a numeric vector containing the full thinned posterior samples of the posterior distribution of a excluding burn-in samples.

`b_posterior` a numeric vector containing the full thinned posterior samples of the posterior distribution of b excluding burn-in samples.

`c_posterior` a numeric vector containing the full thinned posterior samples of the posterior distribution of c excluding burn-in samples.

`sigma_beta_posterior`
a numeric vector containing the full thinned posterior samples of the posterior distribution of σ_β excluding burn-in samples.

`phi_beta_posterior`
a numeric vector containing the full thinned posterior samples of the posterior distribution of ϕ_β excluding burn-in samples.

`sigma_eta_posterior`
a numeric vector containing the full thinned posterior samples of the posterior distribution of σ_η excluding burn-in samples.

`eta_1_posterior`
a numeric vector containing the full thinned posterior samples of the posterior distribution of η_1 excluding burn-in samples.

`eta_2_posterior`
a numeric vector containing the full thinned posterior samples of the posterior distribution of η_2 excluding burn-in samples.

`eta_3_posterior`
a numeric vector containing the full thinned posterior samples of the posterior distribution of η_3 excluding burn-in samples.

`eta_4_posterior`
a numeric vector containing the full thinned posterior samples of the posterior distribution of η_4 excluding burn-in samples.

`eta_5_posterior`
a numeric vector containing the full thinned posterior samples of the posterior distribution of η_5 excluding burn-in samples.

`eta_6_posterior`
: a numeric vector containing the full thinned posterior samples of the posterior distribution of η_6 excluding burn-in samples.

`f_posterior`
: a numeric vector containing the full thinned posterior samples of the posterior distribution of $f(h)$ excluding burn-in samples.

`beta_posterior`
: a numeric vector containing the full thinned posterior samples of the posterior distribution of $\beta(h)$ excluding burn-in samples.

`sigma_eps_posterior`
: a numeric vector containing the full thinned posterior samples of the posterior distribution of $\sigma_\varepsilon(h)$ excluding burn-in samples.

`Deviance_posterior`
: a numeric vector containing the full thinned posterior samples of the posterior distribution of the deviance excluding burn-in samples.

`D_hat`
: deviance at the median value of the parameters.

`num_effective_param`
: number of effective parameters, which is calculated as median(Deviance_posterior) minus D_hat.

`DIC`
: Deviance Information Criterion for the model, calculated as D_hat plus 2*num_effective_parameters.

`autocorrelation`
: a data frame with the autocorrelation of each parameter for different lags.

`acceptance_rate`
: proportion of accepted samples in the thinned MCMC chain (excluding burn-in).

`formula`
: object of type "formula" provided by the user.

`data`
: data provided by the user, ordered by stage.

`run_info`
: information about the input arguments and the specific parameters used in the MCMC chain.

References

Hrafnkelsson, B., Sigurdarson, H., and Gardarsson, S. M. (2020). Generalization of the power-law rating curve using hydrodynamic theory and Bayesian hierarchical modeling. arXiv preprint 2010.04769.

Gelman, A., Carlin, J. B., Stern, H. S., Dunson, D. B., Vehtari, A., and Rubin, D. B. (2013). Bayesian Data Analysis, Third Edition. Chapman & Hall/CRC Texts in Statistical Science. Taylor & Francis.

See Also

`summary.gplm` for summaries, `predict.gplm` for prediction and `plot.gplm` for plots. `spread_draws` and `gather_draws` are also useful to aid further visualization of the full posterior distributions.

Examples

```
data(norn)
set.seed(1)
```

```
gplm.fit <- gplm(formula=Q~W,data=norn,num_cores=2)
summary(gplm.fit)
```

---

gplm0 *Generalized power-law model with a constant variance*

Description

gplm0 is used to fit a discharge rating curve for paired measurements of stage and discharge using a generalized power-law model with a constant variance as described in Hrafnkelsson et al. (2020). See "Details" for a more elaborate description of the model.

Usage

```
gplm0(
  formula,
  data,
  c_param = NULL,
  h_max = NULL,
  parallel = TRUE,
  num_cores = NULL,
  forcepoint = rep(FALSE, nrow(data))
)
```

Arguments

formula	an object of class "formula", with discharge column name as response and stage column name as a covariate, i.e. of the form y~x where y is discharge in m^3/s and x is stage in m (it is very important that the data is in the correct units).
data	data.frame containing the variables specified in formula.
c_param	stage for which there is zero discharge. If NULL, it is treated as unknown in the model and inferred from the data.
h_max	maximum stage to which the rating curve should extrapolate to. If NULL, the maximum stage value in the data is selected as an upper bound.
parallel	logical value indicating whether to run the MCMC in parallel or not. Defaults to TRUE.
num_cores	integer between 1 and 4 (number of MCMC chains) indicating how many cores to use. Only used if parallel=TRUE. If NULL, the number of cores available on the device is detected automatically.
forcepoint	logical vector of the same length as the number of rows in data. If an element at index i is TRUE it indicates that the rating curve should be forced through the i-th measurement. Use with care, as this will strongly influence the resulting rating curve.

