

Package ‘odr’

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Type Package

Title Optimal Design and Statistical Power for Multilevel Experiments

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Description Calculate the optimal sample allocation that produces the highest statistical power for experimental studies under a budget constraint, perform power analyses with and without accommodating cost structures of sampling, and calculate the relative efficiency between two sample allocations.

The references

for the proposed methods include:

(1) Shen, Z., & Kelcey, B. (2020).

Optimal sample allocation under unequal costs in cluster-randomized trials.

Journal of Educational and Behavioral Statistics, 45(4): 446-474.

[doi:10.3102/1076998620912418](https://doi.org/10.3102/1076998620912418).

(2) Shen, Z., & Kelcey, B. (2022). Optimal sampling ratios in three-level multisite experiments.

Journal of Research on Educational Effectiveness, 15 (1), 130-150.

[doi:10.1080/19345747.2021.1953200](https://doi.org/10.1080/19345747.2021.1953200).

(3) Shen, Z., & Kelcey, B. (in press). Optimal sample allocation in multisite randomized trials. The Journal of Experimental Education.

[doi:10.1080/00220973.2020.1830361](https://doi.org/10.1080/00220973.2020.1830361).

(4) Champely, S. (2020). pwr: Basic functions for power analysis (Version 1.3-0) [Software]. Available from

<https://CRAN.R-project.org/package=pwr>.

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R topics documented:

odr-package	2
gen.design.pars	3
od.1	4
od.2	6
od.2.221	8
od.2m	11
od.3	13
od.3m	16
od.4	19
od.4m	23
power.1	26
power.2	28
power.2.221	32
power.2m	34
power.3	37
power.3m	41
power.4	44
power.4m	48
re	51
rpe	53
Index	56

odr-package

Optimal Design and Statistical Power of Multilevel Randomized Trials

Description

This package is to help researchers design cost-efficient experimental studies assessing main treatment effects with adequate statistical precision by (a) solving optimal sample allocations, (b) comparing design precision and efficiency between different sample allocations, and (c) explicitly accommodating costs and budget in power analyses.

Details

The package covers seven types of experiments aiming to detect main and mediation effects. These experiments are individual randomized controlled trials (RCTs), two-, three-, and four-level cluster-randomized trials (CRTs), two-, three-, and four-level multisite randomized trials (MRTs), and two-level CRTs investigating mediation effects with group-level mediators. There are two categorical functions for each type of experiments and a uniform function for all types of experiments. The two categorical functions are 'od' and 'power'. The 'od' function can calculate the optimal sample allocation with and without constraint for each type of experiments. The 'power' function by default can calculate required budget (and required sample size) for desired power, minimum detectable effect size (MDES) under a fixed budget, statistical power under a fixed budget. The 'power' function also can perform conventional power analyses (e.g., required sample size, power, MDES calculation). The uniform function 're' (or 'rpe') is to compare the relative (precision and) efficiency between two designs with different sample allocations.

Author(s)

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gen.design.pars

Generate optimal design parameters using ant colony optimization

Description

This function can generate a set of optimal design parameters based on given distributions of the rank of optimization target (or budget).

Usage

```
gen.design.pars(  
  dist.mean,  
  dist.rank,  
  n.of.ants,  
  nl,  
  q = 1e-04,  
  n.of.archive = 100,  
  xi = 0.5  
)
```

Arguments

dist.mean	List of means - coordinates
dist.rank	Rank of the archived values of objective function
n.of.ants	Number of ants used in each iteration after the initialization of power analysis for calculating required budget, default value is 10.
nl	Neighborhood of the search area

q Locality of the search (0,1), default is 0.0001.
n.of.archive Size of the solution archive, default is 100.
xi Convergence pressure (0, Inf), suggested: (0, 1), default is 0.5.

Value

Generated optimal design parameter value(s) (i.e., a matrix with n.of.ants rows and n.of.design.pars columns)

References

Socha, K., & Dorigo, M. (2008). Ant colony optimization for continuous domains. *European Journal of Operational Research*, 185(3), 1155-1173.

We thank Dr. Krzysztof Socha for providing us the original code (<http://iridia.ulb.ac.be/supp/IridiaSupp2008-001/>) for this function.

od.1 *Optimal sample allocation calculation for single-level experiments detecting main effects*

Description

The optimal design of single-level experiments detecting main effects is to choose the optimal sample allocation that minimizes the variance of a treatment effect under a fixed budget, which is approximately the optimal sample allocation that maximizes statistical power under a fixed budget. The optimal design parameter is the proportion of individuals to be assigned to treatment (p).

Usage

```
od.1(  
  p = NULL,  
  r12 = NULL,  
  c1 = NULL,  
  c1t = NULL,  
  m = NULL,  
  plots = TRUE,  
  plim = NULL,  
  varlim = NULL,  
  plab = NULL,  
  varlab = NULL,  
  vartitle = NULL,  
  verbose = TRUE  
)
```

Arguments

p	The proportion of individuals to be assigned to treatment.
r12	The proportion of outcome variance explained by covariates.
c1	The cost of sampling one unit in control condition.
c1t	The cost of sampling one unit in treatment condition.
m	Total budget, default value is the total costs of sampling 60 individuals across treatment conditions.
plots	Logical, provide variance plots if TRUE, otherwise not; default value is TRUE.
plim	The plot range for p, default value is c(0, 1).
varlim	The plot range for variance, default value is c(0, 0.05).
plab	The plot label for p , default value is "Proportion of Individuals in Treatment: p".
varlab	The plot label for variance, default value is "Variance".
vartitle	The title of variance plot, default value is NULL.
verbose	Logical; print the value of p if TRUE, otherwise not; default value is TRUE.

Value

Unconstrained or constrained optimal sample allocation (p). The function also returns the variance of the treatment effect, function name, design type, and parameters used in the calculation.

Examples

```
# Unconstrained optimal design #-----
myod1 <- od.1(r12 = 0.5, c1 = 1, c1t = 5, varlim = c(0, 0.2))
myod1$out # output

# Constrained p, no calculation performed #-----
myod2 <- od.1(r12 = 0.5, c1 = 1, c1t = 5, varlim = c(0, 0.2), p = 0.5)
myod2$out
# Relative efficiency (RE)
myre <- re(od = myod1, subod = myod2)
myre$re # RE = 0.87

# When sampling costs are equal, a balanced design with p = 0.5 is the best #-----
myod3 <- od.1(r12 = 0.5, c1 = 1, c1t = 1, varlim = c(0, 0.2))
myod3$out # output
```

od.2 *Optimal sample allocation calculation for two-level CRTs detecting main effects*

Description

The optimal design of two-level cluster randomized trials (CRTs) detecting main effects is to calculate the optimal sample allocation that minimizes the variance of a treatment effect under a fixed budget, which is approximately the optimal sample allocation that maximizes statistical power under a fixed budget. The optimal design parameters include the level-1 sample size per level-2 unit (n) and the proportion of level-2 clusters/groups to be assigned to treatment (p). This function solves the optimal n and/or p with and without constraints.

Usage

```
od.2(
  n = NULL,
  p = NULL,
  icc = NULL,
  r12 = NULL,
  r22 = NULL,
  c1 = NULL,
  c2 = NULL,
  c1t = NULL,
  c2t = NULL,
  m = NULL,
  plots = TRUE,
  plot.by = NULL,
  nlim = NULL,
  plim = NULL,
  varlim = NULL,
  nlab = NULL,
  plab = NULL,
  varlab = NULL,
  vartitle = NULL,
  verbose = TRUE
)
```

Arguments

n	The level-1 sample size per level-2 unit.
p	The proportion of level-2 clusters/units to be assigned to treatment.
icc	The unconditional intraclass correlation coefficient (ICC) in population or in each treatment condition.
$r12$	The proportion of level-1 variance explained by covariates.
$r22$	The proportion of level-2 variance explained by covariates.

c1	The cost of sampling one level-1 unit in control condition.
c2	The cost of sampling one level-2 unit in control condition.
c1t	The cost of sampling one level-1 unit in treatment condition.
c2t	The cost of sampling one level-2 unit in treatment condition.
m	Total budget, default value is the total costs of sampling 60 level-2 units across treatment conditions.
plots	Logical, provide variance plots if TRUE, otherwise not; default value is TRUE.
plot.by	Plot the variance by n and/or p; default value is plot.by = list(n = "n", p = "p").
nlim	The plot range for n, default value is c(2, 50).
plim	The plot range for p, default value is c(0, 1).
varlim	The plot range for variance, default value is c(0, 0.05).
nlab	The plot label for n, default value is "Level-1 Sample Size: n".
plab	The plot label for p, default value is "Proportion Level-2 Units in Treatment: p".
varlab	The plot label for variance, default value is "Variance".
vartitle	The title of variance plot, default value is NULL.
verbose	Logical; print the values of n and p if TRUE, otherwise not; default value is TRUE.

Value

Unconstrained or constrained optimal sample allocation (n and p). The function also returns the variance of the treatment effect, function name, design type, and parameters used in the calculation.

References

Shen, Z., & Kelcey, B. (2020). Optimal sample allocation under unequal costs in cluster-randomized trials. *Journal of Educational and Behavioral Statistics*, 45(4): 446–474. <<https://doi.org/10.3102/1076998620912418>>

Examples

```
# Unconstrained optimal design #-----
myod1 <- od.2(icc = 0.2, r12 = 0.5, r22 = 0.5, c1 = 1, c2 = 5, c1t = 1, c2t = 50,
             varlim = c(0.01, 0.02))
myod1$out # output
# Plot by p
myod1 <- od.2(icc = 0.2, r12 = 0.5, r22 = 0.5, c1 = 1, c2 = 5, c1t = 1, c2t = 50,
             varlim = c(0.01, 0.02), plot.by = list(p = 'p'))

# Constrained optimal design with n = 20 #-----
myod2 <- od.2(icc = 0.2, r12 = 0.5, r22 = 0.5, c1 = 1, c2 = 5, c1t = 1, c2t = 50,
             n = 20, varlim = c(0.005, 0.025))
myod2$out
# Relative efficiency (RE)
myre <- re(od = myod1, subod = myod2)
myre$re # RE = 0.88
```

```

# Constrained optimal design with p = 0.5 #-----
myod3 <- od.2(icc = 0.2, r12 = 0.5, r22 = 0.5, c1 = 1, c2 = 5, c1t = 1, c2t = 50,
             p = 0.5, varlim = c(0.005, 0.025))
myod3$out
# Relative efficiency (RE)
myre <- re(od = myod1, subod= myod3)
myre$re # RE = 0.90

# Constrained n and p, no calculation performed #-----
myod4 <- od.2(icc = 0.2, r12 = 0.5, r22 = 0.5, c1 = 1, c2 = 5, c1t = 1, c2t = 50,
             n = 20, p = 0.5, varlim = c(0.005, 0.025))
myod4$out
# Relative efficiency (RE)
myre <- re(od = myod1, subod= myod4)
myre$re # RE = 0.83

```

od.2.221

Optimal sample allocation calculation for two-level CRTs probing mediation effects with cluster-level mediators

Description

The optimal design of two-level cluster randomized trials (CRTs) probing mediation effects with cluster-level mediators, for the Sobel test, is to calculate the optimal sample allocation that minimizes the variance of a mediation effect under a fixed budget. For the joint significance test, it is to identify the optimal sample allocation that requires the minimum budget to achieve certain power level. The optimal design parameters include the level-1 sample size per level-2 unit (n) and the proportion of level-2 clusters/groups to be assigned to treatment (p). This function solves the optimal n and/or p with and without a constraint.

