Package 'boussinesq'

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License GPL (>= 2)

Title Analytic Solutions for (Ground-Water) Boussinesq Equation

Type Package

Depends R (>= 2.10)

Author Emanuele Cordano

Description A collection of R functions were implemented
from published and available analytic solutions for the
One-Dimensional Boussinesq Equation (ground-water). In
particular, the function ``beq.lin()'' is the analytic solution of
the linearized form of Boussinesq Equation between two
different head-based boundary (Dirichlet) conditions;
``beq.song'' is the non-linear power-series analytic solution of
the motion of a wetting front over a dry bedrock (Song at al,
2007, see complete reference on function documentation).
Bugs/comments/questions/collaboration of any kind are warmly
welcomed.

Version 1.0.4

Repository CRAN

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Collate 'beq.lin.dimensionless.R' 'beq.lin.R'
'beq.song.dimensionless.R' 'beq.song.R' 'boussinesq-package.R'
'coefficient.song.solution.R'

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RoxygenNote 7.1.2

R topics documented:

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  boussinesq-package   *Analytic solutions for (ground-water) Boussinesq Equation*

Description

Analytic solutions for (ground-water) Boussinesq Equation

Details

Package:	boussinesq
Type:	Package
Version:	1.0.2
Date:	2013-04-18
License:	GPL (>= 2)
LazyLoad:	yes
Depends:	R(>=2.12)

Author(s)

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  beq.lin   *Analytic exact solution for One-Dimensional Boussinesq Equation in*
                                       a two-bounded domain with two constant-value Dirichlet Condition

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Description

Analytic exact solution for One-Dimensional Boussinesq Equation in a two-bounded domain with two constant-value Dirichlet Condition

Usage

```
beq.lin(
  t = 0,
  x = seq(from = 0, to = L, by = by),
```

```
    h1 = 1,
    h2 = 1,
    L = 100,
    ks = 0.01,
    s = 0.4,
    big = 10^7,
    by = L/100,
    p = 0.5
)
```

Arguments

t	time coordinate.
x	spatial coordinate. Default is seq(from=0,to=L,by=by).
h1	water surface level at x=0. Left Dirichlet Bounday Condition.
h2	water surface level at x=L. Right Dirichlet Bondary Condition.
L	length of the domain.
ks	Hydraulic conductivity
s	drainable pororosity (assumed to be constant)
big	maximum level of Fourier series considered. Default is 10^7.
by	see [seq](#)
p	empirical coefficient to estimate hydraulic diffusivity $D = ks/(s * (p * h1 + (1 - p) * h2))$. It ranges between 0 and 1.

Value

Solutions for the indicated values of x and t.

Author(s)

Emanuele Cordano

See Also

[beq.lin.dimensionless](#)

Examples

```
L <- 1000
x <- seq(from=0,to=L,by=L/100)
t <- 4 # 4 days
h_sol0 <- beq.lin(x=x,t=t*24*3600,h1=2,h2=1,ks=0.01,L=L,s=0.4,big=100,p=0.0)
h_solp <- beq.lin(x=x,t=t*24*3600,h1=2,h2=1,ks=0.01,L=L,s=0.4,big=100,p=0.5)
h_sol1 <- beq.lin(x=x,t=t*24*3600,h1=2,h2=1,ks=0.01,L=L,s=0.4,big=100,p=1.0)

plot(x,h_sol0,type="l",lty=1,main=paste("Water Surface Elevetion after",
t,"days",sep=" "),xlab="x[m]",ylab="h[m]")
lines(x,h_solp,lty=2)
```

```
lines(x,h_sol1,lty=3)
legend("topright",lty=1:3,legend=c("p=0","p=0.5","p=1"))
```

---

beq.lin.dimensionless *Analytic exact solution for Dimentionless (i. e. diffusivity equal to 1 -*
unity) One Dimensional Heat Equation in a two-bounded domain with
two constant-value Dirichlet Conditions

Description

Analytic exact solution for Dimentionless (i. e. diffusivity equal to 1 - unity) One Dimensional
Heat Equation in a two-bounded domain with two constant-value Dirichlet Conditions

Usage

```
beq.lin.dimensionless(
  t = 0,
  x = seq(from = 0, to = L, by = by),
  big = 1e+05,
  by = L * 0.01,
  L = 1
)
```

Arguments

t	time coordinate.
x	spatial coordinate. Default is seq(from=0,to=L,by=by).
big	maximum level of Fourier series considered. Default is 100000.
by	see seq
L	length of the domain. It is used if x is not specified.