Details

The generalized power-law model is of the form

$$Q = a(h - c)^{f(h)}$$

where Q is discharge, h is stage, a and c are unknown constants and f is a function of h referred to as the generalized power-law exponent.

The generalized power-law model is here inferred by using a Bayesian hierarchical model. The function f is modeled at the latent level as a fixed constant \$b\$ plus a continuous stochastic process,$\beta(h)$, which is assumed to be twice differentiable. The model is on a logarithmic scale

$$\log(Q_i) = \log(a) + (b + \beta(h_i)) \log(h_i - c) + \varepsilon, i = 1, ..., n$$

where ε follows a normal distribution with mean zero and variance σ_ε^2, independent of stage. The stochastic process $\beta(h)$ is assumed a priori to be a Gaussian process governed by a Matern covariance function with smoothness parameter $\nu = 2.5$. An efficient posterior simulation is achieved by sampling from the joint posterior density of the hyperparameters of the model, and then sampling from the density of the latent parameters conditional on the hyperparameters.

Bayesian inference is based on the posterior density and summary statistics such as the posterior mean and 95% posterior intervals are based on the posterior density. Analytical formulas for these summary statistics are intractable in most cases and thus they are computed by generating samples from the posterior density using a Markov chain Monte Carlo simulation.

Value

gplm0 returns an object of class "gplm0". An object of class "gplm0" is a list containing the following components:

`rating_curve` a data frame with 2.5%, 50% and 97.5% percentiles of the posterior predictive distribution of the rating curve.

`rating_curve_mean` a data frame with 2.5%, 50% and 97.5% percentiles of the posterior distribution of the mean of the rating curve.

`param_summary` a data frame with 2.5%, 50% and 97.5% percentiles of the posterior distribution of latent- and hyperparameters. Additionally contains columns with r_hat and the effective number of samples for each parameter as defined in Gelman et al. (2013).

`beta_summary` a data frame with 2.5%, 50% and 97.5% percentiles of the posterior distribution of β.

`Deviance_summary` a data frame with 2.5%, 50% and 97.5% percentiles of the posterior distribution of the deviance.

`rating_curve_posterior` a matrix containing the full thinned posterior samples of the posterior predictive distribution of the rating curve (excluding burn-in).

`rating_curve_mean_posterior`
: a matrix containing the full thinned posterior samples of the posterior distribution of the mean of the rating curve (excluding burn-in).

`a_posterior`
: a numeric vector containing the full thinned posterior samples of the posterior distribution of a.

`b_posterior`
: a numeric vector containing the full thinned posterior samples of the posterior distribution of b.

`c_posterior`
: a numeric vector containing the full thinned posterior samples of the posterior distribution of c.

`sigma_eps_posterior`
: a numeric vector containing the full thinned posterior samples of the posterior distribution of σ_ε.

`sigma_beta_posterior`
: a numeric vector containing the full thinned posterior samples of the posterior distribution of σ_β.

`phi_beta_posterior`
: a numeric vector containing the full thinned posterior samples of the posterior distribution of ϕ_β.

`sigma_eta_posterior`
: a numeric vector containing the full thinned posterior samples of the posterior distribution of σ_η.

`beta_posterior`
: a numeric vector containing the full thinned posterior samples of the posterior distribution of β.

`Deviance_posterior`
: a numeric vector containing the full thinned posterior samples of the posterior distribution of the deviance excluding burn-in samples.

`D_hat`
: deviance at the median value of the parameters.

`num_effective_param`
: number of effective parameters, which is calculated as median(Deviance_posterior) minus D_hat.

`DIC`
: Deviance Information Criterion for the model, calculated as D_hat plus 2*num_effective_parameters.

`autocorrelation`
: a data frame with the autocorrelation of each parameter for different lags.

`acceptance_rate`
: proportion of accepted samples in the thinned MCMC chain (excluding burn-in).

`formula`
: object of type "formula" provided by the user.

`data`
: data provided by the user, ordered by stage.

`run_info`
: information about the input arguments and the specific parameters used in the MCMC chain.

