

# Package ‘rqPen’

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**Type** Package

**Title** Penalized Quantile Regression

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lifecycle, plyr

**RdMacros** Rdpack

**Suggests** splines, knitr

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## Description

Performs penalized quantile regression with LASSO, elastic net, SCAD and MCP penalty functions including group penalties. Provides a function that automatically generates lambdas and evaluates different models with cross validation or BIC, including a large p version of BIC.

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---

beta\_plots

*Plots of coefficients by lambda for cv.rq.group.pen and cv.rq.pen*


---

### Description

Warning: this function is deprecated and will not be exported in future versions.

### Usage

```
beta_plots(model, voi = NULL, logLambda = TRUE, loi = NULL, ...)
```

**Arguments**

model	cv.rq.pen or cv.rq.group.pen object
voi	Index of betas to include. Default is all of them.
logLambda	Plot of lambdas is on the log scale.
loi	Index of lambdas to use, default is all of them.
...	Additional arguments to be sent to plot()

**Value**

Plot of how beta estimates change with lambda.

**Author(s)**

Ben Sherwood, <ben.sherwood@ku.edu>

**Examples**

```
## Not run:
set.seed(1)
x <- matrix(rnorm(800),nrow=100)
y <- 1 + x[,1] - 3*x[,5] + rnorm(100)
lassoModels <- cv.rq.pen(x,y)
b_plot <- beta_plots(lassoModels)

## End(Not run)
```

---

bytau.plot

*Plot of how coefficients change with tau*


---

**Description**

Plot of how coefficients change with tau

**Usage**

```
bytau.plot(x, ...)
```

**Arguments**

x	A rq.pen.seq or rq.pen.seq.cv object.
...	Additional arguments see bytau.plot.rq.pen.seq() or bytau.plot.rq.pen.seq.cv() for more information.

**Value**

Returns the plot of how coefficients change with tau.

**Author(s)**

Ben Sherwood, <ben.sherwood@ku.edu>

---

bytau.plot.rq.pen.seq *Plot of how coefficients change with tau.*

---

**Description**

Plot of how coefficients change with tau.

**Usage**

```
## S3 method for class 'rq.pen.seq'  
bytau.plot(x, a = NULL, lambda = NULL, lambdaIndex = NULL, ...)
```

**Arguments**

x	An rq.pen.seq object
a	The tuning parameter a of interest
lambda	The lambda value of interest.
lambdaIndex	The lambda index of interest. Only specify lambdaIndex or lambda, not both.
...	Additional parameters sent to plot()

**Value**

A plot of coefficient values by tau.

**Author(s)**

Ben Sherwood, <ben.sherwood@ku.edu>

**Examples**

```
set.seed(1)  
x <- matrix(rnorm(800),nrow=100)  
y <- 1 + x[,1] - 3*x[,5] + rnorm(100)  
lassoModels <- rq.pen(x,y,tau=seq(.1,.9,.1))  
bytau.plot(lassoModels,lambda=lassoModels$lambda[5])
```

---

`bytau.plot.rq.pen.seq.cv`*Plot of coefficients varying by quantiles for rq.pen.seq.cv object*

---

**Description**

Produces plots of how coefficient estimates vary by quantile for models selected by using cross validation.

**Usage**

```
## S3 method for class 'rq.pen.seq.cv'  
bytau.plot(x, septau = TRUE, cvmin = TRUE, useDefaults = TRUE, ...)
```

**Arguments**

<code>x</code>	An <code>rq.pen.seq.cv</code> object
<code>septau</code>	Whether optimal tuning parameters are estimated separately for each quantile.
<code>cvmin</code>	Whether the minimum cv error should be used or the one standard error rule.
<code>useDefaults</code>	Set to <code>FALSE</code> if you want to use something besides minimum cv or 1se.
<code>...</code>	Additional parameters sent to <code>plot()</code>

**Value**

Returns plots of coefficient estimates varying by quantile.

**Author(s)**

Ben Sherwood, <ben.sherwood@ku.edu>

**Examples**

```
set.seed(1)  
x <- matrix(runif(800), nrow=100)  
y <- 1 + x[,1] - 3*x[,5] + (1+x[,4])*rnorm(100)  
lmcv <- rq.pen.cv(x,y,tau=seq(.1,.9,.1))  
bytau.plot(lmcv)
```

---

coef.cv.rq.group.pen    *Coefficients from a cv.rq.group.pen object*

---

### Description

Coefficients from a cv.rq.group.pen object

### Usage

```
## S3 method for class 'cv.rq.group.pen'
coef(object, lambda = "min", ...)
```

### Arguments

object	A cv.rq.group.pen object.
lambda	The lambda value, default is to use the one associated with the minimum cv error.
...	Additional parameters.

### Value

Vector of coefficients.

---

coef.cv.rq.pen    *Returns Coefficients of a cv.rq.pen object*

---

### Description

Warning: this function will be deprecated and not exported in future versions of rqPen, due to the switch from cv.rq.pen() to rq.pen.cv().

### Usage

```
## S3 method for class 'cv.rq.pen'
coef(object, lambda = "min", ...)
```

### Arguments

object	cv.rq.pen object
lambda	Value of lambda, default is to use the minimum value.
...	Additional parameters.

### Value

Coefficients for a given lambda, or the lambda associated with the minimum cv value.

**Author(s)**

Ben Sherwood, <ben.sherwood@ku.edu>

---

coef.rq.pen.seq      *Returns coefficients of a rq.pen.seq object*

---

**Description**

Returns coefficients of a rq.pen.seq object

**Usage**

```
## S3 method for class 'rq.pen.seq'
coef(
  object,
  tau = NULL,
  a = NULL,
  lambda = NULL,
  modelsIndex = NULL,
  lambdaIndex = NULL,
  ...
)
```

**Arguments**

object	rq.pen.seq object
tau	Quantile of interest. Default is NULL, which will return all quantiles. Should not be specified if modelsIndex is used.
a	Tuning parameter of a. Default is NULL, which returns coefficients for all values of a. Should not be specified if modelsIndex is used.
lambda	Tuning parameter of $\lambda$ . Default is NULL, which returns coefficients for all values of $\lambda$ .
modelsIndex	Index of the models for which coefficients should be returned. Does not need to be specified if tau or a are specified.
lambdaIndex	Index of the lambda values for which coefficients should be returned. Does not need to be specified if lambda is specified.
...	Additional parameters.

**Value**

A list of a matrix of coefficients for each tau and a combination

**Author(s)**

Ben Sherwood, <ben.sherwood@ku.edu>

**Examples**

```
x <- matrix(runif(800),ncol=8)
y <- 1 + x[,1] + x[,8] + (1+.5*x[,3])*rnorm(100)
m1 <- rq.pen(x,y,penalty="ENet",a=c(0,.5,1),tau=c(.25,.75),lambda=c(.1,.05,.01))
allCoefs <- coef(m1)
targetCoefs <- coef(m1,tau=.25,a=.5,lambda=.1)
idxApproach <- coef(m1,modelsIndex=2)
bothIdxApproach <- coef(m1,modelsIndex=2,lambdaIndex=1)
```

---

coef.rq.pen.seq.cv      *Returns coefficients from a rq.pen.seq.cv object.*

---

**Description**

Returns coefficients from a rq.pen.seq.cv object.

**Usage**

```
## S3 method for class 'rq.pen.seq.cv'
coef(object, septau = TRUE, cvmin = TRUE, useDefaults = TRUE, tau = NULL, ...)
```

**Arguments**

object	An rq.pen.seq.cv object.
septau	Whether tuning parameter should be optimized separately for each quantile.
cvmin	If TRUE then minimum error is used, if FALSE then one standard error rule is used.
useDefaults	Whether the default results are used. Set to FALSE if you you want to specify specific models and lambda values.
tau	Quantiles of interest.
...	Additional parameters sent to coef.rq.pen.seq()

**Value**

Returns coefficients

**Author(s)**

Ben Sherwood, <ben.sherwood@ku.edu>



**Examples**

```
## Not run:
set.seed(1)
x <- matrix(rnorm(800),nrow=100)
y <- 1 + x[,1] - 3*x[,5] + rnorm(100)
lassoModels <- rq.pen.cv(x,y,tau=seq(.1,.9,.1))
coefficients(lassoModels,septaui=FALSE)
coefficients(lassoModels,cvmin=FALSE)

## End(Not run)
```

---

cv.rq.group.pen

*Old cross validation function for group penalty*


---

**Description**

This function is deprecated. Recommend using `rq.group.pen.cv()` instead.

