

# Package ‘incubate’

October 13, 2022

**Title** Parametric Time-to-Event Analysis with Variable Incubation Phases

**Version** 1.2.0

**Date** 2022-07-25

**Description** Fit parametric models for time-to-event data that show an initial 'incubation period', i.e., a variable delay phase where the hazard is zero. The delayed Weibull distribution serves as the foundational data model. The specific method of 'MPSE' (maximum product of spacings estimation) is used for parameter estimation. Bootstrap confidence intervals for parameters and significance tests in a two group setting are provided.

**License** LGPL (>= 3)

**Encoding** UTF-8

**LazyData** true

**Imports** future (>= 1.21), future.apply (>= 1.6), glue (>= 1.4), MASS, purrr (>= 0.3), rlang (>= 0.4), stats, survival, tibble

**Suggests** boot, future.callr, ggplot2 (>= 3.3), knitr, testthat (>= 3.0.0)

**URL** <https://gitlab.com/imb-dev/incubate/>

**BugReports** <https://gitlab.com/imb-dev/incubate/-/issues/>

**RoxygenNote** 7.2.0

**Config/testthat/edition** 3

**Depends** R (>= 2.10)

**NeedsCompilation** no

**Author** Matthias Kuhn [aut, cre] (<<https://orcid.org/0000-0003-2868-5155>>)

**Maintainer** Matthias Kuhn <matthias.kuhn@tu-dresden.de>

**Repository** CRAN

**Date/Publication** 2022-07-25 13:30:08 UTC

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|            |                                       |
|------------|---------------------------------------|
| as_percent | <i>Format a number as percentage.</i> |
|------------|---------------------------------------|

---

### Description

Internal helper function that is not exported.

### Usage

```
as_percent(x, digits = 1)
```

### Arguments

|        |  |
|--------|--|
| x      | numeric vector to be formatted as percentage         |
| digits | requested number of decimal digits of the percentage |

### Value

number formatted as percentage character

---

|            |  |
|------------|--|
| bsDataStep | <i>Generate bootstrap distribution of model parameters to fitted incubate model.</i> |
|------------|--|

---

### Description

Bootstrap data are here estimated coefficients from models fitted to bootstrap samples. The bootstrap data is used to make bootstrap inference in the second step. It is an internal function, the main entry point is `confint.incubate_fit()`.

### Usage

```
bsDataStep(
  object,
  bs_data = c("parametric", "ordinary"),
  R,
  useBoot = FALSE,
  smd_factor = 0.25
)
```

### Arguments

|            |   |
|------------|---|
| object     | an incubate_fit-object  |
| bs_data    | character. Which type of bootstrap method to generate data?   |
| R          | integer. Number of bootstrapped model coefficient estimates   |
| useBoot    | flag. Do you want to use the boot-package? Default value is FALSE.  |
| smd_factor | numeric. smooth-delay factor: influence the amount of smoothing. 0 means no smoothing at all. Default is 0.25 (as was optimal in simulation for log-quantile together with log-delay-shift = 5) |

### Value

bootstrap data, either as matrix or of class boot (depending on the useBoot-flag)

---

|                   |   |
|-------------------|---|
| coef.incubate_fit | <i>Coefficients of a delay-model fit.</i> |
|-------------------|---|

---

### Description

Coefficients of a delay-model fit.

### Usage

```
## S3 method for class 'incubate_fit'
coef(object, group = NULL, ...)
```

**Arguments**

|        |   |
|--------|---|
| object | object that is a incubate_fit                                     |
| group  | character string to request the canonical parameter for one group |
| ...    | further arguments, currently not used.                            |

**Value**

named coefficient vector

---

confint.incubate\_fit *Confidence intervals for parameters of incubate-model fits.*

---

**Description**

Bias-corrected bootstrap confidence limits (either quantile-based or normal-approximation based) are generated. Optionally, there are also variants that use a log-transformation first. At least R=1000 bootstrap replications are recommended. Default are quantile-based confidence intervals that internally use a log-transformation.