Value

Solutions for the specifiied values of x and t

Author(s)

Emanuele Cordano

References

Rozier-Cannon, J. (1984), The One-Dimensional Heat Equation, Addison-Wesley Publishing Com-
pany, Manlo Park, California, encyclopedia of Mathematics and its applications.

See Also

beq.lin

beq.song	*Song et al.'s analytic solution to Boussinesq equation in a 1D semi-infinite domain with a Dirichlet boundary condition*

Description

Song et al.'s analytic solution to Boussinesq equation in a 1D semi-infinite domain with a Dirichlet boundary condition

Usage

```
beq.song(t = 0.5, x = 1, s = 0.4, h1 = 1, ks = 0.01, nmax = 4, alpha = 1)
```

Arguments

t	time coordinate.
x	spatial coordinate. Default is seq(from=0,to=L,by=by).
s	drainable pororosity (assumed to be constant)
h1	water surface level or boundary condition coefficient at x=0. Left Dirichlet Bounday Condition.
ks	Hydraulic conductivity
nmax	order of power series considered for the analytic solution solution. Default is 4.
alpha	α exponent see Song at al, 2007

Value

The water surface eletion vs time and space obtained by the analytic solution of Boussinesq Equation

Note

For major details, see Song at al, 2007

Author(s)

Emanuele Cordano

References

Song, Zhi-yao;Li, Ling;David, Lockington. (2007), "Note on Barenblatt power series solution to Boussinesq equation",Applied Mathematics and Mechanics, https://link.springer.com/article/10.1007/s10483-007-0612-x ,doi: 10.1007/s104830070612x

See Also

beq.song.dimensionless

Examples

```
L <- 1000
x <- seq(from=0,to=L,by=L/100)
t <- c(4,5,20) #  days

h_sol1 <- beq.song(t=t[1]*3600*24,x=x,s=0.4,h1=1,ks=0.01,nmax=10,alpha=0)
h_sol2 <- beq.song(t=t[2]*3600*24,x=x,s=0.4,h1=1,ks=0.01,nmax=10,alpha=0)
h_sol3 <- beq.song(t=t[3]*3600*24,x=x,s=0.4,h1=1,ks=0.01,nmax=10,alpha=0)


plot(x,h_sol1,type="l",lty=1,
main="Water Surface Elevetion (Song at's solution) ",
xlab="x[m]",ylab="h[m]")
lines(x,h_sol2,lty=2)
lines(x,h_sol3,lty=3)
legend("topright",lty=1:3,legend=paste("t=",t,"days",sep=" "))
```

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beq.song.dimensionless

Dimensionless solution for one-dimensional derived equation from scaling Boussinesq Equation (Song et al, 2007)

Description

Dimensionless solution for one-dimensional derived equation from scaling Boussinesq Equation (Song et al, 2007)

Usage

```
beq.song.dimensionless(xi, xi0, a)
```

Arguments

xi	dimensionless coordinate (see Note)
xi0	displacement of wetting front expressed as dimensionless coordinate (see Note)
a	vector of coefficient returned by coefficient.song.solution

Value

the dimesioneless solution, i.e. the variable H

Note

The expession for the dimensionless coordinate (Song at al., 2007) is $\xi = x(\frac{2\,s}{\eta_1\,K_s\,t^{\alpha+1}})^{1/2}$ and the solution for the dimensionless equation derived by Boussinesq Equation is: $H = \sum_{n=0}^{\infty} a_n(1-\frac{\xi}{\xi_0})^n$ for $\xi < \xi_0$, otherwise is 0.

Author(s)

Emanuele Cordano

References

Song, Zhi-yao;Li, Ling;David, Lockington. (2007), "Note on Barenblatt power series solution to Boussinesq equation",Applied Mathematics and Mechanics, https://link.springer.com/article/10.1007/s10483-007-0612-x ,doi: [10.1007/s104830070612x](10.1007/s104830070612x)

See Also

beq.song

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coefficient.song.solution

Alogorithm for resolution of the series coefficient a_n for the dimensionless formula for H in beq.song.dimensionless

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Description

Alogorithm for resolution of the series coefficient a_n for the dimensionless formula for H in beq.song.dimensionless

Usage

```
coefficient.song.solution(n = 4, lambda = 0)
```

Arguments

n	approximation order
lambda	dimensionless parameter related to α see Song at al, 2007

Value

the a_n series coefficient

Note

For major details, see Song at al, 2007

Author(s)

Emanuele Cordano

References

Song, Zhi-yao;Li, Ling;David, Lockington. (2007), "Note on Barenblatt power series solution to Boussinesq equation",Applied Mathematics and Mechanics, https://link.springer.com/article/10.1007/s10483-007-0612-x ,doi: [10.1007/s104830070612x](10.1007/s104830070612x)

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