# Package 'sarima'

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Type Package

**Title** Simulation and Prediction with Seasonal ARIMA Models

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Description Functions, classes and methods for time series modelling with ARIMA and related models. The aim of the package is to provide consistent interface for the user. For example, a single function autocorrelations() computes various kinds of theoretical and sample autocorrelations. This is work in progress, see the documentation and vignettes for the current functionality. Function sarima() fits extended multiplicative seasonal ARIMA models with trends, exogenous variables and arbitrary roots on the unit circle, which can be fixed or estimated (for the algebraic basis for this see <arXiv:2208.05055>, a paper on the methodology is being prepared). The suggested package 'FitARMA' can be installed with 'remotes::install\_github(``cran/FitARMA'')' if necessary but is no longer needed in normal use.

URL https://github.com/GeoBosh/sarima(devel)
 https://geobosh.github.io/sarima/(doc)

BugReports https://github.com/GeoBosh/sarima/issues

**Depends** R (>= 2.10), stats4

**Imports** methods, graphics, stats, utils, PolynomF (>= 1.0-0), Formula, lagged (>= 0.2.1), Rcpp (>= 0.12.14), Rdpack, numDeriv, Itsa

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RdMacros Rdpack

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## **Description**

Functions, classes and methods for time series modelling with ARIMA and related models. The aim of the package is to provide consistent interface for the user. For example, a single function autocorrelations() computes various kinds of theoretical and sample autocorrelations. This is work in progress, see the documentation and vignettes for the current functionality. Function sarima() fits extended multiplicative seasonal ARIMA models with trends, exogenous variables and arbitrary roots on the unit circle, which can be fixed or estimated (for the algebraic basis for this see <arXiv:2208.05055>, a paper on the methodology is being prepared). The suggested package 'FitARMA' can be installed with 'remotes::install\_github("cran/FitARMA")' if necessary but is no longer needed in normal use.

#### **Details**

There is a large number of packages for time series modelling. They provide a huge number of functions, often with similar or overlapping functionality and different argument conventions. One of the aims of package **sarima** is to provide consistent interface to some frequently used functionality.

In package **sarima** a consistent naming scheme is used as much as possible. Names of functions start with a lowercase letter and consist of whole words, acronyms or commonly used abbreviations. In multiword names, the second and subsequent words start with capital letters (camelCase). Only the first letter in acronyms is capitalised, e.g. Arma stands for ARMA. Formal (S4) classes follow the same rules but the first letter of the first word is capitalised, as well.

For example, the functions that compute autocorrelations, autocovariances, partial autocorrelations are called autocorrelations, autocovariances, and partialAutocorrelations, respectively.

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Moreover, they recognise from their argument(s) what exactly is needed. If they are given times series, they compute sample autocorrelations, etc; if they are given model specifications, they compute the corresponding theoretical properties.

This is work in progress, see also the vignette(s).

#### Author(s)

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#### References

Boshnakov GN (1996). "Bartlett's formulae—closed forms and recurrent equations." *Ann. Inst. Statist. Math.*, **48**(1), 49–59. ISSN 0020-3157, doi: 10.1007/BF00049288.

Halliday J, Boshnakov GN (2022). "Partial autocorrelation parameterisation of models with unit roots on the unit circle." doi: 10.48550/ARXIV.2208.05055, https://arxiv.org/abs/2208.05055.

Brockwell PJ, Davis RA (1991). *Time series: theory and methods. 2nd ed.*. Springer Series in Statistics. Berlin etc.: Springer-Verlag..

Francq C, Zakoian J (2010). *GARCH models: structure, statistical inference and financial applications*. John Wiley & Sons. ISBN 978-0-470-68391-0.

Li WK (2004). Diagnostic checks in time series. Chapman & Hall/CRC Press.

McLeod AI, Yu H, Krougly Z (2007). "Algorithms for Linear Time Series Analysis: With R Package." *Journal of Statistical Software*, **23**(5). doi: 10.18637/jss.v023.i05.

#### See Also

ArmaModel autocorrelations

```
## simulate a white noise ts (model from Francq & Zakoian)
n <- 5000
x <- sarima:::rgarch1p1(n, alpha = 0.3, beta = 0.55, omega = 1, n.skip = 100)

## acf and pacf
( x.acf <- autocorrelations(x) )
( x.pacf <- partialAutocorrelations(x) )

## portmanteau test for iid, by default gives also ci's for the acf under H0
x.iid <- whiteNoiseTest(x.acf, h0 = "iid", nlags = c(5,10,20), x = x, method = "LiMcLeod")
x.iid

x.iid2 <- whiteNoiseTest(x.acf, h0 = "iid", nlags = c(5,10,20), x = x, method = "LjungBox")
x.iid2

## portmanteau test for garch H0
x.garch <- whiteNoiseTest(x.acf, h0 = "garch", nlags = c(5,10,20), x = x)
x.garch</pre>
```

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```
## plot methods give the CI's under H0
plot(x.acf)

## if the data are given, the CI's under garch H0 are also given.
plot(x.acf, data = x)

## Tests based on partial autocorrelations are also available:
plot(x.pacf)
plot(x.pacf, data = x)

## Models

## AR
( ar2a1 <- ArModel(ar = c(-0.3, -0.7), sigma2 = 1) )
autocorrelations(ar2a1, maxlag = 6)
partialAutocorrelations(ar2a1, maxlag = 6)
autocovariances(ar2a1, maxlag = 6)
partialVariances(ar2a1, maxlag = 6)

## see examples for ArmaModel()</pre>
```

acfGarchTest

Tests for weak white noise

# Description

Carry out tests for weak white noise under GARCH, GARCH-type, and stochastic volatility null hypotheses.

## Usage

```
acfGarchTest(acr, x, nlags, interval = 0.95)
acfWnTest(acr, x, nlags, interval = 0.95, ...)
```

## **Arguments**

acr autocorrelations.

x time series.

nlags how many lags to use.

interval If not NULL, compute also confidence intervals with the specified coverage probability.

... additional arguments for the computation of the variance matrix under the null hypothesis, passed on to nvarOfAcfKP.

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## **Details**

Unlike the autocorrelation IID test, the time series is needed here to estimate the covariance matrix of the autocorrelations under the null hypothesis.

acfGarchTest performs a test for uncorrelatedness of a time series. The null hypothesis is that the time series is GARCH, see Francq and Zakoian (2010).

acfWnTest performs a test for uncorrelatedness of a time series under a weaker null hypothesis. The null hypothesis is that the time series is GARCH-type or from a stochasite volatily model, see Kokoszka and Politis (2011).

See the references for details and precise specification of the hypotheses.

The format of the return value is the same as for acflidTest.

#### Value

```
a list with components "test" and "ci"
```

## Author(s)

Georgi N. Boshnakov

#### References

Francq C, Zakoian J (2010). *GARCH models: structure, statistical inference and financial applications*. John Wiley & Sons. ISBN 978-0-470-68391-0.

Kokoszka PS, Politis DN (2011). "Nonlinearity of ARCH and stochastic volatility models and Bartlett's formula." *Probability and Mathematical Statistics*, **31**(1), 47–59.

# See Also

```
whiteNoiseTest, acfIidTest;
plot-methods for graphical representations of results
```

```
## see also the examples for \code{\link{whiteNoiseTest}}
set.seed(1234)
n <- 5000
x <- sarima:::rgarch1p1(n, alpha = 0.3, beta = 0.55, omega = 1, n.skip = 100)
x.acf <- autocorrelations(x)
x.pacf <- partialAutocorrelations(x)

acfGarchTest(x.acf, x = x, nlags = c(5,10,20))
acfGarchTest(x.pacf, x = x, nlags = c(5,10,20))
# do not compute CI's:
acfGarchTest(x.pacf, x = x, nlags = c(5,10,20), interval = NULL)
## plot methods call acfGarchTest() suitably if 'x' is given:
plot(x.acf, data = x)</pre>
```

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```
plot(x.pacf, data = x)

## use 90% limits:
plot(x.acf, data = x, interval = 0.90)

acfWnTest(x.acf, x = x, nlags = c(5,10,20))
nvarOfAcfKP(x, maxlag = 20)
whiteNoiseTest(x.acf, h0 = "arch-type", x = x, nlags = c(5,10,20))
```

acfIidTest

Carry out IID tests using sample autocorrelations

#### **Description**

Carry out tests for IID from sample autocorrelations.

## Usage

# **Arguments**

acf autocorrelations. length of the corresponding time series. number of df to subtract. npar nlags number of autocorrelations to use for the portmonteau statistic, can be a vector to request several such statistics. method a character string, one of "LiMcLeod", "LjungBox" or "BoxPierce". interval a number or NULL. expandCI logical flag, if TRUE return a CI for each lag up to max(nlags). Used only if CI's are requested. additional arguments passed on to methods. In particular, some methods have argument x for the time series.

# **Details**

Performs one of several tests for IID based on sample autocorrelations. A correction of the degrees of freedom for residuals from fitted models can be specified with argument npar. nlags specifies the number of autocorrelations to use in the test, it can be a vector to request several tests.

The results of the test are gathered in a matrix with one row for each element of nlags. The test statistic is in column "ChiSq", degrees of freedom in "DF" and the p-value in "pvalue". The method is in attribute "method".

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If interval is not NULL confidence intervals for the autocorrelations are computed, under the null hypothesis of independence. The coverage probability (or probabilities) is specified by interval.

If argument expandCI is TRUE, there is one row for each lag, up to max(nlags). It is best to use this feature with a single coverage probability.

If expandCI to FALSE the confidence intervals are put in a matrix with one row for each coverage probability.

#### Value

a list with components "test" and (if requested) "ci", as described in Details

#### Methods

```
signature(acf = "ANY") In this method acf contains the autocorrelations.
signature(acf = "missing") The autocorrelations are computed from argument x (the time series).
signature(acf = "SampleAutocorrelations") This is a convenience method in which argument n is taken from acf and thus does not need to be specified by the user.
```

#### Author(s)

Georgi N. Boshnakov

#### References

Li WK (2004). Diagnostic checks in time series. Chapman & Hall/CRC Press.

#### See Also

```
whiteNoiseTest, acfGarchTest, acfMaTest;
plot-methods for graphical representations of results
```

```
set.seed(1234)
ts1 <- rnorm(100)

a1 <- drop(acf(ts1)$acf)
acfIidTest(a1, n = 100, nlags = c(5, 10, 20))
acfIidTest(a1, n = 100, nlags = c(5, 10, 20), method = "LjungBox")
acfIidTest(a1, n = 100, nlags = c(5, 10, 20), interval = NULL)
acfIidTest(a1, n = 100, method = "LjungBox", interval = c(0.95, 0.90), expandCI = FALSE)

## acfIidTest() is called behind the scenes by methods for autocorrelation objects
ts1_acrf <- autocorrelations(ts1)
class(ts1_acrf) # "SampleAutocorrelations"
whiteNoiseTest(ts1_acrf, h0 = "iid", nlags = c(5,10,20), method = "LiMcLeod")
plot(ts1_acrf)</pre>
```

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```
## use 10% level of significance in the plot:
plot(ts1_acrf, interval = 0.9)
```

acfMaTest

Autocorrelation test for MA(q)

# Description

Carry out autocorrelation test for MA(q).

# Usage

```
acfMaTest(acf, ma, n, nlags, interval = 0.95)
```

## **Arguments**

acf autocorrelations.

ma a positive integer, the moving average order.

n length of the corresponding time series.

nlags number of autocorrelations to use for the portmonteau statistic, can be a vector

to request several such statistics.

interval a number or NULL.

## **Details**

acfMaTest performs a test that the time series is MA(ma), under the classical assumptions of Bartlett's formulas.

When intervals are requested, they are confidence intervals for lags from 1 to ma. For lags greater than the moving average order, ma, autocorrelations outside them suggest to reject the null hypothesis that the process is MA(ma).

# Value

```
a list with components "test" and (if requested) "ci"
```

## Author(s)

Georgi N. Boshnakov

## See Also

```
whiteNoiseTest, acfIidTest acfGarchTest
```

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Crosscovariances between an ARMA process and its innovations

#### **Description**

Compute autocovariances of ARMA models and crosscovariances between an ARMA process and its innovations.

## Usage

```
armaccf_xe(model, lag.max = 1)
armaacf(model, lag.max, compare)
```

# **Arguments**

model the model, a list with components ar, ma and sigma2 (for the time being, sigmasq

is also accepted, if model\$sigma2 is NULL).

lag.max maximal lag for the result.

compare if TRUE compute the autocovariances also using tacvfARMA() and return both

results for comparison.

#### **Details**

Given a causal ARMA model, armaccf\_xe computes theoretical crosscovariances  $R_{xe}(0)$ ,  $R_{xe}(1)$ ,  $R_{xe}(lag.max)$ , where  $R_{xe}(k) = E(X_t e_{t-k})$ , between an ARMA process and its innovations. Negative lags are not considered since  $R_{xe}(k) = 0$  for k < 0. The moving average polynomial may have roots on the unit circle.

This is a simple illustration of the equations I give in my time series courses.

armaacf computes ARMA autocovariances. The default method computes computes the zero lag autocovariance using armaccf\_xe() and multiplies the autocorrelations obtained from ARMAacf (which computes autocorrelations, not autocovariances). If compare = TRUE it also uses tacvfARMA from package **ltsa** and returns both results in a matrix for comparison. The matrix has columns "native", "tacvfARMA" and "difference", where the last column contains the (zapped) differences between the autocorrelations obtained by the two methods.

The ARMA parameters in argument model follow the Brockwell-Davis convention for the signs. Since tacvfARMA() uses the Box-Jenkins convention for the signs, the moving average parameters are negated for calls to tacvfARMA().

#### Value

```
for armaccf_xe, the crosscovariances for lags 0, ..., maxlag. for armaccf, the autocovariances, see Details.
```

#### Note

armaacf is useful for exploratory computations but autocovariances is more convenient and eliminates the need to know function names for particular cases.

armaccf\_xe

## Author(s)

Georgi N. Boshnakov

#### References

McLeod AI, Yu H, Krougly Z (2007). "Algorithms for Linear Time Series Analysis: With R Package." *Journal of Statistical Software*, **23**(5). doi: 10.18637/jss.v023.i05.