Usage

```

od.2.221(
  a = NULL,
  b = NULL,
  icc = NULL,
  c1 = NULL,
  c1t = NULL,
  c2 = NULL,
  c2t = NULL,
  m = NULL,
  r2m = 0,
  r12 = 0,
  r22 = 0,
  q.a = 0,
  q.b = 0,
  test = "joint",

```



```

n = NULL,
p = NULL,
iter = 100,
tol = 1e-11,
power.joint = 0.8,
d.p = c(0.1, 0.5),
d.n = c(1, 50),
sig.level = 0.05,
two.tailed = TRUE,
plots = TRUE,
plot.by = NULL,
n.rep = 1000,
nlim = c(0, 50),
plim = c(0, 1),
varlim = c(0, 0.05),
Jlim = c(4, 1e+05),
nlab = NULL,
plab = NULL,
varlab = NULL,
vartitle = NULL,
verbose = TRUE,
max.value = Inf,
max.iter = 150,
e = 1e-10,
n.of.ants = 10,
n.of.archive = 50,
q = 1e-04,
xi = 0.5
)

```

Arguments

a	The treatment effect on the mediator.
b	The within treatment correlation between the outcome and the mediator.
icc	The unconditional intraclass correlation coefficient (ICC) in population or in each treatment condition.
c1	The cost of sampling one level-1 unit in control condition.
c1t	The cost of sampling one level-1 unit in treatment condition.
c2	The cost of sampling one level-2 unit in control condition.
c2t	The cost of sampling one level-2 unit in treatment condition.
m	Total budget.
r2m	The proportion of within treatment mediator variance explained by covariates.
r12	The proportion of within treatment individual-level outcome variance explained by covariates.
r22	The proportion of within treatment group-level outcome variance explained by covariates and the mediator.

q.a	The number of covariates in the outcome model (except the treatment indicator and the mediator).
q.b	The number of covariates in the mediator model (except the treatment indicator).
test	The type of test will be used to detect mediation effects. Default is the joint significance test (i.e., test = "joint"). Other choices are the Sobel test and Monte Carlo confidence interval test by specifying the argument as test = "sobel" or test = "mcci".
n	The level-1 sample size per level-2 unit.
p	The proportion of level-2 clusters/units to be assigned to treatment.
iter	number of iteration used for solving roots in Sobel test.
tol	convergence tolerance.
power.joint	Statistical power specified for the joint significance test, default is .80.
d.p	The initial sampling domains for p. Default is c(0.03, 0.97).
d.n	The initial sampling domain for n. Default is c(0.5, 500).
sig.level	Significance level or type I error rate, default value is 0.05.
two.tailed	Logical; two-tailed tests if TRUE, otherwise one-tailed tests; default value is TRUE.
plots	Logical, provide variance plots if TRUE, otherwise not; default value is TRUE.
plot.by	Plot the variance by n and/or p; default value is plot.by = list(n = "n", p = "p").
n.rep	Number of replications in MCCI power calculation.
nlim	The plot range for n, default value is c(2, 50).
plim	The plot range for p, default value is c(0, 1).
varlim	The plot range for variance, default value is c(0, 0.05).
Jlim	The range for J to search for a numerical solution. Default is c(4, 10e4).
nlab	The plot label for n, default value is "Level-1 Sample Size: n".
plab	The plot label for p, default value is "Proportion Level-2 Units in Treatment: p".
varlab	The plot label for variance, default value is "Variance".
vartitle	The title of variance plot, default value is NULL.
verbose	Print out evaluation process if TRUE, default is TRUE.
max.value	Maximal value of optimization when used as the stopping criterion. Default is infinite.
max.iter	Maximal number of function evaluations when used as the stopping criterion.
e	Maximum error value used when solution quality used as the stopping criterion, default is 1e-10.
n.of.ants	Number of ants used in each iteration after the initialization of power analysis for calculating required budget, default value is 10.
n.of.archive	Size of the solution archive, default is 100.
q	Locality of the search (0,1), default is 0.0001.
xi	Convergence pressure (0, Inf), suggested: (0, 1), default is 0.5.

Value

Unconstrained or constrained optimal sample allocation (n and p). The function also returns the variance of a mediation effect or statistical power, function name, design type, and parameters used in the calculation.

od.2m	<i>Optimal sample allocation calculation for two-level MRTs detecting main effects</i>
-------	--

Description

The optimal design of two-level multisite randomized trials (MRTs) detecting main effects is to calculate the sample allocation that minimizes the variance of a treatment effect under a fixed budget, which is approximately the optimal sample allocation that maximizes statistical power under a fixed budget. The optimal design parameters include the level-one sample size per site (n) and the proportion of level-one unit to be assigned to treatment (p). This function solves the optimal n and/or p with and without a constraint.

Usage

```
od.2m(  
  n = NULL,  
  p = NULL,  
  icc = NULL,  
  r12 = NULL,  
  r22m = NULL,  
  c1 = NULL,  
  c2 = NULL,  
  c1t = NULL,  
  omega = NULL,  
  m = NULL,  
  plots = TRUE,  
  plot.by = NULL,  
  nlim = NULL,  
  plim = NULL,  
  varlim = NULL,  
  nlab = NULL,  
  plab = NULL,  
  varlab = NULL,  
  vartitle = NULL,  
  verbose = TRUE,  
  iter = 100,  
  tol = 1e-10  
)
```

Arguments

n	The level-1 sample size per level-2 unit.
p	The proportion of level-4 clusters/units to be assigned to treatment.
icc	The unconditional intraclass correlation coefficient (ICC) in population or in each treatment condition.
r12	The proportion of level-1 variance explained by covariates.
r22m	The proportion of variance of site-specific treatment effect explained by covariates.
c1	The cost of sampling one level-1 unit in control condition.
c2	The cost of sampling one level-2 unit in control condition.
c1t	The cost of sampling one level-1 unit in treatment condition.
omega	The standardized variance of site-specific treatment effect.
m	Total budget, default is the total costs of sampling 60 sites.
plots	Logical, provide variance plots if TRUE, otherwise not; default value is TRUE.
plot.by	Plot the variance by n and/or p; default value is plot.by = list(n = "n", p = "p").
nlim	The plot range for n, default value is c(2, 50).
plim	The plot range for p, default value is c(0, 1).
varlim	The plot range for variance, default value is c(0, 0.05).
nlab	The plot label for n, default value is "Level-1 Sample Size: n".
plab	The plot label for p, default value is "Proportion Level-1 Units in Treatment: p".
varlab	The plot label for variance, default value is "Variance".
vartitle	The title of variance plot, default value is NULL.
verbose	Logical; print the values of n and p if TRUE, otherwise not; default value is TRUE.
iter	Number of iterations; default value is 100.
tol	Tolerance for convergence; default value is 1e-10.

Value

Unconstrained or constrained optimal sample allocation (n and p). The function also returns the variance of the treatment effect, function name, design type, and parameters used in the calculation.

References

Shen, Z., & Kelcey, B. (in press). Optimal sample allocation in multisite randomized trials. *The Journal of Experimental Education*. <<https://doi.org/10.1080/00220973.2020.1830361>>

Examples

```

# Unconstrained optimal design #-----
myod1 <- od.2m(icc = 0.2, omega = 0.02, r12 = 0.5, r22m = 0.5,
              c1 = 1, c2 = 10, c1t = 10,
              varlim = c(0, 0.005))
myod1$out # n = 20, p = 0.37
# Plots by p
myod1 <- od.2m(icc = 0.2, omega = 0.02,
              r12 = 0.5, r22m = 0.5,
              c1 = 1, c2 = 10, c1t = 10,
              varlim = c(0, 0.005), plot.by = list(p = 'p'))

# Constrained optimal design with p = 0.5 #-----
myod2 <- od.2m(icc = 0.2, omega = 0.02,
              r12 = 0.5, r22m = 0.5,
              c1 = 1, c2 = 10, c1t = 10,
              varlim = c(0, 0.005), p = 0.5)
myod2$out
# Relative efficiency (RE)
myre <- re(od = myod1, subod = myod2)
myre$re # RE = 0.86

# Constrained optimal design with n = 5 #-----
myod3 <- od.2m(icc = 0.2, omega = 0.02,
              r12 = 0.5, r22m = 0.5, c1 = 1, c2 = 10,
              c1t = 10, varlim = c(0, 0.005), n = 5)
myod3$out
# Relative efficiency (RE)
myre <- re(od = myod1, subod = myod3)
myre$re # RE = 0.79

# Constrained n and p, no calculation performed #-----
myod4 <- od.2m(icc = 0.2, omega = 0.02, r12 = 0.5, r22m = 0.5,
              c1 = 1, c2 = 10, c1t = 10,
              varlim = c(0, 0.005), p = 0.5, n = 10)
myod4$out
# Relative efficiency (RE)
myre <- re(od = myod1, subod = myod4)
myre$re # RE = 0.84

```

Description

The optimal design of three-level cluster randomized trials (CRTs) is to calculate the optimal sample allocation that minimizes the variance of treatment effect under fixed budget, which is approximately the optimal sample allocation that maximizes statistical power under a fixed budget. The

optimal design parameters include the level-1 sample size per level-2 unit (n), the level-2 sample size per level-3 unit (J), and the proportion of level-3 clusters/groups to be assigned to treatment (p). This function solves the optimal n , J and/or p with and without constraints.

Usage

```
od.3(
  n = NULL,
  J = NULL,
  p = NULL,
  icc2 = NULL,
  icc3 = NULL,
  r12 = NULL,
  r22 = NULL,
  r32 = NULL,
  c1 = NULL,
  c2 = NULL,
  c3 = NULL,
  c1t = NULL,
  c2t = NULL,
  c3t = NULL,
  m = NULL,
  plots = TRUE,
  plot.by = NULL,
  nlim = NULL,
  Jlim = NULL,
  plim = NULL,
  varlim = NULL,
  nlab = NULL,
  Jlab = NULL,
  plab = NULL,
  varlab = NULL,
  vartitle = NULL,
  verbose = TRUE,
  iter = 100,
  tol = 1e-10
)
```

Arguments

n	The level-1 sample size per level-2 unit.
J	The level-2 sample size per level-3 unit.
p	The proportion of level-3 clusters/units assigned to treatment.
$icc2$	The unconditional intraclass correlation coefficient (ICC) at level 2.
$icc3$	The unconditional intraclass correlation coefficient (ICC) at level 3.
$r12$	The proportion of level-1 variance explained by covariates.
$r22$	The proportion of level-2 variance explained by covariates.

r32	The proportion of level-3 variance explained by covariates.
c1	The cost of sampling one level-1 unit in control condition.
c2	The cost of sampling one level-2 unit in control condition.
c3	The cost of sampling one level-3 unit in control condition.
c1t	The cost of sampling one level-1 unit in treatment condition.
c2t	The cost of sampling one level-2 unit in treatment condition.
c3t	The cost of sampling one level-3 unit in treatment condition.
m	Total budget, default is the total costs of sampling 60 level-3 units across treatment conditions.
plots	Logical, provide variance plots if TRUE, otherwise not; default value is TRUE.
plot.by	Plot the variance by n, J and/or p; default is plot.by = list(n = "n", J = "J", p = "p").
nlim	The plot range for n, default value is c(2, 50).
Jlim	The plot range for J, default value is c(2, 50).
plim	The plot range for p, default value is c(0, 1).
varlim	The plot range for variance, default value is c(0, 0.05).
nlab	The plot label for n, default value is "Level-1 Sample Size: n".
Jlab	The plot label for J, default value is "Level-2 Sample Size: J".
plab	The plot label for p, default is "Proportion Level-3 Units in Treatment: p".
varlab	The plot label for variance, default value is "Variance".
vartitle	The title of variance plot, default value is NULL.
verbose	Logical; print the values of n, J, and p if TRUE, otherwise not; default is TRUE.
iter	Number of iterations; default value is 100.
tol	Tolerance for convergence; default value is 1e-10.

Value

Unconstrained or constrained optimal sample allocation (n, J, and p). The function also returns the variance of the treatment effect, function name, design type, and parameters used in the calculation.

References

Shen, Z., & Kelcey, B. (2020). Optimal sample allocation under unequal costs in cluster-randomized trials. *Journal of Educational and Behavioral Statistics*, 45(4): 446–474. <<https://doi.org/10.3102/1076998620912418>>

Examples

```
# Unconstrained optimal design #-----
myod1 <- od.3(icc2 = 0.2, icc3 = 0.1, r12 = 0.5, r22 = 0.5, r32 = 0.5,
             c1 = 1, c2 = 5, c3 = 25, c1t = 1, c2t = 50, c3t = 250,
             varlim = c(0.005, 0.025))
myod1$out # output
# Plots by p and J
```

```

myod1 <- od.3(icc2 = 0.2, icc3 = 0.1, r12 = 0.5, r22 = 0.5, r32 = 0.5,
             c1 = 1, c2 = 5, c3 = 25, c1t = 1, c2t = 50, c3t = 250,
             varlim = c(0.005, 0.025), plot.by = list(p = 'p', J = 'J'))

# Constrained optimal design with J = 20 #-----
myod2 <- od.3(icc2 = 0.2, icc3 = 0.1, r12 = 0.5, r22 = 0.5, r32 = 0.5, J = 20,
             c1 = 1, c2 = 5, c3 = 25, c1t = 1, c2t = 50, c3t = 250,
             varlim = c(0, 0.025))
myod2$out
# Relative efficiency (RE)
myre <- re(od = myod1, subod= myod2)
myre$re # RE = 0.53

# Constrained optimal design with p = 0.5 #-----
myod3 <- od.3(icc2 = 0.2, icc3 = 0.1, r12 = 0.5, r22 = 0.5, r32 = 0.5, p = 0.5,
             c1 = 1, c2 = 5, c3 = 25, c1t = 1, c2t = 50, c3t = 250,
             varlim = c(0.005, 0.025))
myod3$out
# Relative efficiency (RE)
myre <- re(od = myod1, subod= myod3)
myre$re # RE = 0.84

# Constrained n, J and p, no calculation performed #-----
myod4 <- od.3(icc2 = 0.2, icc3 = 0.1, r12 = 0.5, r22 = 0.5, r32 = 0.5, n = 10, J = 10, p = 0.5,
             c1 = 1, c2 = 5, c3 = 25, c1t = 1, c2t = 50, c3t = 250,
             varlim = c(0, 0.025))
myod4$out
# Relative efficiency (RE)
myre <- re(od = myod1, subod= myod4)
myre$re # RE = 0.61

```

od.3m

Optimal sample allocation calculation for three-level MRTs detecting main effects

Description

The optimal design of three-level multisite randomized trials (MRTs) is to calculate the optimal sample allocation that minimizes the variance of treatment effect under fixed budget, which is approximately the optimal sample allocation that maximizes statistical power under a fixed budget. The optimal design parameters include the level-1 sample size per level-2 unit (n), the level-2 sample size per level-3 unit (J), and the proportion of level-2 unit to be assigned to treatment (p). This function solves the optimal n , J and/or p with and without constraints.

