Package 'MVar'

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Type Package

Title Multivariate Analysis

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Imports graphics,grDevices,MASS,stats

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Description Package for multivariate analysis, having functions that perform simple correspondence analysis (CA) and multiple correspondence analysis (MCA), principal components analysis (PCA), canonical correlation analysis (CCA), factorial analysis (FA), multidimensional scaling (MDS), linear (LDA) and quadratic discriminant analysis (QDA), hierarchical and non-hierarchical cluster analysis, simple and multiple linear regression, multiple factor analysis (MFA) for quantitative, qualitative, frequency (MFACT) and mixed data, biplot, scatter plot, projection pursuit (PP), grant tour method and other useful functions for the multivariate analysis.

License GPL (>= 2)

NeedsCompilation yes

Repository CRAN

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R topics documented:

`Biplot` *Biplot graph.*

Description

Plots the Biplot graph.

Usage

```
Biplot(data, alpha = 0.5, title = NA, xlabel = NA, ylabel = NA,
       size = 1.1, grid = TRUE, color = TRUE, var = TRUE,
       obs = TRUE, linlab = NA, class = NA, classcolor = NA,
       posleg = 2, boxleg = TRUE, axes = TRUE, savptc = FALSE,
       width = 3236, height = 2000, res = 300)
```

Arguments

data	Data for plotting.
alpha	Representativeness of the individuals (alpha), representativeness of the variables (1 - alpha), being 0.5 the default.
title	Titles of the graphics, if not set, assumes the default text.
xlabel	Names the X axis, if not set, assumes the default text.
ylabel	Names the Y axis, if not set, assumes the default text.
size	Size of the points in the graphs.
grid	Put grid on graphs (default = TRUE).
color	Colored graphics (default = TRUE).
var	Adds the variable projections to graph (default = TRUE).
obs	Adds the observations to graph (default = TRUE).
linlab	Vector with the labels for the observations.
class	Vector with names of data classes.
classcolor	Vector with the colors of the classes.
posleg	0 with no caption, 1 for caption in the left upper corner, 2 for caption in the right upper corner (default), 3 for caption in the right lower corner, 4 for caption in the left lower corner.
boxleg	Puts the frame in the caption (default = TRUE).
axes	Plots the X and Y axes (default = TRUE).
savptc	Saves graphics images to files (default = FALSE).
width	Graphics images width when savptc = TRUE (defaul = 3236).
height	Graphics images height when savptc = TRUE (default = 2000).
res	Nominal resolution in ppi of the graphics images when savptc = TRUE (default = 300).

Value

Biplot	Biplot graph.
Md	Matrix eigenvalues.
Mu	Matrix U (eigenvectors).
Mv	Matrix V (eigenvectors).
coorI	Coordinates of the individuals.
coorV	Coordinates of the variables.
pvar	Proportion of the principal components.

Author(s)

Paulo Cesar Ossani

Marcelo Angelo Cirillo

References

RENCHER, A. C. *Methods of multivariate analysis.* 2th. ed. New York: J.Wiley, 2002. 708 p.

Examples

```
data(iris) # dataset

data <- iris[,1:4]

Biplot(data)


cls <- iris[,5]
res <- Biplot(data, alpha = 0.6, title = "Biplot of data valuing individuals",
              class = cls, classcolor = c("goldenrod3","gray56","red"),
              posleg = 2, boxleg = FALSE, axes = TRUE, savptc = FALSE,
              width = 3236, height = 2000, res = 300)
print(res$pvar)


res <- Biplot(data, alpha = 0.4, title = "Graph valuing the variables",
              xlabel = "", ylabel = "", color = FALSE, obs = FALSE,
              savptc = FALSE, width = 3236, height = 2000, res = 300)
print(res$pvar)
```

CA *Correspondence Analysis (CA).*

Description

Performs simple correspondence analysis (CA) and multiple (MCA) in a data set.