```
## Example 1 from ?ltsa::tacvfARMA
z <- sqrt(sunspot.year)</pre>
n \leftarrow length(z)
p <- 9
q <- 0
ML <- 5
out <- arima(z, order = c(p, 0, q))
phi <- theta <- numeric(0)</pre>
if (p > 0) phi <- coef(out)[1:p]
if (q > 0) theta <- coef(out)[(p+1):(p+q)]
zm \leftarrow coef(out)[p+q+1]
sigma2 <- out$sigma2
armaacf(list(ar = phi, ma = theta, sigma2 = sigma2), lag.max = 20)
## this illustrates that the methods
## based on ARMAacf and tacvARMA are equivalent:
armaacf(list(ar = phi, ma = theta, sigma2 = sigma2), lag.max = 20, compare = TRUE)
## In the original example in ?ltsa::tacvfARMA
## the comparison is with var(z), not with the theoretical variance:
rA <- ltsa::tacvfARMA(phi, - theta, maxLag=n+ML-1, sigma2=sigma2)
rB <- var(z) * ARMAacf(ar=phi, ma=theta, lag.max=n+ML-1)
## so rA and rB are different.
## but the difference is due to the variance:
rB2 <- rA[1] * ARMAacf(ar=phi, ma=theta, lag.max=n+ML-1)
cbind(rA[1:5], rB[1:5], rB2[1:5])
## There is no need to use specific functions,
## autocovariances() is most convenient for routine use:
armalist <- list(ar = phi, ma = theta, sigma2 = sigma2)</pre>
autocovariances(armalist, maxlag = 10)
## even better, set up an ARMA model:
mo <- new("ArmaModel", ar = phi, ma = theta, sigma2 = sigma2)</pre>
autocovariances(mo, maxlag = 10)
```

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ArmaModel

Create ARMA objects

# **Description**

Create ARMA objects.

# Usage

```
ArmaModel(...)
ArModel(...)
MaModel(...)
```

## Arguments

.. the arguments are passed to new(). Typical arguments are ar, ma and mean.

#### Value

an object representing an ARMA, AR or MA model

## Author(s)

Georgi N. Boshnakov

## See Also

```
ArmaModel, ArModel, MaModel
```

```
## MA
( ma2a1 <- MaModel(ma = c(0.3, 0.7), sigma2 = 1) )
autocorrelations(ma2a1, maxlag = 6)
partialAutocorrelations(ma2a1, maxlag = 6)
autocovariances(ma2a1, maxlag = 6)
partialVariances(ma2a1, maxlag = 6)

## sigma2 is set to NA if not specified
## but things that don't depend on it are computed:
( ma2a2 <- MaModel(ma = c(0.3, 0.7)) )
autocorrelations(ma2a2, maxlag = 6)
partialAutocorrelations(ma2a2, maxlag = 6)

## AR
( ar2a1 <- ArModel(ar = c(-0.3, -0.7), sigma2 = 1) )
autocorrelations(ar2a1, maxlag = 6)
partialAutocorrelations(ar2a1, maxlag = 6)
autocovariances(ar2a1, maxlag = 6)</pre>
```

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```
partialVariances(ar2a1, maxlag = 6)
## ARMA
(arma2a1 < -ArmaModel(ar = 0.5, ma = c(0.3, 0.7), sigma2 = 1))
autocorrelations(arma2a1, maxlag = 6)
partialAutocorrelations(arma2a1, maxlag = 6)
## modelCoef() returns a list with components 'ar' and 'ma'
modelCoef(arma2a1)
modelCoef(ma2a1)
modelCoef(ar2a1)
## modelOrder() returns a list with components 'ar' and 'ma'
modelOrder(arma2a1)
modelOrder(ma2a1)
modelOrder(ar2a1)
as(ma2a1, "ArmaModel") # success, as expected
as(ar2a1, "ArModel") # success, as expected
as(ArmaModel(ar = c(-0.3, -0.7)), "ArModel")
## But these fail:
## as(ma2a1, "ArModel") # fails
## as(arma2a1, "ArModel") # fails
## as(arma2a1, "MaModel") # fails
```

ArmaModel-class

Classes ArmaModel, ArModel and MaModel in package sarima

#### **Description**

Classes ArmaModel, ArModel and MaModel in package sarima.

# **Objects from the Class**

Classes "ArModel" and "MaModel" are subclasses of "ArmaModel" with the corresponding order always zero.

The recommended way to create objects from these classes is with the functions ArmaModel, ArModel and MaModel. Objects can also be created by calls of the form new("ArmaModel", ..., ar, ma, mean, check). See also coerce-methods for further ways to create objects from these classes.

## **Slots**

```
center: Object of class "numeric" ~~
intercept: Object of class "numeric" ~~
sigma2: Object of class "numeric" ~~
ar: Object of class "BJFilter" ~~
ma: Object of class "SPFilter" ~~
```

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#### **Extends**

```
Class "ArmaSpec", directly. Class "VirtualArmaModel", directly. Class "ArmaFilter", by class "ArmaSpec", distance 2. Class "VirtualFilterModel", by class "VirtualArmaModel", distance 2. Class "VirtualStationaryModel", by class "VirtualArmaModel", distance 2. Class "VirtualArmaFilter", by class "ArmaSpec", distance 3. Class "VirtualAutocovarianceModel", by class "VirtualArmaModel", distance 3. Class "VirtualMeanModel", by class "VirtualArmaModel", distance 3. Class "VirtualMonicFilter", by class "ArmaSpec", distance 4.
```

#### Methods

```
modelOrder signature(object = "ArmaModel", convention = "ArFilter"): ...
modelOrder signature(object = "ArmaModel", convention = "MaFilter"): ...
modelOrder signature(object = "ArmaModel", convention = "missing"): ...
modelOrder signature(object = "SarimaModel", convention = "ArmaModel"): ...
sigmaSq signature(object = "ArmaModel"): ...
```

#### Author(s)

Georgi N. Boshnakov

#### See Also

ArmaModel, ArModel, MaModel, coerce-methods

```
arma1p1 \leftarrow new("ArmaModel", ar = 0.5, ma = 0.9, sigma2 = 1)
autocovariances(arma1p1, maxlag = 10)
autocorrelations(arma1p1, maxlag = 10)
partialAutocorrelations(arma1p1, maxlag = 10)
partialAutocovariances(arma1p1, maxlag = 10)
new("ArmaModel", ar = 0.5, ma = 0.9, intercept = 4)
new("ArmaModel", ar = 0.5, ma = 0.9, center = 1.23)
new("ArModel", ar = 0.5, center = 1.23)
new("MaModel", ma = 0.9, center = 1.23)
# argument 'mean' is an alias for 'center':
new("ArmaModel", ar = 0.5, ma = 0.9, mean = 1.23)
## both center and intercept may be given
## (the mean is not equal to the intercept in this case)
new("ArmaModel", ar = 0.5, ma = 0.9, center = 1.23, intercept = 2)
## Don't use 'mean' together with 'center' and/or 'intercept'.
##
     new("ArmaModel", ar = 0.5, ma = 0.9, center = 1.23, mean = 4)
     new("ArmaModel", ar = 0.5, ma = 0.9, intercept = 2, mean = 4)
##
## Both give error message:
   Use argument 'mean' only when 'center' and 'intercept' are missing or zero
```

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ArmaSpectrum-class

Class "ArmaSpectrum"

# **Description**

Objects from class "ArmaSpectrum" spectra computed by spectrum.

## **Details**

The methods for show, print and plot work analogously to those for class "Spectrum" (which is a super class of "ArmaSpectrum"). In addition, print and show print also the parameters of the ARMA model.

# **Objects from the Class**

Objects contain spectra produced by sarima::spectrum (recommended), see spectrum for details.

Objects can also be created by calls of the form new("ArmaSpectrum", ar = , ma = , sigma2 = , ...), where ar and ma are numeric vectors and sigma2 is a number. sigma2 may be omitted but then only normalized spectra can be computed. There further possibilities for the arguments but they should be considered internal and subject to change.

## **Slots**

```
All slots are inherited from class "Spectrum".

.Data: Object of class "function".

call: Object of class "call".

model: Object of class "ANY".
```

#### Methods

```
initialize signature(.Object = "ArmaSpectrum"): ...
```

#### Author(s)

Georgi N. Boshnakov

## See Also

```
class "Spectrum" for further details,
spectrum for further examples
```

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## **Examples**

arma\_Q0Gardner

Computing the initial state covariance matrix of ARMA

# **Description**

Wrappers for the internals 'stats' functions used by arima() to compute the initial state covariance matrix of ARMA models.

# Usage

```
arma_Q0naive(phi, theta, tol = .Machine$double.eps)
arma_Q0gnbR(phi, theta, tol = .Machine$double.eps)
```

# **Arguments**

phi autoregressive coefficients.
theta moving average coefficients.
tol tollerance.

arma\_Q0gnb

#### **Details**

arima() uses one of two methods to compute the initial state covariance matrix of a stationary ARMA model. Both methods are implemented by internal non-exported C functions. arma\_Q0Gardner() and arma\_Q0bis are simple R wrappers for those functions. They are defined in the tests (**TODO:** put in the examples?) bit are not defined in the namespace of the package since they use unexported functions.

arma\_Q0Gardner() implements the original method from Gardner et al (1980). arma\_Q0bis() is a more recent method that deals better with roots very close to the unit circle.

These functions can be useful for comparative testing. They cannot be put in package 'sarima' since they use `:::` operator and are hence inadmissible to CRAN.

#### Value

a matrix

#### References

Gardner G, Harvey AC, Phillips GDA (1980). "Algorithm AS154. An algorithm for exact maximum likelihood estimation of autoregressive-moving average models by means of Kalman filtering." *Applied Statistics*, 311–322.

## **Examples**

```
## arma_Q0Gardner(phi, theta, tol = .Machine$double.eps)
## arma_Q0bis(phi, theta, tol = .Machine$double.eps)
```

arma\_Q0gnb

Compute the initial state covariance of ARMA model

# **Description**

Compute the initial state covariance of ARMA model

# Usage

```
arma_Q0gnb(phi, theta, tol = 2.220446e-16)
```

#### **Arguments**

phi autoregression parameters.
theta moving average parameters.
tol tollerance. (TODO: explain)

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#### **Details**

Experimental computation of the initial state covariance matrix of ARMA models.

The numerical results are comparable to SSinit = "Rossignol2011" method in arima and related functions. The method seems about twice faster than "Rossignol2011" on the models I tried but I haven't done systematic tests.

See section 'examples' below and, for more tests based on the tests from stats, the tests in test/testthat/test-arma-q0.R.

#### Value

a matrix

## Author(s)

Georgi N. Boshnakov

#### References

Gardner G, Harvey AC, Phillips GDA (1980). "Algorithm AS154. An algorithm for exact maximum likelihood estimation of autoregressive-moving average models by means of Kalman filtering." *Applied Statistics*, 311–322.

R bug report PR#14682 (2011-2013) <URL: https://bugs.r-project.org/bugzilla3/show\_bug.cgi?id=14682>.

# See Also

makeARIMA, arima

```
Q0a \leftarrow arma_Q0gnb(c(0.2, 0.5), c(0.3))
Q0b <- makeARIMA(c(0.2, 0.5), c(0.3), Delta = numeric(0))$Pn
all.equal(Q0a, Q0b) ## TRUE
## see test/testthat/test-arma-q0.R for more;
## these functions cannot be defined in the package due to their use of
## \code{:::} on exported base R functions.
##
## "Gardner1980"
arma_Q0Gardner <- function(phi, theta, tol = .Machine$double.eps){</pre>
    ## tol is not used here
    .Call(stats:::C_getQ0, phi, theta)
## "Rossignol2011"
arma_Q0bis <- function(phi, theta, tol = .Machine$double.eps){</pre>
    .Call(stats:::C_getQ0bis, phi, theta, tol)
}
arma_Q0Gardner(c(0.2, 0.5), c(0.3))
arma_Q0bis(c(0.2, 0.5), c(0.3))
Q0a
Q0b
```

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as.SarimaModel

Convert S3 model objects to class SarimaModel

# **Description**

Convert S3 model objects to class SarimaModel.

## Usage

```
as.SarimaModel(x, ...)
## S3 method for class 'Arima'
as.SarimaModel(x, ...)
```

## **Arguments**

x an objects from a class representing Seasonal ARIMA models.

... further arguments for methods.

# **Details**

This function can be useful when one needs to manipulate the components of SARIMA models.

The method for class Arima (objects generated by stats::arima()) extracts the model information and convert it to "SarimaModel".

For S4 classes, there are methods for as(), where suitable. modelCoef provides a more powerful conversion mechanism.

# Value

an object from class "SarimaModel"

# See Also

SarimaModel

autocorrelations

Compute autocorrelations and related quantities

## **Description**

Generic functions for computation of autocorrelations, autocovariances and related quantities. The idea is to free the user from the need to look for specific functions that compute the desired property for their object.

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#### Usage

```
autocovariances(x, maxlag, ...)
autocorrelations(x, maxlag, lag_0, ...)
partialAutocorrelations(x, maxlag, lag_0 = TRUE, ...)
partialAutocovariances(x, maxlag, ...)
partialVariances(x, ...)
```

## **Arguments**

x an object for which the requested property makes sense.

maxlag the maximal lag to include in the result.

lag\_0 if TRUE include lag zero.

... further arguments for methods.

#### **Details**

autocorrelations is a generic function for computation of autocorrelations. It deduces the appropriate type of autocorrelation from the class of the object. For example, for models it computes theoretical autocorrelations, while for time series it computes sample autocorrelations.

The other functions described are similar for other second order properties of x.

These functions return objects from suitable classes, all inheriting from "Lagged". The latter means that indexing starts from zero, so the value for lag zero is accessed by r[0]). Subscripting always returns the underlying data unclassed (i.e. ordinary vectors or arrays). In particular, "[]" extracts the underlying data.

Functions computing autocorrelations and partial autocorrelations have argument lag\_0 — if it is set to FALSE, the value for lag zero is dropped from the result and the returned object is an ordinary vector or array, as appropriate.

See the individual methods for the format of the result and further details.

There are plot methods for sample autocorrelations and sample partial autocorrelations with overlaid significance limits under null hypotheses for independence or weak white noise, see plot-methods and the examples there. More details can be found in the vignettes, see section 'See also' below.

#### Value

an object from a class suitable for the requested property and x

#### Author(s)

Georgi N. Boshnakov

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#### See Also

plot-methods for plotting with significance limits computed under strong white noise and weak white noise hypotheses;

 $autocorrelations-\texttt{methods}, partial \texttt{Autocorrelations-methods} \ for \ details \ on \ individual \ methods;$ 

```
vignette("white_noise_tests", package = "sarima") and
vignette("garch_tests_example", package = "sarima") for extensive worked examples.
armaccf_xe, armaacf
```

```
set.seed(1234)
v1 <- rnorm(100)
autocorrelations(v1)
v1.acf <- autocorrelations(v1, maxlag = 10)
v1.acf[1:10] # drop lag zero value (and the class)
autocorrelations(v1, maxlag = 10, lag_0 = FALSE) # same
partialAutocorrelations(v1)
partialAutocorrelations(v1, maxlag = 10)
## compute 2nd order properties from raw data
autocovariances(v1)
autocovariances(v1, maxlag = 10)
partialAutocovariances(v1, maxlag = 6)
partialAutocovariances(v1)
partialVariances(v1, maxlag = 6)
pv1 <- partialVariances(v1)</pre>
## compute 2nd order properties from raw data
autocovariances(AirPassengers, maxlag = 6)
autocorrelations(AirPassengers, maxlag = 6)
partialAutocorrelations(AirPassengers, maxlag = 6)
partialAutocovariances(AirPassengers, maxlag = 6)
partialVariances(AirPassengers, maxlag = 6)
acv <- autocovariances(AirPassengers, maxlag = 6)</pre>
autocovariances(acv) # no-op
autocovariances(acv, maxlag = 4) # trim the available lags
## compute 2nd order properties from sample autocovariances
acr <- autocorrelations(acv)</pre>
acr
partialAutocorrelations(acv)
partialAutocovariances(acv)
partialVariances(acv)
## compute 2nd order properties from sample autocorrelations
partialAutocorrelations(acr)
```

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```
## These cannot be computed, since the variance is needed but unknown:
## autocovariances(acr)
## partialAutocovariances(acr)
## to treat autocorrelations as autocovariances,
## convert them to autocovariances explicitly:
as(acr, "Autocovariances")
as(acr, "SampleAutocovariances")

partialVariances(as(acr, "Autocovariances"))
partialVariances(as(acr, "SampleAutocovariances"))
```

autocorrelations-methods

*Methods for function autocorrelations()* 

# Description

Methods for function autocorrelations().

#### Methods

```
signature(x = "ANY", maxlag = "ANY", lag_0 = "ANY")
signature(x = "ANY", maxlag = "ANY", lag_0 = "missing")
signature(x = "Autocorrelations", maxlag = "ANY", lag_0 = "missing")
signature(x = "Autocorrelations", maxlag = "missing", lag_0 = "missing")
signature(x = "Autocovariances", maxlag = "ANY", lag_0 = "missing")
signature(x = "PartialAutocorrelations", maxlag = "ANY", lag_0 = "missing")
signature(x = "PartialAutocovariances", maxlag = "ANY", lag_0 = "missing")
signature(x = "SamplePartialAutocorrelations", maxlag = "ANY", lag_0 = "missing")
signature(x = "SamplePartialAutocovariances", maxlag = "ANY", lag_0 = "missing")
signature(x = "VirtualArmaModel", maxlag = "ANY", lag_0 = "missing")
signature(x = "VirtualSarimaModel", maxlag = "ANY", lag_0 = "missing")
```

# Author(s)

Georgi N. Boshnakov

```
## see the examples for ?autocorrelations
```

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```
autocovariances-methods
```

Methods for function autocovariances()

## **Description**

Methods for function autocovariances().