**Usage**

```
cv.rq.group.pen(
  x,
  y,
  groups,
  tau = 0.5,
  lambda = NULL,
  penalty = "SCAD",
  intercept = TRUE,
  criteria = "CV",
  cvFunc = "check",
  nfolds = 10,
  foldid = NULL,
  nlambda = 100,
  eps = 1e-04,
  init.lambda = 1,
  alg = "huber",
  penGroups = NULL,
  ...
)
```

**Arguments**

x	Matrix of predictors.
y	Vector of responses.
groups	Vector of groups.
tau	Quantile being modeled.

lambda	Vector of lambdas. Default is for lambdas to be automatically generated.
penalty	Type of penalty: "LASSO", "SCAD" or "MCP".
intercept	Whether model should include an intercept. Constant does not need to be included in "x".
criteria	How models will be evaluated. Either cross-validation "CV", BIC "BIC" or large P BIC "PBIC".
cvFunc	If cross-validation is used how errors are evaluated. Check function "check", "SqErr" (Squared Error) or "AE" (Absolute Value).
nfolds	K for K-folds cross-validation.
foldid	Group id for cross-validation. Function will randomly generate groups if not specified.
nlambda	Number of lambdas for which models are fit.
eps	Multiple of lambda max for Smallest lambda used.
init.lambda	Initial lambda used to find the maximum lambda. Not needed if lambda values are set.
alg	Algorithm used for fit. "QICD" or "LP".
penGroups	Specify which groups will be penalized. Default is to penalize all groups.
...	Additional arguments to be sent to rq.group.fit or groupQICDMultLambda.

## Value

Returns the following:

- beta Matrix of coefficients for different values of lambda
- residuals Matrix of residuals for different values of lambda.
- rhoVector of rho, unpenalized portion of the objective function, for different values of lambda.
- cv Data frame with "lambda" and second column is the evaluation based on the criteria selected.
- lambda.min Lambda which provides the smallest statistic for the selected criteria.
- penalty Penalty selected.
- intercept Whether intercept was included in model.
- groupsGroup structure for penalty function.

## References

- Yuan, M. and Lin, Y. (2006). Model selection and estimation in regression with grouped variables. *J. R. Statist. Soc. B*, **68**, 49-67.
- Peng, B. and Wang, L. (2015). An Iterative Coordinate Descent Algorithm for High-Dimensional Nonconvex Penalized Quantile Regression. *Journal of Computational and Graphical Statistics*, **24**, 676-694.

## Examples

```
## Not run:
x <- matrix(rnorm(800),nrow=100)
y <- 1 + x[,1] - 3*x[,5] + rnorm(100)
cv_model <- cv.rq.group.pen(x,y,groups=c(rep(1,4),rep(2,4)),criteria="BIC")

## End(Not run)
```

---

cv.rq.pen

*Cross Validated quantile regression*

---

## Description

Warning: this function is deprecated and will not be exported in future rqPen releases. Produces penalized quantile regression models for a range of lambdas and penalty of choice. If lambda is unselected than an iterative algorithm is used to find a maximum lambda such that the penalty is large enough to produce an intercept only model. Then range of lambdas goes from the maximum lambda found to "eps" on the log scale. For non-convex penalties local linear approximation approach used by Wang, Wu and Li to extend LLA as proposed by Zou and Li (2008) to the quantile regression setting.

## Usage

```
cv.rq.pen(
  x,
  y,
  tau = 0.5,
  lambda = NULL,
  weights = NULL,
  penalty = "LASSO",
  intercept = TRUE,
  criteria = "CV",
  cvFunc = "check",
  nfolds = 10,
  foldid = NULL,
  nlambda = 100,
  eps = 1e-04,
  init.lambda = 1,
  penVars = NULL,
  alg = ifelse(ncol(x) < 50, "LP", "QICD"),
  internal = FALSE,
  ...
)
```

**Arguments**

x	Matrix of predictors.
y	Numeric vector of response values.
tau	Conditional quantile being modelled.
lambda	Vector of lambdas. Default is for lambdas to be automatically generated.
weights	Weights for the objective function.
penalty	Type of penalty: "LASSO", "SCAD" or "MCP".
intercept	Whether model should include an intercept. Constant does not need to be included in "x".
criteria	How models will be evaluated. Either cross-validation "CV", BIC "BIC" or large P BIC "PBIC".
cvFunc	If cross-validation is used how errors are evaluated. Check function "check", "SqErr" (Squared Error) or "AE" (Absolute Value).
nfolds	K for K-folds cross-validation.
foldid	Group id for cross-validation. Function will randomly generate groups if not specified.
nlambda	Number of lambdas for which models are fit.
eps	Smallest lambda used.
init.lambda	Initial lambda used to find the maximum lambda. Not needed if lambda values are set.
penVars	Variables that should be penalized. With default value of NULL all variables are penalized.
alg	Algorithm that will be used, either linear programming (LP) or coordinate descent (QICD) algorithm from Peng and Wang (2015).
internal	If this is an internal call to this function.
...	Additional arguments to be sent to rq.lasso.fit or rq.nc.fit.

**Value**

Returns the following:

- modelsList of penalized models fit. Number of models will match number of lambdas and correspond to cv\$lambda.
- cvData frame with "lambda" and second column is the evaluation based on the criteria selected.
- lambda.minLambda which provides the smallest statistic for the selected criteria.
- penaltyPenalty selected.

**Author(s)**

Ben Sherwood, <ben.sherwood@ku.edu>

**Examples**

```
## Not run:
x <- matrix(rnorm(800),nrow=100)
y <- 1 + x[,1] - 3*x[,5] + rnorm(100)
cv_model <- cv.rq.pen(x,y)

## End(Not run)
```

---

cv\_plots

*Plots of cross validation results as a function of lambda.*

---

**Description**

Plots of cross validation results as a function of lambda.

**Usage**

```
cv_plots(model, logLambda = TRUE, loi = NULL, ...)
```

**Arguments**

model	A cv.rq.pen() object.
logLambda	Whether lambda values should be logged or not.
loi	Lambda indexes of interest, if null all lambda values will be used.
...	Additional parameters sent to plot function.

**Value**

returns a cross validation plot

**Author(s)**

Ben Sherwood, <ben.sherwood@ku.edu>

---

plot.cv.rq.group.pen    *Cross validation plot for cv.rq.group.pen object*

---

**Description**

Cross validation plot for cv.rq.group.pen object

**Usage**

```
## S3 method for class 'cv.rq.group.pen'  
plot(x, ...)
```

**Arguments**

x                    A cv.rq.group.pen object  
...                  Additional parameters for plot function.

**Value**

A cross validation plot.

---

plot.rq.pen.seq            *Plot of coefficients of rq.pen.seq object as a function of lambda*

---

**Description**

Plot of coefficients of rq.pen.seq object as a function of lambda

**Usage**

```
## S3 method for class 'rq.pen.seq'  
plot(  
  x,  
  vars = NULL,  
  logLambda = TRUE,  
  tau = NULL,  
  a = NULL,  
  lambda = NULL,  
  modelsIndex = NULL,  
  lambdaIndex = NULL,  
  main = NULL,  
  ...  
)
```

**Arguments**

x	rq.pen.seq object
vars	Variables of interest
logLambda	Whether lambda should be reported on the log scale
tau	Quantiles of interest
a	Tuning parameter a values of interest.
lambda	Values of lambda of interest.
modelsIndex	Specific models of interest.
lambdaIndex	Specific lambda values of interest.
main	Title of the plots. Can be a vector of multiple titles if multiple plots are created.
...	Additional arguments sent to plot

**Value**

Returns plot(s) of coefficients as they change with lambda.

**Author(s)**

Ben Sherwood, <ben.sherwood@ku.edu>

**Examples**

```
set.seed(1)
x <- matrix(rnorm(100*8),sd=10),ncol=8)
y <- 1 + x[,1] + 3*x[,3] - x[,8] + rt(100,3)
m1 <- rq.pen(x,y,tau=c(.1,.5,.7),penalty="SCAD",a=c(3,4))
plot(m1,a=3,tau=.7)
plot(m1)
m1list <- list()
for(i in 1:6){
m1list[[i]] <- paste("Plot",i)
}
plot(m1,main=m1list)
```

---

plot.rq.pen.seq.cv      *Plots cross validation results from a rq.pen.seq.cv object*

---

**Description**

Provides plots of cross-validation results by lambda. If septau is set to TRUE then plots the cross-validation results for each quantile. If septau is set to FALSE then provides one plot for cross-validation results across all quantiles.