Usage

```
CA(data, typdata = "f", typmatrix = "I")
```

Arguments

`data`	Data to be analyzed (contingency table).
`typdata`	"f" for frequency data (default), "c" for qualitative data.
`typmatrix`	Matrix used for calculations when typdata = "c". "I" for indicator matrix (default), "B" for Burt's matrix.

Value

depdata	Verify if the rows and columns are dependent, or independent by the chi-square test, at the 5% significance level.
typdata	Data type: "F" frequency or "C" qualitative.
numcood	Number of principal components.
mtxP	Matrix of the relative frequency.
vtrR	Vector with sums of the rows.
vtrC	Vector with sums of the columns.
mtxPR	Matrix with profile of the rows.
mtxPC	Matrix with profile of the columns
mtxZ	Matrix Z.
mtxU	Matrix with the eigenvectors U.
mtxV	Matrix with the eigenvectors V.
mtxL	Matrix with eigenvalues.
mtxX	Matrix with the principal coordinates of the rows.
mtxY	Matrix with the principal coordinates of the columns.
mtxAutvlr	Matrix of the inertias (variances), with the proportions and proportions accumulated.

Author(s)

Paulo Cesar Ossani

Marcelo Angelo Cirillo

References

MINGOTI, S. A. *Analise de dados atraves de metodos de estatistica multivariada:* uma abordagem aplicada. Belo Horizonte: UFMG, 2005. 297 p.

RENCHER, A. C. *Methods of multivariate analysis.* 2th. ed. New York: J.Wiley, 2002. 708 p.

See Also

Plot.CA

Examples

```
data(DataFreq) # frequency data set

data <- DataFreq[,2:ncol(DataFreq)]

rownames(data) <- as.character(t(DataFreq[1:nrow(DataFreq),1]))

res <- CA(data = data, "f") # performs CA

print("Is there dependency between rows and columns?"); res$depdata
```

```
print("Number of principal coordinates:"); res$numcood

print("Principal coordinates of the rows:"); round(res$mtxX,2)

print("Principal coordinates of the columns:"); round(res$mtxY,2)

print("Inertia of the principal components:"); round(res$mtxAutvlr,2)
```

CCA *Canonical Correlation Analysis(CCA).*

Description

Perform Canonical Correlation Analysis (CCA) on a data set.

Usage

```
CCA(X = NULL, Y = NULL, type = 1, test = "Bartlett", sign = 0.05)
```

Arguments

X	First group of variables of a data set.
Y	Second group of variables of a data set.
type	1 for analysis using the covariance matrix (default), 2 for analysis using the correlation matrix.
test	Test of significance of the relationship between the group X and Y: "Bartlett" (default) or "Rao".
sign	Test significance level (default 5%).

Value

Cxx	Covariance matrix or correlation Cxx.
Cyy	Covariance matrix or correlation Cyy.
Cxy	Covariance matrix or correlation Cxy.
Cyx	Covariance matrix or correlation Cyx.
var.UV	Matrix with eigenvalues (variances) of the canonical pairs U and V.
corr.UV	Matrix of the correlation of the canonical pairs U and V.
coef.X	Matrix of the canonical coefficients of the group X.
coef.Y	Matrix of the canonical coefficients of the group Y.
corr.X	Matrix of the correlations between canonical variables and the original variables of the group X.
corr.Y	Matrix of the correlations between the canonical variables and the original variables of the group Y.

score.X	Matrix with the scores of the group X.
score.Y	Matrix with the scores of the group Y.
sigtest	Returns the significance test of the relationship between group X and Y: "Bartlett" (default) or "Rao".

Author(s)

Paulo Cesar Ossani

Marcelo Angelo Cirillo

References

MINGOTI, S. A. *Analise de dados atraves de metodos de estatistica multivariada:* uma abordagem aplicada. Belo Horizonte: UFMG, 2005. 297 p.

FERREIRA, D. F. *Estatistica Multivariada.* 2a ed. revisada e ampliada. Lavras: Editora UFLA, 2011. 676 p.

RENCHER, A. C. *Methods of multivariate analysis.* 2th. ed. New York: J.Wiley, 2002. 708 p.