#### Methods

```
signature(x = "ANY", maxlag = "ANY")
signature(x = "Autocovariances", maxlag = "ANY")
signature(x = "Autocovariances", maxlag = "missing")
signature(x = "VirtualArmaModel", maxlag = "ANY")
signature(x = "VirtualAutocovariances", maxlag = "ANY")
```

#### Author(s)

Georgi N. Boshnakov

#### See Also

```
autocorrelations
```

## **Examples**

```
## see the examples for ?autocorrelations
```

coerce-methods

setAs methods in package sarima

## **Description**

Methods for as() in package sarima.

## Methods

This section shows the methods for converting objects from one class to another, defined via setAs(). Use as(obj, "classname") to convert object obj to class "classname".

```
signature(from = "ANY", to = "Autocorrelations")
signature(from = "ANY", to = "ComboAutocorrelations")
signature(from = "ANY", to = "ComboAutocovariances")
signature(from = "ANY", to = "PartialAutocorrelations")
```

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```
signature(from = "ANY", to = "PartialAutocovariances")
    signature(from = "ANY", to = "PartialVariances")
    signature(from = "ArmaSpec", to = "list")
    signature(from = "Autocorrelations", to = "ComboAutocorrelations")
    signature(from = "Autocorrelations", to = "ComboAutocovariances")
    signature(from = "Autocovariances", to = "ComboAutocorrelations")
    signature(from = "Autocovariances", to = "ComboAutocovariances")
    signature(from = "BJFilter", to = "SPFilter")
    signature(from = "numeric", to = "BJFilter") Convert a numeric vector to a BJFilter object.
        This is a way to state that the coefficients follow the Box-Jenkins convention for the signs, see
        the examples.
    signature(from = "numeric", to = "SPFilter") Convert a numeric vector to an SPFilter ob-
        ject. This is a way to state that the coefficients follow the signal processing (SP) convention
        for the signs, see the examples.
    signature(from = "PartialVariances", to = "Autocorrelations")
    signature(from = "PartialVariances", to = "Autocovariances")
    signature(from = "PartialVariances", to = "ComboAutocorrelations")
    signature(from = "PartialVariances", to = "ComboAutocovariances")
    signature(from = "SarimaFilter", to = "ArmaFilter")
    signature(from = "SarimaModel", to = "list")
    signature(from = "SPFilter", to = "BJFilter")
    signature(from = "vector", to = "Autocorrelations")
    signature(from = "vector", to = "Autocovariances")
    signature(from = "vector", to = "PartialAutocorrelations")
    signature(from = "vector", to = "PartialAutocovariances")
    signature(from = "VirtualArmaFilter", to = "list")
    signature(from = "VirtualSarimaModel", to = "ArmaModel")
Author(s)
   Georgi N. Boshnakov
```

```
## the default for ARMA model is BJ for ar and SP for ma:
mo \leftarrow new("ArmaModel", ar = 0.9, ma = 0.4, sigma2 = 1)
modelPoly(mo)
## here we declare explicitly that 0.4 uses the SP convention
      (not necessary, the result is the same, but the intention is clear).
mo1 < -new("ArmaModel", ar = 0.9, ma = as(0.4, "SPFilter"), sigma2 = 1)
modelPoly(mo1)
```

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```
identical(mo, mo1) ## TRUE
## if the sign of theta follows the BJ convention, this can be stated unambiguously.
   This creates the same model:
mo2 \leftarrow new("ArmaModel", ar = 0.9, ma = as(-0.4, "BJFilter"), sigma2 = 1)
modelPoly(mo2)
identical(mo, mo2) ## TRUE
## And this gives the intended model whatever the default conventions:
ar3 <- as(0.9, "BJFilter")
ma3 <- as(-0.4, "BJFilter")
mo3 <- new("ArmaModel", ar = ar3, ma = ma3, sigma2 = 1)</pre>
modelPoly(mo3)
identical(mo, mo3) ## TRUE
## The coefficients can be extracted in any particular form,
## e.g. to pass them to functions with specific requirements:
modelCoef(mo3) # coefficients of the model with the default (BD) sign convention
modelCoef(mo3, convention = "BD") # same result
modelCoef(mo3, convention = "SP") # signal processing convention
## for ltsa::tacvfARMA() the convention is BJ, so:
co <- modelCoef(mo3, convention = "BJ") # Box-Jenkins convention</pre>
ltsa::tacvfARMA(co$ar, co$ma, maxLag = 6, sigma2 = 1)
autocovariances(mo3, maxlag = 6) ## same
```

confint

Confidence and acceptance intervals in package sarima

# Description

Compute confidence and acceptance intervals for sample autocorrelations under assumptions chosen by the user.

## Usage

```
## S4 method for signature 'SampleAutocorrelations'
confint(object, parm, level = 0.95, se = FALSE, maxlag, ..., assuming)
```

#### **Arguments**

se

object an object containing sample autocorrelations (sacfs).

parm which parameters to include, as for stats::confint.

If TRUE return also standard errors.

level coverage level, such as 0.95.

assuming under what assumptions to do the computations? Currently can be "iid", "garch",

a fitted model, or a theoretical model, see Details.

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```
maxlag maximal lag to include
... further arguments for se.
```

#### **Details**

For lags not fixed by the assumed model the computed intervals are confidence intervals.

The autocorrelations postulated by the null model (argument assuming) are usually fixed for some lags. For such lags it doesn't make sense to talk about confidence intervals. We use the term *acceptance interval* in this case since the sacfs for such lags fall in the corresponding intervals with high probability if the null model is correct.

If assuming is "iid" (strong white noise), then all autocorrelations in the null model are fixed (to zero) and the limits of the resulting acceptance intervals are ethose from the familiar plots produced by base-R's function acf.

If assuming is a fitted MA(q) model, e.g. obtained from arima(), then for lags  $1, \ldots, q$  we get confidence intervals, while for lags greater than q the intervals are acceptance intervals.

The autocorrelations of ARMA models with non-trivial autoregressive part may also have structural patterns of zeroes (for example some seasonal models), leading to acceptance intervals for such lags.

If assuming specifies a theoretical (non-fitted) model, then the autocorrelation function of the null model is completely fixed and we get acceptance intervals for all lags.

The return value is a matrix with one row for each requested lag, containg the lag, lower bound, upper bound, estimate for acf(lag) and the value of acf(lag) under H0 (if fixed) and NA if not fixed under H0. The null model is stored as attribute "assuming".

**Note:** When assuming = "garch" it is currently necessary to submit the time series from which the autocorrelations were computed as argument x.

#### Value

```
a matrix as described in section 'Details'; if se = TRUE, a column giving the standard errors of the sample autocorrelations is appended.
```

## See Also

```
se
vignette("white_noise_tests", package = "sarima")
vignette("garch_tests_example", package = "sarima")
```

```
set.seed(1234)
v1 <- arima.sim(n = 100, list(ma = c(0.8, 0.1), sd = 1))
v1.acf <- autocorrelations(v1, maxlag = 10)

confint(v1.acf, parm = 1:4, assuming = "iid")
confint(v1.acf, assuming = "iid", maxlag = 4) # same

## a fitted MA(2) - rho_1, rho_2 not fixed, the rest fixed
ma2fitted <- arima(v1, order = c(0,0,2), include.mean=FALSE)</pre>
```

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```
confint(v1.acf, assuming = ma2fitted, maxlag = 4)
## a theoretical MA(2) model, all acfs fixed under H0
ma2 <- MaModel(ma = c(0.8, 0.1), sigma2 = 1)
confint(v1.acf, assuming = ma2, maxlag = 4)
# a weak white noise null
confint(v1.acf, assuming = "garch", maxlag = 4, x = v1)</pre>
```

filterCoef

Coefficients and other basic properties of filters

## **Description**

Coefficients and other basic properties of filters.

# Usage

```
filterCoef(object, convention, ...)
filterOrder(object, ...)
filterPoly(object, ...)
filterPolyCoef(object, lag_0 = TRUE, ...)
```

## **Arguments**

object object.

convention convention for the sign.

lag\_0 if FALSE, drop the coefficient of order zero.

... further arguments for methods.

# Details

Generic functions to extract basic properties of filters: filterCoef returns coefficients, filterOrder returns the order, filterPoly, returns the characteristic polynomial, filterPolyCoef gives the coefficients of the characteristic polynomial.

For further details on argument convention see filterCoef-methods.

What exactly is returned depends on the specific filter classes, see the description of the corresponding methods. For the core filters, the values are as can be expected. For "ArmaFilter", the value is a list with components "ar" and "ma" giving the requested property for the corresponding part of the filter. Similarly, for "SarimaFilter" the values are lists, maybe with additional quantities.

## Value

the requested property as described in Details.

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#### Note

The filterXXX() functions are somewhat low level and technical. They should be rarely needed in routine work. The corresponding modelXXX are more flexible.

#### Author(s)

Georgi N. Boshnakov

#### See Also

modelOrder, modelCoef, modelPoly, modelPolyCoef, for the recommended higher level alternatives for models.

filterOrder-methods, filterCoef-methods, filterPoly-methods, filterPolyCoef-methods, for more information on the methods and the arguments.

```
filterPoly(as(c(0.3, 0.5), "BJFilter")) # 1 - 0.3*x - 0.5*x^2
filterPoly(as(c(0.3, 0.5), "SPFilter")) # 1 + 0.3*x + 0.5*x^2
## now two representations of the same filter:
fi1 <- as(c(0.3, 0.5), "BJFilter")
fi2 \leftarrow as(c(-0.3, -0.5), "SPFilter")
identical(fi2, fi1) # FALSE, but
## fi1 and fi2 represent the same filter, eg. same ch. polynomials:
filterPoly(fi1)
filterPoly(fi2)
identical(filterPolyCoef(fi2), filterPolyCoef(fi1))
# same as above, using new()
fila <- new("BJFilter", coef = c(0.3, 0.5))
identical(fi1a, fi1) # TRUE
fi2a <- new("SPFilter", coef = c(-0.3, -0.5))
identical(fi2a, fi2) # TRUE
## conversion by as() changes the internal representation
## but represents the same filter:
identical(as(fi1, "SPFilter"), fi2) # TRUE
c(filterOrder(fi1), filterOrder(fi2))
## these give the internally stored coefficients:
filterCoef(fi1)
filterCoef(fi2)
## with argument 'convention' the result doesn't depend
## on the internal representation:
co1 <- filterCoef(fi1, convention = "SP")</pre>
co2 <- filterCoef(fi2, convention = "SP")</pre>
identical(co1, co2) # TRUE
```

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## Description

Methods for filterCoef in package sarima.

#### Methods

filterCoef() returns the coefficients of object. The format of the result depends on the type of filter, see the descriptions of the individual methods below.

If argument convention is omitted, the sign convention for the coefficients is the one used in the object. convention can be set to "BJ" or "SP" to request, respectively, the Box-Jenkins or the signal processing convention. Also, "-" is equivalent to "BJ" and "+" to "SP".

For ARMA filters, "BJ" and "SP" request the corresponding convention for both parts (AR and MA). A widely used convention, e.g., by base R and (Brockwell and Davis 1991), is "BJ" for the AR part and "SP" for the MA part. It can be requested with convention = "BD". For convenience, "—" is equivalent to "BJ", "++" to "SP", "-+" to "BD". For completeness, "+-" can be used to request "SP" for the AR part and "BJ" for the MA part.

Invalid values of convention throw error. In particular, low level filters, such as "BJFilter" don't know if they are AR or MA, so they throw error if convention is "BD" or "+-" (but "++" and "-" are ok, since they are unambiguous). Similarly and to avoid subtle errors, the ARMA filters do not accept "+" or "-".

```
signature(object = "VirtualMonicFilterSpec", convention = "missing") returns object@coef.
```

- signature(object = "VirtualBJFilter", convention = "character") returns the filter coefficients in the requested convention.
- signature(object = "VirtualSPFilter", convention = "character") returns the filter coefficients in the requested convention.
- signature(object = "BJFilter", convention = "character") returns the filter coefficients in
  the requested convention.
- signature(object = "SPFilter", convention = "character") returns the filter coefficients in
  the requested convention.

```
signature(object = "VirtualArmaFilter", convention = "missing")
```

signature(object = "VirtualArmaFilter", convention = "character") Conceptually, calls
 filterCoef(), with one argument, on the AR and MA parts of the model. If convention
 is present, converts the result to the specified convention. Returns a list with the following
 components:

```
ar AR coefficients.
```

ma MA coefficients.

```
signature(object = "SarimaFilter", convention = "missing")
```

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signature(object = "SarimaFilter", convention = "character") If convention is present, converts the coefficients to the specified convention. AR-like coefficients get the convention for the AR part, Ma-like coefficients get the convention for the MA part. Returns a list with the following components:

nseasons number of seasons.

iorder integration order, number of (non-seasonal) differences.

siorder seasonal integration order, number of seasonal differences.

ar ar coefficients.

ma ma coefficients.

sar seasonal ar coefficients.

sma seasonal ma coefficients.

#### Author(s)

Georgi N. Boshnakov

#### References

Brockwell PJ, Davis RA (1991). *Time series: theory and methods. 2nd ed.*. Springer Series in Statistics. Berlin etc.: Springer-Verlag..

## See Also

filterCoef for examples and related functions

#### **Examples**

## see the examples for ?filterCoef

filterOrder-methods

Methods for function filterOrder in package sarima

#### **Description**

Methods for function filterOrder in package sarima.

## Methods

The following methods ensure that all filters in package sarima have a method for filterOrder.

signature(object = "VirtualMonicFilterSpec") Returns object@order.

signature(object = "SarimaFilter") Returns a list with the following components:

nseasons number of seasons.

iorder integration order, number of (non-seasonal) differences.

siorder seasonal integration order, number of seasonal differences.

ar autoregression order

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```
ma moving average order
sar seasonal autoregression order
sma seasonal moving average order
signature(object = "VirtualArmaFilter") Returns a list with the following components:
    ar autoregression order.
    ma moving average order.
```

## Author(s)

Georgi N. Boshnakov

#### See Also

filterCoef for examples and related functions

## **Examples**

```
## see the examples for ?filterCoef
```

filterPoly-methods

Methods for filterPoly in package sarima

## Description

Methods for filterPoly in package sarima.

#### Methods

The methods for filterPoly take care implicitly for the sign convention used to store the coefficients in the object.