**Usage**

```
## S3 method for class 'rq.pen.seq.cv'
plot(x, septau = TRUE, tau = NULL, logLambda = FALSE, main = NULL, ...)
```

**Arguments**

x	The rq.pen.seq.cv object
septau	If set to true then optimal tuning parameters are selected separately for each quantile and there will be a different plot for each quantile.
tau	Quantiles of interest.
logLambda	Whether log(lambda) is used for the x-axis
main	Title to the plot
...	Additional parameters sent to the plot function.

**Value**

Plots of the cross validation results by lambda.

**Author(s)**

Ben Sherwood, <ben.sherwood@ku.edu>

**Examples**

```
set.seed(1)
x <- matrix(rnorm(100*8),sd=1,ncol=8)
y <- 1 + x[,1] + 3*x[,3] - x[,8] + rt(100,3)
m1 <- rq.pen.cv(x,y,tau=c(.1,.3,.7))
plot(m1)
plot(m1,septau=FALSE)
```

---

predict.cv.rq.pen      *Prediction for a cv.rq.pen object*

---

**Description**

This function is deprecated and will not be exported in future versions.

**Usage**

```
## S3 method for class 'cv.rq.pen'
predict(object, newx, lambda = "lambda.min", ...)
```



**Arguments**

object	A cv.rq.pen object.
newx	Matrix of new data to make predictions with.
lambda	Lambda value used, default is the value associated with the minimum cross validation result.
...	Additional parameters that are currently ignored

**Value**

A vector of predictions.

---

predict.qic.select      *Predictions from a qic.select object*

---

**Description**

Predictions from a qic.select object

**Usage**

```
## S3 method for class 'qic.select'
predict(object, newdata, ...)
```

**Arguments**

object	qic.select object
newdata	Data matrix to make predictions from.
...	optional arguments

**Value**

A matrix of predicted values.

**Author(s)**

Ben Sherwood, <ben.sherwood@ku.edu>

**Examples**

```
x <- matrix(runif(800),ncol=8)
y <- 1 + x[,1] + x[,8] + (1+.5*x[,3])*rnorm(100)
m1 <- rq.pen(x,y,tau=c(.25,.75))
q1 <- qic.select(m1)
newx <- matrix(runif(80),ncol=8)
preds <- predict(q1,newx)
```

---

predict.rq.pen	<i>Prediction for a rq.pen object</i>
----------------	---------------------------------------

---

**Description**

This function is deprecated and will not be exported in future versions.

**Usage**

```
## S3 method for class 'rq.pen'
predict(object, newx, ...)
```

**Arguments**

object	An rq.pen object.
newx	Matrix of new data to make predictions with.
...	Additional parameters that are currently ignored

**Value**

A vector of predictions.

---

predict.rq.pen.seq	<i>Predictions from rq.pen.seq object</i>
--------------------	---

---

**Description**

Predictions from rq.pen.seq object

**Usage**

```
## S3 method for class 'rq.pen.seq'
predict(
  object,
  newx,
  tau = NULL,
  a = NULL,
  lambda = NULL,
  modelsIndex = NULL,
  lambdaIndex = NULL,
  ...
)
```

**Arguments**

object	rq.pen.seq object
newx	Matrix of predictors
tau	Quantile of interest. Default is NULL, which will return all quantiles. Should not be specified if modelsIndex is used.
a	Tuning parameter of a. Default is NULL, which returns coefficients for all values of a. Should not be specified if modelsIndex is used.
lambda	Tuning parameter of $\lambda$ . Default is NULL, which returns coefficients for all values of $\lambda$ .
modelsIndex	Index of the models for which coefficients should be returned. Does not need to be specified if tau or a are specified.
lambdaIndex	Index of the lambda values for which coefficients should be returned. Does not need to be specified if lambda is specified.
...	Additional parameters passed to coef.rq.pen.seq()

**Value**

A matrix of predictions for each tau and a combination

**Author(s)**

Ben Sherwood, <ben.sherwood@ku.edu>

**Examples**

```
x <- matrix(runif(800),ncol=8)
y <- 1 + x[,1] + x[,8] + (1+.5*x[,3])*rnorm(100)
m1 <- rq.pen(x,y,penalty="ENet",a=c(0,.5,1),tau=c(.25,.75),lambda=c(.1,.05,.01))
newx <- matrix(runif(80),ncol=8)
allCoefs <- predict(m1,newx)
targetCoefs <- predict(m1,newx,tau=.25,a=.5,lambda=.1)
idxApproach <- predict(m1,newx,modelsIndex=2)
bothIdxApproach <- predict(m1,newx,modelsIndex=2,lambdaIndex=1)
```

---

predict.rq.pen.seq.cv *Predictions from rq.pen.seq.cv object*

---

**Description**

Predictions from rq.pen.seq.cv object

**Usage**

```
## S3 method for class 'rq.pen.seq.cv'
predict(
  object,
  newx,
  tau = NULL,
  septau = TRUE,
  cvmin = TRUE,
  useDefaults = TRUE,
  ...
)
```

**Arguments**

object	rq.pen.seq.cv object
newx	Matrix of predictors
tau	Quantile of interest. Default is NULL, which will return all quantiles. Should not be specified if modelsIndex is used.
septau	Whether tuning parameter should be optimized separately for each quantile.
cvmin	If TRUE then minimum error is used, if FALSE then one standard error rule is used.
useDefaults	Whether the default results are used. Set to FALSE if you you want to specify specific models and lambda values.
...	Additional parameters sent to coef.rq.pen.seq.cv().

**Value**

A matrix of predictions for each tau and a combination

**Author(s)**

Ben Sherwood, <ben.sherwood@ku.edu>

**Examples**

```
x <- matrix(runif(1600),ncol=8)
y <- 1 + x[,1] + x[,8] + (1+.5*x[,3])*rnorm(200)
m1 <- rq.pen.cv(x,y,penalty="ENet",a=c(0,.5,1),tau=c(.25,.75),lambda=c(.1,.05,.01))
newx <- matrix(runif(80),ncol=8)
cvpreds <- predict(m1,newx)
```

---

print.cv.rq.pen      *Prints a cv.rq.pen object.*

---

### Description

Warning: this function is deprecated and will not be exported in future releases.

### Usage

```
## S3 method for class 'cv.rq.pen'  
print(x, ...)
```

```
## S3 method for class 'cv.rq.pen'  
print(x, ...)
```

### Arguments

x                    A cv.rq.pen object  
...                  Additional arguments

### Details

Warning this function is deprecated and will not be exported in future releases.

### Value

Prints cross validation or information criterion values by lambda.

Prints coefficients and cross validation results.

### Author(s)

Ben Sherwood, <ben.sherwood@ku.edu>

---

print.qic.select      *Print a qic.select object*

---

### Description

Print a qic.select object

### Usage

```
## S3 method for class 'qic.select'  
print(x, ...)
```

**Arguments**

x                    qic.select object  
...                   optional arguments

**Value**

Prints the coefficients of the qic.select object

**Author(s)**

Ben Sherwood, <ben.sherwood@ku.edu>

---

print.rq.pen                    *Prints an rq.pen object*

---

**Description**

Warning this function is deprecated and will not be exported in future releases.

**Usage**

```
## S3 method for class 'rq.pen'  
print(x, ...)
```

```
## S3 method for class 'rq.pen'  
print(x, ...)
```

**Arguments**

x                    A rq.pen object  
...                   Additional arguments

**Value**

Prints the coefficients of the object.

**Author(s)**

Ben Sherwood, <ben.sherwood@ku.edu>

---

```
print.rq.pen.seq      Print a rq.pen.seq object
```

---

**Description**

Print a rq.pen.seq object

**Usage**

```
## S3 method for class 'rq.pen.seq'
print(x, ...)
```

**Arguments**

x	rq.pen.seq object
...	optional arguments

**Value**

If only one model, prints a data.frame of the number of nonzero coefficients and lambda. Otherwise prints information about the quantiles being modeled and choices for a.

**Author(s)**

Ben Sherwood, <ben.sherwood@ku.edu>

---

```
print.rq.pen.seq.cv  Prints a rq.pen.seq.cv object
```

---

**Description**

Prints a rq.pen.seq.cv object

**Usage**

```
## S3 method for class 'rq.pen.seq.cv'
print(x, ...)
```

**Arguments**

x	A req.pen.seq.cv object.
...	Additional arguments.