References

Hrafnkelsson, B., Sigurdarson, H., and Gardarsson, S. M. (2020). Generalization of the power-law rating curve using hydrodynamic theory and Bayesian hierarchical modeling. arXiv preprint 2010.04769.

Gelman, A., Carlin, J. B., Stern, H. S., Dunson, D. B., Vehtari, A., and Rubin, D. B. (2013). Bayesian Data Analysis, Third Edition. Chapman & Hall/CRC Texts in Statistical Science. Taylor & Francis.

See Also

summary.gplm0 for summaries, predict.gplm0 for prediction. It is also useful to look at spread_draws and plot.gplm0 to help visualize the full posterior distributions.

Examples

```
data(krokfors)
set.seed(1)
gplm0.fit <- gplm0(formula=Q~W,data=krokfors,num_cores=2)
summary(gplm0.fit)
```

---

krokfors *Krokfors stream gauging station in Sweden*

Description

Data on discharge and stage from Krokfors stream gauging station in Sweden.

Usage

```
krokfors
```

Format

A data frame with columns:

W Measurements of water stage in meters

Q Measurements of water discharge in cubic meters per second

Source

Swedish Meteorological and Hydrological Institute.

norn *Norn stream gauging station in Sweden*

Description

Data on discharge and stage from Norn stream gauging station in Sweden.

Usage

```
norn
```

Format

A data frame with columns:

W Measurements of water stage in meters

Q Measurements of water discharge in cubic meters per second

Source

Swedish Meteorological and Hydrological Institute.

plm *Power-law model with variance that varies with stage.*

Description

plm is used to fit a discharge rating curve for paired measurements of stage and discharge using a power-law model with variance that varies with stage as described in Hrafnkelsson et al. (2020). See "Details" for a more elaborate description of the model.

Usage

```
plm(
  formula,
  data,
  c_param = NULL,
  h_max = NULL,
  parallel = TRUE,
  num_cores = NULL,
  forcepoint = rep(FALSE, nrow(data))
)
```

Arguments

formula	an object of class "formula", with discharge column name as response and stage column name as a covariate, i.e. of the form y~x where y is discharge in m^3/s and x is stage in m (it is very important that the data is in the correct units).
data	data.frame containing the variables specified in formula.
c_param	stage for which there is zero discharge. If NULL, it is treated as unknown in the model and inferred from the data.
h_max	maximum stage to which the rating curve should extrapolate to. If NULL, the maximum stage value in the data is selected as an upper bound.
parallel	logical value indicating whether to run the MCMC in parallel or not. Defaults to TRUE.
num_cores	integer between 1 and 4 (number of MCMC chains) indicating how many cores to use. Only used if parallel=TRUE. If NULL, the number of cores available on the device is detected automatically.
forcepoint	logical vector of the same length as the number of rows in data. If an element at index i is TRUE it indicates that the rating curve should be forced through the i-th measurement. Use with care, as this will strongly influence the resulting rating curve.

Details

The power-law model, which is commonly used in hydraulic practice, is of the form

$$Q = a(h - c)^b$$

where Q is discharge, h is stage and a, b and c are unknown constants.

The power-law model is here inferred by using a Bayesian hierarchical model. The model is on a logarithmic scale

$$\log(Q_i) = \log(a) + b\log(h_i - c) + \varepsilon_i, i = 1, ..., n$$

where ε_i follows a normal distribution with mean zero and variance $\sigma_\varepsilon(h_i)^2$ that varies with stage. The error variance, $\sigma_\varepsilon^2(h)$, of the log-discharge data is modeled as an exponential of a B-spline curve, that is, a linear combination of six B-spline basis functions that are defined over the range of the stage observations. An efficient posterior simulation is achieved by sampling from the joint posterior density of the hyperparameters of the model, and then sampling from the density of the latent parameters conditional on the hyperparameters.

Bayesian inference is based on the posterior density and summary statistics such as the posterior mean and 95% posterior intervals are based on the posterior density. Analytical formulas for these summary statistics are intractable in most cases and thus they are computed by generating samples from the posterior density using a Markov chain Monte Carlo simulation.

Value

plm returns an object of class "plm". An object of class "plm" is a list containing the following components:

`rating_curve` a data frame with 2.5%, 50% and 97.5% percentiles of the posterior predictive distribution of the rating curve.

`rating_curve_mean`
a data frame with 2.5%, 50% and 97.5% percentiles of the posterior distribution of the mean of the rating curve. Additionally contains columns with r_hat and the effective number of samples for each parameter as defined in Gelman et al. (2013).

`param_summary` a data frame with 2.5%, 50% and 97.5% percentiles of the posterior distribution of latent- and hyperparameters.