```
signature(object = "BJFilter") A polynomial whose coefficients are the negated filter coeffi-
cients.
```

signature(object = "SPFilter") A polynomial whose coefficients are as stored in the object.

signature(object = "SarimaFilter") Returns a list with the following components:

nseasons number of seasons.

iorder integration order, number of (non-seasonal) differences.

siorder seasonal integration order, number of seasonal differences.

arpoly autoregression polynomial

mapoly moving average polynomial

sarpoly seasonal autoregression polynomial

smapoly seasonal moving average polynomial

**fullarpoly** the polynomial obtained by multiplying out all AR-like terms, including differences.

fullmapoly the polynomial obtained by multiplying out all MA terms

**core\_sarpoly** core seasonal autoregression polynomial. It is such that  $\operatorname{sarpoly}(z) = \operatorname{core\_sarpoly}(z^{nseasons})$  **core\_smapoly** core seasonal moving average polynomial. It is such that  $\operatorname{smapoly}(z) = \operatorname{core\_smapoly}(z^{nseasons})$ 

signature(object = "VirtualArmaFilter") Returns a list with the following components:

ar autoregression polynomial.

ma moving average polynomial.

signature(object = "VirtualMonicFilterSpec") Calls filterPolyCoef(object) and converts the result to a polynomial. Thus, it is sufficient to have a method for filterPolyCoef().

#### Author(s)

Georgi N. Boshnakov

#### See Also

filterCoef for examples and related functions

## **Examples**

## see the examples for ?filterCoef

filterPolyCoef-methods

Methods for filterPolyCoef

# Description

Methods for filterPolyCoef in package sarima.

## Methods

The filterPolyCoef methods return results with the same structure as the corresponding methods for filterPoly but with polynomials replaced by their coefficients. If lag\_0 is FALSE the order 0 coefficients are dropped.

signature(object = "VirtualBJFilter") Calls filterCoef(object), negates the result and
prepends 1 if lag\_0 is TRUE.

signature(object = "VirtualSPFilter") Calls filterCoef(object) and prepends 1 to the
 result if lag\_0 is TRUE.

signature(object = "VirtualArmaFilter") Returns a list with the following components:

ar coefficients of the autoregression polynomial.

ma coefficients of the moving average polynomial.

signature(object = "BJFilter") The coefficients of a polynomial whose coefficients are the negated filter coefficients. This is equivalent to the method for "VirtualBJFilter" but somewhat more efficient.

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signature(object = "SPFilter") The coefficients of a polynomial whose coefficients are as stored in the object. This is equivalent to the method for "VirtualSPFilter" but somewhat more efficient.

signature(object = "SarimaFilter") Returns a list with the same components as the "SarimaFilter" method for filterPoly, where the polynomials are replaced by their coefficients.

## Author(s)

Georgi N. Boshnakov

#### See Also

filterCoef for examples and related functions

## **Examples**

```
## see the examples for ?filterCoef
```

FisherInformation-methods

Fisher information

## **Description**

Compute the Fisher information for the parameters of a model.

#### Usage

```
FisherInformation(model, ...)

## S3 method for class 'Arima'
FisherInformation(model, ...)
```

## Arguments

model a fitted or theoretical model for which a method is available.

... further arguments for methods.

## **Details**

FisherInformation computes the information matrix for the parameters of model. This is a generic function. The methods for objects from S4 classes are listed in section 'Methods'.

Currently package **sarima** defines methods for objects representing fitted or theoretical ARMA and seasonal ARMA models. For integrated models the result should be interpreted as the information matrix after differencing.

For ARMA models the implementation is based on (Friedlander 1984) and (for the seasonal specifics) (Godolphin and Godolphin 2007).

#### Value

a square matrix with attribute "nseasons"

## Methods

This section lists FisherInformation methods for S4 classes.

```
signature(model = "ANY")
signature(model = "SarimaModel")
signature(model = "ArmaModel")
```

#### Author(s)

Georgi Boshnakov

#### References

Friedlander B (1984). "On the computation of the Cramer-Rao bound for ARMA parameter estimation." *IEEE Transactions on Acoustics, Speech, and Signal Processing*, **32**(4), 721-727. doi: 10.1109/TASSP.1984.1164391.

Godolphin EJ, Godolphin JD (2007). "A Note on the Information Matrix for Multiplicative Seasonal Autoregressive Moving-Average Models." Wiley-Blackwell: Journal of Time Series Analysis.

```
## a fitted model (over-parameterised)
seas_spec <- list(order = c(1,0,1), period = 4)
fitted <- arima(rnorm(100), order = c(1,0,1), seasonal = seas_spec)
(fi <- FisherInformation(fitted))
## asymptotic covariance matrix of the ARMA parameters:
fitted$sigma2 * solve(fi) / 100

## a theoretical seasonal ARMA model:
sarima1 <- new("SarimaModel", ar = 0.9, ma = 0.1, sar = 0.5, sma = 0.9, nseasons = 12)
FisherInformation(sarima1)

## a non-seasonal ARMA model:
arma2a1 <- ArmaModel(ar = 0.5, ma = c(0.3, 0.7), sigma2 = 1)
FisherInformation(arma2a1)
## sigma2 is not needed for the information matrix:
arma2a1a <- ArmaModel(ar = 0.5, ma = c(0.3, 0.7))
FisherInformation(arma2a1a) # same as above</pre>
```

fun.forecast 35

fun.forecast	Forecasting functions for seasonal ARIMA models	
--------------	---	--

## **Description**

Forecasting functions for seasonal ARIMA models.

# Usage

```
fun.forecast(past, n = max(2 * length(past), 12), eps = numeric(n), pasteps, ...)
```

# Arguments

past	past values of the time series, by default zeroes.
n	number of forecasts to compute.
eps	values of the white noise sequence (for simulation of future). Currently not used!
pasteps	past values of the white noise sequence for models with MA terms, 0 by default.
•••	specification of the model, passed to new() to create a "SarimaModel" object, see Details.

# **Details**

fun.forecast computes predictions from a SARIMA model. The model is specified using the "..." arguments which are passed to new("SarimaModel", ...), see the description of class "SarimaModel" for details.

Argument past, if provided, should contain a least as many values as needed for the prediction equation. It is harmless to provide more values than necessary, even a whole time series.

fun. forecast can be used to illustrate, for example, the inherent difference for prediction of integrated and seasonally integrated models to corresponding models with roots close to the unit circle.

## Value

the forecasts as an object of class "ts"

#### Author(s)

Georgi N. Boshnakov

```
f1 <- fun.forecast(past = 1, n = 100, ar = c(0.85), center = 5) plot(f1)

f2 <- fun.forecast(past = 8, n = 100, ar = c(0.85), center = 5) plot(f2)
```

36 fun.forecast

```
f3 <- fun.forecast(past = 10, n = 100, ar = c(-0.85), center = 5)
plot(f3)
frw1 <- fun.forecast(past = 1, n = 100, iorder = 1)</pre>
frw2 <- fun.forecast(past = 3, n = 100, iorder = 1)
plot(frw2)
frwa1 <- fun.forecast(past = c(1, 2), n = 100, ar = c(0.85), iorder = 1)
plot(frwa1)
fi2a \leftarrow fun.forecast(past = c(3, 1), n = 100, iorder = 2)
plot(fi2a)
fi2b \leftarrow fun.forecast(past = c(1, 3), n = 100, iorder = 2)
plot(fi2b)
fari1p2 <- fun.forecast(past = c(0, 1, 3), ar = c(0.9), n = 20, iorder = 2)
plot(fari1p2)
fsi1 \leftarrow fun.forecast(past = rnorm(4), n = 100, siorder = 1, nseasons = 4)
plot(fsi1)
fexa <- fun.forecast(past = rnorm(5), n = 100, ar = c(0.85), siorder = 1,
                      nseasons = 4)
plot(fexa)
fi2a \leftarrow fun.forecast(past = rnorm(24, sd = 5), n = 120, siorder = 2,
                      nseasons = 12)
plot(fi2a)
fi1si1a \leftarrow fun.forecast(past = rnorm(24, sd = 5), n = 120, iorder = 1,
                         siorder = 1, nseasons = 12)
plot(fi1si1a)
filsila <- fun.forecast(past = AirPassengers[120:144], n = 120, iorder = 1,
                         siorder = 1, nseasons = 12)
plot(fi1si1a)
m1 \leftarrow list(iorder = 1, siorder = 1, ma = 0.8, nseasons = 12, sigma2 = 1)
m1
x <- sim_sarima(model = m1, n = 500)
acf(diff(diff(x), lag = 12), lag.max = 96)
pacf(diff(diff(x), lag = 12), lag.max = 96)
m2 \leftarrow list(iorder = 1, siorder = 1, ma = 0.8, sma = 0.5, nseasons = 12,
           sigma2 = 1)
m2
x2 <- sim_sarima(model = m2, n = 500)
acf(diff(diff(x2), lag = 12), lag.max = 96)
```

InterceptSpec-class 37

```
pacf(diff(x2), lag = 12), lag.max = 96)
fit2 <- arima(x2, order = c(0, 1, 1),
              seasonal = list(order = c(0, 1, 0), nseasons = 12))
fit2
tsdiag(fit2)
tsdiag(fit2, gof.lag = 96)
x2past <- rnorm(13, sd = 10)
x2 \leftarrow sim_sarima(model = m2, n = 500, x = list(init = x2past))
plot(x2)
fun.forecast(ar = 0.5, n = 100)
fun.forecast(ar = 0.5, n = 100, past = 1)
fun.forecast(ma = 0.5, n = 100, past = 1)
fun.forecast(iorder = 1, ma = 0.5, n = 100, past = 1)
fun.forecast(iorder = 1, ma = 0.5, ar = 0.8, n = 100, past = 1)
fun.forecast(m1, n = 100)
fun.forecast(m2, n = 100)
fun.forecast(iorder = 1, ar = 0.8, ma = 0.5, n = 100, past = 1)
```

InterceptSpec-class Class In

Class InterceptSpec

# **Description**

A helper class from which a number of models inherit intercept, centering and innovations variance.

### **Objects from the Class**

Objects can be created by calls of the form new("InterceptSpec", ...).

### **Slots**

```
center: Object of class "numeric", centering parameter, defaults to zero. intercept: Object of class "numeric", intercept parameter, defaults to zero. sigma2: Object of class "numeric", innovations variance, defaults to NA.
```

#### Methods

```
sigmaSq signature(object = "InterceptSpec"): ...
```

#### Author(s)

Georgi N. Boshnakov

### See Also

```
ArmaModel, SarimaModel
```

38 isStationaryModel

# **Examples**

```
showClass("InterceptSpec")
```

isStationaryModel

Check if a model is stationary

# Description

Check if a model is stationary.

# Usage

```
isStationaryModel(object)
```

# **Arguments**

object

an object

### **Details**

This is a generic function. It returns TRUE if object represents a stationary model and FALSE otherwise.

### Value

TRUE or FALSE

### Methods

```
signature(object = "SarimaSpec")
signature(object = "VirtualIntegratedModel")
signature(object = "VirtualStationaryModel")
```

# Author(s)

Georgi N. Boshnakov

# See Also

nUnitRoots

modelCenter 39

modelCenter

model center

# Description

model center

# Usage

```
modelCenter(object)
```

# Arguments

object

an object

# Methods

```
signature(object = "InterceptSpec")
```

# Author(s)

Georgi N. Boshnakov

modelCoef

Get the coefficients of models

# Description

Get the coefficients of an object, optionally specifying the expected format.

# Usage

```
modelCoef(object, convention, component, ...)
```

# **Arguments**

object an object.

convention the convention to use for the return value, a character string or any object from

a supported class, see Details.

component if not missing, specifies a component to extract, see Details.

. . . not used, further arguments for methods.

40 modelCoef

#### **Details**

modelCoef is a generic function for extraction of coefficients of model objects. What 'coeff-cients' means depends on the class of object but it can be changed with the optional argument convention. In effect, modelCoef provides a very flexible and descriptive way of extracting coefficients from models in various forms.

The one-argument form, modelCoef(object), gives the coefficients of object. In effect it defines, for the purposes of modelCoef, the meaning of 'coefficients' for class class(modelCoef).

Argument convention can be used to specify what kind of value to return.

If convention is not a character string, only its class is used. Conceptually, the value will have the format and meaning of the value that would be returned by a call to modelCoef(obj) with obj from class class(convention).

If convention is a character string, it is typically the name of a class. In this case modelCoef(object, "someclass") is equivalent to modelCoef(object, new("someclass")). Note that this is conceptual - argument convention can be the name of a virtual class, for example. Also, for some classes of object character values other than names of classes may be supported.

For example, if obj is from class "ArmaModel", modelCoef(obj) returns a list with components "ar" and "ma", which follow the "BD" convention. So, to get such a list of coefficients from an object from any class capable of representing ARMA models, set convention = "ArmaModel" in the call to modelCoef{}.

modelCoef() will signal an error if object is not compatible with target (e.g. if it contains unit roots). (see filterCoef if you need to expand any multiplicative filters). **TODO: rethink this, it does not reflect current behaviour!** 

If there is no class which returns exactly what is needed some additional computation may be necessary. In the above "ArmaModel" example we might need the coefficients in the "BJ" convention, so we would need to change the signs of the MA coefficients to achieve this. Since this is a very common operation, a convenience feature is available. Setting convention = "BJ" requests ARMA coefficients with "BJ" convention. For completeness, the the settings "SP" (signal processing) and "BD" (Brockwell-Davis) are also available.

The methods for modelCoef() in package "sarima" return a list with components depending on argument "convention", as outlined above.

#### Value

a list, with components depending on the target class, as described in Details

#### Author(s)

Georgi N. Boshnakov

#### See Also

modelOrder, modelPoly, modelPolyCoef

modelCoef-methods 41

### **Examples**

```
## define a seasonal ARIMA model, it has a number of components
m1 < -new("SarimaModel", iorder = 1, siorder = 1, ma = -0.3, sma = -0.1, nseasons = 12)
## Get the coefficients corresponding to a 'flat' ARMA model,
## obtained by multiplying out AR-like and MA-like terms.
## A simple way is to use modelCoef() with a suitable convention:
modelCoef(m1, "ArmaModel")
modelCoef(m1, "ArmaFilter") ## same
## Here is another model
m1a <- new("SarimaModel", iorder = 1, siorder = 1, ar = 0.6, nseasons = 12)
modelCoef(m1a, "ArmaModel")
modelCoef(m1a, "ArmaFilter") ## same
## if only AR-like terms are allowed in a computation,
## use convention = "ArModel" to state it explicitly.
## this works, since m1a contains only AR-like terms:
modelCoef(m1a, "ArModel")
modelCoef(m1a, "ArFilter") ## same
## ... but these would throw errors if evaluated,
## since model m1a contains both AR-like and MA-like terms,
## Not run:
modelCoef(m1, "ArModel")
modelCoef(m1, "ArFilter")
modelCoef(m1, "MaModel")
modelCoef(m1, "MaFilter")
## End(Not run)
```

modelCoef-methods

Methods for generic function modelCoef

### **Description**

Methods for generic function modelCoef.

#### Methods

```
signature(object = "Autocorrelations", convention = "ComboAutocorrelations", component = "missing")
signature(object = "Autocorrelations", convention = "PartialAutocorrelations", component = "missing")
signature(object = "Autocovariances", convention = "Autocorrelations", component = "missing")
signature(object = "Autocovariances", convention = "ComboAutocorrelations", component = "missing")
```

42 modelCoef-methods

```
signature(object = "Autocovariances", convention = "ComboAutocovariances", component = "missing")
signature(object = "Autocovariances", convention = "PartialAutocorrelations", component = "missing")
signature(object = "ComboAutocorrelations", convention = "Autocorrelations", component = "missing")
signature(object = "ComboAutocorrelations", convention = "PartialAutocorrelations", component = "missin
signature(object = "ComboAutocovariances", convention = "Autocovariances", component = "missing")
signature(object = "ComboAutocovariances", convention = "PartialAutocovariances", component = "missing"
signature(object = "ComboAutocovariances", convention = "PartialVariances", component = "missing")
signature(object = "ComboAutocovariances", convention = "VirtualAutocovariances", component = "missing"
signature(object = "PartialAutocorrelations", convention = "Autocorrelations", component = "missing")
signature(object = "SarimaModel", convention = "ArFilter", component = "missing")
signature(object = "SarimaModel", convention = "ArmaFilter", component = "missing")
signature(object = "SarimaModel", convention = "MaFilter", component = "missing")
signature(object = "SarimaModel", convention = "SarimaFilter", component = "missing")
signature(object = "VirtualAutocovariances", convention = "character", component = "missing")
signature(object = "VirtualAutocovariances", convention = "missing", component = "missing")
signature(object = "VirtualAutocovariances", convention = "VirtualAutocovariances", component = "missin
signature(object = "SarimaModel", convention = "ArModel", component = "missing")
signature(object = "SarimaModel", convention = "MaModel", component = "missing")
signature(object = "VirtualFilterModel", convention = "BD", component = "missing")
signature(object = "VirtualFilterModel", convention = "BJ", component = "missing")
signature(object = "VirtualFilterModel", convention = "character", component = "missing")
signature(object = "VirtualFilterModel", convention = "missing", component = "missing")
signature(object = "VirtualFilterModel", convention = "SP", component = "missing")
signature(object = "ArmaModel", convention = "ArmaFilter", component = "missing")
signature(object = "VirtualAutocovariances", convention = "Autocovariances", component = "missing")
```

modelIntercept 43

### Author(s)

Georgi N. Boshnakov

modelIntercept

Give the intercept parameter of a model

# Description

Give the intercept parameter of a model.

# Usage