**Usage**

```
## S3 method for class 'incubate_fit'
confint(
  object,
  parm,
  level = 0.95,
  R = 199L,
  bs_data,
  bs_infer = c("logquantile", "lognormal", "quantile", "quantile0", "normal",
              "normal0"),
  useBoot = FALSE,
  ...
)
```

**Arguments**

|         |   |
|---------|---|
| object  | object of class incubate_fit  |
| parm    | character. Which parameters to get confidence interval for?   |
| level   | numeric. Which is the requested confidence level for the interval? Default value is 0.95  |
| R       | number of bootstrap replications. Used only if not bs_data-object is provided.  |
| bs_data | character or bootstrap data object. If character, it specifies which type of bootstrap is requested and the bootstrap data will be generated. Data can also be provided here directly. If missing it uses parametric bootstrap. |

|          |  |
|----------|--|
| bs_infer | character. Which type of bootstrap inference is requested to generate the confidence interval? |
| useBoot  | logical. Delegate bootstrap confint calculation to the boot-package?                           |
| ...      | further arguments, currently not used.   |

**Value**

A matrix (or vector) with columns giving lower and upper confidence limits for each parameter.

---

DelayedExponential      *Delayed Exponential Distribution*

---

**Description**

Density, distribution function, quantile function and random generation for the delayed exponential distribution with rate-parameter.

**Usage**

```
dexp_delayed(x, delay, rate = 1, ...)
```

```
pexp_delayed(q, delay, rate = 1, ...)
```

```
qexp_delayed(p, delay, rate = 1, ...)
```

```
rexp_delayed(n, delay, rate = 1)
```

**Arguments**

|       |   |
|-------|---|
| x     | A numeric vector of values for which to get the density.  |
| delay | numeric. The delay, must be non-negative.   |
| rate  | numeric. The event rate, must be non-negative.  |
| ...   | further arguments are passed on to the underlying non-delayed function, e.g., <a href="#">stats::dexp()</a> |
| q     | A numeric vector of quantile values.  |
| p     | A numeric vector of probabilities.  |
| n     | integer. Number of random observations requested.   |

**Details**

Additional arguments are forwarded via ... to the underlying functions of the exponential distribution in the stats-package. The numerical arguments other than n are recycled to the length of the result. Only the first elements of the logical arguments are used.

**Value**

dexp\_delayed gives the density, pexp\_delayed gives the distribution function, qexp\_delayed gives the quantile function, and rexp\_delayed generates a pseudo-random sample from the delayed exponential distribution.

The length of the result is determined by n for rexp\_delayed, and is the maximum of the lengths of the numerical arguments for the other functions.

---

|                |                                     |
|----------------|-------------------------------------|
| DelayedWeibull | <i>Delayed Weibull Distribution</i> |
|----------------|-------------------------------------|

---

**Description**

Density, distribution function, quantile function and random generation for the delayed Weibull distribution with parameters as in the Weibull distribution functions in R's stats-package, namely:

- delay
- shape
- scale (inverse of rate)

**Usage**

```
dweib_delayed(x, delay, shape, scale = 1, ...)
```

```
pweib_delayed(q, delay, shape, scale = 1, ...)
```

```
qweib_delayed(p, delay, shape, scale = 1, ...)
```

```
rweib_delayed(n, delay, shape, scale = 1)
```

**Arguments**

|       |   |
|-------|---|
| x     | A numeric vector of values for which to get the density.  |
| delay | numeric. The delay, must be non-negative.   |
| shape | numeric. Shape parameter, must be positive.   |
| scale | numeric. Scale parameter (inverse of rate), must be positive.   |
| ...   | further arguments are passed on to the underlying non-delayed function, e.g., <a href="#">stats::dweibull()</a> |
| q     | A numeric vector of quantile values.  |
| p     | A numeric vector of probabilities.  |
| n     | integer. Number of random observations requested.   |

**Details**

Additional arguments are forwarded via `...` to the underlying functions of the exponential distribution in the `stats`-package.

The numerical arguments other than `n` are recycled to the length of the result. Only the first elements of the logical arguments are used.

**Value**

`dweib_delayed` gives the density, `pweib_delayed` gives the distribution function, `qweib_delayed` gives the quantile function, and `rweib_delayed` generates a pseudo-random sample from the delayed Weibull distribution.

The length of the result is determined by `n` for `rweib_delayed`, and is the maximum of the lengths of the numerical arguments for the other functions.

---

|                        |  |
|------------------------|--|
| <code>delay_fit</code> | <i>Fit optimal parameters according to the objective function (either MPSE or MLE0).</i> |
|------------------------|--|

---

**Description**

The objective function carries the given data in its environment and it is to be minimized. R's standard routine `stats::optim` does the numerical optimization, using numerical derivatives. or the analytical solution is returned directly if available.