`sigma_eps_summary`
a data frame with 2.5%, 50% and 97.5% percentiles of the posterior of σ_ε.

`Deviance_summary`
a data frame with 2.5%, 50% and 97.5% percentiles of the posterior distribution of the deviance.

`rating_curve_posterior`
a matrix containing the full thinned posterior samples of the posterior predictive distribution of the rating curve (excluding burn-in).

`rating_curve_mean_posterior`
a matrix containing the full thinned posterior samples of the posterior distribution of the mean of the rating curve (excluding burn-in).

`a_posterior` a numeric vector containing the full thinned posterior samples of the posterior distribution of a.

`b_posterior` a numeric vector containing the full thinned posterior samples of the posterior distribution of b.

`c_posterior` a numeric vector containing the full thinned posterior samples of the posterior distribution of c.

`sigma_eps_posterior`
a numeric vector containing the full thinned posterior samples of the posterior distribution of σ_ε.

`eta_1_posterior`
a numeric vector containing the full thinned posterior samples of the posterior distribution of η_1.

`eta_2_posterior`
a numeric vector containing the full thinned posterior samples of the posterior distribution of η_2.

`eta_3_posterior`
a numeric vector containing the full thinned posterior samples of the posterior distribution of η_3.

`eta_4_posterior`
a numeric vector containing the full thinned posterior samples of the posterior distribution of η_4.

`eta_5_posterior`
a numeric vector containing the full thinned posterior samples of the posterior distribution of η_5.

`eta_6_posterior`
: a numeric vector containing the full thinned posterior samples of the posterior distribution of η_6.

`Deviance_posterior`
: a numeric vector containing the full thinned posterior samples of the posterior distribution of the deviance excluding burn-in samples.

`D_hat`
: deviance at the median value of the parameters.

`num_effective_param`
: number of effective parameters, which is calculated as median(Deviance_posterior) minus D_hat.

`DIC`
: Deviance Information Criterion for the model, calculated as D_hat plus 2*num_effective_parameters.

`autocorrelation`
: a data frame with the autocorrelation of each parameter for different lags.

`acceptance_rate`
: proportion of accepted samples in the thinned MCMC chain (excluding burn-in).

`formula`
: object of type "formula" provided by the user.

`data`
: data provided by the user, ordered by stage.

`run_info`
: information about the input arguments and the specific parameters used in the MCMC chain.

References

Hrafnkelsson, B., Sigurdarson, H., and Gardarsson, S. M. (2020). Generalization of the power-law rating curve using hydrodynamic theory and Bayesian hierarchical modeling. arXiv preprint 2010.04769.

Gelman, A., Carlin, J. B., Stern, H. S., Dunson, D. B., Vehtari, A., and Rubin, D. B. (2013). Bayesian Data Analysis, Third Edition. Chapman & Hall/CRC Texts in Statistical Science. Taylor & Francis.

See Also

`summary.plm` for summaries, `predict.plm` for prediction. It is also useful to look at `spread_draws` and `plot.plm` to help visualize the full posterior distributions.

Examples

```
data(spanga)
set.seed(1)
plm.fit <- plm(formula=Q~W,data=spanga,num_cores=2)
summary(plm.fit)
```

plm0 *Power-law model with a constant variance*

Description

plm0 is used to fit a discharge rating curve for paired measurements of stage and discharge using a power-law model with a constant variance as described in Hrafnkelsson et al. (2020). See "Details" for a more elaborate description of the model.

Usage

```
plm0(
  formula,
  data,
  c_param = NULL,
  h_max = NULL,
  parallel = TRUE,
  num_cores = NULL,
  forcepoint = rep(FALSE, nrow(data))
)
```

Arguments

formula	an object of class "formula", with discharge column name as response and stage column name as a covariate, i.e. of the form y~x where y is discharge in m^3/s and x is stage in m (it is very important that the data is in the correct units).
data	data.frame containing the variables specified in formula.
c_param	stage for which there is zero discharge. If NULL, it is treated as unknown in the model and inferred from the data.
h_max	maximum stage to which the rating curve should extrapolate to. If NULL, the maximum stage value in the data is selected as an upper bound.
parallel	logical value indicating whether to run the MCMC in parallel or not. Defaults to TRUE.
num_cores	integer between 1 and 4 (number of MCMC chains) indicating how many cores to use. Only used if parallel=TRUE. If NULL, the number of cores available on the device is detected automatically.
forcepoint	logical vector of the same length as the number of rows in data. If an element at index i is TRUE it indicates that the rating curve should be forced through the i-th measurement. Use with care, as this will strongly influence the resulting rating curve.