```
modelIntercept(object)
```

# Arguments

object

an object from a class for which intercept is defined.

### Methods

```
signature(object = "InterceptSpec")
```

### Author(s)

Georgi N. Boshnakov

modelOrder

Get the model order and other properties of models

# **Description**

Get the model order and other properties of models.

# Usage

```
modelOrder(object, convention, ...)
modelPoly(object, convention, ...)
modelPolyCoef(object, convention, lag_0 = TRUE, ...)
```

# **Arguments**

```
object a model object. convention convention.
```

lag\_0 if TRUE include lag\_0 coef, otherwise drop it.

. . . further arguments for methods.

44 modelOrder

#### **Details**

These functions return the requested quantity, optionally requesting the returned value to follow a specific convention, see also modelCoef.

When called with one argument, these functions return corresponding property in the native format for the object's class.

Argument convention requests the result in some other format. The mental model is that the returned value is as if the object was first converted to the class specified by convention and then the property extracted or computed. Normally, the object is not actually converted to that class. one obvious reason is efficiency but it may also not be possible, for example if argument convention is the name of a virtual class.

For example, the order of a seasonal SARIMA model is specified by several numbers. The call modelOrder(object) returns it as a list with components ar, ma, sar, sma, iorder, siorder and nseasons. For some computations all that is needed are the overall AR and MA orders obtained by multiplying out the AR-like and MA-like terms in the model. The result would be an ARMA filter and could be requested by modelOrder(object, "ArmaFilter").

The above operation is valid for any ARIMA model, so will always succeed. On the other hand, if further computation would work only if there are no moving average terms in the model one could use modelOrder(object, "ArFilter"). Here, if object contains MA terms an error will be raised.

The concept is powerful and helps in writing expressive code. In this example a simple check on the returned value would do but even so, such a check may require additional care.

#### Author(s)

Georgi N. Boshnakov

### See Also

modelCoef

```
m1 <- new("SarimaModel", iorder = 1, siorder = 1, ma = -0.3, sma = -0.1, nseasons = 12)
modelOrder(m1)
modelOrder(m1, "ArmaFilter")
modelOrder(m1, new("ArmaFilter"))
modelPoly(m1, "ArmaModel")
modelPolyCoef(m1, "ArmaModel")</pre>
```

modelOrder-methods 45

modelOrder-methods

Get the order of a model

### **Description**

Get the order of a model.

#### Methods

```
signature(object = "ArmaModel", convention = "ArFilter")
signature(object = "ArmaModel", convention = "MaFilter")
signature(object = "SarimaModel", convention = "ArFilter")
signature(object = "SarimaModel", convention = "ArmaFilter")
signature(object = "SarimaModel", convention = "ArmaModel")
signature(object = "SarimaModel", convention = "ArModel")
signature(object = "SarimaModel", convention = "MaFilter")
signature(object = "SarimaModel", convention = "MaModel")
signature(object = "VirtualFilterModel", convention = "missing")
signature(object = "VirtualFilterModel", convention = "character")
```

#### Author(s)

Georgi N. Boshnakov

modelPoly-methods

Get polynomials associated with SARIMA models

### **Description**

Get polynomials associated with SARIMA models.

#### Methods

```
signature(object = "SarimaModel", convention = "ArmaFilter")
signature(object = "VirtualMonicFilter", convention = "missing")
signature(object = "VirtualFilterModel", convention = "character")
```

#### Author(s)

Georgi N. Boshnakov

46 nSeasons

```
{\tt modelPolyCoef-methods} \ \ \textit{Methods for modelPolyCoef}
```

# **Description**

Methods for modelPolyCoef, e generic function for getting the coefficients of polynomials associated with SARIMA models.

#### Methods

```
signature(object = "SarimaModel", convention = "ArmaFilter")
signature(object = "VirtualMonicFilter", convention = "missing")
signature(object = "VirtualFilterModel", convention = "character")
```

# Author(s)

Georgi N. Boshnakov

nSeasons

Number of seasons

# **Description**

Number of seasons.

# Usage

```
nSeasons(object)
```

# Arguments

object

an object for which the notion of number of seasons makes sense.

#### **Details**

This is a generic function.

#### Value

an integer number

### Methods

```
signature(object = "SarimaFilter")
signature(object = "VirtualArmaFilter")
```

nUnitRoots 47

# Author(s)

Georgi N. Boshnakov

nUnitRoots

Number of unit roots in a model

# Description

Gives the number of roots with modulus one in a model.

# Usage

```
nUnitRoots(object)
```

# Arguments

object

an object.

# **Details**

nUnitRoots() gives the number of roots with modulus one in a model. This number is zero for stationary models, see also isStationaryModel().

### Value

```
a non-negative integer number
```

# Methods

```
signature(object = "SarimaSpec")
signature(object = "VirtualStationaryModel")
```

### Author(s)

Georgi N. Boshnakov

48 nvarOfAcfKP

nvarOfAcfKP

Compute variances of autocorrelations under ARCH-type hypothesis

# Description

Compute variances of autocorrelations under ARCH-type hypothesis.

### Usage

```
nvarOfAcfKP(x, maxlag, center = FALSE, acfscale = c("one", "mom"))
```

### **Arguments**

x time series.

maxlag a positive integer, the maximal lag.

center logical flag, if FALSE, the default, don't center the time series before squaring,

see Details.

acfscale character string, specifying what factor to use for the autocovariances. "one"

stands for 1/n, "mom" for 1/(n-k), where n is the length of x and k is lag.

#### **Details**

nvarOfAcfKP computes estimates of n times the variances of sample autocorrelations of white noise time series. It implements the result of (Kokoszka and Politis 2011) which holds under weak assumptions. In particular, it can be used to test if the true autocorrelations of a time series are equal to zero in GARCH modelling.

### Value

a numeric vector

#### Author(s)

Georgi N. Boshnakov

#### References

Kokoszka PS, Politis DN (2011). "Nonlinearity of ARCH and stochastic volatility models and Bartlett's formula." *Probability and Mathematical Statistics*, **31**(1), 47–59.

### See Also

whiteNoiseTest

```
## see examples for whiteNoisTest()
```

nvcovOfAcf 49

Tiveovor Act Covariances of sample autocorrelations	nvcovOfAcf	Covariances of sample autocorrelations
---	------------	--

### **Description**

Compute covariances of autocorrelations.

#### **Usage**

```
nvcovOfAcf(model, maxlag)
nvcovOfAcfBD(acf, ma, maxlag)
acfOfSquaredArmaModel(model, maxlag)
```

# **Arguments**

model a model, see Details.

maxlag a positive integer number, the maximal lag.

acf autocorrelations.

ma a positive integer number, the order of the MA(q) model. The default is the

maximal lag available in acf.

#### **Details**

nvcov0fAcf computes the unscaled asymptotic autocovariances of sample autocorrelations of ARMA models, under the classical assumptions when the Bartlett's formulas are valid. It works directly with the parameters of the model and uses Boshnakov (1996). Argument model can be any specification of ARMA models for which autocorrelations() will work, e.g. a list with components "ar", "ma", and "sigma2".

nvcov0fAcfBD computes the same quantities but uses the formula given by Brockwell & Davis (1991) (eq. (7.2.6.), p. 222), which is based on the autocorrelations of the model. Argument acf contains the autocorrelations.

For nvcovOfAcfBD, argument ma asks to treat the provided acf as that of MA(ma). Only the values for lags up to ma are used and the rest are set to zero, since the autocorrelations of MA(ma) models are zero for lags greater than ma. To force the use of all autocorrelations provided in acf, set ma to the maximal lag available in acf or omit ma, since this is its default.

acfOfSquaredArmaModel(model, maxlag) is a convenience function which computes the autocovariances of the "squared" model, see Boshnakov (1996).

#### Value

```
an (maxlag, maxlag)-matrix
```

#### Note

The name of nvcov0fAcf stands for "n times the variance-covariance matrix", so it needs to be divided by n to get the asymptotic variances and covariances.

### Author(s)

Georgi N. Boshnakov

#### References

Boshnakov GN (1996). "Bartlett's formulae—closed forms and recurrent equations." *Ann. Inst. Statist. Math.*, **48**(1), 49–59. ISSN 0020-3157, doi: 10.1007/BF00049288.

Brockwell PJ, Davis RA (1991). *Time series: theory and methods. 2nd ed.*. Springer Series in Statistics. Berlin etc.: Springer-Verlag..

#### See Also

```
whiteNoiseTest
```

# **Examples**

```
## MA(2)
ma2 <- list(ma = c(0.8, 0.1), sigma2 = 1)
nv <- nvcovOfAcf(ma2, maxlag = 4)
d <- diag(nvcovOfAcf(ma2, maxlag = 7))
cbind(ma2 = 1.96 * sqrt(d) / sqrt(200), iid = 1.96/sqrt(200))
acr <- autocorrelations(list(ma = c(0.8, 0.1)), maxlag = 7)
nvBD <- nvcovOfAcfBD(acr, 2, maxlag = 4)
all.equal(nv, nvBD) # TRUE</pre>
```

partialAutocorrelations-methods

Methods for function partialAutocorrelations

# Description

Methods for function partial Autocorrelations.

# Methods

```
signature(x = "ANY", maxlag = "ANY", lag_0 = "ANY")
signature(x = "mts", maxlag = "ANY", lag_0 = "missing")
signature(x = "PartialAutocovariances", maxlag = "ANY", lag_0 = "missing")
signature(x = "ts", maxlag = "ANY", lag_0 = "missing")
```

periodogram 51

### Author(s)

Georgi N. Boshnakov

periodogram Obtain the most important period lags of a time series according to a periodogram.	periodogram	Obtain the most important period lags of a time series according to a periodogram.
--	-------------	--

# **Description**

Obtain the most important period lags of a time series according to a periodogram.

### Usage

```
periodogram(x, ..., no.results = 20)
```

# **Arguments**

x A vector containing the time series values

... Arguments to be passed to spectrum

no.results The number of results to be printed at the end. Defaults to the 20 most important

frequencies.

### **Details**

Using the spectral function, obtain spectral density estimates at a number of frequencies and rather than plotting, obtain the rank and period of the values. Return a given number of results based on the level of interest of the user.

### Value

A data.frame containing the following columns:

rank numeric vector containing the ranked importance of the frequency.

spectrum estimates of the spectral density at frequencies corresponding to freq.

frequency vector at which the spectral density is estimated.

period vector of corresponding periods.

52 plot-methods

plot-methods

Plot methods in package sarima

### **Description**

Plot methods in package sarima.

#### Methods

```
signature(x = "SampleAutocorrelations", y = "matrix")
signature(x = "SampleAutocorrelations", y = "missing") plots the sample autocorrelations
with (individual) rejection limits computed under the null hypothesis of i.i.d. (strong white
noise) If argument data is provided, it should be the time series from which the autocorre-
lations were computed. In this case rejection limits for null hypothesis that the time series is
(garch) weak white noise are provided, as well.
```

Additional arguments can be supplied, see whiteNoiseTest the examples, and the vignettes.

signature(x = "SamplePartialAutocorrelations", y = "missing") plots the sample partial autocorrelations with rejection limits for the hypotheses and controlling arguments as for "SampleAutocorrelations".

#### Author(s)

Georgi N. Boshnakov

#### See Also

whiteNoiseTest for the computations for the rejection levels;

```
set.seed(1234)
n <- 5000
x <- sarima:::rgarch1p1(n, alpha = 0.3, beta = 0.55, omega = 1, n.skip = 100)
x.acf <- autocorrelations(x)
x.acf
x.pacf <- partialAutocorrelations(x)
x.pacf

plot(x.acf)
## add limits for a weak white noise test:
plot(x.acf, data = x)

## similarly for pacf
plot(x.pacf)
plot(x.pacf, data = x)

plot(x.acf, data = x, main = "Autocorrelation test")
plot(x.pacf, data = x, main = "Partial autocorrelation test")</pre>
```

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```
plot(x.acf, ylim = c(NA,1))
plot(x.acf, ylim.fac = 1.5)
plot(x.acf, data = x, ylim.fac = 1.5)
plot(x.acf, data = x, ylim = c(NA, 1))
```

prepareSimSarima

Prepare SARIMA simulations

#### **Description**

Prepare SARIMA simulations.

### Usage

# Arguments

model	an object from a suitable class or a list, see Details.
X	initial/before values of the time series, a list, a numeric vector or time series, see Details.
eps	initial/before values of the innovations, a list or a numeric vector, see Details.
n	number of observations to generate, if missing an attempt is made to infer it from $\boldsymbol{x}$ and eps.
n.start	number of burn-in observations.
xintercept	non-constant intercept which may represent trend or covariate effects.
rand.gen	random number generator, defaults to $N(0,1)$ .
	ignored.

#### **Details**

prepareSimSarima does the preparatory work for simulation from a Sarima model, given the specifications and returns a function, which can be called as many times as needed.

The variance of the innovations is specified by the model and the simulated innovations are multiplied by the corresponding standard deviation. So, it is expected that the random number generator simulates from a standardised distribution.

Argument model can be from any class representing models in the SARIMA family, such as "SarimaModel", or a list with components suitable to be passed to =new()= for such models.

The canonical form of argument x is a list with components before, init and main. If any of these components is missing or NULL, it is filled suitably. Any other components of x are ignored. If x is

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not a list, it is put in component main. Conceptually, the three components are concatenated in the given order, the simulated values are put in main (before and init are not changed), the before part is dropped and the rest is returned. In effect, before and init can be viewed as initial values but init is considered part of the generated series.

The format for eps is the same as that of x. The lengths of missing components in x are inferred from the corresponding components of eps, and vice versa.

The format for xintercept is the same as that of x and eps.

print.simSarimaFun is a print method for the objects generated by prepareSimSarima.

#### Value

for prepareSimSarima, a function to simulate time series, see Details. it is typically called multiple times without arguments. All arguments have defaults set by prepareSimSarima.

```
n length of the simulated time series,
rand.gen random number generator,
... arguments for the random number generator, passed on to arima.sim.
```

### Author(s)

Georgi N. Boshnakov

#### See Also

```
sim_sarima
```

```
mo1 <- list(ar = 0.9, iorder = 1, siorder = 1, nseasons = 4, sigma2 = 2)
fs1 <- prepareSimSarima(mo1, x = list(before = rep(0,6)), n = 100)
tmp1 <- fs1()
tmp1
plot(ts(tmp1))

fs2 <- prepareSimSarima(mo1, x = list(before = rep(1,6)), n = 100)
tmp2 <- fs2()
plot(ts(tmp2))

mo3 <- mo1
mo3[["ar"]] <- 0.5
fs3 <- prepareSimSarima(mo3, x = list(before = rep(0,6)), n = 100)
tmp3 <- fs3()
plot(ts(tmp3))</pre>
```

		٠	
sa	r	1	ma

Fit extended SARIMA models

# **Description**

Fit extended SARIMA models, which can include lagged exogeneous variables, general unit root non-stationary factors, multiple periodicities, and multiplicative terms in the SARIMA specification. The models are specified with a flexible formula syntax and contain as special cases many models with specialised names, such as ARMAX and reg-ARIMA.