**Value**

Print of btr and gtr from a rq.pen.seq.cv object. If only one quantile is modeled then only btr is returned.

---

qic	<i>Calculate information criterion for penalized quantile regression models</i>
-----	---

---

**Description**

Calculate information criterion for penalized quantile regression models

**Usage**

```
qic(model, n, method = c("BIC", "AIC", "PBIC"))
```

**Arguments**

model	model from a rq.pen.seq() object
n	Sample size
method	Choice of BIC, AIC or PBIC, a large p BIC.

**Value**

Let  $\hat{\beta}$  be the coefficient vectors for the estimated model. Function returns the value

$$\log\left(\sum_{i=1}^n \rho_{\tau}(y_i - x_i^{\top} \hat{\beta})\right) + d * b / (2n),$$

where d is the number of nonzero coefficients and b depends on the method used. For AIC  $b = 2$ , for BIC  $b = \log(n)$  and for PBIC  $b = \log(n) * \log(p)$  where p is the dimension of  $\hat{\beta}$ . Returns this value for each coefficient vector in the model, so one for every value of  $\lambda$ .

**Author(s)**

Ben Sherwood, <ben.sherwood@ku.edu>

**References**

Lee ER, Noh H, Park BU (2014). "Model Selection via Bayesian Information Criterion for Quantile Regression Models." *Journal of the American Statistical Association*, **109**(505), 216–229. ISSN 01621459.

**Examples**

```
set.seed(1)
x <- matrix(runif(800), ncol=8)
y <- 1 + x[,1] + x[,8] + (1+.5*x[,3])*rnorm(100)
m1 <- rq.pen(x,y,tau=c(.25,.75))
# returns the IC values for tau=.25
qic(m1$models[[1]],m1$n)
# returns the IC values for tau=.75
qic(m1$models[[2]],m1$n)
```



---

qic.select                      *Select tuning parameters using IC*

---

**Description**

Select tuning parameters using IC

**Usage**

```
qic.select(obj, ...)
```

**Arguments**

obj                      A rq.pen.seq or rq.pen.seq.cv object.  
 ...                      Additional arguments see qic.select.rq.pen.seq() or qic.select.rq.pen.seq.cv() for more information.

**Value**

Returns the plot of how coefficients change with tau.

**Author(s)**

Ben Sherwood, <ben.sherwood@ku.edu>

---

qic.select.rq.pen.seq    *Select tuning parameters using IC*

---

**Description**

Selects tuning parameter  $\lambda$  and  $a$  according to information criterion of choice. For a given  $\hat{\beta}$  the information criterion is calculated as

$$\log\left(\sum_{i=1}^n \rho_{\tau}(y_i - x_i^{\top} \hat{\beta})\right) + d * b / (2n),$$

where  $d$  is the number of nonzero coefficients and  $b$  depends on the method used. For AIC  $b = 2$ , for BIC  $b = \log(n)$  and for PBIC  $d = \log(n) * \log(p)$  where  $p$  is the dimension of  $\hat{\beta}$ . If `septa` set to `FALSE` then calculations are made across the quantiles. Let  $\hat{\beta}^q$  be the coefficient vector for the  $q$ th quantile of  $Q$  quantiles. In addition let  $d_q$  and  $b_q$  be  $d$  and  $b$  values from the  $q$ th quantile model. Note, for all of these we are assuming  $eqn$  and  $a$  are the same. Then the summary across all quantiles is

$$\sum_{q=1}^Q w_q \left[ \log\left(\sum_{i=1}^n \rho_{\tau}(y_i - x_i^{\top} \hat{\beta}^q)\right) + d_q * b_q / (2n) \right],$$

where  $w_q$  is the weight assigned for the  $q$ th quantile model.

**Usage**

```
## S3 method for class 'rq.pen.seq'
qic.select(
  obj,
  method = c("BIC", "AIC", "PBIC"),
  septau = TRUE,
  weights = NULL,
  ...
)
```

**Arguments**

obj	A rq.pen.seq or rq.pen.seq.cv object.
method	Choice of BIC, AIC or PBIC, a large p BIC.
septau	If optimal values of $\lambda$ and $a$ can vary with $\tau$ . Default is TRUE.
weights	Weights for each quantile. Useful if you set septau to FALSE but want different weights for the different quantiles. If not specified default is to have $w_q = 1$ for all quantiles.
...	Additional arguments.

**Value**

- coefficients Coefficients of the selected models.
- ic Information criterion values for all considered models.
- models Info Model info for the selected models related to the original object obj.
- gic Information criterion summarized across all quantiles. Only returned if septau set to FALSE

**Author(s)**

Ben Sherwood, <ben.sherwood@ku.edu>

**References**

Lee ER, Noh H, Park BU (2014). "Model Selection via Bayesian Information Criterion for Quantile Regression Models." *Journal of the American Statistical Association*, **109**(505), 216–229. ISSN 01621459.

**Examples**

```
set.seed(1)
x <- matrix(runif(800), ncol=8)
y <- 1 + x[,1] + x[,8] + (1+.5*x[,3])*rnorm(100)
m1 <- rq.pen(x,y,penalty="ENet",a=c(0,.5,1),tau=c(.25,.75))
qic.select(m1)
```

---

qic.select.rq.pen.seq.cv

*Select tuning parameters using IC*


---

## Description

Selects tuning parameter  $\lambda$  and  $a$  according to information criterion of choice. For a given  $\hat{\beta}$  the information criterion is calculated as

$$\log\left(\sum_{i=1}^n \rho_{\tau}(y_i - x_i^{\top} \hat{\beta})\right) + d * b / (2n),$$

where  $d$  is the number of nonzero coefficients and  $b$  depends on the method used. For AIC  $b = 2$ , for BIC  $b = \log(n)$  and for PBIC  $b = \log(n) * \log(p)$  where  $p$  is the dimension of  $\hat{\beta}$ . If `septau` set to `FALSE` then calculations are made across the quantiles. Let  $\hat{\beta}^q$  be the coefficient vector for the  $q$ th quantile of  $Q$  quantiles. In addition let  $d_q$  and  $b_q$  be  $d$  and  $b$  values from the  $q$ th quantile model. Note, for all of these we are assuming eqn and  $a$  are the same. Then the summary across all quantiles is

$$\sum_{q=1}^Q w_q \left[ \log\left(\sum_{i=1}^n \rho_{\tau}(y_i - x_i^{\top} \hat{\beta}^q)\right) + d_q * b_q / (2n) \right],$$

where  $w_q$  is the weight assigned for the  $q$ th quantile model.

## Usage

```
## S3 method for class 'rq.pen.seq.cv'
qic.select(
  obj,
  method = c("BIC", "AIC", "PBIC"),
  septau = TRUE,
  weights = NULL,
  ...
)
```

## Arguments

<code>obj</code>	A <code>rq.pen.seq.cv</code> object.
<code>method</code>	Choice of BIC, AIC or PBIC, a large $p$ BIC.
<code>septau</code>	If optimal values of $\lambda$ and $a$ can vary with $\tau$ . Default is <code>TRUE</code> .
<code>weights</code>	Weights for each quantile. Useful if you set <code>septau</code> to <code>FALSE</code> but want different weights for the different quantiles. If not specified default is to have $w_q = 1$ for all quantiles.
<code>...</code>	Additional arguments.

**Value**

- coefficients Coefficients of the selected models.
- ic Information criterion values for all considered models.
- modelsInfo Model info for the selected models related to the original object obj.
- gic Information criterion summarized across all quantiles. Only returned if `septa` set to `FALSE`

**Author(s)**

Ben Sherwood, <ben.sherwood@ku.edu>

**References**

Lee ER, Noh H, Park BU (2014). “Model Selection via Bayesian Information Criterion for Quantile Regression Models.” *Journal of the American Statistical Association*, **109**(505), 216–229. ISSN 01621459.