**Usage**

```
delay_fit(objFun, optim_args = NULL, verbose = 0)
```

**Arguments**

|                         |   |
|-------------------------|---|
| <code>objFun</code>     | objective function to be minimized  |
| <code>optim_args</code> | list of own arguments for optimization. If <code>NULL</code> it uses the default <code>optim</code> arguments associated to the objective function. |
| <code>verbose</code>    | integer that indicates the level of verbosity. Default 0 is quiet.  |

**Value**

optimization object including a named parameter vector or `NULL` in case of errors during optimization

---

|             |  |
|-------------|--|
| delay_model | <i>Fit a delayed Exponential or Weibull model to one or two given sample(s).</i> |
|-------------|--|

---

### Description

Maximum product spacing is used to fit the parameters. Numerical optimization is done by `stats::optim`.

### Usage

```
delay_model(
  x = stop("Specify observations!", call. = FALSE),
  y = NULL,
  distribution = c("exponential", "weibull"),
  method = c("MPSE", "MLE0"),
  bind = NULL,
  ties = c("density", "equidist", "random", "error"),
  optim_args = NULL,
  verbose = 0
)
```

### Arguments

|              |   |
|--------------|---|
| x            | numeric. observations of 1st group. Can also be a list of data from two groups.   |
| y            | numeric. observations from 2nd group  |
| distribution | character. Which delayed distribution is assumed? Exponential or Weibull.   |
| method       | character. Which method to fit the model? 'MPSE' = maximum product of spacings estimation <i>or</i> 'MLE0' = standard maximum likelihood estimation |
| bind         | character. parameter names that are bind together in 2-group situation.   |
| ties         | character. How to handle ties.  |
| optim_args   | list. optimization arguments to use. Use NULL to use the data-dependent default values.   |
| verbose      | integer. level of verboseness. Default 0 is quiet.  |

### Value

`incubate_fit` the delay-model fit object. Or NULL if optimization failed (e.g. too few observations).

---

|                    |  |
|--------------------|--|
| estimRoundingError | <i>Estimate rounding error based on given sample of metric values The idea is to check at which level of rounding the sample values do not change.</i> |
|--------------------|--|

---

**Description**

Estimate rounding error based on given sample of metric values The idea is to check at which level of rounding the sample values do not change.

**Usage**

```
estimRoundingError(obs, roundDigits = seq.int(-4L, 6L), maxObs = 100L)
```

**Arguments**

|             |  |
|-------------|--|
| obs         | numeric. Metric values from a sample to estimate the corresponding rounding error                                      |
| roundDigits | integer. Which level of rounding to test? Negative numbers round to corresponding powers of 10                         |
| maxObs      | integer. How many observations to consider at most? If the provided sample has more observations a sub-sample is used. |

**Value**

estimated rounding error

---

|         |  |
|---------|--|
| getDist | <i>Get delay distribution function</i> |
|---------|--|

---

**Description**

Get delay distribution function

**Usage**

```
getDist(
  distribution = c("exponential", "weibull"),
  type = c("cdf", "prob", "density", "random", "param"),
  twoGroup = FALSE,
  bind = NULL
)
```

**Arguments**

|              |   |
|--------------|---|
| distribution | character(1). delay distribution.   |
| type         | character(1). type of function, cdf: cumulative distribution function, density or random function |
| twoGroup     | logical(1). Do we have two groups?  |
| bind         | character. Names of parameters that are bind between the two groups.                              |

**Value**

selected distribution function or parameter names

---

getPars

*Extract the parameters for the specified group.*

---

**Description**

The parameters of the requested group are named using the canonical parameter names of the distribution.

**Usage**

```
getPars(par, group = "x", twoGroup, oNames, bind)
```

**Arguments**

|          |   |
|----------|---|
| par      | named parameters (as simple vector or as list)                        |
| group    | character. Which group to extract parameters for?                     |
| twoGroup | flag. Is it a two-group setting?                                      |
| oNames   | character. Original parameter names from distribution.                |
| bind     | character. Which parameters are bind together in a two-group setting? |

**Details**

For a one-group setting or when group=NULL it simply returns the given parameter. This is an internal helper function used in `coef.incubate_fit()`, `bsDataStep()` and in the factory method `objFunFactory()` below.

**Value**

named vector of parameters from the relevant group

---

|          |                         |
|----------|-------------------------|
| incubate | <i>Incubate Package</i> |
|----------|-------------------------|

---

**Description**

Estimation and statistical tests on parameters in parametric time-to-event analyses with delay.