#### Usage

### **Arguments**

model a model formula specifying the model.

data a list or data frame, usually can be omitted.

ss.method state space engine to use, defaults to "sarima". (Note: this argument will probably be renamed.)

use.symmetry a logical argument indicating whether symmetry should be used to estimate the unit polynomial.

SSinit method to use for computation of the stationary part of the initial covariance matrix, one of "Rossignol2011", "gnb", "Gardner1980".

#### **Details**

sarima fits extended SARIMA models, which can include exogeneous variables, general unit root non-stationary factors and multiplicative terms in the SARIMA specification.

Let  $\{Y_t\}$  be a time series and f(t) and g(t) be functions of time and/or (possibly lagged) exogeneous variables.

An extended pure SARIMA model for  $Y_t$  can be written with the help of the backward shift operator as

$$U(B)\Phi(B)Y_t = \Theta(B)\varepsilon_t,$$

where  $\{\varepsilon_t\}$  is white noise, and U(z),  $\Phi(z)$ , and  $\Theta(z)$  are polynomials, such that all roots of U(z) are on the unit circle, while the roots of  $\Phi(z)$  and  $\Theta(z)$  are outside the unit circle. If unit roots are missing, ie  $U(z) \equiv 1$ , the model is stationary with mean zero.

A reg-SARIMA or X-SARIMA model can be defined as a regression with SARIMA residuals:

$$Y_t = f(t) + Y_t^c$$

$$U(B)\Phi(B)Y_t^c = \Theta(B)\varepsilon_t,$$

where  $Y_t^c = Y_t - f(t)$  is the centred  $Y_t$ . This can be written equivalently as a single equation:

$$U(B)\Phi(B)(Y_t - f(t)) = \Theta(B)\varepsilon_t.$$

The regression function f(t) can depend on time and/or (possibly lagged) exogeneous variables. We call it centering function. If  $Y_t^c$  is stationary with mean zero, f(t) is the mean of  $Y_t$ . If f(t) is constant, say mu,  $Y_t$  is stationary with mean mu. Note that the two-equation form above shows that in that case mu is the intercept in the first equation, so it is perfectly reasonable to refer to it also as intercept but to avoid confusion we reserve the term **intercept** for g(t) below.

If the SARIMA part is stationary, then  $EY_t = f(t)$ , so f(t) can be interpreted as trend. In this case the above specification is often referred to as **mean corrected form** of the model.

An alternative way to specify the regression part is to add the regression function, say  $\{g(t)\}\$ , to the right-hand side of the SARIMA equation:

$$U(B)\Phi(B)Y_t = g(t) + \Theta(B)\varepsilon_t.$$

In the stationary case this is the classical ARMAX specification. This can be written in two-stage form in various ways, eg

$$U(B)\Phi(B)Y_t = (1 - \Theta(B))\varepsilon_t + u_t,$$
  
$$u_t = g(t) + \varepsilon_t.$$

So, in a sense, g(t) is a trend associated with the residuals from the SARIMA modelling. We refer to this form as intercept form of the model (as opposed to the mean-corrected form discussed previously).

In general, if there are no exogeneous variables the mean-corrected model is equivalent to some intercept model, which gives some justification of the terminology, as well. If there are exogeneous variables equivalence may be achievable but at the expense of introducing more lags in the model, whish is not desirable in general.

Some examples of equivalence. Let Y be a stationary SARIMA process (U(z) = 1) with mean  $\mu$ . Then the mean-corrected form of the SARIMA model is

$$\Phi(B)(Y_t - \mu) = \Theta(B)\varepsilon_t$$

while the intercept form is

$$\Phi(B)Y_t = c + \Theta(B)\varepsilon_t,$$

where  $c = \Phi(B)\mu$ . So, in this case the mean-corrected model X-SARIMA model with  $f(t) = \mu$  is equivalent to the intercept model with  $g(t) = \Phi(B)\mu$ .

As another example, with f(t) = bt, the mean-corrected model is  $(1-B)(Y_t - bt) = \varepsilon_t$ . Expanding the left-hand side we obtain the intercept form  $(1-B)Y_t = b + \varepsilon_t$ , which demonstrates that  $Y_t$  is a random walk with drift g(t) = b.

# Model specification

Argument model specifies the model with a syntax similar to other model fitting functions in R. A formula can be given for each of the components discussed above as  $y \sim f$  | SARIMA | g, where f, SARIMA and g are model formulas giving the specifications for the centering function f, the SARIMA specification, and the intercept function g. In normal use only one of f or g will be different from zero. f should always be given (use 0 to specify that it is identical to zero), but g can be omitted altogether. Sometimes we refer to the terms specified by f and g by xreg and regx, respectively.

### Model formulas for trends and exogeneous regressions

The formulas for the centering and intercept (ie f and g) use the same syntax as in linear models with some additional functions for trigonometric trends, polynomial trends and lagged variables.

Here are the available specialised terms:

.p(d) Orthogonal polynomials over 1:length(y) of degree d (starting from degree 1, no constant).

t Stands for 1:length(y). Note that powers need to be protected by I(), e.g.  $y \sim 1 + .t + I(.t^2)$ .

.cs(s, k) cos/sin pair for the k-th harmonic of 2pi/s. Use vector k to specify several harmonics.

**.B**(x, lags) Include lagged terms of x,  $B^{lags}(x[t]) = x[t - lags]$ . lags can be a vector. If x is a matrix, the specified lags are taken from each column.

# Model formulas for SARIMA models

A flexible syntax is provided for the specification of the SARIMA part of the model. It is formed using a number of primitives for stationary and unit root components, which have non-seasonal and seasonal variants. Arbitrary number of multiplicative factors and multiple seasonalities can be specified.

The SARIMA part of the model can contain any of the following terms. They can be repeated as needed. The first argument for all seasonal operators is the number of seasons.

ar(p) autoregression term of order p

ma(q) moving average term of order q

sar(s,p) seasonal autoregression term (s seasons, order p)

sma(s,q) seasonal moving average term (s seasons, order q)

**i(d)**  $(1 - B)^d$ 

s(seas) summation operator,  $(1 + B + \cdots + B^{seas-1})$ 

 $\mathbf{u}(\mathbf{x})$  quadratic unit root term, corresponding to a complex pair on the unit circle. If x is real, it specifies the argument of one of the roots as a fraction of  $2\pi$ . If z is complex, it is the root itself.

The real roots of modulus one (1 and -1) should be specified using i(1) and s(2), which correspond to 1 - B and 1 + B, respectively.

**su(s, h)** quadratic unit root terms corresponding to seasonal differencing factors. h specifies the desired harmonic which should be one of 1,2, ..., [s/2]. Several harmonics can be specified by setting h to a vector.

```
ss(s, p) seasonal summation operator, (1 + B^s + \cdots + B^{(s-1)p})
```

Terms with parameters can contain additional arguments specifying initial values, fixed parameters, and transforms. For ar, ma, sar, sma, values of the coefficients can be specified by an unnamed argument after the parameters given in the descriptions above. In estimation these values will be taken as initial values for optimisation. By default, all coefficients are taken to be non-fixed.

Argument fixed can be used to fix some of them. If it is a logical vector it should be of length one or have the same length as the coefficients. If fixed is of length one and TRUE, all coefficients are fixed. If FALSE, all are non-fixed. Otherwise, the TRUE/FALSE values in fixed determine the fixedness of the corresponding coefficients.

fixed can also be a vector of positive integer numbers specifying the indices of fixed coefficients, the rest are non-fixed.

Sometimes it may be easier to declare more (e.g. all) coefficients as fixed and then 'unfix' selectively. Argument nonfixed can be used to mark some coefficients as non-fixed after they have been declared fixed. Its syntax is the same as for fixed.

TODO: streamline "atanh.tr"

TODO: describe SSinit

### Value

an object from S3 class Sarima

(**Note:** the format of the object is still under development and may change; use accessor functions, such as coef(), where provided.)

#### Note

Currently the implementation of the intercept form (ie the third part of the model formula) is incomplete.

# Author(s)

Georgi N. Boshnakov

#### References

Halliday J, Boshnakov GN (2022). "Partial autocorrelation parameterisation of models with unit roots on the unit circle." doi: 10.48550/ARXIV.2208.05055, https://arxiv.org/abs/2208.05055.

#### See Also

arima

```
## AirPassengers example
## fit the classic airline model using arima()
ap.arima <- arima(log(AirPassengers), order = c(0,1,1), seasonal = c(0,1,1))
## same model using two equivalent ways to specify it
ap.baseA <- sarima(log(AirPassengers) ~</pre>
                    0 \mid ma(1, c(-0.3)) + sma(12,1, c(-0.1)) + i(1) + si(12,1),
                    ss.method = "base")
ap.baseB <- sarima(log(AirPassengers) ~</pre>
                    0 \mid ma(1, c(-0.3)) + sma(12,1, c(-0.1)) + i(2) + s(12),
                    ss.method = "base")
ap.baseA
summary(ap.baseA)
ap.baseB
summary(ap.baseB)
## as above, but drop 1-B from the model:
ap2.arima \leftarrow arima(log(AirPassengers), order = c(0,0,1), seasonal = c(0,1,1))
ap2.baseA <- sarima(log(AirPassengers) ~
                     0 \mid ma(1, c(-0.3)) + sma(12,1, c(-0.1)) +
                                                                     si(12,1),
                     ss.method = "base")
ap2.baseB <- sarima(log(AirPassengers) ~</pre>
                     0 \mid ma(1, c(-0.3)) + sma(12,1, c(-0.1)) + i(1) + s(12),
                     ss.method = "base")
```

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```
## for illustration, here the non-stationary part is
       (1-B)^2(1+B+...+B^5) = (1-B)(1-B^6)
##
       ( compare to (1-B)(1-B^{12}) = (1-B)(1-B^{6})(1+B^{6}))
ap3.base <- sarima(log(AirPassengers) ~</pre>
                   0 \mid ma(1, c(-0.3)) + sma(12,1, c(-0.1)) + i(2) + s(6),
                   ss.method = "base")
## further unit roots, equivalent specifications for the airline model
tmp.su <- sarima(log(AirPassengers) ~</pre>
                 0 \mid ma(1, c(-0.3)) + sma(12,1, c(-0.1)) + i(2) + s(2) + su(12,1:5),
                 ss.method = "base")
tmp.su$interna$delta_poly
prod(tmp.su$interna$delta_poly)
zapsmall(coef(prod(tmp.su$interna$delta_poly)))
tmp.su
tmp.u <- sarima(log(AirPassengers) ~</pre>
                0 \mid ma(1, c(-0.3)) + sma(12,1, c(-0.1)) + i(2) + s(2) + u((1:5)/12),
                ss.method = "base")
tmp.u
```

SarimaModel-class

Class SarimaModel in package sarima

# Description

Class SarimaModel in package sarima.

### **Objects from the Class**

Class "SarimaModel" represents standard SARIMA models. Objects can be created by calls of the form new("SarimaModel", ..., ar, ma, sar, sma), using named arguments in the form slotname = value, where slotname is one of the slots, see below. The arguments have natural defaults. It may be somewhat surprising though that the default for the variance of the innovations (slot "sigma2") is NA. The rationale for this choice is that for some calculations the innovations' variance is not needed and, more importantly, it is far too easy to forget to include it in the model (at least for the author) when the variance matters. The latter may may lead silently to wrong results if the "natural" default value of one is used when sigma2 matters.

The models may be specified in intercept (center = 0) or mean-corrected (intercept = 0) form. Setting both to non-zero values is accepted but rarely needed.

If you waih to modify an existing object from class "SarimaModel", give it as an unnamed argument to "new" and specify only the slots to be changed, see the examples.

Use as. SarimaModel to convert a model fitted with stats::arima() to "SarimaModel".

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#### Slots

center: Object of class "numeric", a number, the ARIMA equation is for X(t) - center.

intercept: Object of class "numeric", a number, the intercept in the ARIMA equation.

sigma2: Object of class "numeric", a positive number, the innovations variance.

nseasons: Object of class "numeric", a positive integer, the number of seasons. For non-seasonal models this is NA.

iorder: Object of class "numeric", non-negative integer, the integration order.

siorder: Object of class "numeric", non-negative integer, the seasonal integration order.

ar: Object of class "BJFilter", the non-seasonal AR part of the model.

ma: Object of class "SPFilter", the non-seasonal MA part of the model.

sar: Object of class "BJFilter", the seasonal AR part of the model.

sma: Object of class "SPFilter", the seasonal MA part of the model.

#### **Extends**

Class "VirtualFilterModel", directly. Class "SarimaSpec", directly. Class "SarimaFilter", by class "SarimaSpec", distance 2. Class "VirtualSarimaFilter", by class "SarimaSpec", distance 3. Class "VirtualCascadeFilter", by class "SarimaSpec", distance 4. Class "VirtualMonicFilter", by class "SarimaSpec", distance 5.

#### Methods

SARIMA models contain as special cases a number of models. The one-argument method of modelCoef is essentially a definition of model coefficients for SARIMA models. The two-argument methods request the model coefficients according to the convention of the class of the second argument. The second argument may also be a character string naming the target class.

Essentially, the methods for modelCoef are a generalisation of as() methods and can be interpreted as such (to an extent, the result is not necessarilly from the target class, not least because the target class may be virtual).

- modelCoef signature(object = "SarimaModel", convention = "missing"): Converts object
  to "SarimaFilter".
- modelCoef signature(object = "SarimaModel", convention = "SarimaFilter"): Converts object
  to "SarimaFilter", equivalent to the one-argument call modelCoef(object).
- **modelCoef** signature(object = "SarimaModel", convention = "ArFilter"): Convert object to "ArFilter". An error is raised if object has non-trivial moving average part.
- modelCoef signature(object = "SarimaModel", convention = "MaFilter"): Convert object
  to "MaFilter". An error is raised if object has non-trivial autoregressive part.
- modelCoef signature(object = "SarimaModel", convention = "ArmaFilter"): Convert object
  to "ArmaFilter". This operation always successeds.
- modelCoef signature(object = "SarimaModel", convention = "character"): The second argument gives the name of the target class. This is conceptually equivalent to modelCoef(object, new(convention)).

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modelOrder gives the order of the model according to the conventions of the target class. An error is raised if object is not compatible with the target class.

```
modelOrder signature(object = "SarimaModel", convention = "ArFilter"): ...
modelOrder signature(object = "SarimaModel", convention = "ArmaFilter"): ...
modelOrder signature(object = "SarimaModel", convention = "ArmaModel"): ...
modelOrder signature(object = "SarimaModel", convention = "Armodel"): ...
modelOrder signature(object = "SarimaModel", convention = "MaFilter"): ...
modelOrder signature(object = "SarimaModel", convention = "MaModel"): ...
modelOrder signature(object = "SarimaModel", convention = "missing"): ...
```

The polynomials associated with object can be obtained with the following methods. Note that target "ArmaFilter" gives the fully expanded products of the AR and MA polynomials, as needed, e.g., for filtering.