Details

The power-law model, which is commonly used in hydraulic practice, is of the form

$$Q = a(h - c)^b$$

where Q is discharge, h is stage and a, b and c are unknown constants.

The power-law model is here inferred by using a Bayesian hierarchical model. The model is on a logarithmic scale

$$\log(Q_i) = \log(a) + b\log(h_i - c) + \varepsilon, i = 1, ..., n$$

where ε follows a normal distribution with mean zero and variance σ_ε^2, independent of stage. An efficient posterior simulation is achieved by sampling from the joint posterior density of the hyperparameters of the model, and then sampling from the density of the latent parameters conditional on the hyperparameters.

Bayesian inference is based on the posterior density and summary statistics such as the posterior mean and 95% posterior intervals are based on the posterior density. Analytical formulas for these summary statistics are intractable in most cases and thus they are computed by generating samples from the posterior density using a Markov chain Monte Carlo simulation.

Value

plm0 returns an object of class "plm0". An object of class "plm0" is a list containing the following components:

`rating_curve` a data frame with 2.5%, 50% and 97.5% percentiles of the posterior predictive distribution of the rating curve.

`rating_curve_mean` a data frame with 2.5%, 50% and 97.5% percentiles of the posterior distribution of the mean of the rating curve.

`param_summary` a data frame with 2.5%, 50% and 97.5% percentiles of the posterior distribution of latent- and hyperparameters. Additionally contains columns with r_hat and the effective number of samples for each parameter as defined in Gelman et al. (2013).

`Deviance_summary` a data frame with 2.5%, 50% and 97.5% percentiles of the posterior distribution of the deviance.

`rating_curve_posterior` a matrix containing the full thinned posterior samples of the posterior predictive distribution of the rating curve (excluding burn-in).

`rating_curve_mean_posterior` a matrix containing the full thinned posterior samples of the posterior distribution of the mean of the rating curve (excluding burn-in).

`a_posterior` a numeric vector containing the full thinned posterior samples of the posterior distribution of a.

`b_posterior` a numeric vector containing the full thinned posterior samples of the posterior distribution of b.

`c_posterior` a numeric vector containing the full thinned posterior samples of the posterior distribution of c.

`sigma_eps_posterior` a numeric vector containing the full thinned posterior samples of the posterior distribution of σ_ε.

`Deviance_posterior`
: a numeric vector containing the full thinned posterior samples of the posterior distribution of the deviance excluding burn-in samples.

`D_hat`
: deviance at the median value of the parameters

`num_effective_param`
: number of effective parameters, which is calculated as median(Deviance_posterior) minus D_hat.

`DIC`
: Deviance Information Criterion for the model, calculated as D_hat plus 2*num_effective_parameters.

`autocorrelation`
: a data frame with the autocorrelation of each parameter for different lags.

`acceptance_rate`
: proportion of accepted samples in the thinned MCMC chain (excluding burn-in).

`formula`
: object of type "formula" provided by the user.

`data`
: data provided by the user, ordered by stage.

`run_info`
: information about the input arguments and the specific parameters used in the MCMC chain.

References

Hrafnkelsson, B., Sigurdarson, H., and Gardarsson, S. M. (2020). Generalization of the power-law rating curve using hydrodynamic theory and Bayesian hierarchical modeling. arXiv preprint 2010.04769.

Gelman, A., Carlin, J. B., Stern, H. S., Dunson, D. B., Vehtari, A., and Rubin, D. B. (2013). Bayesian Data Analysis, Third Edition. Chapman & Hall/CRC Texts in Statistical Science. Taylor & Francis.

See Also

`summary.plm0` for summaries, `predict.plm0` for prediction. It is also useful to look at `spread_draws` and `plot.plm0` to help visualize the full posterior distributions.

Examples

```
data(skogsliden)
set.seed(1)
plm0.fit <- plm0(formula=Q~W,data=skogsliden,num_cores=2)
summary(plm0.fit)
```

plot.plm0 *Plot method for discharge rating curves*

Description

Visualize discharge rating curve model objects

Usage

```
## S3 method for class 'plm0'
plot(x, type = "rating_curve", param = NULL, transformed = FALSE, ...)

## S3 method for class 'plm'
plot(x, type = "rating_curve", param = NULL, transformed = FALSE, ...)

## S3 method for class 'gplm0'
plot(x, type = "rating_curve", param = NULL, transformed = FALSE, ...)

## S3 method for class 'gplm'
plot(x, type = "rating_curve", param = NULL, transformed = FALSE, ...)
```