**Examples**

```
set.seed(1)
x <- matrix(runif(800), ncol=8)
y <- 1 + x[,1] + x[,8] + (1+.5*x[,3])*rnorm(100)
m1 <- rq.pen.cv(x,y,penalty="ENet",a=c(0,.5,1),tau=c(.25,.75))
qic.select(m1)
```

---

QICD

*Implements QICD algorithm*

---

**Description**

Implements QICD algorithm

**Usage**

```
QICD(
  y,
  x,
  tau = 0.5,
  lambda,
  intercept = TRUE,
  penalty = "SCAD",
  initial_beta = NULL,
  maxin = 100,
  maxout = 20,
  eps = 1e-05,
  coef.cutoff = 1e-08,
  a = 3.7,
```

```

    scalex = TRUE,
    ...
)

```

### Arguments

y	response variable, length n vector
x	input nxp matrix, of dimension nobs x nvars; each row is an observation vector.
tau	the quantile value
lambda	the tuning parameter (numeric value > 0)
intercept	a logical value, should intercept be fitted (default=TRUE) (intercept should be included when using splines)
penalty	The name of the penalty function ("SCAD", "MCP", "LASSO")
initial_beta	Vector containing initial values for intercept (if included) and x coefficients. Should be in the form (intercept, coefficients) intercept should be left out if intercept=FALSE.
maxin	maximum number of iterations for inside coordinate descent, default value is 100
maxout	maximum number of iterations for outside MM step, default value is 20
eps	The convergence threshold for coordinate descent and majorization minimization step
coef.cutoff	Threshold for determining nonzero coefficients
a	Scale parameter, the default value is 3.7 (>2 for SCAD, >1 for MCP, not used in LASSO)
scalex	Whether predictors are centered and scaled
...	additional parameters

---

QICD.nonpen

*Implements QICD algorithm with some variables not being penalized*

---

### Description

Implements QICD algorithm with some variables not being penalized

### Usage

```

QICD.nonpen(
  y,
  x,
  z,
  tau = 0.5,
  lambda,
  intercept = TRUE,
  penalty = "SCAD",

```

```

initial_beta = NULL,
maxin = 100,
maxout = 20,
eps = 1e-05,
coef.cutoff = 1e-08,
a = 3.7,
method = "br",
scalex = TRUE,
...
)

```

### Arguments

y	response variable, length n vector
x	input nxp matrix, of dimension nobs x nvars; each row is an observation vector.
z	nxq matrix of bases; the coefficients for these columns will be unpenalized
tau	the quantile value
lambda	the tuning parameter (numeric value > 0)
intercept	a logical value, should intercept be fitted (default=TRUE) (intercept should be included when using splines)
penalty	The name of the penalty function ("SCAD", "MCP", "LASSO")
initial_beta	Vector containing initial values for intercept (if included) and x coefficients. Should be in the form (intercept, coefficients) intercept should be left out if intercept=FALSE. The intercept should be included to be consistent with other methods, but intercept and z coefficients will be initialized to by a rq() fit of residuals from initial beta against the unpenalized predictors, z.
maxin	maximum number of iterations for inside coordinate descent, default value is 100
maxout	maximum number of iterations for outside MM step, default value is 20
eps	The convergence threshold for coordinate descent and majorization minimization step
coef.cutoff	Threshold for determining nonzero coefficients
a	Scale parameter, the default value is 3.7 (>2 for SCAD, >1 for MCP, not used in LASSO)
method	quantile regression initialization method, can be "br" or "fn".
scalex	Whether predictors are centered and scaled
...	additional parameters

---

rq.group.fit	<i>Estimates a quantile regression model with a group penalized objective function.</i>
--------------	---

---

### Description

Warning: function is deprecated and will not be exported in future R packages. Recommend using `rq.group.pen()` instead. Similar to `cv.rq.pen` function, but uses group penalty. Group penalties use the L1 norm instead of L2 for computational convenience. As a result of this the group lasso penalty is the same as the typical lasso penalty and thus you should only use a SCAD or MCP penalty. Only the SCAD and MCP penalties incorporate the group structure into the penalty. The group lasso penalty is implemented because it is needed for the SCAD and MCP algorithm. We use a group penalty extension of the QICD algorithm presented by Peng and Wang (2015).

### Usage

```
rq.group.fit(
  x,
  y,
  groups,
  tau = 0.5,
  lambda,
  intercept = TRUE,
  penalty = "SCAD",
  alg = "QICD",
  a = 3.7,
  penGroups = NULL,
  ...
)
```

### Arguments

x	Matrix of predictors.
y	Vector of responses.
groups	Vector of group assignments.
tau	Single quantile to be modeled.
lambda	Single value or separate value for each group.
intercept	Whether intercept should be included in the model or not.
penalty	Type of penalty used: SCAD, MCP or LASSO.
alg	Type of algorithm used: QICD or LP.
a	Additional tuning parameter for SCAD and MCP.
penGroups	Vector of TRUE and FALSE entries for each group determining if they should be penalized. Default is TRUE for all groups.
...	Additional arguments sent to <code>rq.group.lin.prog()</code>

**Value**

Returns the following:

- coefficients Coefficients of the model.
- residuals Residuals from the fitted model.
- rho Unpenalized portion of the objective function.
- tau Quantile being modeled.
- n Sample size.
- intercept Whether intercept was included in model.

**Author(s)**

Ben Sherwood, <ben.sherwood@ku.edu> and Adam Maidman

**References**

- Yuan, M. and Lin, Y. (2006). Model selection and estimation in regression with grouped variables. *J. R. Statist. Soc. B*, **68**, 49-67.
- Peng, B. and Wang, L. (2015). An Iterative Coordinate Descent Algorithm for High-Dimensional Nonconvex Penalized Quantile Regression. *Journal of Computational and Graphical Statistics*, **24**, 676-694.

---

rq.group.pen

*Fits quantile regression models using a group penalized objective function.*

---

**Description**

Let the predictors be divided into  $G$  groups with  $G$  corresponding vectors of coefficients,  $\beta_1, \dots, \beta_G$ . Let  $\rho_\tau(a) = a[\tau - I(a < 0)]$ . Fits quantile regression models for  $Q$  quantiles by minimizing the penalized objective function of

$$\sum_{q=1}^Q \frac{1}{n} \sum_{i=1}^n \rho_\tau(y_i - x_i^\top \beta^q) + \sum_{q=1}^Q \sum_{g=1}^G P(\|\beta_g^q\|_k, w_q * v_j * \lambda, a).$$

Where  $w_q$  and  $v_j$  are designated by `penalty.factor` and `tau.penalty.factor` respectively. The value of  $k$  is chosen by `norm`. Value of  $P()$  depends on the penalty. Briefly, but see references or vignette for more details,

- Group LASSO (gLASSO)  $P(\|\beta\|_k, \lambda, a) = \lambda \|\beta\|_k$
- Group SCAD  $P(\|\beta\|_k, \lambda, a) = SCAD(\|\beta\|_k, \lambda, a)$
- Group MCP  $P(\|\beta\|_k, \lambda, a) = MCP(\|\beta\|_k, \lambda, a)$
- Group Adaptive LASSO  $P(\|\beta\|_k, \lambda, a) = \frac{\lambda \|\beta\|_k}{|\beta_0|^\alpha}$



Note if  $k = 1$  and the group lasso penalty is used then this is identical to the regular lasso and thus function will stop and suggest that you use `rq.pen()` instead. For Adaptive LASSO the values of  $\beta_0$  come from a Ridge solution with the same value of  $\lambda$ . If the Huber algorithm is used than  $\rho_\tau(y_i - x_i^\top \beta)$  is replaced by a Huber-type approximation. Specifically, it is replaced by  $h_\gamma^\tau(y_i - x_i^\top \beta)/2$  where

$$h_\gamma^\tau(a) = a^2/(2\gamma)I(|a| \leq \gamma) + (|a| - \gamma/2)I(|a| > \gamma) + (2\tau - 1)a.$$

Where if  $\tau = .5$ , we get the usual Huber loss function.

## Usage

```
rq.group.pen(
  x,
  y,
  tau = 0.5,
  groups = 1:ncol(x),
  penalty = c("gLASSO", "gAdLASSO", "gSCAD", "gMCP"),
  lambda = NULL,
  nlambda = 100,
  eps = ifelse(nrow(x) < ncol(x), 0.05, 0.01),
  alg = c("huber", "br", "qicd"),
  a = NULL,
  norm = 2,
  group.pen.factor = rep(1, length(unique(groups))),
  tau.penalty.factor = rep(1, length(tau)),
  scalex = TRUE,
  coef.cutoff = 1e-08,
  max.iter = 10000,
  converge.eps = 1e-07,
  gamma = IQR(y)/10,
  lambda.discard = TRUE,
  ...
)
```

## Arguments

<code>x</code>	Matrix of predictors.
<code>y</code>	Vector of responses.
<code>tau</code>	Vector of quantiles.
<code>groups</code>	Vector of group assignments for predictors.
<code>penalty</code>	Penalty used, choices are group lasso ("gLASSO"), group adaptive lasso ("gAdLASSO"), group SCAD ("gSCAD") and group MCP ("gMCP")
<code>lambda</code>	Vector of lambda tuning parameters. Will be automatically generated if it is not set.
<code>nlambda</code>	The number of lambda tuning parameters.
<code>eps</code>	The value to be multiplied by the largest lambda value to determine the smallest lambda value.