```
modelPoly signature(object = "SarimaModel", convention = "ArmaFilter"): 'Gives the fully
expanded polynomials as a list
```

modelPoly signature(object = "SarimaModel", convention = "missing"): Gives the polynomials associated with the model as a list.

modelPolyCoef signature(object = "SarimaModel", convention = "ArmaFilter"): Give the
 coefficients of the fully expanded polynomials as a list.

modelPolyCoef signature(object = "SarimaModel", convention = "missing"): Gives the coefficients of the polynomials associated with the model as a list.

#### Author(s)

Georgi N. Boshnakov

#### See Also

ArmaModel

```
ar1 <- new("SarimaModel", ar = 0.9)
ar1c <- new("SarimaModel", ar = 0.9, intercept = 3)
ar1c
ar1m <- new("SarimaModel", ar = 0.9, center = 1)
ar1m

sm0 <- new("SarimaModel", nseasons = 12)
sm1 <- new("SarimaModel", nseasons = 12, intercept = 3)
sm1
## alternatively, pass a model and modify with named arguments
sm1b <- new("SarimaModel", sm0, intercept = 3)
identical(sm1, sm1b) # TRUE

## in the above models sigma2 is NA</pre>
```

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```
## sm2 - from scratch, the rest modefy an existing model
sm2 <- new("SarimaModel", ar = 0.9, nseasons = 12, intercept = 3, sigma2 = 1)</pre>
sm2a <- new("SarimaModel", sm0, ar = 0.9, intercept = 3, sigma2 = 1)</pre>
sm2b <- new("SarimaModel", sm1, ar = 0.9, sigma2 = 1)</pre>
sm2c <- new("SarimaModel", ar1c, nseasons =12, sigma2 = 1)</pre>
identical(sm2, sm2a) # TRUE
identical(sm2, sm2b) # TRUE
identical(sm2, sm2c) # TRUE
sm3 <- new("SarimaModel", ar = 0.9, sar = 0.8, nseasons = 12, intercept = 3,</pre>
           sigma2 = 1)
sm3b <- new("SarimaModel", sm2, sar = 0.8)
identical(sm3, sm3b) # TRUE
## The classic 'airline model' (from examples for AirPassengers)
(fit <- arima(log10(AirPassengers), c(0, 1, 1),</pre>
              seasonal = list(order = c(0, 1, 1), period = 12)))
as.SarimaModel(fit)
```

se

Compute standard errors

### **Description**

Compute standard errors.

### Usage

```
se(object, ...)
## S4 method for signature 'SampleAutocorrelations'
vcov(object, assuming = "iid", maxlag = maxLag(object), ...)
```

### **Arguments**

object an object containing estimates, such as a fitted model.

... further arguments for vcov.

assuming under what assumptions to do the computations? Currently can be "iid", "garch", a fitted model, or a theoretical model, see Details.

maxlag maximal lag to include

### **Details**

se is a convenience function for the typical case where only the square root of the diagonal of the variance-covariance matrix is needed.

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The method for vcov gives the variance-covariance matrix of the first maxlag autocorrelation coefficients in the object. The result depends on the underlying assumptions and the method of calculation. These can be specifyed with the additional arguments.

Argument "assuming" can be though also as specifying a null hypothesis. Setting it to "iid" or "garch" corresponds to strong white noise (iid) and weak white noise, respectively.

Setting "assuming" to an ARMA model (theoretical or fitted) specifies that as the null model.

**Note:** The method for vcov is not finalised yet. It is used by a method for confint. Bug reports and requests on the github repo may bring this closer to the top of my task list.

### Value

```
for se, a numeric vector giving standard errors; for the vcov method, a square matrix
```

### See Also

```
link{confint}, vcov
```

sigmaSq

Get the innovation variance of models

# **Description**

Get the innovation variance of models.

### Usage

```
sigmaSq(object)
```

#### Arguments

object

an object from a suitable class.

#### **Details**

sigmaSq() gives the innovation variance of objects from classes for which it makes sense, such as ARMA models.

The value depends on the class of the object, e.g. for ARMA models it is a scalar in the univariate case and a matrix in the multivariate one.

#### Methods

```
signature(object = "InterceptSpec")
```

# Author(s)

Georgi N. Boshnakov

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sim_sarima	Simulate trajectories of seasonal arima models	

### **Description**

Simulate trajectories of seasonal arima models.

# Usage

### **Arguments**

model specification of the model, a list or a model object, see 'Details'.

rand.gen random number generator for the innovations.

n length of the time series.

n.start number of burn-in observations.

x initial/before values of the time series, a list, a numeric vector or time series, see Details.

eps initial/before values of the innovations, a list or a numeric vector, see Details.

xintercept non-constant intercept which may represent trend or covariate effects.

xcenter currently ignored.

#### **Details**

The model can be specified by a model object, e.g., from class SarimaModel. It can also be a list with elements suitable to be passed to new("SarimaModel", ...), see the description of class "SarimaModel". Here are some of the possible components:

additional arguments for arima. sim and rand. gen, see 'Details'.

**nseasons** number of seasons in a year (or whatever is the larger time unit) **iorder** order of differencing, specifies the factor  $(1-B)^{d1}$  for the model. **siorder** order of seasonal differencing, specifies the factor  $(1-B^{period})^{ds}$  for the model. **ar** ar parameters (non-seasonal) **ma** ma parameters (non-seasonal) **sar** seasonal ar parameters **sma** seasonal ma parameters

Additional arguments for rand.gen may be specified via the "..." argument. In particular, the length of the generated series is specified with argument n. Arguments for rand.gen can also be passed via the "..." argument.

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If the model is stationary the generated time series is stationary starting with the first value. In particular, there is no need for a 'warm-up' period.

Information about the model is printed on the screen if info = "print". To suppress this, set info to any other value.

For multple simulations with the same (or almost the same) setup, it is better to execute prepareSimSarima once and call the function returned by it as many times as needed.

### Value

an object of class "ts", a simulated time series from the given model

#### Author(s)

Georgi N. Boshnakov

```
require("PolynomF") # guaranteed to be available since package "sarima" imports it.
x <- sim_sarima(n=144, model = list(ma=0.8))
                                                             # MA(1)
x <- sim_sarima(n=144, model = list(ar=0.8))</pre>
                                                             # AR(1)
x \leftarrow sim_sarima(n=144, model = list(ar=c(rep(0,11),0.8))) # SAR(1), 12 seasons
x \leftarrow sim_sarima(n=144, model = list(ma=c(rep(0,11),0.8))) # SMA(1)
                                   # more enlightened SAR(1) and SMA(1)
x < -sim_sarima(n=144, model=list(sar=0.8, nseasons=12, sigma2 = 1)) # SAR(1), 12 seasons
x < - sim_sarima(n=144, model=list(sma=0.8, nseasons=12, sigma2 = 1)) # SMA(1)
x <- sim_sarima(n=144, model = list(iorder=1, sigma2 = 1)) # (1-B)X_t = e_t (random walk)
acf(x)
acf(diff(x))
x <- sim_sarima(n=144, model = list(iorder=2, sigma2 = 1)) # (1-B)^2 X_t = e_t
x <- sim_sarima(n=144, model = list(siorder=1,</pre>
                                     nseasons=12, sigma2 = 1)) # (1-B)^{12} X_t = e_t
x <- sim_sarima(n=144, model = list(iorder=1, siorder=1,
                                     nseasons=12, sigma2 = 1))
x <- sim_sarima(n=144, model = list(ma=0.4, iorder=1, siorder=1,
                                     nseasons=12, sigma2 = 1))
x <- sim_sarima(n=144, model = list(ma=0.4, sma=0.7, iorder=1, siorder=1,
                                     nseasons=12, sigma2 = 1))
x <- sim_sarima(n=144, model = list(ar=c(1.2,-0.8), ma=0.4,
                                     sar=0.3, sma=0.7, iorder=1, siorder=1,
                                     nseasons=12, sigma2 = 1))
x <- sim_sarima(n=144, model = list(iorder=1, siorder=1,</pre>
                                     nseasons=12, sigma2 = 1),
                x = list(init=AirPassengers[1:13]))
```

66 spectrum

```
p \leftarrow polynom(c(1,-1.2,0.8))
solve(p)
abs(solve(p))
sim_sarima(n=144, model = list(ar=c(1.2,-0.8), ma=0.4, sar=0.3, sma=0.7,
                                iorder=1, siorder=1, nseasons=12))
x <- sim_sarima(n=144, model=list(ma=0.4, iorder=1, siorder=1, nseasons=12))
acf(x, lag.max=48)
x <- sim_sarima(n=144, model=list(sma=0.4, iorder=1, siorder=1, nseasons=12))
acf(x, lag.max=48)
x <- sim_sarima(n=144, model=list(sma=0.4, iorder=0, siorder=0, nseasons=12))
acf(x, lag.max=48)
x <- sim_sarima(n=144, model=list(sar=0.4, iorder=0, siorder=0, nseasons=12))
acf(x, lag.max=48)
x \leftarrow sim_sarima(n=144, model=list(sar=-0.4, iorder=0, siorder=0, nseasons=12))
acf(x, lag.max=48)
x <- sim_sarima(n=144, model=list(ar=c(1.2, -0.8), ma=0.4, sar=0.3, sma=0.7,
                                   iorder=1, siorder=1, nseasons=12))
## use xintercept to include arbitrary trend/covariates
sim_sarima(n = 144, model = list(sma = 0.4, ma = 0.4, sar = 0.8, ar = 0.5,
    nseasons = 12, sigma2 = 1), xintercept = 1:144)
```

spectrum

Spectral Density

### **Description**

Estimate the spectral density of a time series or compute the spectral density associated with a time series model.

### Usage

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```
## $3 method for class 'SarimaModel'
spectrum(x, standardize = TRUE, ...)
## $3 method for class 'function'
spectrum(x, standardize = TRUE, param = list(), ...)
```

#### **Arguments**

x a model or a univariate or multivariate time series.

standardize if TRUE, the default method standardises the time series before computing the

periodogram, while the methods for models scale the spectral density so that it

is a probability density function.

raw if TRUE, the default, compute a completely raw periodogram, unless further ar-

guments request otherwise, see section Details.

taper, demean, detrend

see spec.pgram and section 'Details'.

... further arguments for the default method. Currently not used by other methods.

n.head how many rows to print?

sort TRUE, FALSE or "max", see section 'Details".

param a named list, specying model parameters for the "function" method, see sec-

tion 'Details'.

#### **Details**

spectrum in package **sarima** is a generic function with a default method its namesake in package **stats**, see spectrum for a full description of its functionality.

Autoprinting of objects returned by spectrum prints concise information and plots the spectrum. This means that a plot is produced, for example, when the result of a call to spectrum() is not assigned to a variable or if a command containing just the name of the object is executed. If you don't want the graph, just assign the result to a variable. For more control over the printing (for example, number of digits) use print(object, ...) explicitly. In that case no plot is produced. If additional graphical parameters are desired, call plot, ....

All methods print some basic information about the object and a table giving the most influential frequencies and their contributions to the spectrum.

Methods for objects representing ARIMA and SARIMA models (fitted or theoretical) compute the corresponding spectral densities. For non-stationary models, the spectral density for the stationary part. These methods for spectrum return objects from class "Spectrum". If standardize = TRUE the spectral density is scaled, so that it integrates to one (and so is a probability density function). For fitted models confidence bands are not computed currently.

The method for class "function" can be used to create objects from class "Spectrum" using a user specified function. The first argument of that function needs to be a vector of frequencies for which to calculate the spectrum. It is conventionally called freq but this is not required. If there are parameters they should not be part of the signature of the function but need to be listed and given values as a named list via argument param, see the examples for class "Spectrum". This method is somewhat experimental but the restrictions might be relaxed in a future release.

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The rest of this section describes the default method. For futher details on the other methods see "Spectrum".

### The default method for spectrum:

The default method is a wrapper for stats::spectrum().

The default method returns an object from class "genspec". It inherits from "spec", the class returned by stats::spectrum, and adds some additional components. The main difference though is that it has a print method, which plots the object as discussed above. raw = FALSE with no further arguments is equivalent to stats::spectrum(object) and computes a raw periodogram (for the standardised time series if standardize = TRUE). This still detrends and tapers the series though. raw = TRUE sets detrend to FALSE, taper to zero, and demean to TRUE, to compute a 'completely raw' periodogram. In both cases, further arguments are respected.

Argument sort of the print method for "genspec" controls the sorting order of the columns of the printed table. If FALSE, no sorting is done. If TRUE, the spectrum is sorted in decreasing order, so the first row contains the frequency with the highest value of the spectrum. If "max", the local maxima are found and sorted in decreasing order, followed by the rest, also sorted in decreasing order. Note that due to aliasing the local maxima may be shifted from the "true" frequency (e.g. not be exactly on the harmonics of the number of seasons). Tapering and smoothing parameters may help.

The plot method for class "genspec" is inherited from that for "spec", see ?plot.spec.

#### Value

for the default method, an object of class "genspec", which inherits from "spec", and contains the following additional components:

```
standardized TRUE or FALSE,

nseasons number of seasons,

freq.range numeric(2), the frequency range - (-m/2, m/2], where m = floor(frequency(x));

for the remaining methods, an object of class "Spectrum".
```

# Author(s)

Georgi N. Boshnakov

#### See Also

```
spectrum which is called by the default method to do the work.

class "Spectrum" for further details on the methods for objects returned by spectrum().
```

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```
(TODO: complete the reference)
spectrum(ArmaModel(ma = c(-1, 0.6), sigma2 = 1))
spectrum(ArmaModel(ar = 0.5, sigma2 = 1))
spectrum(ArmaModel(ar = 0.5, ma = -0.8, sigma2 = 1))
spectrum(new("SarimaModel", ar = 0.5, sar = 0.9, nseasons = 12, sigma2 = 1))
mo < -new("SarimaModel", ma = -0.4, sma = -0.9, nseasons = 12, sigma2 = 1)
sp1.mo <- spectrum(mo)</pre>
## this also plots the object. (if you are reading the web version, generated
       by pkgdown, it may not be showing some of the graphs,
##
       I haven't figured out why.)
show(sp1.mo) # equivalently, just sp1.mo
print(sp1.mo)
print(sp1.mo, digits = 4)
plot(sp1.mo)
plot(sp1.mo, standardize = FALSE)
## the object can be used as a function:
head(sp1.mo())
sp1.mo(seq(0, 0.5, length.out = 12))
sp1.mo(seq(0, 0.5, length.out = 12), standardize = FALSE)
sarima1b <- new("SarimaModel", ar = 0.9, ma = 0.1, sar = 0.5, sma = 0.9,</pre>
                nseasons = 12, sigma2 = 1)
spectrum(sarima1b)
## default method for spectrum()
## frequency range is c(-1/2, 1/2] since frequency(x) = 1
frequency(lh)
spectrum(lh)
## frequency range is c(-12/2, 12/2] since frequency(x) = 12
frequency(ldeaths)
( sp <- spectrum(ldeaths) )</pre>
print(sp) # equivalently: print(sp, sort = TRUE)
print(sp, sort = FALSE, n.head = 3)
print(sp, sort = "max")
plot(sp)
plot(sp, log = "dB") # see ?plot.spec for further arguments
```

Spectrum-class

Class "Spectrum"

### **Description**

Objects from class "Spectrum" spectra computed by spectrum.

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### Usage

```
## S3 method for class 'Spectrum'
print(x, ..., n = 128, standardize = TRUE)

## S3 method for class 'Spectrum'
plot(x, y, to, from = y, n = 128, standardize = TRUE,
    log = NULL, main = "Spectral density", xlab = "Frequency", ylab = NULL, ...)
```

### **Arguments**

x	a "Spectrum" object.
у	not used but same as from
from, to	interval of frequencies to plot, defaults to $[0, 1/2]$ .
n	number of points to plot (for the plot method), number of points to look at for the peaks and troughs (print method).
standardize	if TRUE make the spectral density integrate to one (i.e., be a probability density function).
log	if log = "y" plot the logarithm of the spectral density, see ?plot.default.
main	a character string, the title of the plot.
xlab	a character string, the label for the x-axis.
ylab	a character string, the label for the y-axis. If NULL, the default, the label is set to "Spd" or " $\log(Spd)$ ", depending on the value of argument $\log$ .