Usage

```

od.3m(
  n = NULL,

```



```

J = NULL,
p = NULL,
icc2 = NULL,
icc3 = NULL,
r12 = NULL,
r22 = NULL,
r32m = NULL,
c1 = NULL,
c2 = NULL,
c3 = NULL,
c1t = NULL,
c2t = NULL,
omega = NULL,
m = NULL,
plots = TRUE,
plot.by = NULL,
nlim = NULL,
Jlim = NULL,
plim = NULL,
varlim = NULL,
nlab = NULL,
Jlab = NULL,
plab = NULL,
varlab = NULL,
vartitle = NULL,
verbose = TRUE,
iter = 100,
tol = 1e-10
)

```

Arguments

n	The level-1 sample size per level-2 unit.
J	The level-2 sample size per level-3 unit.
p	The proportion of level-4 clusters/units to be assigned to treatment.
icc2	The unconditional intraclass correlation coefficient (ICC) at level 2.
icc3	The unconditional intraclass correlation coefficient (ICC) at level 3.
r12	The proportion of level-1 variance explained by covariates.
r22	The proportion of level-2 variance explained by covariates.
r32m	The proportion of variance of site-specific treatment effect explained by covariates.
c1	The cost of sampling one level-1 unit in control condition.
c2	The cost of sampling one level-2 unit in control condition.
c3	The cost of sampling one level-3 unit in control condition.
c1t	The cost of sampling one level-1 unit in treatment condition.

c2t	The cost of sampling one level-2 unit in treatment condition.
omega	The standardized variance of site-specific treatment effect.
m	Total budget, default is the total costs of sampling 60 level-3 units.
plots	Logical, provide variance plots if TRUE, otherwise not; default value is TRUE.
plot.by	Plot the variance by n, J and/or p; default value is plot.by = list(n = "n", J = "J", p = "p").
nlim	The plot range for n, default value is c(2, 50).
Jlim	The plot range for J, default value is c(2, 50).
plim	The plot range for p, default value is c(0, 1).
varlim	The plot range for variance, default value is c(0, 0.05).
nlab	The plot label for n, default value is "Level-1 Sample Size: n".
Jlab	The plot label for J, default value is "Level-2 Sample Size: J".
plab	The plot label for p, default value is "Proportion Level-2 Units in Treatment: p".
varlab	The plot label for variance, default value is "Variance".
vartitle	The title of variance plot, default value is NULL.
verbose	Logical; print the values of n, J, and p if TRUE, otherwise not; default value is TRUE.
iter	Number of iterations; default value is 100.
tol	Tolerance for convergence; default value is 1e-10.

Value

Unconstrained or constrained optimal sample allocation (n, J, and p). The function also returns the variance of the treatment effect, function name, design type, and parameters used in the calculation.

References

Shen, Z., & Kelcey, B. (2022). Optimal sampling ratios in three-level multisite experiments. *Journal of Research on Educational Effectiveness*.

Examples

```
# Unconstrained optimal design #-----
myod1 <- od.3m(icc2 = 0.2, icc3 = 0.1, omega = 0.02,
              r12 = 0.5, r22 = 0.5, r32m = 0.5,
              c1 = 1, c2 = 5,
              c1t = 1, c2t = 200, c3 = 200,
              varlim = c(0, 0.005))
myod1$out # output
# Plots by p and J
myod1 <- od.3m(icc2 = 0.2, icc3 = 0.1, omega = 0.02,
              r12 = 0.5, r22 = 0.5, r32m = 0.5,
              c1 = 1, c2 = 5,
              c1t = 1, c2t = 200, c3 = 200,
              varlim = c(0, 0.005), plot.by = list(p = 'p', J = 'J'))
```

```

# Constrained optimal design with p = 0.5 #-----
myod2 <- od.3m(icc2 = 0.2, icc3 = 0.1, omega = 0.02,
              r12 = 0.5, r22 = 0.5, r32m = 0.5,
              c1 = 1, c2 = 5,
              c1t = 1, c2t = 200, c3 = 200,
              varlim = c(0, 0.005), p = 0.5)
myod2$out
# Relative efficiency (RE)
myre <- re(od = myod1, subod= myod2)
myre$re # RE = 0.81

# Constrained optimal design with n = 5 #-----
myod3 <- od.3m(icc2 = 0.2, icc3 = 0.1, omega = 0.02,
              r12 = 0.5, r22 = 0.5, r32m = 0.5,
              c1 = 1, c2 = 5,
              c1t = 1, c2t = 200, c3 = 200,
              varlim = c(0, 0.005), n = 5)
myod3$out
# Relative efficiency (RE)
myre <- re(od = myod1, subod= myod3)
myre$re # RE = 0.89

# Constrained n, J and p, no calculation performed #-----
myod4 <- od.3m(icc2 = 0.2, icc3 = 0.1, omega = 0.02,
              r12 = 0.5, r22 = 0.5, r32m = 0.5,
              c1 = 1, c2 = 5,
              c1t = 1, c2t = 200, c3 = 200,
              varlim = c(0, 0.005), p = 0.5, n = 15, J = 20)
myod4$out
# Relative efficiency (RE)
myre <- re(od = myod1, subod= myod4)
myre$re # RE = 0.75

```

Description

The optimal design of four-level cluster randomized trials (CRTs) is to calculate the optimal sample allocation that minimizes the variance of treatment effect under fixed budget, which is approximately the optimal sample allocation that maximizes statistical power under a fixed budget. The optimal design parameters include the level-1 sample size per level-2 unit (n), the level-2 sample size per level-3 unit (J), the level-3 sample size per level-4 unit (K), and the proportion of level-4 clusters/groups to be assigned to treatment (p). This function solves the optimal n , J , K and/or p with and without constraints.

Usage

```
od.4(  
  n = NULL,  
  J = NULL,  
  K = NULL,  
  p = NULL,  
  icc2 = NULL,  
  icc3 = NULL,  
  icc4 = NULL,  
  r12 = NULL,  
  r22 = NULL,  
  r32 = NULL,  
  r42 = NULL,  
  c1 = NULL,  
  c2 = NULL,  
  c3 = NULL,  
  c4 = NULL,  
  c1t = NULL,  
  c2t = NULL,  
  c3t = NULL,  
  c4t = NULL,  
  m = NULL,  
  plots = TRUE,  
  plot.by = NULL,  
  nlim = NULL,  
  Jlim = NULL,  
  Klim = NULL,  
  plim = NULL,  
  varlim = NULL,  
  nlab = NULL,  
  Jlab = NULL,  
  Klab = NULL,  
  plab = NULL,  
  varlab = NULL,  
  vartitle = NULL,  
  verbose = TRUE,  
  iter = 100,  
  tol = 1e-10  
)
```

Arguments

n	The level-1 sample size per level-2 unit.
J	The level-2 sample size per level-3 unit.
K	The level-3 sample size per level-4 unit.
p	The proportion of level-4 clusters/units to be assigned to treatment.
icc2	The unconditional intraclass correlation coefficient (ICC) at level 2.

icc3	The unconditional intraclass correlation coefficient (ICC) at level 3.
icc4	The unconditional intraclass correlation coefficient (ICC) at level 4.
r12	The proportion of level-1 variance explained by covariates.
r22	The proportion of level-2 variance explained by covariates.
r32	The proportion of level-3 variance explained by covariates.
r42	The proportion of level-4 variance explained by covariates.
c1	The cost of sampling one level-1 unit in control condition.
c2	The cost of sampling one level-2 unit in control condition.
c3	The cost of sampling one level-3 unit in control condition.
c4	The cost of sampling one level-4 unit in control condition.
c1t	The cost of sampling one level-1 unit in treatment condition.
c2t	The cost of sampling one level-2 unit in treatment condition.
c3t	The cost of sampling one level-3 unit in treatment condition.
c4t	The cost of sampling one level-4 unit in treatment condition.
m	Total budget, default value is the total costs of sampling 60 level-4 units across treatment conditions.
plots	Logical, provide variance plots if TRUE, otherwise not; default value is TRUE.
plot.by	Plot the variance by n, J, K and/or p; default value is plot.by = list(n = "n", J = "J", K = 'K', p = "p").
nlim	The plot range for n, default value is c(2, 50).
Jlim	The plot range for J, default value is c(2, 50).
Klim	The plot range for K, default value is c(2, 50).
plim	The plot range for p, default value is c(0, 1).
varlim	The plot range for variance, default value is c(0, 0.05).
nlab	The plot label for n, default value is "Level-1 Sample Size: n".
Jlab	The plot label for J, default value is "Level-2 Sample Size: J".
Klab	The plot label for K, default value is "Level-3 Sample Size: K".
plab	The plot label for p, default value is "Proportion Level-4 Units in Treatment: p".
varlab	The plot label for variance, default value is "Variance".
vartitle	The title of variance plot, default value is NULL.
verbose	Logical; print the values of n, J, K, and p if TRUE, otherwise not; default value is TRUE.
iter	Number of iterations; default value is 100.
tol	Tolerance for convergence; default value is 1e-10.

Value

Unconstrained or constrained optimal sample allocation (n, J, K, and p). The function also returns the variance of the treatment effect, function name, design type, and parameters used in the calculation.

Examples

```

# Unconstrained optimal design #-----
myod1 <- od.4(icc2 = 0.2, icc3 = 0.1, icc4 = 0.05,
             r12 = 0.5, r22 = 0.5, r32 = 0.5, r42 = 0.5,
             c1 = 1, c2 = 5, c3 = 25, c4 = 125,
             c1t = 1, c2t = 50, c3t = 250, c4t = 2500,
             varlim = c(0, 0.01))
myod1$out # output
# Plots by p and K
myod1 <- od.4(icc2 = 0.2, icc3 = 0.1, icc4 = 0.05,
             r12 = 0.5, r22 = 0.5, r32 = 0.5, r42 = 0.5,
             c1 = 1, c2 = 5, c3 = 25, c4 = 125,
             c1t = 1, c2t = 50, c3t = 250, c4t = 2500,
             varlim = c(0, 0.01), plot.by = list(p = 'p', K = 'K'))

# Constrained optimal design with p = 0.5 #-----
myod2 <- od.4(icc2 = 0.2, icc3 = 0.1, icc4 = 0.05, p = 0.5,
             r12 = 0.5, r22 = 0.5, r32 = 0.5, r42 = 0.5,
             c1 = 1, c2 = 5, c3 = 25, c4 = 125,
             c1t = 1, c2t = 50, c3t = 250, c4t = 2500,
             varlim = c(0, 0.01))
myod2$out
# Relative efficiency (RE)
myre <- re(od = myod1, subod = myod2)
myre$re # RE = 0.78

# Constrained optimal design with K = 20 #-----
myod3 <- od.4(icc2 = 0.2, icc3 = 0.1, icc4 = 0.05, K = 20,
             r12 = 0.5, r22 = 0.5, r32 = 0.5, r42 = 0.5,
             c1 = 1, c2 = 5, c3 = 25, c4 = 125,
             c1t = 1, c2t = 50, c3t = 250, c4t = 2500,
             varlim = c(0, 0.01))
myod3$out
# Relative efficiency (RE)
myre <- re(od = myod1, subod = myod3)
myre$re # RE = 0.67

# Constrained n, J, K and p, no calculation performed #-----
myod4 <- od.4(icc2 = 0.2, icc3 = 0.1, icc4 = 0.05,
             r12 = 0.5, n = 10, J = 10, K = 20, p = 0.5,
             r22 = 0.5, r32 = 0.5, r42 = 0.5,
             c1 = 1, c2 = 5, c3 = 25, c4 = 125,
             c1t = 1, c2t = 50, c3t = 250, c4t = 2500,
             varlim = c(0, 0.01))
myod4$out
# Relative efficiency (RE)
myre <- re(od = myod1, subod = myod4)
myre$re # RE = 0.27

```

`od.4m`*Optimal sample allocation calculation for four-level MRTs detecting main effects*

Description

The optimal design of four-level multisite randomized trials (MRTs) is to calculate the optimal sample allocation that minimizes the variance of treatment effect under fixed budget, which is approximately the optimal sample allocation that maximizes statistical power under a fixed budget. The optimal design parameters include the level-1 sample size per level-2 unit (n), the level-2 sample size per level-3 unit (J), the level-3 sample size per level-4 unit (K), and the proportion of level-3 units to be assigned to treatment (p). This function solves the optimal n , J , K and/or p with and without constraints.