<code>alg</code>	Algorithm used. Choices are Huber approximation ("huber"), linear programming ("lp") or quantile iterative coordinate descent ("qicd").
<code>a</code>	The additional tuning parameter for adaptive lasso, SCAD and MCP.
<code>norm</code>	Whether a L1 or L2 norm is used for the grouped coefficients.
<code>group.pen.factor</code>	Penalty factor for each group.
<code>tau.penalty.factor</code>	Penalty factor for each quantile.
<code>scalex</code>	Whether $X$ should be centered and scaled so that the columns have mean zero and standard deviation of one. If set to TRUE, the coefficients will be returned to the original scale of the data.
<code>coef.cutoff</code>	Coefficient cutoff where any value below this number is set to zero. Useful for the lp algorithm, which are prone to finding almost, but not quite, sparse solutions.
<code>max.iter</code>	The maximum number of iterations for the algorithm.
<code>converge.eps</code>	The convergence criteria for the algorithms.
<code>gamma</code>	The tuning parameter for the Huber loss.
<code>lambda.discard</code>	Whether lambdas should be discarded if for small values of lambda there is very little change in the solutions.
<code>...</code>	Additional parameters

### Value

An `rq.pen.seq` object.

- `models`A list of each model fit for each tau and a combination.
- `nSample` size.
- `pNumber` of predictors.
- `alg`Algorithm used.
- `tau`Quantiles modeled.
- `penalty`Penalty used.
- `a`Tuning parameters a used.
- `lambda`Lambda values used for all models. If a model has fewer coefficients than lambda, say k. Then it used the first k values of lambda. Setting `lambda.discard` to TRUE will gurantee all values use the same lambdas, but may increase computational time noticeably and for little gain.
- `modelsInfo`Information about the quantile and a value for each model.
- `call`Original call.

Each model in the `models` list has the following values.

- `coefficients`Coefficients for each value of lambda.
- `rho`The unpenalized objective function for each value of lambda.

- PenRhoThe penalized objective function for each value of lambda.
- nzeroThe number of nonzero coefficients for each value of lambda.
- tauQuantile of the model.
- aValue of a for the penalized loss function.

### Author(s)

Ben Sherwood, <ben.sherwood@ku.edu>, Shaobo Li <shaobo.li@ku.edu> and Adam Maidman

### References

Peng B, Wang L (2015). “An iterative coordinate descent algorithm for high-dimensional nonconvex penalized quantile regression.” *J. Comput. Graph. Statist.*, **24**(3), 676-694.

### Examples

```
## Not run:
set.seed(1)
x <- matrix(rnorm(200*8),sd=1,ncol=8)
y <- 1 + x[,1] + 3*x[,3] - x[,8] + rt(200,3)
g <- c(1,1,1,2,2,2,3,3)
tvals <- c(.25,.75)
r1 <- rq.group.pen(x,y,groups=g)
r5 <- rq.group.pen(x,y,groups=g,tau=tvals)
#Linear programming approach with group SCAD penalty and L1-norm
m2 <- rq.group.pen(x,y,groups=g,alg="br",penalty="gSCAD",norm=1,a=seq(3,4))
# No penalty for the first group
m3 <- rq.group.pen(x,y,groups=g,group.pen.factor=c(0,rep(1,2)))
# Smaller penalty for the median
m4 <- rq.group.pen(x,y,groups=g,tau=c(.25,.5,.75),tau.penalty.factor=c(1,.25,1))

## End(Not run)
```

---

rq.group.pen.cv      *Performs cross validation for a group penalty. #'*

---

### Description

Performs cross validation for a group penalty. #'

### Usage

```
rq.group.pen.cv(
  x,
  y,
  tau = 0.5,
  groups = 1:ncol(x),
  lambda = NULL,
```

```

a = NULL,
cvFunc = NULL,
nfolds = 10,
foldid = NULL,
groupError = TRUE,
cvSummary = mean,
tauWeights = rep(1, length(tau)),
printProgress = FALSE,
...
)

```

### Arguments

x	Matrix of predictors.
y	Vector of responses.
tau	Vector of quantiles.
groups	Vector of group assignments for the predictors.
lambda	Vector of lambda values, if set to NULL they will be generated automatically.
a	Vector of the other tuning parameter values.
cvFunc	Function used for cross-validation error, default is quantile loss.
nfolds	Number of folds used for cross validation.
foldid	Fold assignments, if not set this will be randomly created.
groupError	If errors are to be reported as a group or as the average for each fold.
cvSummary	The
tauWeights	Weights for the tau penalty.
printProgress	If set to TRUE will print which fold the process is working on.
...	Additional parameters that will be sent to rq.group.pen().

### Value

- `cverrMatrix` of `cvSummary` function, default is average, cross-validation error for each model, tau and a combination, and lambda.
- `cvseMatrix` of the standard error of `cverr` foreach model, tau and a combination, and lambda.
- `fit` The `rq.pen.seq` object fit to the full data.
- `btrA` data.table of the values of a and lambda that are best as determined by the minimum cross validation error and the one standard error rule, which fixes a. In `btr` the values of lambda and a are selected separately for each quantile.
- `gtrA` data.table for the combination of a and lambda that minimize the cross validation error across all tau.
- `gcveGroup`, across all quantiles, cross-validation error results for each value of a and lambda.
- `callOriginal` call to the function.

**Author(s)**

Ben Sherwood, <ben.sherwood@ku.edu> and Shaobo Li <shaobo.li@ku.edu>

**Examples**

```
set.seed(1)
x <- matrix(rnorm(100*8),sd=1,ncol=8)
y <- 1 + x[,1] + 3*x[,3] - x[,8] + rt(100,3)
g <- c(1,1,1,1,2,2,3,3)
tvals <- c(.25,.75)
## Not run:
m1 <- rq.group.pen.cv(x,y,tau=c(.1,.3,.7),groups=g)
m2 <- rq.group.pen.cv(x,y,penalty="gAdLASSO",tau=c(.1,.3,.7),groups=g)
m3 <- rq.group.pen.cv(x,y,penalty="gSCAD",tau=c(.1,.3,.7),a=c(3,4,5),groups=g)
m4 <- rq.group.pen.cv(x,y,penalty="gMCP",tau=c(.1,.3,.7),a=c(3,4,5),groups=g)

## End(Not run)
```

---

rq.lasso.fit

*Estimates a quantile regression model with a lasso penalized quantile loss function.*

---

**Description**

Fits a quantile regression model with the LASSO penalty. Uses the augmented data approach similar to the proposal in Sherwood and Wang (2016).

**Usage**

```
rq.lasso.fit(
  x,
  y,
  tau = 0.5,
  lambda = NULL,
  weights = NULL,
  intercept = TRUE,
  coef.cutoff = 1e-08,
  method = "br",
  penVars = NULL,
  scalex = TRUE,
  lambda.discard = TRUE,
  ...
)
```

**Arguments**

x	Matrix of predictors.
y	Vector of responses.
tau	Quantile of interest.
lambda	Tuning parameter.
weights	Weights for the objective function.
intercept	Whether model should include an intercept. Constant does not need to be included in "x".
coef.cutoff	Coefficients below this value will be set to zero.
method	Use method "br" or "fn" as outlined in quantreg package. We have found "br" to be more stable for penalized regression problems.
penVars	Variables that should be penalized. With default value of NULL all variables are penalized.
scalex	If set to true the predictors will be scaled to have mean zero and standard deviation of one before fitting the model. The output returned will be on the original scale of the data.
lambda.discard	If TRUE lambda sequence will stop early if for small values of lambda the estimates do not change much.
...	Additional items to be sent to rq. Note this will have to be done carefully as rq is run on the augmented data to account for penalization and could provide strange results if this is not taken into account.

**Value**

Returns the following:

- coefficients Coefficients from the penalized model.
- PenRho Penalized objective function value.
- residuals Residuals from the model.
- rho Objective function evaluation without the penalty.
- tau Conditional quantile being modeled.
- n Sample size.