Arguments

x	object of class "plm0", "plm", "gplm0" or "gplm".
type	a character denoting what type of plot should be drawn. Defaults to "rating_curve". Possible types are • "rating_curve" to plot the rating curve. • "rating_curve_mean" to plot the posterior mean of the rating curve. • "f" to plot the power-law exponent. • "beta" to plot the random effect in the power-law exponent. • "sigma_eps" to plot the standard deviation on the data level. • "residuals" to plot the log residuals. • "trace" to plot trace plots of parameters given in param. • "histogram" to plot histograms of parameters given in param. • "panel" to plot a 2x2 panel of plots: "rating curve", "residuals", "f" and "sigma_eps"
param	a character vector with the parameters to plot. Defaults to NULL and is only used if type is "trace" or "histogram". Allowed values are the parameters given in the model summary of x as well as "hyperparameters" or "latent_parameters" for specific groups of parameters.
transformed	a logical value indicating whether the quantity should be plotted on a transformed scale used during the Bayesian inference. Defaults to FALSE.
...	further arguments passed to other methods. Currently supports: • "title" a character denoting the title of the plot

- "xlim" numeric vector of length 2, denoting the limits on the x axis of the plot. Applicable for types "rating_curve","rating_curve_mean","f","beta","sigma_eps","residuals".
- "ylim" numeric vector of length 2, denoting the limits on the y axis of the plot. Applicable for types "rating_curve","rating_curve_mean","f","beta","sigma_eps","residuals".

Value

No return value, called for side effects.

Functions

- `plot.plm0`: Plot method for plm0
- `plot.plm`: Plot method for plm
- `plot.gplm0`: Plot method for gplm0
- `plot.gplm`: Plot method for gplm

See Also

`plm0`, `plm`, `gplm0` and `gplm` for fitting a discharge rating curve and `summary.plm0`, `summary.plm`, `summary.gplm0` and `summary.gplm` for summaries. It is also useful to look at `spread_draws` and `gather_draws` to work directly with the MCMC samples.

Examples

```
data(krokfors)
set.seed(1)
plm0.fit <- plm0(formula=Q~W,data=krokfors,num_cores=2)

plot(plm0.fit)
plot(plm0.fit,transformed=TRUE)
plot(plm0.fit,type='histogram',param='c')
plot(plm0.fit,type='histogram',param='c',transformed=TRUE)
plot(plm0.fit,type='histogram',param='hyperparameters')
plot(plm0.fit,type='histogram',param='latent_parameters')
plot(plm0.fit,type='residuals')
plot(plm0.fit,type='f')
plot(plm0.fit,type='sigma_eps')
```

`plot.tournament` *Plot method for discharge rating curve tournament*

Description

Compare the four models from the tournament object in multiple ways

Usage

```
## S3 method for class 'tournament'
plot(x, type = "tournament_results", transformed = FALSE, ...)
```

Arguments

`x`	an object of class "tournament"
`type`	a character denoting what type of plot should be drawn. Possible types are • "deviance" to plot the deviance of the four models. • "rating_curve" to plot the rating curve. • "rating_curve_mean" to plot the posterior mean of the rating curve. • "f" to plot the power-law exponent. • "sigma_eps" to plot the standard deviation on the data level. • "residuals" to plot the log residuals. • "residuals" to plot tournament results visually, game for game.
`transformed`	a logical value indicating whether the quantity should be plotted on a transformed scale used during the Bayesian inference. Defaults to FALSE.
`...`	further arguments passed to other methods.

Value

No return value, called for side effects

See Also

`tournament` to run a discharge rating curve tournament and `summary.tournament` for summaries.

Examples

```
data(krokfors)
set.seed(1)
t_obj <- tournament(formula=Q~W,data=krokfors,num_cores=2)
plot(t_obj)
plot(t_obj,transformed=TRUE)
plot(t_obj,type='deviance')
plot(t_obj,type='f')
plot(t_obj,type='sigma_eps')
```

```
plot(t_obj,type='residuals')
plot(t_obj,type='tournament_results')
```

`predict.plm0` *Predict method for discharge rating curves*

Description

Predict the discharge for given stage values based on a discharge rating curve model object.

Usage

```
## S3 method for class 'plm0'
predict(object, newdata = NULL, wide = FALSE, ...)

## S3 method for class 'plm'
predict(object, newdata = NULL, wide = FALSE, ...)

## S3 method for class 'gplm0'
predict(object, newdata = NULL, wide = FALSE, ...)

## S3 method for class 'gplm'
predict(object, newdata = NULL, wide = FALSE, ...)
```

Arguments

`object`	an object of class "plm0", "plm", "gplm0" or "gplm".
`newdata`	a numeric vector of stage values for which to predict. If omitted, the stage values in the data are used.
`wide`	a logical value denoting whether to produce a wide prediction output.If TRUE, then the output is a table with median prediction values for an equally spaced grid of stages with 1 cm increments, each row containing predictions in a decimeter range of stages.
`...`	not used in this function

Value

an object of class "data.frame" with four columns, h (stage), lower (2.5% posterior predictive quantile), median (50% posterior predictive quantile), upper (97.5% posterior predictive quantile). If wide=TRUE, a matrix as described above (see wide parameter) is returned.