Usage

```
od.4m(  
  n = NULL,  
  J = NULL,  
  K = NULL,  
  p = NULL,  
  icc2 = NULL,  
  icc3 = NULL,  
  icc4 = NULL,  
  r12 = NULL,  
  r22 = NULL,  
  r32 = NULL,  
  r42m = NULL,  
  c1 = NULL,  
  c2 = NULL,  
  c3 = NULL,  
  c4 = NULL,  
  c1t = NULL,  
  c2t = NULL,  
  c3t = NULL,  
  omega = NULL,  
  m = NULL,  
  plots = TRUE,  
  plot.by = NULL,  
  nlim = NULL,  
  Jlim = NULL,  
  Klim = NULL,  
  plim = NULL,  
  varlim = NULL,  
  nlab = NULL,  
  Jlab = NULL,  
  Klab = NULL,  
)
```

```

plab = NULL,
varlab = NULL,
vartitle = NULL,
verbose = TRUE,
iter = 100,
tol = 1e-10
)

```

Arguments

n	The level-1 sample size per level-2 unit.
J	The level-2 sample size per level-3 unit.
K	The level-3 sample size per level-4 unit.
p	The proportion of level-3 units to be assigned to treatment.
icc2	The unconditional intraclass correlation coefficient (ICC) at level 2.
icc3	The unconditional intraclass correlation coefficient (ICC) at level 3.
icc4	The unconditional intraclass correlation coefficient (ICC) at level 4.
r12	The proportion of level-1 variance explained by covariates.
r22	The proportion of level-2 variance explained by covariates.
r32	The proportion of level-3 variance explained by covariates.
r42m	The proportion of variance of site-specific treatment effect explained by covariates.
c1	The cost of sampling one level-1 unit in control condition.
c2	The cost of sampling one level-2 unit in control condition.
c3	The cost of sampling one level-3 unit in control condition.
c4	The cost of sampling one level-4 unit.
c1t	The cost of sampling one level-1 unit in treatment condition.
c2t	The cost of sampling one level-2 unit in treatment condition.
c3t	The cost of sampling one level-3 unit in treatment condition.
omega	The standardized variance of site-specific treatment effect.
m	Total budget, default is the total costs of sampling 60 level-4 units.
plots	Logical, provide variance plots if TRUE, otherwise not; default value is TRUE.
plot.by	Plot the variance by n, J, K and/or p; default value is plot.by = list(n = "n", J = "J", K = 'K', p = "p").
nlim	The plot range for n, default value is c(2, 50).
Jlim	The plot range for J, default value is c(2, 50).
Klim	The plot range for K, default value is c(2, 50).
plim	The plot range for p, default value is c(0, 1).
varlim	The plot range for variance, default value is c(0, 0.05).
nlab	The plot label for n, default value is "Level-1 Sample Size: n".

Jlab	The plot label for J, default value is "Level-2 Sample Size: J".
Klab	The plot label for K, default value is "Level-3 Sample Size: K".
plab	The plot label for p, default value is "Proportion Level-3 Units in Treatment: p".
varlab	The plot label for variance, default value is "Variance".
vartitle	The title of variance plot, default value is NULL.
verbose	Logical; print the values of n, J, K, and p if TRUE, otherwise not; default value is TRUE.
iter	Number of iterations; default value is 100.
tol	Tolerance for convergence; default value is 1e-10.

Value

Unconstrained or constrained optimal sample allocation (n, J, K, and p). The function also returns the variance of the treatment effect, function name, design type, and parameters used in the calculation.

Examples

```
# Unconstrained optimal design #-----
myod1 <- od.4m(icc2 = 0.2, icc3 = 0.1, icc4 = 0.05, omega = 0.02,
             r12 = 0.5, r22 = 0.5, r32 = 0.5, r42m = 0.5,
             c1 = 1, c2 = 5, c3 = 25,
             c1t = 1, c2t = 50, c3t = 250, c4 = 500,
             varlim = c(0, 0.005))
myod1$out # output
# Plots by p and K
myod1 <- od.4m(icc2 = 0.2, icc3 = 0.1, icc4 = 0.05, omega = 0.02,
             r12 = 0.5, r22 = 0.5, r32 = 0.5, r42m = 0.5,
             c1 = 1, c2 = 5, c3 = 25,
             c1t = 1, c2t = 50, c3t = 250, c4 = 500,
             varlim = c(0, 0.005), plot.by = list(p = 'p', K = 'K'))

# Constrained optimal design with p = 0.5 #-----
myod2 <- od.4m(icc2 = 0.2, icc3 = 0.1, icc4 = 0.05, omega = 0.02,
             r12 = 0.5, r22 = 0.5, r32 = 0.5, r42m = 0.5,
             c1 = 1, c2 = 5, c3 = 25,
             c1t = 1, c2t = 50, c3t = 250, c4 = 500,
             varlim = c(0, 0.005), p = 0.5)
myod2$out
# Relative efficiency (RE)
myre <- re(od = myod1, subod = myod2)
myre$re # RE = 0.88

# Constrained optimal design with J = 20 #-----
myod3 <- od.4m(icc2 = 0.2, icc3 = 0.1, icc4 = 0.05, omega = 0.02,
             r12 = 0.5, r22 = 0.5, r32 = 0.5, r42m = 0.5,
             c1 = 1, c2 = 5, c3 = 25,
             c1t = 1, c2t = 50, c3t = 250, c4 = 500,
             varlim = c(0, 0.005), J = 20)
```

```

myod3$out
# Relative efficiency (RE)
myre <- re(od = myod1, subod= myod3)
myre$re # RE = 0.58

# Constrained n, J, K and p, no calculation performed #-----
myod4 <- od.4m(icc2 = 0.2, icc3 = 0.1, icc4 = 0.05, omega = 0.02,
              r12 = 0.5, r22 = 0.5, r32 = 0.5, r42m = 0.5,
              c1 = 1, c2 = 5, c3 = 25,
              c1t = 1, c2t = 50, c3t = 250, c4 = 500,
              varlim = c(0, 0.005), p = 0.5, n = 15, J = 20, K = 5)
myod4$out
# Relative efficiency (RE)
myre <- re(od = myod1, subod= myod4)
myre$re # RE = 0.46

```

power.1

Budget and/or sample size, power, MDES calculation for single-level experiments detecting main effects

Description

This function can calculate required budget for desired power, power or minimum detectable effect size (MDES) under fixed budget for single-level experiments. It also can perform conventional power analyses (e.g., required sample size, power, and MDES calculation).

Usage

```

power.1(
  cost.model = TRUE,
  expr = NULL,
  constraint = NULL,
  sig.level = 0.05,
  two.tailed = TRUE,
  d = NULL,
  power = NULL,
  m = NULL,
  n = NULL,
  p = NULL,
  r12 = NULL,
  q = NULL,
  c1 = NULL,
  c1t = NULL,
  dlim = NULL,
  powerlim = NULL,
  nlim = NULL,
  mlim = NULL,

```

```

    rounded = TRUE
  )

```

Arguments

<code>cost.model</code>	Logical; power analyses accommodating costs and budget (e.g., required budget for desired power, power/MDES under fixed budget) if TRUE, otherwise conventional power analyses (e.g., required sample size, power, or MDES calculation); default value is TRUE.
<code>expr</code>	Returned object from function <code>od.1</code> ; default value is NULL; if <code>expr</code> is specified, parameter values of <code>r12</code> , <code>c1</code> , <code>c1t</code> , and <code>p</code> used or solved in function <code>od.1</code> will be passed to the current function; only the value of <code>p</code> that specified or solved in function <code>od.1</code> can be overwritten if <code>constraint</code> is specified.
<code>constraint</code>	Specify the constrained value of <code>p</code> in list format to overwrite that from <code>expr</code> ; default value is NULL.
<code>sig.level</code>	Significance level or type I error rate, default value is 0.05.
<code>two.tailed</code>	Logical; two-tailed tests if TRUE, otherwise one-tailed tests; default value is TRUE.
<code>d</code>	Effect size.
<code>power</code>	Statistical power.
<code>m</code>	Total budget.
<code>n</code>	The total sample size.
<code>p</code>	The proportion of individuals to be assigned to treatment.
<code>r12</code>	The proportion of outcome variance explained by covariates.
<code>q</code>	The number of covariates.
<code>c1</code>	The cost of sampling one unit in control condition.
<code>c1t</code>	The cost of sampling one unit in treatment condition.
<code>dlim</code>	The range for searching the root of effect size (<code>d</code>) numerically, default value is <code>c(0, 5)</code> .
<code>powerlim</code>	The range for searching the root of power (<code>power</code>) numerically, default value is <code>c(1e-10, 1 - 1e-10)</code> .
<code>nlim</code>	The range for searching the root of sample size (<code>n</code>) numerically, default value is <code>c(4, 10e10)</code> .
<code>mlim</code>	The range for searching the root of budget (<code>m</code>) numerically, default value is the costs sampling <code>nlim</code> units across treatment conditions or <code>c(4 * ncost, 10e10 * ncost)</code> with <code>ncost = ((1 - p) * c1 + p * c1t)</code> .
<code>rounded</code>	Logical; round <code>p</code> that is from functions <code>od.1</code> to two decimal places if TRUE, otherwise no rounding; default value is TRUE.

Value

Required budget (or required sample size), statistical power, or MDES depending on the specification of parameters. The function also returns the function name, design type, and parameters used in the calculation.

Examples

```

# Unconstrained optimal design
myod1 <- od.1(r12 = 0.5, c1 = 1, c1t = 5, varlim = c(0, 0.2))
myod1$out # p = 0.31

# ----- Power analyses by default considering costs and budget -----
# Required budget and sample size
mym.1 <- power.1(expr = myod1, d = 0.2, q = 1, power = 0.8)
mym.1$out # m = 1032 n = 461
# mym.1$par # parameters and their values used for the function
# Or, equivalently, specify every argument in the function
mym.1 <- power.1(d = 0.2, power = 0.8, c1 = 1, c1t = 5,
                 r12 = 0.5, p = 0.31, q = 1)
# Required budget and sample size with constrained p
mym.2 <- power.1(expr = myod1, d = 0.2, q = 1, power = 0.8,
                 constraint = list(p = 0.5))
mym.2$out # m = 1183, n = 394

# Power calculation
mypower <- power.1(expr = myod1, q = 1, d = 0.2, m = 1032)
mypower$out # power = 0.80
# Power calculation under constrained p (p = 0.5)
mypower.1 <- power.1(expr = myod1, q = 1, d = 0.2, m = 1032,
                    constraint = list(p = 0.5))
mypower.1$out # power = 0.74

# MDES calculation
mymdes <- power.1(expr = myod1, q = 1, power = 0.80, m = 1032)
mymdes$out # d = 0.20

# ----- Conventional power analyses with cost.model = FALSE -----
# Required sample size n
myn <- power.1(cost.model = FALSE, expr = myod1, d = 0.2, q = 1, power = 0.8)
myn$out # n = 461
# myn$par # parameters and their values used for the function
# Or, equivalently, specify every argument in the function
myn <- power.1(cost.model = FALSE, d = 0.2, power = 0.8,
               r12 = 0.5, p = 0.31, q = 1)

# Power calculation
mypower1 <- power.1(cost.model = FALSE, expr = myod1, n = 461, d = 0.2, q = 1)
mypower1$out # power = 0.80

# MDES calculation
mymdes1 <- power.1(cost.model = FALSE, expr = myod1, n = 461, power = 0.8, q = 1)
mymdes1$out # d = 0.20

```

power.2 *Budget and/or sample size, power, MDES calculation for two-level CRTs detecting main effects*

Description

This function can calculate required budget for desired power, power or minimum detectable effect size (MDES) under fixed budget for two-level cluster randomized trials (CRTs). It also can perform conventional power analyses (e.g., required sample size, power, and MDES calculation).

Usage

```
power.2(
  cost.model = TRUE,
  expr = NULL,
  constraint = NULL,
  sig.level = 0.05,
  two.tailed = TRUE,
  d = NULL,
  power = NULL,
  m = NULL,
  n = NULL,
  J = NULL,
  p = NULL,
  icc = NULL,
  r12 = NULL,
  r22 = NULL,
  q = NULL,
  c1 = NULL,
  c2 = NULL,
  c1t = NULL,
  c2t = NULL,
  dlim = NULL,
  powerlim = NULL,
  Jlim = NULL,
  mlim = NULL,
  rounded = TRUE
)
```

Arguments

cost.model	Logical; power analyses accommodating costs and budget (e.g., required budget for desired power, power/MDES under fixed budget) if TRUE, otherwise conventional power analyses (e.g., required sample size, power, or MDES calculation); default value is TRUE.
expr	Returned object from function od.2 ; default is NULL; if expr is specified, parameter values of icc, r12, r22, c1, c2, c1t, c2t, n, and p used or solved in function od.2 will be passed to the current function; only the values of n and

	p that specified or solved in function <code>od.2</code> can be overwritten if constraint is specified.
<code>constraint</code>	Specify the constrained values of n and/or p in list format to overwrite those from <code>expr</code> ; default is NULL.
<code>sig.level</code>	Significance level or type I error rate, default value is 0.05.
<code>two.tailed</code>	Logical; two-tailed tests if TRUE, otherwise one-tailed tests; default value is TRUE.
<code>d</code>	Effect size.
<code>power</code>	Statistical power.
<code>m</code>	Total budget.
<code>n</code>	The level-1 sample size per level-2 unit.
<code>J</code>	The total level-2 sample size.
<code>p</code>	The proportion of level-2 clusters/units to be assigned to treatment.
<code>icc</code>	The unconditional intraclass correlation coefficient (ICC) in population or in each treatment condition.
<code>r12</code>	The proportion of level-1 variance explained by covariates.
<code>r22</code>	The proportion of level-2 variance explained by covariates.
<code>q</code>	The number of level-2 covariates.
<code>c1</code>	The cost of sampling one level-1 unit in control condition.
<code>c2</code>	The cost of sampling one level-2 unit in control condition.
<code>c1t</code>	The cost of sampling one level-1 unit in treatment condition.
<code>c2t</code>	The cost of sampling one level-2 unit in treatment condition.
<code>dlim</code>	The range for searching the root of effect size (d) numerically, default value is <code>c(0, 5)</code> .
<code>powerlim</code>	The range for searching the root of power (power) numerically, default value is <code>c(1e-10, 1 - 1e-10)</code> .
<code>Jlim</code>	The range for searching the root of level-2 sample size (J) numerically, default is <code>c(4, 10e10)</code> .
<code>mlim</code>	The range for searching the root of budget (m) numerically, default is the costs sampling <code>Jlim</code> level-2 units across treatment conditions or <code>c(4 * Jcost, 10e10 * Jcost)</code> , with $Jcost = ((1 - p) * (c1 * n + c2) + p * (c1t * n + c2t))$.
<code>rounded</code>	Logical; round n and p that are from functions <code>od.2</code> to integer and two decimal places, respectively if TRUE, otherwise no rounding; default value is TRUE.