**References**

- Tibshirani, R. (1996). Regression shrinkage and selection via the lasso. *Journal of the Royal Statistical Society. Series B*, **58**, 267–288.
- Wu, Y. and Liu, Y. (2009). Variable selection in quantile regression. *Statistica Sinica*, **19**, 801–817.
- Sherwood, B. and Wang, L. (2016) Partially linear additive quantile regression in ultra-high dimension. *Annals of Statistics* **44**, 288–317.

**Examples**

```
x <- matrix(rnorm(800),nrow=100)
y <- 1 + x[,1] - 3*x[,5] + rnorm(100)
lassoModel <- rq.lasso.fit(x,y,lambda=.1)
```

rq.nc.fit

*Non-convex penalized quantile regression***Description**

Warning: this function is deprecated and will not be exported in future releases. Produces penalized quantile regression models for a range of lambdas and penalty of choice. If lambda is unselected than an iterative algorithm is used to find a maximum lambda such that the penalty is large enough to produce an intercept only model. Then range of lambdas goes from the maximum lambda found to "eps" on the log scale. Local linear approximation approach used by Wang, Wu and Li to extend LLA as proposed by Zou and Li (2008) to the quantile regression setting.

**Usage**

```
rq.nc.fit(
  x,
  y,
  tau = 0.5,
  lambda = NULL,
  weights = NULL,
  intercept = TRUE,
  penalty = "SCAD",
  a = 3.7,
  iterations = 1,
  converge_criteria = 1e-06,
  alg = ifelse(p < 50, "LP", "QICD"),
  penVars = NULL,
  internal = FALSE,
  ...
)
```

**Arguments**

x	Matrix of predictors.
y	Vector of response values.
tau	Conditional quantile being modelled.
lambda	Vector of lambdas. Default is for lambdas to be automatically generated.
weights	Weights for the objective function.
intercept	Whether model should include an intercept. Constant does not need to be included in "x".

penalty	Type of penalty: "LASSO", "SCAD" or "MCP".
a	Additional tuning parameter for SCAD and MCP
iterations	Number of iterations to be done for iterative LLA algorithm.
converge_criteria	Difference in betas from iteration process that would satisfy convergence.
alg	Defaults for small p to linear programming (LP), see Wang, Wu and Li (2012) for details. Otherwise a coordinate descent algorithm is used (QICD), see Peng and Wang (2015) for details. Both methods rely on the One-step sparse estimates algorithm.
penVars	Variables that should be penalized. With default value of NULL all variables are penalized.
internal	Whether call to this function has been made internally or not.
...	Additional items to be sent to rq.lasso.fit.

### Value

Returns the following:

- coefficients Coefficients from the penalized model.
- PenRho Penalized objective function value.
- residuals Residuals from the model.
- rho Objective function evaluation without the penalty.
- coefficients Coefficients from the penalized model.
- tau Conditional quantile being modeled.
- n Sample size.
- penalty Penalty used, SCAD or MCP.
- penalty Penalty selected.

### Author(s)

Ben Sherwood, <ben.sherwood@ku.edu> and Adam Maidman.

### References

- Wang, L., Wu, Y. and Li, R. (2012). Quantile regression of analyzing heterogeneity in ultra-high dimension. *J. Am. Statist. Ass.*, **107**, 214–222.
- Wu, Y. and Liu, Y. (2009). Variable selection in quantile regression. *Statistica Sinica*, **19**, 801–817.
- Zou, H. and Li, R. (2008). One-step sparse estimates in nonconcave penalized likelihood models. *Ann. Statist.*, **36**, 1509–1533.
- Peng, B. and Wang, L. (2015). An iterative coordinate-descent algorithm for high-dimensional nonconvex penalized quantile regression. *J. Comp. Graph.*, **24**, 676–694.



**Examples**

```
x <- matrix(rnorm(800),nrow=100)
y <- 1 + x[,1] - 3*x[,5] + rnorm(100)
scadModel <- rq.nc.fit(x,y,lambda=1)
```

---

rq.pen	<i>Fit a quantile regression model using a penalized quantile loss function.</i>
--------	--

---

**Description**

Let  $q$  index the  $Q$  quantiles of interest. Let  $\rho_\tau(a) = a[\tau - I(a < 0)]$ . Fits quantile regression models by minimizing the penalized objective function of

$$\frac{1}{n} \sum_{q=1}^Q \sum_{i=1}^n \rho_\tau(y_i - x_i^\top \beta^q) + \sum_{q=1}^Q \sum_{j=1}^p P(\beta_p^q, w_q * v_j * \lambda, a).$$

Where  $w_q$  and  $v_j$  are designated by `penalty.factor` and `tau.penalty.factor` respectively. Value of  $P()$  depends on the penalty. See references or vignette for more details,

- LASSO:  $P(\beta, \lambda, a) = \lambda|\beta|$
- SCAD:  $P(\beta, \lambda, a) = SCAD(\beta, \lambda, a)$
- MCP:  $P(\beta, \lambda, a) = MCP(\beta, \lambda, a)$
- Ridge:  $P(\beta, \lambda, a) = \lambda\beta^2$
- Elastic Net:  $P(\beta, \lambda, a) = a * \lambda|\beta| + (1 - a) * \lambda * \beta^2$
- Adaptive LASSO:  $P(\beta, \lambda, a) = \frac{\lambda|\beta|}{|\beta_0|^a}$

For Adaptive LASSO the values of  $\beta_0$  come from a Ridge solution with the same value of  $\lambda$ . Three different algorithms are implemented

- `huber`: Uses a Huber approximation of the quantile loss function. See Yi and Huang 2017 for more details.
- `br`: Solution is found by re-formulating the problem so it can be solved with the `rq()` function from `quantreg` with the `br` algorithm.
- `QICD`: A coordinate descent algorithm for SCAD and MCP penalties, see Peng and Wang (2015) for details.

The `huber` algorithm offers substantial speed advantages without much, if any, loss in performance. However, it should be noted that it solves an approximation of the quantile loss function.

**Usage**

```

rq.pen(
  x,
  y,
  tau = 0.5,
  lambda = NULL,
  penalty = c("LASSO", "Ridge", "ENet", "aLASSO", "SCAD", "MCP"),
  a = NULL,
  nlambda = 100,
  eps = ifelse(nrow(x) < ncol(x), 0.05, 0.01),
  penalty.factor = rep(1, ncol(x)),
  alg = c("huber", "br", "QICD", "fn"),
  scalex = TRUE,
  tau.penalty.factor = rep(1, length(tau)),
  coef.cutoff = 1e-08,
  max.iter = 10000,
  converge.eps = 1e-07,
  lambda.discard = TRUE,
  ...
)

```

**Arguments**

x	matrix of predictors
y	vector of responses
tau	vector of quantiles
lambda	vector of lambda, if not set will be generated automatically
penalty	choice of penalty
a	Additional tuning parameter, not used for lasso or ridge penalties. However, will be set to the elastic net values of 1 and 0 respectively. Defaults are ENet(0), aLASSO(1), SCAD(3.7) and MCP(3).
nlambda	number of lambda, ignored if lambda is set
eps	If not pre-specified the lambda vector will be from lambda_max to lambda_max times eps
penalty.factor	penalty factor for the predictors
alg	Algorithm used.
scalex	Whether x should be scaled before fitting the model. Coefficients are returned on the original scale.
tau.penalty.factor	A penalty factor for each quantile.
coef.cutoff	Some of the linear programs will provide very small, but not sparse solutions. Estimates below this number will be set to zero. This is ignored if a non-linear programming algorithm is used.
max.iter	Maximum number of iterations of non-linear programming algorithms.

converge.eps	Convergence threshold for non-linear programming algorithms.
lambda.discard	Algorithm may stop for small values of lambda if the coefficient estimates are not changing drastically. One example of this is it is possible for the LLA weights of the non-convex functions to all become zero and smaller values of lambda are extremely likely to produce the same zero weights.
...	Extra parameters.

## Value

An rq.pen.seq object.

- models: A list of each model fit for each tau and a combination.
- n: Sample size.
- p: Number of predictors.
- alg: Algorithm used. Options are "huber", "qicd" or any method implemented in rq(), such as "br".
- tau: Quantiles modeled.
- a: Tuning parameters a used.
- modelsInfo: Information about the quantile and a value for each model.
- lambda: Lambda values used for all models. If a model has fewer coefficients than lambda, say k. Then it used the first k values of lambda. Setting lambda.discard to TRUE will gurantee all values use the same lambdas, but may increase computational time noticeably and for little gain.
- penalty: Penalty used.
- call: Original call.

Each model in the models list has the following values.