---

|               |  |
|---------------|--|
| objFunFactory | <i>Factory method for objective function, either according to maximum product of spacings estimation ('MPSE') or according to standard maximum likelihood estimation ('MLE0').</i> |
|---------------|--|

---

**Description**

Given the observed data this factory method produces an MPSE objective function implementation which is the negative of the MPSE-criterion H or the negative log-likelihood for MLE.

**Usage**

```
objFunFactory(
  x,
  y = NULL,
  method = c("MPSE", "MLE0"),
  distribution = c("exponential", "weibull"),
  bind = NULL,
  ties = c("density", "equidist", "random", "error"),
  verbose = 0L
)
```

**Arguments**

|              |  |
|--------------|--|
| x            | numeric. observations  |
| y            | numeric. observations in second group.   |
| method       | character(1). Specifies the method for which to build the objective function. Default value is MPSE. MLE0 is the standard MLE-method, calculating the likelihood function as the product of density values |
| distribution | character(1). delayed distribution family  |
| bind         | character. parameter names that are bind together (i.e. equated) between both groups   |
| ties         | character. How to handle ties within data of a group.  |
| verbose      | integer flag. How much verbosity in output? The higher the more output. Default value is 0 which is no output.   |

**Details**

From the observations, negative or infinite values are discarded. In any case, the objective function is to be minimized.

**Value**

the objective function (e.g., the negative MPSE criterion) for given choice of model parameters or NULL upon errors

---

|            |   |
|------------|---|
| power_diff | <i>Power simulation function for a two-group comparison of the delay parameter.</i> |
|------------|---|

---

**Description**

There are two ways of operation:

1. power=NULL Given sample size n it simulates the power.
2. n=NULL Given a power an iterative search is started to find a suitable n within a specified range.

**Usage**

```
power_diff(
  distribution = c("exponential", "weibull"),
  param = "delay",
  test = c("bootstrap", "pearson", "morán", "lr", "lr_pp"),
  eff = stop("Provide parameters for both group that reflect the effect!"),
  n = NULL,
  r = 1,
  sig.level = 0.05,
  power = NULL,
  nPowerSim = 1600,
  R = 201,
  nRange = c(5, 50)
)
```

**Arguments**

|              |   |
|--------------|---|
| distribution | character. Which assumed distribution is used for the power calculation.  |
| param        | character. Parameter name(s) for which to simulate the power.   |
| test         | character. Which test to use for this power estimation?   |
| eff          | list. The two list elements contain the model parameters (as understood by the delay-distribution functions provided by this package) for the two groups. |
| n            | integer. Number of observations per group for the power simulation or NULL when n is to be estimated for a given power.                                   |

|           |   |
|-----------|---|
| r         | numeric. Ratio of both groups sizes, $n_y / n_x$ . Default value is 1, i.e., balanced group sizes. Must be positive.  |
| sig.level | numeric. Significance level. Default is 0.05.   |
| power     | numeric. NULL when power is to be estimated for a given sample size or a desired power is specified (and n is estimated).   |
| nPowerSim | integer. Number of simulation rounds. Default value 1600 yields a standard error of 0.01 for power if the true power is 80%.  |
| R         | integer. Number of bootstrap samples for test of difference in parameter within each power simulation. It affects the resolution of the P-value for each simulation round. A value of around $R=200$ gives a resolution of 0.5% which might be enough for power analysis. |
| nRange    | integer. Admissible range for sample size when power is pre-specified and sample size is requested.   |

### Details

In any case, the distribution, the parameters that are tested for, the type of test and the effect size ( $\text{eff}=\text{}$ ) need to be specified. The more power simulation rounds (parameter  $\text{nPowerSim}=\text{}$ ) the more densely the space of data according to the specified model is sampled.

Note that this second modus (when n is estimated) is computationally quite heavy. The iterative search for n uses some heuristics and the estimated sample size might actually give a different power-level. It is important to check the stated power in the output. The search algorithm comes to results closer to the power aimed at when the admissible range for sample size ( $\text{nRange}=\text{}$ ) is chosen sensibly. In case the estimated sample size and the achieved power is too high it might pay off to rerun the function with an adapted admissible range.

### Value

List of results of power simulation. Or NULL in case of errors.

---

stankovic

*Survival of mice with glioma under different treatments.*

---

### Description

A dataset from an animal experiment described in Stankovic (2018), shown in Figure 6J and 6K.

### Usage

stankovic

**Format**

- Figure** The figure in the publication where the data is shown
- Time** Survival in days
- Status** Right-censor status: 1 means observed event
- Group** Experimental group identifier
- Colour** Colour used in the Stankovic publication to mark this group

**Details**

The data were read directly from the survival plots in the publication with the help of Plot Digitizer, version 2.6.9.