Functions

- `predict.plm0`: Predict method for plm0
- `predict.plm`: Predict method for plm
- `predict.gplm0`: Predict method for gplm0
- `predict.gplm`: Predict method for gplm

See Also

plm0, plm, gplm0 and gplm for fitting a discharge rating curve and summary.plm0, summary.plm, summary.gplm0 and summary.gplm for summaries. It is also useful to look at plot.plm0, plot.plm, plot.gplm0 and plot.gplm to help visualize all aspects of the fitted discharge rating curve. Additionally, spread_draws and spread_draws help working directly with the MCMC samples.

Examples

```
data(krokfors)
set.seed(1)
plm0.fit <- plm0(formula=Q~W,data=krokfors,h_max=10,num_cores=2)
#predict rating curve on a equally 10 cm spaced grid from 9 to 10 meters
predict(plm0.fit,newdata=seq(9,10,by=0.1))
```

---

print.plm0 *Print method for discharge rating curves*

Description

Print a discharge rating curve model object

Usage

```
## S3 method for class 'plm0'
print(x, ...)

## S3 method for class 'plm'
print(x, ...)

## S3 method for class 'gplm0'
print(x, ...)

## S3 method for class 'gplm'
print(x, ...)
```

Arguments

x	an object of class "plm0", "plm", "gplm0" or "gplm".
...	not used in this function

Functions

- print.plm0: Print method for plm0
- print.plm: Print method for plm
- print.gplm0: Print method for gplm0
- print.gplm: Print method for gplm

See Also

plm0, plm, gplm0, gplm for fitting a discharge rating curve and summary.plm0, summary.plm, summary.gplm0 and summary.gplm for summaries. It is also useful to look at plot.plm0, plot.plm, plot.gplm0 and plot.gplm to help visualize all aspects of the fitted discharge rating curve. Additionally, spread_draws and spread_draws help working directly with the MCMC samples.

---

print.tournament *Print method for discharge rating curve tournament*

Description

Print the results of a tournament of discharge rating curve model comparisons

Usage

```
## S3 method for class 'tournament'
print(x, ...)
```

Arguments

x	an object of class "tournament"
...	not used in this function

See Also

tournament to run a discharge rating curve tournament, summary.tournament for summaries and plot.tournament for visualizing the mode comparison.

---

skogsliden *Skogsliden stream gauging station in Sweden*

Description

Data on discharge and stage from Skogsliden stream gauging station in Sweden

Usage

```
skogsliden
```

Format

A data frame with columns:

W Measurements of water stage in meters

Q Measurements of water discharge in cubic meters per second

Source

Swedish Meteorological and Hydrological Institute.

`spanga` *Spanga stream gauging station in Sweden*

Description

Data on discharge and stage from Spanga stream gauging station in Sweden.

Usage

```
spanga
```

Format

A data frame with columns:

W Measurements of water stage in meters

Q Measurements of water discharge in cubic meters per second

Source

Swedish Meteorological and Hydrological Institute.

`spread_draws` *Spread MCMC chain draws to data.frame on a wide format*

Description

Useful to convert MCMC chain draws of particular parameters or output from the model object to a wide format for further data wrangling

Usage

```
spread_draws(mod, ..., transformed = FALSE)
```

Arguments

`mod`	an object of class "plm0","plm","gplm0" or "gplm".
`...`	any number of character vectors containing valid names of parameters in the model or "rating_curve" and "rating_curve_mean". Also accepts "latent_parameters" and "hyperparameters".
`transformed`	boolean value determining whether the output is to be represented on the transformed scale used for sampling in the MCMC chain or the original scale. Defaults to FALSE.