Value

Required budget (and/or required level-2 sample size), statistical power, or MDES depending on the specification of parameters. The function also returns the function name, design type, and parameters used in the calculation.

References

Shen, Z., & Kelcey, B. (2020). Optimal sample allocation under unequal costs in cluster-randomized trials. *Journal of Educational and Behavioral Statistics*, 45(4): 446–474. <<https://doi.org/10.3102/1076998620912418>>

Examples

```

# Unconstrained optimal design
myod1 <- od.2(icc = 0.2, r12 = 0.5, r22 = 0.5, c1 = 1, c2 = 5, c1t = 1, c2t = 50)
myod1$out # n = 8.9, p = 0.33

# ----- Power analyses by default considering costs and budget -----
# Required budget and sample size
mym.1 <- power.2(expr = myod1, d = 0.2, q = 1, power = 0.8)
mym.1$out # m = 3755, J = 130.2
#mym.1$par # parameters and their values used for the function
# Or, equivalently, specify every argument in the function
mym.1 <- power.2(d = 0.2, power = 0.8, icc = 0.2,
                 c1 = 1, c2 = 5, c1t = 1, c2t = 50,
                 r12 = 0.5, r22 = 0.5, n = 9, p = 0.33, q = 1)
# Required budget and sample size with constrained p
mym.2 <- power.2(expr = myod1, d = 0.2, q = 1, power = 0.8,
                 constraint = list(p = 0.5))
mym.2$out # m = 4210, J = 115.3
# Required budget and sample size with constrained p and n
mym.3 <- power.2(expr = myod1, d = 0.2, q = 1, power = 0.8,
                 constraint = list(p = 0.5, n = 20))
mym.3$out # m = 4568, J = 96.2

# Power calculation
mypower <- power.2(expr = myod1, q = 1, d = 0.2, m = 3755)
mypower$out # power = 0.80
# Power calculation under constrained p (p = 0.5)
mypower.1 <- power.2(expr = myod1, q = 1, d = 0.2, m = 3755,
                    constraint = list(p = 0.5))
mypower.1$out # power = 0.75

# MDES calculation
mymdes <- power.2(expr = myod1, q = 1, power = 0.80, m = 3755)
mymdes$out # d = 0.20

# ----- Conventional power analyses with cost.model = FALSE -----
# Required J
myJ <- power.2(cost.model = FALSE, expr = myod1, d = 0.2, q = 1, power = 0.8)
myJ$out # J = 130.2
#myJ$par # parameters and their values used for the function
# Or, equivalently, specify every argument in the function
myJ <- power.2(cost.model = FALSE, d = 0.2, power = 0.8, icc = 0.2,
               r12 = 0.5, r22 = 0.5, n = 9, p = 0.33, q = 1)

# Power calculation
mypower1 <- power.2(cost.model = FALSE, expr = myod1, J = 130, d = 0.2, q = 1)
mypower1$out # power = 0.80

# MDES calculation
mymdes1 <- power.2(cost.model = FALSE, expr = myod1, J = 130, power = 0.8, q = 1)
mymdes1$out # d = 0.20

```

`power.2.221`*Budget and/or sample size, power, MDES calculation for CRTs probing mediation effects with cluster-level mediators*

Description

This function can calculate required budget for desired power and power under a fixed budget for experimental studies with group mediators probing mediation effects. It also can perform conventional power analyses (e.g., required sample size and power calculation).

Usage

```
power.2.221(  
  cost.model = TRUE,  
  expr = NULL,  
  constraint = NULL,  
  sig.level = 0.05,  
  two.tailed = TRUE,  
  a = NULL,  
  b = NULL,  
  power = NULL,  
  m = NULL,  
  test = "joint",  
  n = NULL,  
  p = NULL,  
  c1 = NULL,  
  c1t = NULL,  
  c2 = NULL,  
  c2t = NULL,  
  r12 = 0,  
  r22 = 0,  
  r2m = 0,  
  icc = NULL,  
  J = NULL,  
  q = 0,  
  q.a = 0,  
  q.b = 0,  
  powerlim = NULL,  
  Jlim = NULL,  
  mlim = NULL,  
  rounded = TRUE  
)
```


Arguments

cost.model	Logical; power analyses accommodating costs and budget (e.g., required budget for desired power, power/MDES under fixed budget) if TRUE, otherwise conventional power analyses (e.g., required sample size, power, or MDES calculation); default value is TRUE.
expr	returned object from function od.2.221 ; default value is NULL; if expr is specified, parameter values of a, b, c1, c1t, and p used or solved in function od.2.221 will be passed to the current function; only the values of p and n that specified or solved in function od.2.221 can be overwritten if constraint is specified.
constraint	specify the constrained value of p and/or n in a list format to overwrite that/those from expr; default value is NULL.
sig.level	Significance level or type I error rate, default value is 0.05.
two.tailed	Logical; two-tailed tests if TRUE, otherwise one-tailed tests; default value is TRUE.
a	The treatment effect on the mediator.
b	The within treatment correlation between the outcome and the mediator.
power	Statistical power.
m	Total budget.
test	The type of test will be used to detect mediation effects. Default is the joint significance test (i.e., test = "joint"). Other choices are the Sobel test and Monte Carlo confidence interval test by specifying the argument as test = "sobel" or test = "mcci".
n	The level-1 sample size per level-2 unit.
p	The proportion of level-2 clusters/units to be assigned to treatment.
c1	The cost of sampling one level-1 unit in control condition.
c1t	The cost of sampling one level-1 unit in treatment condition.
c2	The cost of sampling one level-2 unit in control condition.
c2t	The cost of sampling one level-2 unit in treatment condition.
r12	The proportion of level-1 variance explained by covariates.
r22	The proportion of level-2 variance explained by covariates.
r2m	The proportion of within treatment mediator variance explained by covariates.
icc	The unconditional intraclass correlation coefficient (ICC) in population or in each treatment condition.
J	The total level-2 sample size.
q	The number of level-2 covariates.
q.a	The number of covariates in the outcome model (except the treatment indicator and the mediator).
q.b	The number of covariates in the mediator model (except the treatment indicator).
powerlim	The range for searching the root of power (power) numerically, default value is c(1e-10, 1 - 1e-10).

Jlim	The range for searching the root of level-2 sample size (J) numerically, default is c(4, 10e10).
mlim	the range for searching the root of budget (m) numerically, default value is the costs sampling nlim units across treatment conditions or c(4 * ncost, 10e10 * ncost) with ncost = ((1 - p) * c1 + p * c1t)
rounded	Logical; round n and p that are from functions od.2 to integer and two decimal places, respectively if TRUE, otherwise no rounding; default value is TRUE.

Value

Required budget (or required sample size), statistical power, or MDES depending on the specification of parameters. The function also returns the function name, design type, and parameters used in the calculation.

power.2m	<i>Budget and/or sample size, power, MDES calculation for two-level MRTs detecting main effects</i>
----------	---

Description

This function can calculate required budget for desired power, power or minimum detectable effect size (MDES) under fixed budget for two-level multisite randomized trials (MRTs). It also can perform conventional power analyses (e.g., required sample size, power, and MDES calculation).

Usage

```
power.2m(
  cost.model = TRUE,
  expr = NULL,
  constraint = NULL,
  sig.level = 0.05,
  two.tailed = TRUE,
  d = NULL,
  power = NULL,
  m = NULL,
  n = NULL,
  J = NULL,
  p = NULL,
  icc = NULL,
  r12 = NULL,
  r22m = NULL,
  q = NULL,
  c1 = NULL,
  c2 = NULL,
  c1t = NULL,
  omega = NULL,
```

```

    dlim = NULL,
    powerlim = NULL,
    Jlim = NULL,
    mlim = NULL,
    rounded = TRUE
  )

```

Arguments

cost.model	Logical; power analyses accommodating costs and budget (e.g., required budget for desired power, power/MDES under fixed budget) if TRUE, otherwise conventional power analyses (e.g., required sample size, power, or MDES calculation); default value is TRUE.
expr	Returned objects from function <code>od.2m</code> ; default is NULL; if expr is specified, parameter values of <code>icc</code> , <code>r12</code> , <code>r22m</code> , <code>c1</code> , <code>c2</code> , <code>c1t</code> , <code>p</code> , and <code>n</code> used or solved in function <code>od.2m</code> will be passed to current function; only the values of <code>p</code> and <code>n</code> that specified or solved in function <code>od.2m</code> can be overwritten if constraint is specified.
constraint	Specify the constrained values of <code>p</code> and/or <code>n</code> in list format to overwrite those from <code>expr</code> ; default value is NULL.
sig.level	Significance level or type I error rate, default value is 0.05.
two.tailed	Logical; two-tailed tests if TRUE, otherwise one-tailed tests; default value is TRUE.
d	Effect size.
power	Statistical power.
m	Total budget.
n	The level-1 sample size per level-2 unit.
J	The level-2 sample size per level-3 unit.
p	The proportion of level-1 units to be assigned to treatment.
icc	The unconditional intraclass correlation coefficient (ICC) in population or in each treatment condition.
r12	The proportion of level-1 variance explained by covariates.
r22m	The proportion of variance of site-specific treatment effect explained by covariates.
q	The number of covariates at level 2.
c1	The cost of sampling one level-1 unit in control condition.
c2	The cost of sampling one level-2 unit.
c1t	The cost of sampling one level-1 unit in treatment condition.
omega	The standardized variance of site-specific treatment effect.
dlim	The range for searching the root of effect size (<code>d</code>) numerically, default value is <code>c(0, 5)</code> .
powerlim	The range for searching the root of power (<code>power</code>) numerically, default value is <code>c(1e-10, 1 - 1e-10)</code> .

Jlim	The range for searching the root of level-2 sample size (J) numerically, default is c(4, 10e10).
mlim	The range for searching the root of budget (m) numerically, default is the costs sampling Jlim level-2 units or c(4 * Jcost, 1e+10 * Jcost) with Jcost = (1 - p) * c1 * n + p * c1t * n + c2.
rounded	Logical; round the values of p, n/J/K that are from functions od.4 to two decimal places and integer, respectively if TRUE, otherwise no rounding; default value is TRUE.

Value

Required budget (and/or required level-2 sample size), statistical power, or MDES depending on the specification of parameters. The function also returns the function name, design type, and parameters used in the calculation.

References

Shen, Z., & Kelcey, B. (in press). Optimal sample allocation in multisite randomized trials. *The Journal of Experimental Education*. <<https://doi.org/10.1080/00220973.2020.1830361>>

Examples

```
# Unconstrained optimal design #-----
myod1 <- od.2m(icc = 0.2, omega = 0.02, r12 = 0.5, r22m = 0.5,
              c1 = 1, c2 = 10, c1t = 10,
              varlim = c(0, 0.005))
myod1$out # n = 19.8, p = 0.37

# ----- Power analyses by default considering costs and budget -----
# Required budget and sample size
mym.1 <- power.2m(expr = myod1, d = 0.2, q = 1, power = 0.8)
mym.1$out # m = 2019, J = 20.9
# mym.1$par # parameters and their values used for the function
# Or, equivalently, specify every argument in the function
mym.1 <- power.2m(d = 0.2, power = 0.8, q = 1,
                 icc = 0.2, omega = 0.02, r12 = 0.5, r22m = 0.5,
                 c1 = 1, c2 = 10, c1t = 10,
                 n = 20, p = 0.37)
# Required budget and sample size with constrained p
mym.2 <- power.2m(expr = myod1, d = 0.2, q = 1, power = 0.8,
                 constraint = list(p = 0.5))
mym.2$out # m = 2373, J = 19.8
# Required budget and sample size with constrained p and n
mym.3 <- power.2m(expr = myod1, d = 0.2, q = 1, power = 0.8,
                 constraint = list(p = 0.5, n = 5))
mym.3$out # m = 2502, J = 66.7

# Power calculation
mypower <- power.2m(expr = myod1, q = 1, d = 0.2, m = 2019)
mypower$out # power = 0.80
# Power calculation under constrained p (p = 0.5)
```

```

mypower.1 <- power.2m(expr = myod1, q = 1, d = 0.2, m = 2019,
  constraint = list(p = 0.5))
mypower.1$out # power = 0.72

# MDES calculation
mymdes <- power.2m(expr = myod1, q = 1, power = 0.80, m = 2019)
mymdes$out # d = 0.20

# ----- Conventional power analyses with cost.model = FALSE-----
# Required sample size
myJ <- power.2m(cost.model = FALSE, expr = myod1, d = 0.2, q = 1, power = 0.8)
myJ$out # J = 6.3
# myL$par # parameters and their values used for the function
# Or, equivalently, specify every argument in the function
myJ <- power.2m(cost.model = FALSE, d = 0.2, power = 0.8, q = 1,
  icc = 0.2, omega = 0.02, r12 = 0.5, r22m = 0.5,
  c1 = 1, c2 = 10, c1t = 10,
  n = 20, p = 0.37)

# Power calculation
mypower1 <- power.2m(cost.model = FALSE, expr = myod1, J = 6.3, d = 0.2, q = 1)
mypower1$out # power = 0.80

# MDES calculation
mymdes1 <- power.2m(cost.model = FALSE, expr = myod1, J = 6.3, power = 0.8, q = 1)
mymdes1$out # d = 0.20

```

power.3

Budget and/or sample size, power, MDES calculation for three-level CRTs detecting main effects

Description

This function can calculate required budget for desired power, power or minimum detectable effect size (MDES) under fixed budget for three-level cluster randomized trials (CRTs). It also can perform conventional power analyses (e.g., required sample size, power, and MDES calculation).