**Source**

Dudvarski Stankovic N, Bicker F, Keller S, et al. EGFL7 enhances surface expression of integrin  $\alpha 5 \beta 1$  to promote angiogenesis in malignant brain tumors. *EMBO Mol Med.* 2018;10(9):e8420. doi:10.15252/emmm.201708420 <https://www.ncbi.nlm.nih.gov/pmc/articles/PMC6127886/>

---

|           |  |
|-----------|--|
| test_diff | <i>Test the difference for delay model parameter(s) between two uncorrelated groups, based on maximum product of spacings estimation (MPSE).</i> |
|-----------|--|

---

**Description**

It is in fact a model comparison between a null model where the parameters are enforced to be equal and an unconstrained full model. As test statistic we use twice the difference in best (=lowest) objective function value, i.e.  $2 * (val_0 - val_1)$ . This is reminiscent of a likelihood ratio test statistic albeit the objective function is not a negative log-likelihood but the negative of the maximum product spacing metric.

**Usage**

```
test_diff(
  x,
  y = stop("Provide data for group y!"),
  distribution = c("exponential", "weibull"),
  param = "delay",
  R = 400,
  ties = c("density", "equidist", "random", "error"),
  type = c("all", "bootstrap", "gof", "morán", "pearson", "lr", "lr_pp"),
  verbose = 0
)
```

**Arguments**

|              |  |
|--------------|--|
| x            | data from reference/control group.   |
| y            | data from the treatment group.   |
| distribution | character(1). Name of the parametric delay distribution to use.                              |
| param        | character. Names of parameters to test difference for. Default value is 'delay'.             |
| R            | numeric(1). Number of bootstrap samples to evaluate the distribution of the test statistic.  |
| ties         | character. How to handle ties in data vector of a group?                                     |
| type         | character. Which type of tests to perform?   |
| verbose      | numeric. How many details are requested? Higher value means more details. 0=off, no details. |

**Details**

High values of this difference speak against the null-model (i.e. high `val_0` indicates bad fit under 0-model and low values of `val_1` indicate a good fit under the more general model1. The test is implemented as a parametric bootstrap test, i.e. we

1. take given null-model fit as ground truth
2. regenerate data according to this model.
3. recalculate the test statistic
4. appraise the observed test statistic in light of the generated distribution under H0

**Value**

list with the results of the test. Element P contains the different P-values, for instance from parametric bootstrap

---

|          |  |
|----------|--|
| test_GOF | <i>Goodness-of-fit (GOF) test statistic.</i> |
|----------|--|

---

**Description**

The GOF-test is performed for a fitted delay-model. There are different GOF-tests implemented:

- **Moran GOF** is based on spacings, like the MPSE-criterion itself.
- **Pearson GOF** uses categories and compares observed to expected frequencies.

**Usage**

```
test_GOF(delayFit, method = c("moran", "pearson"))
```

**Arguments**

delayFit            delay\_model fit  
 method            character(1). which method to use for GOF. Default is 'moran'.

**Value**

An htest-object containing the GOF-test result

---

transform.incubate\_fit

*Transform observed data to unit interval*

---

**Description**

The transformation is the probability integral transform. It uses the cumulative distribution function with the estimated parameters of the model fit. All available data in the model fit is transformed.

**Usage**

```
## S3 method for class 'incubate_fit'
transform(`_data`, ...)
```

**Arguments**

\_data            a fitted model object of class incubate\_fit  
 ...            currently ignored

**Value**

The transformed data, either a vector (for single group) or a list with entries x and y (in two group scenario)

**Note**

This S3-method implementation is quite different from its default method that allows for non-standard evaluation on data frames, primarily for interactive use. But the name transform just fits so nicely to the intended purpose that it is re-used for the probability integral transform.

---

update.incubate\_fit    *Refit an incubate\_fit-object with specified optimization arguments.  
If more things need to be changed use delay\_model.*

---

**Description**

Refit an incubate\_fit-object with specified optimization arguments. If more things need to be changed use delay\_model.

**Usage**

```
## S3 method for class 'incubate_fit'  
update(object, optim_args, verbose = 0, ...)
```

**Arguments**

|            |  |
|------------|--|
| object     | incubate_fit-object                                |
| optim_args | optimization arguments                             |
| verbose    | integer flag. Requested verbosity during delay_fit |
| ...        | further arguments, currently not used.             |

**Value**

The updated fitted object of class incubate\_fit

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