- coefficients: Coefficients for each value of lambda.
- rho: The unpenalized objective function for each value of lambda.
- PenRho: The penalized objective function for each value of lambda.
- nzero: The number of nonzero coefficients for each value of lambda.
- tau: Quantile of the model.
- a: Value of a for the penalized loss function.

If the Huber algorithm is used than  $\rho_\tau(y_i - x_i^\top \beta)$  is replaced by a Huber-type approximation. Specifically, it is replaced by  $h_\gamma^\tau(y_i - x_i^\top \beta)/2$  where

$$h_\gamma^\tau(a) = a^2/(2\gamma)I(|a| \leq \gamma) + (|a| - \gamma/2)I(|a| > \gamma) + (2\tau - 1)a.$$

Where if  $\tau = .5$ , we get the usual Huber loss function. The Huber implementation calls the package hqreg which implements the methods of Yi and Huang (2017) for Huber loss with elastic net penalties. For non-elastic net penalties the LLA algorithm of Zou and Li (2008) is used to approximate those loss functions with a lasso penalty with different weights for each predictor.

**Author(s)**

Ben Sherwood, <ben.sherwood@ku.edu> and Adam Maidman

**References**

Zou H, Li R (2008). "One-step sparse estimates in nonconcave penalized likelihood models." *Ann. Statist.*, **36**(4), 1509-1533.

Yi C, Huang J (2017). "Semismooth Newton Coordinate Descent Algorithm for Elastic-Net Penalized Huber Loss Regression and Quantile Regression." *J. Comput. Graph. Statist.*, **26**(3), 547-557.

Belloni A, Chernozhukov V (2011). "L1-Penalized quantile regression in high-dimensional sparse models." *Ann. Statist.*, **39**(1), 82-130.

Peng B, Wang L (2015). "An iterative coordinate descent algorithm for high-dimensional nonconvex penalized quantile regression." *J. Comput. Graph. Statist.*, **24**(3), 676-694.

**Examples**

```
n <- 200
p <- 8
x <- matrix(runif(n*p),ncol=p)
y <- 1 + x[,1] + x[,8] + (1+.5*x[,3])*rnorm(100)
r1 <- rq.pen(x,y) #Lasso fit for median
# Lasso for multiple quantiles
r2 <- rq.pen(x,y,tau=c(.25,.5,.75))
# Elastic net fit for multiple quantiles, which must use Huber algorithm
r3 <- rq.pen(x,y,penalty="ENet",a=c(0,.5,1),alg="huber")
# First variable is not penalized
r4 <- rq.pen(x,y,penalty.factor=c(0,rep(1,7)))
tvals <- c(.1,.2,.3,.4,.5)
#Similar to penalty proposed by Belloni and Chernouzhukov.
#To be exact you would divide the tau.penalty.factor by n.
r5 <- rq.pen(x,y,tau=tvals, tau.penalty.factor=sqrt(tvals*(1-tvals)))
```

---

rq.pen.cv

*Does k-folds cross validation for rq.pen. If multiple values of a are specified then does a grid based search for best value of  $\lambda$  and a.*

---

**Description**

Does k-folds cross validation for rq.pen. If multiple values of a are specified then does a grid based search for best value of  $\lambda$  and a.

**Usage**

```
rq.pen.cv(
  x,
  y,
  tau = 0.5,
```

```

lambda = NULL,
penalty = c("LASSO", "Ridge", "ENet", "aLASSO", "SCAD", "MCP"),
a = NULL,
cvFunc = NULL,
nfolds = 10,
foldid = NULL,
nlambda = 100,
groupError = TRUE,
cvSummary = mean,
tauWeights = rep(1, length(tau)),
printProgress = FALSE,
...
)

```

### Arguments

x	Matrix of predictors.
y	Vector of responses.
tau	Quantiles to be modeled.
lambda	Values of $\lambda$ . Default will automatically select the $\lambda$ values.
penalty	Choice of penalty between LASSO, Ridge, Elastic Net (ENet), Adaptive Lasso (aLASSO), SCAD and MCP.
a	Tuning parameter of a. LASSO and Ridge has no second tuning parameter, but for notation is set to 1 or 0 respectively, the values for elastic net. Defaults are Ridge ()
cvFunc	Loss function for cross-validation. Defaults to quantile loss, but user can specify their own function.
nfolds	Number of folds.
foldid	Ids for folds. If set will override nfolds.
nlambda	Number of lambda, ignored if lambda is set.
groupError	If set to false then reported error is the sum of all errors, not the sum of error for each fold.
cvSummary	Function to summarize the errors across the folds, default is mean. User can specify another function, such as median.
tauWeights	Weights for the different tau models.
printProgress	If set to TRUE prints which partition is being worked on.
...	Additional arguments passed to rq.pen()

### Details

Two cross validation results are returned. One that considers the best combination of a and lambda for each quantile. The second considers the best combination of the tuning parameters for all quantiles. Let  $y_{b,i}$  and  $x_{b,i}$  index the observations in fold b. Let  $\hat{\beta}_{\tau,a,\lambda}^{-b}$  be the estimator for a given

quantile and tuning parameters that did not use the  $b$ th fold. Let  $n_b$  be the number of observations in fold  $b$ . Then the cross validation error for fold  $b$  is

$$CV(b, \tau) = \frac{1}{n_b} \sum_{i=1}^{n_b} \rho_{\tau}(y_{b,i} - x_{b,i}^{\top} \hat{\beta}_{\tau,a,\lambda}^{-b}).$$

Note that  $\rho_{\tau}(\cdot)$  can be replaced by a different function by setting the `cvFunc` parameter. The function returns two different cross-validation summaries. The first is `btr`, by tau results. It provides the values of `lambda` and `a` that minimize the average, or whatever function is used for `cvSummary`, of  $CV(b)$ . In addition it provides the sparsest solution that is within one standard error of the minimum results.

The other approach is the group tau results, `gtr`. Consider the case of estimating  $Q$  quantiles of  $\tau_1, \dots, \tau_Q$ . It returns the values of `lambda` and `a` that minimize the average, or again whatever function is used for `cvSummary`, of

$$\sum_{q=1}^Q CV(b, \tau_q).$$

If only one quantile is modeled then the `gtr` results can be ignored as they provide the same minimum solution as `btr`.

## Value

- `cverr`: Matrix of `cvSummary` function, default is average, cross-validation error for each model, tau and a combination, and `lambda`.
- `cvse`: Matrix of the standard error of `cverr` foreach model, tau and a combination, and `lambda`.
- `fit`: The `rq.pen.seq` object fit to the full data.
- `btr`: A `data.table` of the values of `a` and `lambda` that are best as determined by the minimum cross validation error and the one standard error rule, which fixes `a`. In `btr` the values of `lambda` and `a` are selected separately for each quantile.
- `gtr`: A `data.table` for the combination of `a` and `lambda` that minimize the cross validation error across all tau.
- `gcve`: Group, across all quantiles, cross-validation error results for each value of `a` and `lambda`.
- `call`: Original call to the function.

## Author(s)

Ben Sherwood, <ben.sherwood@ku.edu>

## Examples

```
## Not run:
x <- matrix(runif(800),ncol=8)
y <- 1 + x[,1] + x[,8] + (1+.5*x[,3])*rnorm(100)
r1 <- rq.pen.cv(x,y) #lasso fit for median
# Elastic net fit for multiple values of a and tau
r2 <- rq.pen.cv(x,y,penalty="ENet",a=c(0,.5,1),tau=c(.25,.5,.75))
#same as above but more weight given to median when calculating group cross validation error.
r3 <- rq.pen.cv(x,y,penalty="ENet",a=c(0,.5,1),tau=c(.25,.5,.75),tauWeights=c(.25,.5,.25))
```

```
# uses median cross-validation error instead of mean.
r4 <- rq.pen.cv(x,y,cvSummary=median)
#Cross-validation with no penalty on the first variable.
r5 <- rq.pen.cv(x,y,penalty.factor=c(1,rep(0,7)))

## End(Not run)
```

---

rqPen

*rqPen: A package for estimating quantile regression models using penalized objective functions.*

---

### **Description**

The package estimates a quantile regression model using LASSO, Adaptive LASSO, SCAD, MCP, elastic net, and their group counterparts, with the exception of elastic net for which there is no group penalty implementation.

### **rqPen functions**

The most important functions are `rq.pen()`, `rq.group.pen()`, `rq.pen.cv()` and `rq.group.pen.cv()`. These functions fit quantile regression models with individual or group penalties. The `cv` functions automate the cross-validation process for selection of tuning parameters.

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