Usage

```

power.3(
  cost.model = TRUE,
  expr = NULL,
  constraint = NULL,
  sig.level = 0.05,
  two.tailed = TRUE,
  d = NULL,
  power = NULL,

```

```

m = NULL,
n = NULL,
J = NULL,
K = NULL,
p = NULL,
icc2 = NULL,
icc3 = NULL,
r12 = NULL,
r22 = NULL,
r32 = NULL,
q = NULL,
c1 = NULL,
c2 = NULL,
c3 = NULL,
c1t = NULL,
c2t = NULL,
c3t = NULL,
dlim = NULL,
powerlim = NULL,
Klim = NULL,
mlim = NULL,
rounded = TRUE
)

```

Arguments

cost.model	Logical; power analyses accommodating costs and budget (e.g., required budget for desired power, power/MDES under fixed budget) if TRUE, otherwise conventional power analyses (e.g., required sample size, power, or MDES calculation); default value is TRUE.
expr	Returned objects from function od.3 ; default is NULL; if expr is specified, parameter values of icc2, icc3, r12, r22, r32, c1, c2, c3, c1t, c2t, c3t, p, n, and J used or solved in function od.3 will be passed to the current function; only the values of p, n, and/or J that specified or solved in function od.3 can be overwritten if constraint is specified.
constraint	Specify the constrained values of p, n, and/or J in list format to overwrite those from expr; default is NULL.
sig.level	Significance level or type I error rate, default value is 0.05.
two.tailed	Logical; two-tailed tests if TRUE, otherwise one-tailed tests; default value is TRUE.
d	Effect size.
power	Statistical power.
m	Total budget.
n	The level-1 sample size per level-2 unit.
J	The level-2 sample size per level-3 unit.
K	The total level-3 sample size.

p	The proportion of level-3 clusters/units assigned to treatment.
icc2	The unconditional intraclass correlation coefficient (ICC) at level 2.
icc3	The unconditional intraclass correlation coefficient (ICC) at level 3.
r12	The proportion of level-1 variance explained by covariates.
r22	The proportion of level-2 variance explained by covariates.
r32	The proportion of level-3 variance explained by covariates.
q	The number of covariates at level 3.
c1	The cost of sampling one level-1 unit in control condition.
c2	The cost of sampling one level-2 unit in control condition.
c3	The cost of sampling one level-3 unit in control condition.
c1t	The cost of sampling one level-1 unit in treatment condition.
c2t	The cost of sampling one level-2 unit in treatment condition.
c3t	The cost of sampling one level-3 unit in treatment condition.
dlim	The range for searching the root of effect size (d) numerically, default value is c(0, 5).
powerlim	The range for searching the root of power (power) numerically, default value is c(1e-10, 1 - 1e-10).
Klim	The range for searching the root of level-3 sample size (K) numerically, default value is c(4, 1e+10).
mlim	The range for searching the root of budget (m) numerically, default value is the costs sampling Klim level-3 units across treatment conditions or $c(4 * Kcost, 1e+10 * Kcost)$ with $Kcost = ((1 - p) * (c1 * n * J + c2 * J + c3) + p * (c1t * n * J + c2t * J + c3t))$.
rounded	Logical; round the values of p, n/J that are from functions od.3 to two decimal places and integer, respectively if TRUE, otherwise no rounding; default value is TRUE.

Value

Required budget (and/or required level-3 sample size), statistical power, or MDES depending on the specification of parameters. The function also returns the function name, design type, and parameters used in the calculation.

References

Shen, Z., & Kelcey, B. (2020). Optimal sample allocation under unequal costs in cluster-randomized trials. *Journal of Educational and Behavioral Statistics*, 45(4): 446–474. <<https://doi.org/10.3102/1076998620912418>>

Examples

```
# Unconstrained optimal design
myod1 <- od.3(icc2 = 0.2, icc3 = 0.1, r12 = 0.5, r22 = 0.5, r32 = 0.5,
             c1 = 1, c2 = 5, c3 = 25, c1t = 1, c2t = 50, c3t = 250)
myod1$out # output # n = 7.9, J = 3.2, p = 0.28
```

```

# ----- Power analyses by default considering costs and budget -----
# Required budget and sample size
mym.1 <- power.3(expr = myod1, d = 0.2, q = 1, power = 0.8)
mym.1$out # m = 16032, K = 97.3
#mym.1$par # parameters and their values used for the function
# Or, equivalently, specify every argument in the function
mym.1 <- power.3(d = 0.2, power = 0.8, q = 1,
  icc2 = 0.2, icc3 = 0.1, r12 = 0.5, r22 = 0.5, r32 = 0.5,
  c1 = 1, c2 = 5, c3 = 25, c1t = 1, c2t = 50, c3t = 250,
  n = 8, J = 3, p = 0.28)
# Required budget and sample size with constrained p
mym.2 <- power.3(expr = myod1, d = 0.2, q = 1, power = 0.8,
  constraint = list(p = 0.5))
mym.2$out # m = 19239, K = 78.8
# Required budget and sample size with constrained p and J
mym.3 <- power.3(expr = myod1, d = 0.2, q = 1, power = 0.8,
  constraint = list(p = 0.5, J = 20))
mym.3$out # m = 39774, K = 46.9

# Power calculation
mypower <- power.3(expr = myod1, q = 1, d = 0.2, m = 16032)
mypower$out # power = 0.80
# Power calculation under constrained p (p = 0.5)
mypower.1 <- power.3(expr = myod1, q = 1, d = 0.2, m = 16032,
  constraint = list(p = 0.5))
mypower.1$out # power = 0.72

# MDES calculation
mymdes <- power.3(expr = myod1, q = 1, power = 0.80, m = 16032)
mymdes$out # d = 0.20

# ----- Conventional power analyses with cost.model = FALSE-----
# Required sample size
myK <- power.3(cost.model = FALSE, expr = myod1, d = 0.2, q = 1, power = 0.8)
myK$out # K = 97.3
#myK$par # parameters and their values used for the function
# Or, equivalently, specify every argument in the function
myK <- power.3(cost.model = FALSE, d = 0.2, power = 0.8, q = 1,
  icc2 = 0.2, icc3 = 0.1, r12 = 0.5, r22 = 0.5, r32 = 0.5,
  n = 8, J = 3, p = 0.28)

# Power calculation
mypower1 <- power.3(cost.model = FALSE, expr = myod1, K = 97, d = 0.2, q = 1)
mypower1$out # power = 0.80

# MDES calculation
mymdes1 <- power.3(cost.model = FALSE, expr = myod1, K = 97, power = 0.8, q = 1)
mymdes1$out # d = 0.20

```

power.3m	<i>Budget and/or sample size, power, MDES calculation for three-level MRTs detecting main effects</i>
----------	---

Description

This function can calculate required budget for desired power, power or minimum detectable effect size (MDES) under fixed budget for three-level multisite randomized trials (MRTs). It also can perform conventional power analyses (e.g., required sample size, power, and MDES calculation).

Usage

```
power.3m(
  cost.model = TRUE,
  expr = NULL,
  constraint = NULL,
  sig.level = 0.05,
  two.tailed = TRUE,
  d = NULL,
  power = NULL,
  m = NULL,
  n = NULL,
  J = NULL,
  K = NULL,
  p = NULL,
  icc2 = NULL,
  icc3 = NULL,
  r12 = NULL,
  r22 = NULL,
  r32m = NULL,
  q = NULL,
  c1 = NULL,
  c2 = NULL,
  c3 = NULL,
  c1t = NULL,
  c2t = NULL,
  omega = NULL,
  dlim = NULL,
  powerlim = NULL,
  Klim = NULL,
  mlim = NULL,
  rounded = TRUE
)
```

Arguments

cost.model	Logical; power analyses accommodating costs and budget (e.g., required budget for desired power, power/MDES under fixed budget) if TRUE, otherwise
------------	--

	conventional power analyses (e.g., required sample size, power, or MDES calculation); default value is TRUE.
expr	Returned objects from function od.3m ; default is NULL; if expr is specified, parameter values of <code>icc2</code> , <code>icc3</code> , <code>r12</code> , <code>r22</code> , <code>r32m</code> , <code>c1</code> , <code>c2</code> , <code>c3</code> , <code>c1t</code> , <code>c2t</code> , <code>p</code> , <code>n</code> , and <code>J</code> used or solved in function od.3m will be passed to current function; only the values of <code>p</code> , <code>n</code> , and/or <code>J</code> that specified or solved in function od.3m can be overwritten if <code>constraint</code> is specified.
constraint	Specify the constrained values of <code>p</code> , <code>n</code> , and/or <code>J</code> , in list format to overwrite those from <code>expr</code> ; default value is NULL.
sig.level	Significance level or type I error rate, default value is 0.05.
two.tailed	Logical; two-tailed tests if TRUE, otherwise one-tailed tests; default value is TRUE.
d	Effect size.
power	Statistical power.
m	Total budget.
n	The level-1 sample size per level-2 unit.
J	The level-2 sample size per level-3 unit.
K	The level-3 sample size per level-4 unit.
p	The proportion of level-2 units to be assigned to treatment.
icc2	The unconditional intraclass correlation coefficient (ICC) at level 2.
icc3	The unconditional intraclass correlation coefficient (ICC) at level 3.
r12	The proportion of level-1 variance explained by covariates.
r22	The proportion of level-2 variance explained by covariates.
r32m	The proportion of variance of site-specific treatment effect explained by covariates.
q	The number of covariates at level 3.
c1	The cost of sampling one level-1 unit in control condition.
c2	The cost of sampling one level-2 unit in control condition.
c3	The cost of sampling one level-3 unit.
c1t	The cost of sampling one level-1 unit in treatment condition.
c2t	The cost of sampling one level-2 unit in treatment condition.
omega	The standardized variance of site-specific treatment effect.
dlim	The range for searching the root of effect size (<code>d</code>) numerically, default value is <code>c(0, 5)</code> .
powerlim	The range for searching the root of power (<code>power</code>) numerically, default value is <code>c(1e-10, 1 - 1e-10)</code> .
Klim	The range for searching the root of level-3 sample size (<code>K</code>) numerically, default value is <code>c(4, 1e+10)</code> .
mlim	The range for searching the root of budget (<code>m</code>) numerically, default is the costs sampling <code>Klim</code> level-3 units or <code>c(4 * Kcost, 1e+10 * Kcost)</code> with <code>Kcost = ((1 - p) * (c1 * n * J + c2 * J) + p * (c1t * n * J + c2t * J) + c3</code> .
rounded	Logical; round the values of <code>p</code> , <code>n</code> / <code>J</code> / <code>K</code> that are from functions od.4 to two decimal places and integer, respectively if TRUE, otherwise no rounding; default value is TRUE.

Value

Required budget (and/or required level-3 sample size), statistical power, or MDES depending on the specification of parameters. The function also returns the function name, design type, and parameters used in the calculation.

References

Shen, Z., & Kelcey, B. (in press). Optimal sampling ratios in three-level multisite experiments. *Journal of Research on Educational Effectiveness*.