#### **Details**

"Spectrum" is an S4 class and as such autoprinting calls the "Spectrum" method for show(), which prints and plots. show has a single argument, the object. For more control over printing, call print which has additional arguments. Similarly, call plot for more flexible graphics.

for print, further arguments for print.default();

for plot, further arguments for curve.

print(object) (i.e., without further arguments) is equivalent to show(object), except that the former returns object while the latter returns NULL (both invisibly), as is standard for these functions. If print is called with further arguments. the spectrum is not plotted.

The peaks and throughs printed by print are computed by evaluating the spectral density at n equially spaced points and recording the maxima of the resulting discrete sequence. Set argument n to get a finer/coarser grid or to force calculations for particular frequencies. For example, a multiple of 12 may be suitable for n if the data is monthly.

Except for x and standardize the arguments of the plot method are as for curve. With the default standardize = TRUE the spectral density integrates to one over one whole period (usually (-1/2,1/2] but due to its symmetry it is usually plotted over the second half of that interval.

### **Objects from the Class**

Objects contain spectra produced by sarima::spectrum, see spectrum for details.

Objects can also be created by calling "new" but this is not recommended and currently considered internal.

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### **Slots**

```
.Data: Object of class "function" ~~
call: Object of class "call" ~~
model: Object of class "ANY", the underlying model.
```

#### Methods

```
plot signature(x = "Spectrum", y = "ANY"): plots x.
show signature(object = "Spectrum"):
    plots object and prints succinct information about it, including the peaks and troughs in the spectral density. It is equivalent to calling print and plot with a single argument, see section
```

### Author(s)

Georgi N. Boshnakov

'Details'.

#### See Also

spectrum for details and further examples, ArmaSpectrum for ARMA spectra

```
## ARFIMA(0,d,0) with parameters 'freq' and 'd'
spARFIMA0d0 \leftarrow function(freq){ sigma2 / (2 * sin(2*pi*freq/2)^(2 * d)) }
sp <- spectrum(spARFIMA0d0, param = list(sigma2 = 1, d = 0.2))</pre>
print(sp, digits = 4)
## evaluate the spd at selected frequencies
sp(c(0:4 / 8))
## argument 'freq' doesn't need to be called 'freq' but it needs to be
## the first one. This is equivalent to above:
spARFIMA0d0b \leftarrow function(x) \{ sigma2 / (2 * sin(2*pi*x/2)^(2 * d)) \}
spb <- spectrum(spARFIMA0d0b, param = list(sigma2 = 1, d = 0.2))</pre>
plot(spb)
## An example without parameters, as above with sigma2 = 1, d = 0.2 hard
## coded:
spARFIMA0d0c \leftarrow function(freq) \{ 1 / (2 * sin(2*pi*freq/2)^(2 * 0.2)) \}
spc <- spectrum(spARFIMA0d0c)</pre>
print(spc, digits = 4)
spc(c(0:4 / 8))
all.equal(spc(c(0:4 / 8)), sp(c(0:4 / 8))) # TRUE
```

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summary.SarimaModel

Methods for summary in package sarima

# Description

Methods for summary in package sarima.

### Usage

```
## S3 method for class 'SarimaModel'
summary(object, ...)
## S3 method for class 'SarimaFilter'
summary(object, ...)
## S3 method for class 'SarimaSpec'
summary(object, ...)
```

# Arguments

object an object from the corresponding class.
... further arguments for methods.

#### Author(s)

Georgi N. Boshnakov

tsdiag.Sarima

Diagnostic Plots for fitted seasonal ARIMA models

# Description

Produce diagnostics for fitted seasonal ARIMA models. The method offers several portmanteau tests (including Ljung-Box, Li-McLeod and Box-Pierce), plots of autocorrelations and partial autocorrelations of the residuals, ability to control which graphs are produced (including interactively), as well as their layout.

# Usage

```
## S3 method for class 'Sarima'
tsdiag(object, gof.lag = NULL, ask = FALSE, ..., plot = 1:3, layout = NULL)
# if 'object' is not produced by sarima(), use the full name,
# 'tsdiag.Sarima()', in the call. The arguments are the same.
```

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# Arguments

object fitted (seasonal) ARIMA model. currently the output of sarima, stats::arima

or compatible (e.g., forecast::Arima and forecast::auto.arima). If object is not from sarima, use the full name, tsdiag.Sarima, of the method when

calling it, see the examples.

gof.lag maximal lag for portmanteau tests.

ask if TRUE present a menu of available plots, see Details.

... not used.

plot if TRUE all available plots; a vector of positive integers specifies a subset of the

available plots.

layout a list with arguments for graphics::layout for the plots. The default is as for

the ARIMA method of stats::tsdiag.

#### **Details**

Compute and graph diagnostics for seasonal ARIMA models. For objects of class "Sarima" (produced by sarima) just call the generic, tsdiag. The method can be called also directly on the output from base R's arima() with tsdiag.Sarima() or sarima::tsdiag.Sarima().

The method offers several portmanteau tests (including Ljung-Box, Li-McLeod and Box-Pierce), plots of autocorrelations and partial autocorrelations of the residuals, ability to control which graphs are produced (including interactively), as well as their layout.

The method always makes a correction of the degrees of freedom of the portmanteau tests (roughly, subtracting the number of estimated ARMA parameters). Note that stats::tsdiag doesn't do that.

plot can be TRUE to ask for all plots or a vector of positive integers specifying which plots to consider. Currently the following options are available:

- 1 residuals
- 2 acf of residuals
- 3 p values for Ljung-Box statistic
- 4 p values for Li-McLeod statistic
- 5 p values for Box-Pierce statistic
- 6 pacf of residuals

The default is plot = 1:3, which produces a plot similar to the one from stats::tsdiag (but with adjusted d.f., see above). If plot is TRUE, you probably need also ask = TRUE.

If argument plot is of length two the graphics window is split into 2 equal subwindows. Argument layout can still be used to change this. If argument plot is of length one the graphics window is not split at all.

In interactive sessions, if the number of requested graphs (as specified by argument plot) is larger than the number of graphs specified by the layout (by default 3), the function makes the first graph and then presents a menu of the requested plots.

Argument layout can be used to change the layout of the plot, for example to put two graphs per plot, see the examples. Currently it should be a list of arguments for layout, see ?layout. Don't call layout youself, as that will change the graphics device prematurely.

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The computed results are returned (invisibly). This is another difference from stats::tsdiag which doesn't return them.

#### Value

a list with components:

residuals

LjungBox

Ljung box test

LiMcLeod test

BoxPierce

BoxPierce test

Only components that are actually computed are included, the rest are NULL or absent.

## Author(s)

Georgi N. boshnakov

#### See Also

tsdiag

# **Examples**

```
ap.baseA <- sarima(log(AirPassengers) ~</pre>
    0 \mid ma(1, c(-0.3)) + sma(12,1, c(-0.1)) + i(1) + si(12,1),
    ss.method = "base")
tsdiag(ap.baseA)
## apply the method on objects from arima()
ap.arima \leftarrow arima(log(AirPassengers), order = c(0,1,1), seasonal = c(0,1,1))
tsdiag.Sarima(ap.arima)
## use Li-McLeod test instead of Ljung-Box
tsdiag.Sarima(ap.arima, plot = c(1:2,4))
## call R's tsdiag method, for comparison:
tsdiag(ap.arima, plot = c(1:2,4))
## plot only acf an p-values
tsdiag.Sarima(ap.arima, plot = c(2:3), layout = list(matrix(1:2, nrow = 2)))
## plot only acf an p-values
tsd <- tsdiag.Sarima(ap.arima, plot = c(2:3), layout = list(matrix(1:2, nrow = 2)))
## the results can be used for further calculations:
head(tsd$LjungBox$test, 4)
## plot resid, acf, and p-values, leaving half the space for residuals
# tsdiag.Sarima(ap.arima, plot = c(1:3), layout = list(matrix(1:3, nrow = 3),
#
                                                        heights = c(1,2,2))
```

whiteNoiseTest 75

	whiteNoiseTest	White noise test
--	----------------	------------------

# Description

White noise tests.

# Usage

```
whiteNoiseTest(object, h0, ...)
```

# **Arguments**

object an object, such as sample autocorrelations or partial autocorrelations.

h0 the null hypothesis, currently "iid" or "garch".

... additional arguments passed on to methods.

#### **Details**

whiteNoiseTest carries out tests for white noise. The null hypothesis is identified by argument h0, based on which whiteNoiseTest chooses a suitable function to call. The functions implementing the tests are also available to be called directly and their documentation should be consulted for further arguments that are available.

If h0 = "iid", the test statistics and rejection regions can be use to test if the underlying time series is iid. Argument method specifies the method for portmanteau tests: one of "LiMcLeod" (default), "LjungBox", "BoxPierce".

If h0 = "garch", the null hypothesis is that the time series is GARCH, see Francq & Zakoian (2010). The tests in this case are based on a non-parametric estimate of the asymptotic covariance matrix.

Portmonteau statistics and p-values are computed for the lags specified by argument nlags. If it is missing, suitable lags are chosen automatically.

If argument interval is TRUE, confidence intervals for the individual autocorrelations or partial autocorrelations are computed.

# Value

a list with component test and, if ci=TRUE, component ci.

## Note

Further methods will be added in the future.

# Author(s)

Georgi N. Boshnakov

## References

Francq C, Zakoian J (2010). *GARCH models: structure, statistical inference and financial applications*. John Wiley & Sons. ISBN 978-0-470-68391-0.

Li WK (2004). Diagnostic checks in time series. Chapman & Hall/CRC Press.

## See Also

```
acfGarchTest (h0 = "garch"), acfIidTest (h0 = "iid");
acfMaTest
```

## **Examples**

```
n <- 5000
x <- sarima:::rgarch1p1(n, alpha = 0.3, beta = 0.55, omega = 1, n.skip = 100)
x.acf <- autocorrelations(x)
x.pacf <- partialAutocorrelations(x)

x.iid <- whiteNoiseTest(x.acf, h0 = "iid", nlags = c(5,10,20), x = x, method = "LiMcLeod")
x.iid

x.iid2 <- whiteNoiseTest(x.acf, h0 = "iid", nlags = c(5,10,20), x = x, method = "LjungBox")
x.iid2

x.garch <- whiteNoiseTest(x.acf, h0 = "garch", nlags = c(5,10,20), x = x)
x.garch</pre>
```

xarmaFilter

Applies an extended ARMA filter to a time series

# **Description**

Filter time series with an extended arma filter. If whiten is FALSE (default) the function applies the given ARMA filter to eps (eps is often white noise). If whiten is TRUE the function applies the "inverse filter" to x, effectively computing residuals.

# Usage

# **Arguments**

X	the time series to be filtered, a vector.
eps	residuals, a vector or NULL.
model	the model parameters, a list with components "ar", "ma", "center" and "intercept", see Details.
from	the index from which to start filtering.

whiten if TRUE use x as input and apply the inverse filter to produce eps ("whiten" x),

if FALSE use eps as input and generate x ("colour" eps).

xcenter a vector of means of the same length as the time series, see Details.

xintercept a vector of intercepts having the length of the series, see Details.

#### **Details**

The model is specified by argument model, which is a list with the following components:

ar the autoregression parameters,

ma the moving average parameters,

center center by this value,

intercept intercept.

model\$center and model\$intercept are scalars and usually at most one of them is nonzero. They can be considered part of the model specification. In contrast, arguments xcenter and xintercept are vectors of the same length as x. They can represent contributions from covariate variables. Usually at most one of xcenter and xintercept is used.

The description below uses  $\mu_t$  and  $c_t$  for the contributions by model\$center plus xcenter and model\$intercept plus xintercept, respectively. The time series  $\{x_t\}$  and  $\{\varepsilon_t\}$  are represented by x and eps in the R code. Let

$$y_t = x_t - \mu_t$$

be the centered series. where the centering term  $\mu_t$  is essentially the sum of center and xcenter and is not necessarilly the mean. The equation relating the centered series,  $y_t = x_t - \mu_t$ , and eps is the following:

$$y_t = c_t + \sum_{i=1}^{p} \phi(i) y_{t-i} + \sum_{i=1}^{q} \theta(i) \varepsilon_{t-i} + \varepsilon_t$$

where  $c_t$  is the intercept (basically the sum of intercept with xintercept).

If whiten = FALSE,  $y_t$  is computed for t=from,...,n using the above formula, i.e. the filter is applied to get y from eps (and some initial values). If eps is white noise, it can be said that y is obtained by "colouring" the white noise eps. This can be used, for example, to simulate ARIMA time series. Finally, the centering term is added back,  $x_t = y_t + \mu_t$  for t=from,...,n, and the modified x is returned. The first from - 1 elements of x are left unchanged.

The inverse filter is obtained by rewriting the above equation as an equation expressing  $\varepsilon_t$  in terms of the remaining quantities:

$$\varepsilon_t = -c_t - \sum_{i=1}^q \theta(i)\varepsilon_{t-i} - \sum_{i=1}^p \phi(i)y_{t-i} + y_t$$

If whiten = TRUE, xarmaFilter uses this formula for t=from, ..., n to compute eps from y (and some initial values). If eps is white noise, then it can be said that the time series y has been whitened.

In both cases the first few values in x and/or eps are used as initial values.

The centering is formed from model\$center and argument xcenter. If model\$center is supplied it is recycled to the length of the series, x, and subtracted from x. If argument xcenter is supplied,

it is subtracted from x. If both model\$center and xcenter are supplied their sum is subtracted from x.

xarmaFilter can be used to simulate ARMA series with the default value of whiten = FALSE. In this case eps is the input series and y the output: Then model\$center and/or xcenter are added to y to form the output vector x.

Residuals corresponding to a series x can be obtained by setting whiten = TRUE. In this case x is the input series. The elements of the output vector eps are calculated by the formula for  $\varepsilon_t$  given above. There is no need in this case to restore x since eps is returned.

In both cases any necessary initial values are assumed to be already in the vectors and provide the first from – 1 values in the returned vectors. Argument from should not be smaller than the default value max(p,q)+1.

xarmaFilter calls the lower level function coreXarmaFilter to do the computation.

#### Value

the result of applying the filter or its inverse, as descibed in Details: if whiten = FALSE, the modified x; if whiten = TRUE, the modified eps.

#### Author(s)

Georgi N. Boshnakov

## **Examples**

```
## define a seasonal ARIMA model
m1 < -new("SarimaModel", iorder = 1, siorder = 1, ma = -0.3, sma = -0.1, nseasons = 12)
model0 <- modelCoef(m1, "ArmaModel")</pre>
model1 <- as(model0, "list")</pre>
ap.1 <- xarmaFilter(model1, x = AirPassengers, whiten = TRUE)
ap.2 <- xarmaFilter(model1, x = AirPassengers, eps = ap.1, whiten = FALSE)
ap <- AirPassengers</pre>
ap[-(1:13)] \leftarrow 0  # check that the filter doesn't use x, except for initial values.
ap.2a <- xarmaFilter(model1, x = ap, eps = ap.1, whiten = FALSE)</pre>
ap.2a - ap.2 \# indeed = 0
##ap.3 <- xarmaFilter(model1, x = list(init = AirPassengers[1:13]), eps = ap.1, whiten = TRUE)</pre>
## now set some non-zero initial values for eps
eps1 <- numeric(length(AirPassengers))</pre>
eps1[1:13] <- rnorm(13)
ap.A <- xarmaFilter(model1, x = AirPassengers, eps = eps1, whiten = TRUE)</pre>
ap.Ainv <- xarmaFilter(model1, x = ap, eps = ap.A, whiten = FALSE)
AirPassengers - ap.Ainv # = 0
## compare with sarima.f (an old function)
## compute predictions starting at from = 14
pred1 <- sarima.f(past = AirPassengers[1:13], n = 131, ar = model1$ar, ma = model1$ma)</pre>
pred2 <- xarmaFilter(model1, x = ap, whiten = FALSE)</pre>
pred2 <- pred2[-(1:13)]</pre>
```

all(pred1 == pred2) ##TRUE

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