Value

Data frame with columns `chain` `iter` `param` `value`

References

B. Hrafnkelsson, H. Sigurdarson, S.M. Gardarsson, 2020, Generalization of the power-law rating curve using hydrodynamic theory and Bayesian hierarchical modeling. arXiv preprint 2010.04769

See Also

`plm0`, `plm`, `gplm0`, `gplm` for further information on parameters

Examples

```
data(krokfors)
set.seed(1)
plm0.fit <- plm0(formula=Q~W,data=krokfors,num_cores=2)
hyp_samples <- spread_draws(plm0.fit,'hyperparameters')
head(hyp_samples)
rating_curve_samples <- spread_draws(plm0.fit,'rating_curve','rating_curve_mean')
head(rating_curve_samples)
```

---

summary.plm0 *Summary method for discharge rating curves*

Description

Summarize a discharge rating curve model object

Usage

```
## S3 method for class 'plm0'
summary(object, ...)

## S3 method for class 'plm'
summary(object, ...)

## S3 method for class 'gplm0'
summary(object, ...)

## S3 method for class 'gplm'
summary(object, ...)
```

Arguments

`object`	an object of class "plm0", "plm", "gplm0" or "gplm".
`...`	Not used for this function

Functions

- `summary.plm0`: Summary method for plm0
- `summary.plm`: Summary method for plm
- `summary.gplm0`: Summary method for gplm0
- `summary.gplm`: Summary method for gplm

See Also

`plm0`, `plm`, `gplm0` and `gplm` for fitting a discharge rating curve. It is also useful to look at `plot.plm0`, `plot.plm`, `plot.gplm0` and `plot.gplm` to help visualize all aspects of the fitted discharge rating curve. Additionally, `spread_draws` and `spread_draws` help working directly with the MCMC samples.

Examples

```
data(krokfors)
set.seed(1)
plm0.fit <- plm0(formula=Q~W,data=krokfors,num_cores=2)
summary(plm0.fit)
```

---

summary.tournament *Summary method for a discharge rating curve tournament*

Description

Print the summary of a tournament of model comparisons

Usage

```
## S3 method for class 'tournament'
summary(object, ...)
```

Arguments

`object`	an object of class "tournament"
`...`	not used in this function

See Also

`tournament` to run a discharge rating curve tournament and `plot.tournament` for visualizing the mode comparison

Examples

```
data(krokfors)
set.seed(1)
t_obj <- tournament(Q~W,krokfors,num_cores=2)
summary(t_obj)
```

`tournament` *Tournament - Model comparison*

Description

tournament compares four rating curve models of different complexities and determines the model that provides the best fit of the data at hand.

Usage

```
tournament(formula = NULL, data = NULL, ..., winning_criteria = 0.75)
```

Arguments

`formula`	an object of class "formula", with discharge column name as response and stage column name as a covariate.
`data`	data.frame containing the variables specified in formula.
`...`	optional arguments passed to the model functions. Also, if data and formula are NULL, one can add four model objects of types "gplm", "gplm0", "plm" and "plm0". This runs the tournament for the input models and prevents running all four models explicitly.
`winning_criteria`	a numerical value between 0 and 1 which sets the threshold for which the probability of the more complex model given the data in each model comparison, must exceed for it to be declared the better model. This value defaults to 0.75 to favor the less complex models when the superiority of the more complex model is somewhat ambiguous. See the Details section.

Details

Tournament is a comparison method that uses Bayes factor to compute the posterior probabilities of the models and select the most appropriate of the four models given the data. The first round of model comparisons sets up model types "gplm" vs. "gplm0" and "plm" vs. "plm0". If the posterior probability of the more complex model ("gplm" and "plm", respectively) exceeds the "winning_criteria" (default value = 0.75) then it is chosen as the more appropriate model and moves on to the second and final round, where the winners from the first round will be compared in the same way. In the second round, if the more complex model (now the generalized power-law model) exceeds the same "winning_criteria" then it is chosen as the overall tournament winner and deemed

the most appropriate model given the data. In each of the three matches, the posterior probabilities of the models are computed using the Bayes factor and assuming a priori that the two models were equally likely [see Jeffreys (1961) and Kass and Raftery (1995)].

Value

An object of type "tournament" with the following elements

`summary` a data frame with information on results of the different games in the tournament.

`contestants` model objects of types "plm0","plm","gplm0" and "gplm" being compared.

`winner` model object of the tournament winner.

References

B. Hrafnkelsson, H. Sigurdarson, S.M. Gardarsson, 2020, Generalization of the power-law rating curve using hydrodynamic theory and Bayesian hierarchical modeling. arXiv preprint 2010.04769.

Jeffreys, H. (1961). Theory of Probability, Third Edition. Oxford University Press.

Kass, R., and A. Raftery, A. (1995). Bayes Factors. Journal of the American Statistical Association, 90, 773-795.

See Also

`summary.tournament` and `plot.tournament`

Examples

```
data(krokfors)
set.seed(1)
t_obj <- tournament(formula=Q~W,data=krokfors,num_cores=2)
t_obj
summary(t_obj)
```

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