Examples

```
# Unconstrained optimal design #-----
myod1 <- od.3m(icc2 = 0.2, icc3 = 0.1, omega = 0.02,
              r12 = 0.5, r22 = 0.5, r32m = 0.5,
              c1 = 1, c2 = 5,
              c1t = 1, c2t = 200, c3 = 200,
              varlim = c(0, 0.005))
myod1$out # n = 13.1, J = 15.3, p = 0.23

# ----- Power analyses by default considering costs and budget -----
# Required budget and sample size
mym.1 <- power.3m(expr = myod1, d = 0.2, q = 1, power = 0.8)
mym.1$out # m = 15491, K = 13.6
# mym.1$par # parameters and their values used for the function
# Or, equivalently, specify every argument in the function
mym.1 <- power.3m(d = 0.2, power = 0.8, q = 1,
                 icc2 = 0.2, icc3 = 0.1, omega = 0.02,
                 r12 = 0.5, r22 = 0.5, r32m = 0.5,
                 c1 = 1, c2 = 5,
                 c1t = 1, c2t = 200, c3 = 200,
                 n = 13, J = 15, p = 0.23)
# Required budget and sample size with constrained p
mym.2 <- power.3m(expr = myod1, d = 0.2, q = 1, power = 0.8,
                 constraint = list(p = 0.5))
mym.2$out # m = 21072, K = 10.9
# Required budget and sample size with constrained p and n
mym.3 <- power.3m(expr = myod1, d = 0.2, q = 1, power = 0.8,
                 constraint = list(p = 0.5, n = 20))
mym.3$out # m = 21252, K = 10.4

# Power calculation
mypower <- power.3m(expr = myod1, q = 1, d = 0.2, m = 15491)
mypower$out # power = 0.80
# Power calculation under constrained p (p = 0.5)
mypower.1 <- power.3m(expr = myod1, q = 1, d = 0.2, m = 15491,
                    constraint = list(p = 0.5))
mypower.1$out # power = 0.62

# MDES calculation
mymdes <- power.3m(expr = myod1, q = 1, power = 0.80, m = 15491)
mymdes$out # d = 0.20
```

```

# ----- Conventional power analyses with cost.model = FALSE-----
# Required sample size
myK <- power.3m(cost.model = FALSE, expr = myod1, d = 0.2, q = 1, power = 0.8)
myK$out # K = 13.6
# myK$par # parameters and their values used for the function
# Or, equivalently, specify every argument in the function
myK <- power.3m(cost.model = FALSE, d = 0.2, power = 0.8, q = 1,
  icc2 = 0.2, icc3 = 0.1, omega = 0.02,
  r12 = 0.5, r22 = 0.5, r32m = 0.5,
  c1 = 1, c2 = 5,
  c1t = 1, c2t = 200, c3 = 200,
  n = 13, J = 15, p = 0.23)

# Power calculation
mypower1 <- power.3m(cost.model = FALSE, expr = myod1, K = 13.6, d = 0.2, q = 1)
mypower1$out # power = 0.80

# MDES calculation
mymdes1 <- power.3m(cost.model = FALSE, expr = myod1, K = 13.6, power = 0.8, q = 1)
mymdes1$out # d = 0.20

```

power.4

Budget and/or sample size, power, MDES calculation for four-level CRTs detecting main effects

Description

This function can calculate required budget for desired power, power or minimum detectable effect size (MDES) under fixed budget for four-level cluster randomized trials (CRTs). It also can perform conventional power analyses (e.g., required sample size, power, and MDES calculation).

Usage

```

power.4(
  cost.model = TRUE,
  expr = NULL,
  constraint = NULL,
  sig.level = 0.05,
  two.tailed = TRUE,
  d = NULL,
  power = NULL,
  m = NULL,
  n = NULL,
  J = NULL,
  K = NULL,
  L = NULL,

```

```

p = NULL,
icc2 = NULL,
icc3 = NULL,
icc4 = NULL,
r12 = NULL,
r22 = NULL,
r32 = NULL,
r42 = NULL,
q = NULL,
c1 = NULL,
c2 = NULL,
c3 = NULL,
c4 = NULL,
c1t = NULL,
c2t = NULL,
c3t = NULL,
c4t = NULL,
dlim = NULL,
powerlim = NULL,
Llim = NULL,
mlim = NULL,
rounded = TRUE
)

```

Arguments

cost.model	Logical; power analyses accommodating costs and budget (e.g., required budget for desired power, power/MDES under fixed budget) if TRUE, otherwise conventional power analyses (e.g., required sample size, power, or MDES calculation); default value is TRUE.
expr	Returned objects from function od.4 ; default value is NULL; if expr is specified, parameter values of icc2, icc3, icc4, r12, r22, r32, r42, c1, c2, c3, c4, c1t, c2t, c3t, c4t, p, n, J, and K used or solved in function od.4 will be passed to current function; only the values of p, n, J, and/or K that specified or solved in function od.4 can be overwritten if constraint is specified.
constraint	Specify the constrained values of p, n, J, and/or K in list format to overwrite those from expr; default value is NULL.
sig.level	Significance level or type I error rate, default value is 0.05.
two.tailed	Logical; two-tailed tests if TRUE, otherwise one-tailed tests; default value is TRUE.
d	Effect size.
power	Statistical power.
m	Total budget.
n	The level-1 sample size per level-2 unit.
J	The level-2 sample size per level-3 unit.
K	The level-3 sample size per level-4 unit.

L	The total level-4 sample size.
p	The proportion of level-4 clusters/units to be assigned to treatment.
icc2	The unconditional intraclass correlation coefficient (ICC) at level 2.
icc3	The unconditional intraclass correlation coefficient (ICC) at level 3.
icc4	The unconditional intraclass correlation coefficient (ICC) at level 4.
r12	The proportion of level-1 variance explained by covariates.
r22	The proportion of level-2 variance explained by covariates.
r32	The proportion of level-3 variance explained by covariates.
r42	The proportion of level-4 variance explained by covariates.
q	The number of covariates at level 4.
c1	The cost of sampling one level-1 unit in control condition.
c2	The cost of sampling one level-2 unit in control condition.
c3	The cost of sampling one level-3 unit in control condition.
c4	The cost of sampling one level-4 unit in control condition.
c1t	The cost of sampling one level-1 unit in treatment condition.
c2t	The cost of sampling one level-2 unit in treatment condition.
c3t	The cost of sampling one level-3 unit in treatment condition.
c4t	The cost of sampling one level-4 unit in treatment condition.
dlim	The range for searching the root of effect size (d) numerically, default value is c(0, 5).
powerlim	The range for searching the root of power (power) numerically, default value is c(1e-10, 1 - 1e-10).
Llim	The range for searching the root of level-4 sample size (L) numerically, default value is c(4, 1e+10).
mlim	The range for searching the root of budget (m) numerically, default value is the costs sampling Llim level-4 units across treatment conditions or $c(4 * Lcost, 1e+10 * Lcost)$ with $Lcost = ((1 - p) * (c1 * n * J * K + c2 * J * K + c3 * K + c4) + p * (c1t * n * J * K + c2t * J * K + c3t * K + c4t))$.
rounded	Logical; round the values of p, n/J/K that are from functions od.4 to two decimal places and integer, respectively if TRUE, otherwise no rounding; default value is TRUE.

Value

Required budget (and/or required level-4 sample size), statistical power, or MDES depending on the specification of parameters. The function also returns the function name, design type, and parameters used in the calculation.

Examples

```

# Unconstrained optimal design
myod1 <- od.4(icc2 = 0.2, icc3 = 0.1, icc4 = 0.05,
             r12 = 0.5, r22 = 0.5, r32 = 0.5, r42 = 0.5,
             c1 = 1, c2 = 5, c3 = 25, c4 = 125,
             c1t = 1, c2t = 50, c3t = 250, c4t = 2500)
myod1$out # output # n = 7.1, J = 3.2, K = 4.2, p = 0.23

# ----- Power analyses by default considering costs and budget -----
# Required budget and sample size
mym.1 <- power.4(expr = myod1, d = 0.2, q = 1, power = 0.8)
mym.1$out # m = 71161, L = 57.1
#mym.1$par # parameters and their values used for the function
# Or, equivalently, specify every argument in the function
mym.1 <- power.4(d = 0.2, power = 0.8, q = 1,
                 icc2 = 0.2, icc3 = 0.1, icc4 = 0.05,
                 r12 = 0.5, r22 = 0.5, r32 = 0.5, r42 = 0.5,
                 c1 = 1, c2 = 5, c3 = 25, c4 = 125,
                 c1t = 1, c2t = 50, c3t = 250, c4t = 2500,
                 n = 7, J = 3, K = 4, p = 0.23)
# Required budget and sample size with constrained p (p = 0.5)
mym.2 <- power.4(expr = myod1, d = 0.2, q = 1, power = 0.8,
                 constraint = list(p = 0.5))
mym.2$out # m = 93508, L = 41.1
# Required budget and sample size with constrained p and K
mym.3 <- power.4(expr = myod1, d = 0.2, q = 1, power = 0.8,
                 constraint = list(p = 0.5, K = 20))
mym.3$out # m = 157365, L = 25.7

# Power calculation
mypower <- power.4(expr = myod1, q = 1, d = 0.2, m = 71161)
mypower$out # power = 0.80
# Power calculation under constrained p (p = 0.5)
mypower.1 <- power.4(expr = myod1, q = 1, d = 0.2, m = 71161,
                    constraint = list(p = 0.5))
mypower.1$out # power = 0.68

# MDES calculation
mymdes <- power.4(expr = myod1, q = 1, power = 0.80, m = 71161)
mymdes$out # d = 0.20

# ----- Conventional power analyses with cost.model = FALSE -----
# Required sample size
myL <- power.4(cost.model = FALSE, expr = myod1, d = 0.2, q = 1, power = 0.8)
myL$out # L = 57.1
#myL$par # parameters and their values used for the function
# Or, equivalently, specify every argument in the function
myL <- power.4(cost.model = FALSE, d = 0.2, power = 0.8, q = 1,
               icc2 = 0.2, icc3 = 0.1, icc4 = 0.05,
               r12 = 0.5, r22 = 0.5, r32 = 0.5, r42 = 0.5,
               n = 7, J = 3, K = 4, p = 0.23)

```

```
# Power calculation
mypower1 <- power.4(cost.model = FALSE, expr = myod1, L = 57, d = 0.2, q = 1)
mypower1$out # power = 0.80

# MDES calculation
mymdes1 <- power.4(cost.model = FALSE, expr = myod1, L = 57, power = 0.8, q = 1)
mymdes1$out # d = 0.20
```

power.4m

Budget and/or sample size, power, MDES calculation for four-level MRTs detecting main effects

Description

This function can calculate required budget for desired power, power or minimum detectable effect size (MDES) under fixed budget for four-level multisite randomized trials (MRTs). It also can perform conventional power analyses (e.g., required sample size, power, and MDES calculation).

Usage

```
power.4m(
  cost.model = TRUE,
  expr = NULL,
  constraint = NULL,
  sig.level = 0.05,
  two.tailed = TRUE,
  d = NULL,
  power = NULL,
  m = NULL,
  n = NULL,
  J = NULL,
  K = NULL,
  L = NULL,
  p = NULL,
  icc2 = NULL,
  icc3 = NULL,
  icc4 = NULL,
  r12 = NULL,
  r22 = NULL,
  r32 = NULL,
  r42m = NULL,
  q = NULL,
  c1 = NULL,
  c2 = NULL,
  c3 = NULL,
  c4 = NULL,
```



```

c1t = NULL,
c2t = NULL,
c3t = NULL,
omega = NULL,
dlim = NULL,
powerlim = NULL,
Llim = NULL,
mlim = NULL,
rounded = TRUE
)

```

Arguments

cost.model	Logical; power analyses accommodating costs and budget (e.g., required budget for desired power, power/MDES under fixed budget) if TRUE, otherwise conventional power analyses (e.g., required sample size, power, or MDES calculation); default value is TRUE.
expr	Returned objects from function od.4m ; default is NULL; if expr is specified, parameter values of icc2, icc3, icc4, r12, r22, r32, r42m, c1, c2, c3, c4, c1t, c2t, c3t, p, n, J, and K used or solved in function od.4m will be passed to current function; only the values of p, n, J, and/or K that specified or solved in function od.4m can be overwritten if constraint is specified.
constraint	The constrained values of p, n, J, and/or K in list format to overwrite those from expr; default value is NULL.
sig.level	Significance level or type I error rate, default value is 0.05.
two.tailed	Logical; two-tailed tests if TRUE, otherwise one-tailed tests; default value is TRUE.
d	Effect size.
power	Statistical power.
m	Total budget.
n	The level-1 sample size per level-2 unit.
J	The level-2 sample size per level-3 unit.
K	The level-3 sample size per level-4 unit.
L	The total level-4 sample size.
p	The proportion of level-3 units to be assigned to treatment.
icc2	The unconditional intraclass correlation coefficient (ICC) at level 2.
icc3	The unconditional intraclass correlation coefficient (ICC) at level 3.
icc4	The unconditional intraclass correlation coefficient (ICC) at level 4.
r12	The proportion of level-1 variance explained by covariates.
r22	The proportion of level-2 variance explained by covariates.
r32	The proportion of level-3 variance explained by covariates.
r42m	The proportion of variance of site-specific treatment effect explained by covariates.

q	The number of covariates at level 4.
c1	The cost of sampling one level-1 unit in control condition.
c2	The cost of sampling one level-2 unit in control condition.
c3	The cost of sampling one level-3 unit in control condition.
c4	The cost of sampling one level-4 unit.
c1t	The cost of sampling one level-1 unit in treatment condition.
c2t	The cost of sampling one level-2 unit in treatment condition.
c3t	The cost of sampling one level-3 unit in treatment condition.
omega	The standardized variance of site-specific treatment effect.
dlim	The range for searching the root of effect size (d) numerically, default value is c(0, 5).
powerlim	The range for searching the root of power (power) numerically, default value is c(1e-10, 1 - 1e-10).
Llim	The range for searching the root of level-4 sample size (L) numerically, default value is c(4, 1e+10).
mlim	The range for searching the root of budget (m) numerically, default is the costs sampling Llim level-4 units or c(4 * Lcost, 1e+10 * Lcost) with Lcost = ((1 - p) * (c1 * n * J * K + c2 * J * K + c3 * K) + p * (c1t * n * J * K + c2t * J * K + c3t * K) + c4.
rounded	Logical; round the values of p, n/J/K that are from functions od.4 to two decimal places and integer, respectively if TRUE, otherwise no rounding; default value is TRUE.