LATTIN, J.; CARROL, J. D.; GREEN, P. E. *Analise de dados multivariados.* 1th. ed. Sao Paulo: Cengage Learning, 2011. 455 p.

See Also

Plot.CCA

Examples

```
data(DataMix) # data set

data <- DataMix[,2:ncol(DataMix)]

rownames(data) <- DataMix[,1]

X <- data[,1:2]

Y <- data[,5:6]

res <- CCA(X, Y, type = 2, test = "Bartlett", sign = 0.05)

print("Matrix with eigenvalues (variances) of the canonical pairs U and V:"); round(res$var.UV,3)

print("Matrix of the correlation of the canonical pairs U and V:"); round(res$corr.UV,3)

print("Matrix of the canonical coefficients of the group X:"); round(res$coef.X,3)

print("Matrix of the canonical coefficients of the group Y:"); round(res$coef.Y,3)

print("Matrix of the correlations between the canonical
       variables and the original variables of the group X:"); round(res$corr.X,3)
```

```
print("Matrix of the correlations between the canonical
       variables and the original variables of the group Y:"); round(res$corr.Y,3)

print("Matrix with the scores of the group X:"); round(res$score.X,3)

print("Matrix with the scores of the group Y:"); round(res$score.Y,3)

print("test of significance of the canonical pairs:"); res$sigtest
```

`Cluster` *Cluster Analysis.*

Description

Performs hierarchical and non-hierarchical cluster analysis in a data set.

Usage

```
Cluster(data, titles = NA, hierarquico = TRUE, analise = "Obs",
        corabs = FALSE, normaliza = FALSE, distance = "euclidean",
        method = "complete", horizontal = FALSE, numgrupos = 0,
        lambda = 2, savptc = FALSE, width = 3236, height = 2000,
        res = 300, casc = TRUE)
```

Arguments

`data`	Data to be analyzed.
`titles`	Titles of the graphics, if not set, assumes the default text.
`hierarquico`	Hierarchical groupings (default = TRUE), for non-hierarchical groupings (method K-Means), only for case Analysis = "Obs".
`analise`	"Obs" for analysis on observations (default), "Var" for analysis on variables.
`corabs`	Matrix of absolute correlation case Analyze = "Var" (default = FALSE).
`normaliza`	Normalizes the data only for case Analyze = "Obs" (default = TRUE).
`distance`	Metric of the distances in case of hierarchical groupings: "euclidean" (default), "maximum", "manhattan", "canberra", "binary" or "minkowski". Case Analysis = "Var" the metric will be the correlation matrix, according to corabs.
`method`	Method for analyzing hierarchical groupings: "complete" (default), "ward.D", "ward.D2", "single", "average", "mcquitty", "median" or "centroid".
`horizontal`	Horizontal dendrogram (default = FALSE).
`numgrupos`	Number of groups to be formed.
`lambda`	Value used in the minkowski distance.
`savptc`	Saves graphics images to files (default = FALSE).
`width`	Graphics images width when savptc = TRUE (defaul = 3236).
`height`	Graphics images height when savptc = TRUE (default = 2000).
`res`	Nominal resolution in ppi of the graphics images when savptc = TRUE (default = 300).
`casc`	Cascade effect in the presentation of the graphics (default = TRUE).

Value

Several graphics.

tabres	Table with similarities and distances of the groups formed.
groups	Original data with groups formed.
resgroups	Results of the groups formed.
sqt	Total sum of squares.
mtxD	Matrix of the distances.

Author(s)

Paulo Cesar Ossani

Marcelo Angelo Cirillo

References

MINGOTI, S. A. *analise de dados atraves de metodos de estatistica multivariada:* uma abordagem aplicada. Belo Horizonte: UFMG, 2005. 297 p.

FERREIRA, D. F. *Estatistica Multivariada.* 2a ed. revisada e ampliada. Lavras: Editora UFLA, 2011. 676 p.

RENCHER, A. C. *Methods of multivariate analysis.* 2th. ed. New York: J.Wiley, 2002. 708 p.