Value

Required budget (and/or required level-4 sample size), statistical power, or MDES depending on the specification of parameters. The function also returns the function name, design type, and parameters used in the calculation.

Examples

```
# Unconstrained optimal design #-----
myod1 <- od.4m(icc2 = 0.2, icc3 = 0.1, icc4 = 0.05, omega = 0.02,
              r12 = 0.5, r22 = 0.5, r32 = 0.5, r42m = 0.5,
              c1 = 1, c2 = 5, c3 = 25,
              c1t = 1, c2t = 50, c3t = 250, c4 = 500,
              varlim = c(0, 0.005))
myod1$out # n = 8.3, J = 3.2, K = 4.9, p = 0.36

# ----- Power analyses by default considering costs and budget -----
# Required budget and sample size
mym.1 <- power.4m(expr = myod1, d = 0.2, q = 1, power = 0.8)
mym.1$out # m = 30201, L = 20.6
# mym.1$par # parameters and their values used for the function
# Or, equivalently, specify every argument in the function
mym.1 <- power.4m(d = 0.2, power = 0.8, q = 1,
```

```

        icc2 = 0.2, icc3 = 0.1, icc4 = 0.05, omega = 0.02,
        r12 = 0.5, r22 = 0.5, r32 = 0.5, r42m = 0.5,
        c1 = 1, c2 = 5, c3 = 25,
        c1t = 1, c2t = 50, c3t = 250, c4 = 500,
        n = 8, J = 3, K = 5, p = 0.36)
# Required budget and sample size with constrained p
mym.2 <- power.4m(expr = myod1, d = 0.2, q = 1, power = 0.8,
  constraint = list(p = 0.5))
mym.2$out # m = 33183, L = 19.3
# Required budget and sample size with constrained p and n
mym.3 <- power.4m(expr = myod1, d = 0.2, q = 1, power = 0.8,
  constraint = list(p = 0.5, n = 20))
mym.3$out # m = 34262, L = 18.0

# Power calculation
mypower <- power.4m(expr = myod1, q = 1, d = 0.2, m = 30201)
mypower$out # power = 0.80
# Power calculation under constrained p (p = 0.5)
mypower.1 <- power.4m(expr = myod1, q = 1, d = 0.2, m = 30201,
  constraint = list(p = 0.5))
mypower.1$out # power = 0.76

# MDES calculation
mymdes <- power.4m(expr = myod1, q = 1, power = 0.80, m = 30201)
mymdes$out # d = 0.20

# ----- Conventional power analyses with cost.model = FALSE-----
# Required sample size
myL <- power.4m(cost.model = FALSE, expr = myod1, d = 0.2, q = 1, power = 0.8)
myL$out # L = 20.6
# myL$par # parameters and their values used for the function
# Or, equivalently, specify every argument in the function
myL <- power.4m(cost.model = FALSE, d = 0.2, power = 0.8, q = 1,
  icc2 = 0.2, icc3 = 0.1, icc4 = 0.05, omega = 0.02,
  r12 = 0.5, r22 = 0.5, r32 = 0.5, r42m = 0.5,
  c1 = 1, c2 = 5, c3 = 25,
  c1t = 1, c2t = 50, c3t = 250, c4 = 500,
  n = 8, J = 3, K = 5, p = 0.36)

# Power calculation
mypower1 <- power.4m(cost.model = FALSE, expr = myod1, L = 20.6, d = 0.2, q = 1)
mypower1$out # power = 0.80

# MDES calculation
mymdes1 <- power.4m(cost.model = FALSE, expr = myod1, L = 20.6, power = 0.8, q = 1)
mymdes1$out # d = 0.20

```

Description

Calculate the relative efficiency (RE) between two designs, it returns same results as those from function `rpe`.

Usage

```
re(od, subod, rounded = TRUE, verbose = TRUE)
```

Arguments

od	Returned object of first design (e.g., unconstrained optimal design) from function <code>od.1</code> , <code>od.2</code> , <code>od.3</code> , <code>od.4</code> , <code>od.2m</code> , <code>od.3m</code> , or <code>od.4m</code> .
subod	Returned object of second design (e.g., constrained optimal design) from function <code>od.1</code> , <code>od.2</code> , <code>od.3</code> , <code>od.4</code> , <code>od.2m</code> , <code>od.3m</code> , or <code>od.4m</code> .
rounded	Logical; round the values of p , $n/J/K$ that are from functions to two decimal places and integer, respectively if TRUE, no rounding if FALSE; default is TRUE.
verbose	Logical; print the value of relative efficiency if TRUE, otherwise not; default is TRUE.

Value

Relative efficiency value.

References

- (1) Shen, Z., & Kelcey, B. (2020). Optimal sample allocation under unequal costs in cluster-randomized trials. *Journal of Educational and Behavioral Statistics*, 45(4): 446–474. <<https://doi.org/10.3102/107699862091>>
- (2) Shen, Z., & Kelcey, B. (in press). Optimal sample allocation in multisite randomized trials. *The Journal of Experimental Education*. <<https://doi.org/10.1080/00220973.2020.1830361>>
- (3) Shen, Z., & Kelcey, B. (in press). Optimal sampling ratios in three-level multisite experiments. *Journal of Research on Educational Effectiveness*.

Examples

```
# Unconstrained optimal design of 2-level CRT #-----
myod1 <- od.2(icc = 0.2, r12 = 0.5, r22 = 0.5, c1 = 1, c2 = 5, c1t = 1, c2t = 50,
             varlim = c(0.01, 0.02))
# Constrained optimal design with n = 20
myod2 <- od.2(icc = 0.2, r12 = 0.5, r22 = 0.5, c1 = 1, c2 = 5, c1t = 1, c2t = 50,
             n = 20, varlim = c(0.005, 0.025))
# Relative efficiency (RE)
myre <- re(od = myod1, subod = myod2)
myre$out # RE = 0.88
# Constrained optimal design with p = 0.5
myod2 <- od.2(icc = 0.2, r12 = 0.5, r22 = 0.5, c1 = 1, c2 = 5, c1t = 1, c2t = 50,
             p = 0.5, varlim = c(0.005, 0.025))
# Relative efficiency (RE)
myre <- re(od = myod1, subod = myod2)
```

```

myre$out # RE = 0.90

# Unconstrained optimal design of 3-level CRT #-----
myod1 <- od.3(icc2 = 0.2, icc3 = 0.1, r12 = 0.5, r22 = 0.5, r32 = 0.5,
             c1 = 1, c2 = 5, c3 = 25, c1t = 1, c2t = 50, c3t = 250,
             varlim = c(0.005, 0.025))
# Constrained optimal design with J = 20
myod2 <- od.3(icc2 = 0.2, icc3 = 0.1, r12 = 0.5, r22 = 0.5, r32 = 0.5, J = 20,
             c1 = 1, c2 = 5, c3 = 25, c1t = 1, c2t = 50, c3t = 250,
             varlim = c(0, 0.025))
# Relative efficiency (RE)
myre <- re(od = myod1, subod= myod2)
myre$out # RE = 0.53

# Unconstrained optimal design of 4-level CRT #-----
myod1 <- od.4(icc2 = 0.2, icc3 = 0.1, icc4 = 0.05, r12 = 0.5,
             r22 = 0.5, r32 = 0.5, r42 = 0.5,
             c1 = 1, c2 = 5, c3 = 25, c4 = 125,
             c1t = 1, c2t = 50, c3t = 250, c4t = 2500,
             varlim = c(0, 0.01))
# Constrained optimal design with p = 0.5
myod2 <- od.4(icc2 = 0.2, icc3 = 0.1, icc4 = 0.05, r12 = 0.5, p = 0.5,
             r22 = 0.5, r32 = 0.5, r42 = 0.5,
             c1 = 1, c2 = 5, c3 = 25, c4 = 125,
             c1t = 1, c2t = 50, c3t = 250, c4t = 2500,
             varlim = c(0, 0.01))
# Relative efficiency (RE)
myre <- re(od = myod1, subod= myod2)
myre$out # RE = 0.78

```

rpe

Relative precision and efficiency (RPE) calculation

Description

Calculate the relative precision and efficiency (RPE) between two designs, it returns same results as those from function [re](#).

Usage

```
rpe(od, subod, rounded = TRUE, verbose = TRUE)
```

Arguments

od	Returned object of first design (e.g., unconstrained optimal design) from function od.1 , od.2 , od.3 , od.4 , od.2m , od.3m , or od.4m .
subod	Returned object of second design (e.g., constrained optimal design) from function od.1 , od.2 , od.3 , od.4 , od.2m , od.3m , or od.4m .

rounded	Logical; round the values of p , $n/J/K$ that are from functions to two decimal places and integer, respectively if TRUE, no rounding if FALSE; default is TRUE.
verbose	Logical; print the value of relative precision and efficiency if TRUE, otherwise not; default is TRUE.

Value

Relative precision and efficiency value.

References

- (1) Shen, Z., & Kelcey, B. (2020). Optimal sample allocation under unequal costs in cluster-randomized trials. *Journal of Educational and Behavioral Statistics*, 45(4): 446–474. <<https://doi.org/10.3102/107699862091>>
- (2) Shen, Z., & Kelcey, B. (in press). Optimal sample allocation in multisite randomized trials. *The Journal of Experimental Education*. <<https://doi.org/10.1080/00220973.2020.1830361>>
- (3) Shen, Z., & Kelcey, B. (in press). Optimal sampling ratios in three-level multisite experiments. *Journal of Research on Educational Effectiveness*.

Examples

```
# Unconstrained optimal design of 2-level CRT #-----
myod1 <- od.2(icc = 0.2, r12 = 0.5, r22 = 0.5, c1 = 1, c2 = 5, c1t = 1, c2t = 50,
             varlim = c(0.01, 0.02))
# Constrained optimal design with n = 20
myod2 <- od.2(icc = 0.2, r12 = 0.5, r22 = 0.5, c1 = 1, c2 = 5, c1t = 1, c2t = 50,
             n = 20, varlim = c(0.005, 0.025))
# Relative precision and efficiency (RPE)
myrpe <- rpe(od = myod1, subod = myod2)
myrpe$out # RPE = 0.88
# Constrained optimal design with p = 0.5
myod2 <- od.2(icc = 0.2, r12 = 0.5, r22 = 0.5, c1 = 1, c2 = 5, c1t = 1, c2t = 50,
             p = 0.5, varlim = c(0.005, 0.025))
# Relative precision and efficiency (RPE)
mypre <- rpe(od = myod1, subod = myod2)
mypre$out # RPE = 0.90

# Unconstrained optimal design of 3-level CRT #-----
myod1 <- od.3(icc2 = 0.2, icc3 = 0.1, r12 = 0.5, r22 = 0.5, r32 = 0.5,
             c1 = 1, c2 = 5, c3 = 25, c1t = 1, c2t = 50, c3t = 250,
             varlim = c(0.005, 0.025))
# Constrained optimal design with J = 20
myod2 <- od.3(icc2 = 0.2, icc3 = 0.1, r12 = 0.5, r22 = 0.5, r32 = 0.5, J = 20,
             c1 = 1, c2 = 5, c3 = 25, c1t = 1, c2t = 50, c3t = 250,
             varlim = c(0, 0.025))
# Relative precision and efficiency (RPE)
myrpe <- rpe(od = myod1, subod = myod2)
myrpe$out # RPE = 0.53

# Unconstrained optimal design of 4-level CRT #-----
myod1 <- od.4(icc2 = 0.2, icc3 = 0.1, icc4 = 0.05, r12 = 0.5,
```

```
      r22 = 0.5, r32 = 0.5, r42 = 0.5,
      c1 = 1, c2 = 5, c3 = 25, c4 = 125,
      c1t = 1, c2t = 50, c3t = 250, c4t = 2500,
      varlim = c(0, 0.01))
# Constrained optimal design with p = 0.5
myod2 <- od.4(icc2 = 0.2, icc3 = 0.1, icc4 = 0.05, r12 = 0.5, p = 0.5,
             r22 = 0.5, r32 = 0.5, r42 = 0.5,
             c1 = 1, c2 = 5, c3 = 25, c4 = 125,
             c1t = 1, c2t = 50, c3t = 250, c4t = 2500,
             varlim = c(0, 0.01))
# Relative precision and efficiency (RPE)
myrpe <- rpe(od = myod1, subod = myod2)
myrpe$out # RPE = 0.78
```

Index

gen.design.pars, 3

od.1, 4, 27, 52, 53

od.2, 6, 29, 30, 52, 53

od.2.221, 8, 33

od.2m, 11, 35, 52, 53

od.3, 13, 38, 39, 52, 53

od.3m, 16, 42, 52, 53

od.4, 19, 36, 42, 45, 46, 50, 52, 53

od.4m, 23, 49, 52, 53

odr (odr-package), 2

odr-package, 2

power.1, 26

power.2, 28

power.2.221, 32

power.2m, 34

power.3, 37

power.3m, 41

power.4, 44

power.4m, 48

re, 51, 53

rpe, 52, 53