Examples

```
data(DataQuan) # set of quantitative data

data <- DataQuan[,2:8]

rownames(data) <- DataQuan[1:nrow(DataQuan),1]

res <- Cluster(data, titles = NA, hierarquico = TRUE, analise = "Obs",
               corabs = FALSE, normaliza = FALSE, distance = "euclidean",
               method = "ward.D", horizontal = FALSE, numgrupos = 2,
               savptc = FALSE, width = 3236, height = 2000, res = 300,
               casc = FALSE)

print("Table with similarities and distances:"); res$tabres
print("groups formed:"); res$groups
print("Table with the results of the groups:"); res$resgroups
print("Total sum of squares:"); res$sqt
print("distance Matrix:"); res$mtxD

write.table(file=file.path(tempdir(),"SimilarityTable.csv"), res$tabres, sep=";",
            dec=",",row.names = FALSE)
write.table(file=file.path(tempdir(),"GroupData.csv"), res$groups, sep=";",
            dec=",",row.names = TRUE)
write.table(file=file.path(tempdir(),"GroupResults.csv"), res$resgroups, sep=";",
            dec=",",row.names = TRUE)
```

CoefVar *Coefficient of variation of the data.*

Description

Find the coefficient of variation of the data, either overall or per column.

Usage

```
CoefVar(data, type = 1)
```

Arguments

data	Data to be analyzed.
type	1 Coefficient of overall variation (default), 2 Coefficient of variation per column.

Value

Coefficient of variation, either overall or per column.

Author(s)

Paulo Cesar Ossani

Marcelo Angelo Cirillo

References

FERREIRA, D. F.; *Estatistica Basica.* 2 ed. rev. Lavras: UFLA, 2009. 664 p.

Examples

```
data(DataQuan) # data set

data <- DataQuan[,2:8]

res <- CoefVar(data, type = 1) # Coefficient of overall variation
round(res,2)

res <- CoefVar(data, type = 2) # Coefficient of variation per column
round(res,2)
```

DA *Linear (LDA) and quadratic discriminant analysis (QDA).*

Description

Perform linear and quadratic discriminant analysis.

Usage

```
DA(data, class = NA, type = "lda", validation = "learning",
   method = "moment", prior = NA, testing = NA)
```

Arguments

data	Data to be classified.
class	Vector with data classes names.
type	"lda": linear discriminant analysis (default), or "qda": quadratic discriminant analysis.
validation	Type of validation: "learning" - data training (default), or "testing" - classifies the data of the vector "testing".
method	Classification method: "mle" to MLEs, "mve" to use cov.mv, "moment" (default) for standard mean and variance estimators, or "t" for robust estimates based on the t distribution.
prior	Probabilities of occurrence of classes. If not specified, it will take the proportions of the classes. If specified, probabilities must follow the order of factor levels.
testing	Vector with indices that will be used in data as test. For validation = "learning", one has testing = NA.

Value

confusion	Confusion table.
error.rate	Overall error ratio.
prior	Probability of classes.
type	Type of discriminant analysis.
validation	Type of validation.
num.class	Number of classes.
class.names	Class names.
method	Classification method.
num.correct	Number of correct observations.
results	Matrix with comparative classification results.

Author(s)

Paulo Cesar Ossani

Marcelo Angelo Cirillo

References

FERREIRA, D. F. *Estatistica Multivariada.* 2a ed. revisada e ampliada. Lavras: Editora UFLA, 2011. 676 p.

MINGOTI, S. A. *Analise de dados atraves de metodos de estatistica multivariada:* uma abordagem aplicada. Belo Horizonte: UFMG, 2005. 297 p.

RENCHER, A. C. *Methods of multivariate analysis.* 2th. ed. New York: J.Wiley, 2002. 708 p.

RIPLEY, B. D. *Pattern Recognition and Neural Networks.* Cambridge University Press, 1996.

VENABLESs, W. N. and RIPLEY, B. D. *Modern Applied Statistics with S.* Fourth edition. Springer, 2002.

Examples

```
data(iris) # data set

data  = iris[,1:4] # data to be classified
class = iris[,5]   # data class
prior = c(1,1,1)/3 # a priori probability of the classs

res <- DA(data, class, type = "lda", validation = "learning",
          method = "mle", prior = prior, testing = NA)

print("confusion table:"); res$confusion
print("Overall hit ratio:"); 1 - res$error.rate
print("Probability of classes:"); res$prior
print("classification method:"); res$method
print("type of discriminant analysis:"); res$type
print("class names:"); res$class.names
print("Number of classess:"); res$num.class
print("type of validation:"); res$validation
print("Number of correct observations:"); res$num.correct
print("Matrix with comparative classification results:"); res$results


### cross-validation ###
amostra   = sample(2, nrow(data), replace = TRUE, prob = c(0.7,0.3))
datatrain = data[amostra == 1,] # training data
datatest  = data[amostra == 2,] # test data

dim(datatrain) # training data dimension
dim(datatest)  # test data dimension

testing  = as.integer(rownames(datatest)) # test data index

res <- DA(data, class, type = "qda", validation = "testing",
```

```
          method = "moment", prior = NA, testing = testing)

print("confusion table:"); res$confusion
print("Overall hit ratio:"); 1 - res$error.rate
print("Number of correct observations:"); res$num.correct
print("Matrix with comparative classification results:"); res$results
```

DataCoffee *Frequency data set.*

Description

Set of data categorized by coffees, on sensorial abilities in the consumption of special coffees.

Usage

```
data(DataCoffee)
```

Format

Data set of a research done with the purpose of evaluating the concordance between the responses of different groups of consumers with different sensorial abilities. The experiment relates the sensorial analysis of special coffees defined by (A) Yellow Bourbon, cultivated at altitudes greater than 1200 m; (D) idem to (A) differing only in the preparation of the samples; (B) Acaia cultivated at an altitude of less than 1,100 m; (C) identical to (B) but differentiating the sample preparation. Here the data are categorized by coffees. The example given demonstrates the results found in OSSANI et al. (2017).

References

OSSANI, P. C.; CIRILLO, M. A.; BOREM, F. M.; RIBEIRO, D. E.; CORTEZ, R. M.. Quality of specialty coffees: a sensory evaluation by consumers using the MFACT technique. *Revista Ciencia Agronomica (UFC. Online)*, v. 48, p. 92-100, 2017.

OSSANI, P. C. *Qualidade de cafes especiais e nao especiais por meio da analise de multiplos fatores para tabelas de contingencias.* 2015. 107 p. Dissertacao (Mestrado em Estatistica e Experimentacao Agropecuaria) - Universidade Federal de Lavras, Lavras, 2015.

Examples

```
data(DataCoffee) # categorized data set

data <- DataCoffee[,2:ncol(DataCoffee)]

rownames(data) <- as.character(t(DataCoffee[1:nrow(DataCoffee),1]))

group.names = c("Coffee A", "Coffee B", "Coffee C", "Coffee D")
```

```
mf <- MFA(data, c(16,16,16,16), c(rep("f",4)), group.names)

print("Principal components variances:"); round(mf$mtxA,2)

print("Matrix of the Partial Inertia / Score of the Variables:"); round(mf$mtxEV,2)

tit <- c("Scree-plot","Individuals","Individuals / Types coffees","Inercias Groups")

Plot.MFA(mf, titles = tit, xlabel = NA, ylabel = NA,
         posleg = 2, boxleg = FALSE, color = TRUE,
        namarr = FALSE, linlab = NA, casc = FALSE) # plotting several graphs on the screen
```

DataFreq *Frequency data set.*

Description

Simulated data set with the weekly frequency of the number of coffee cups consumed weekly in some world capitals.

Usage

```
data(DataFreq)
```

Format

Set of data with 6 rows and 9 columns. There are 6 observations described by 9 variables: Group by sex and age, Sao Paulo - Cafe Bourbon, London - Cafe Bourbon, Athens - Cafe Bourbon, London - Cafe Acaia, Athens - Cafe Catuai, Sao Paulo - Cafe Catuai, Athens - Cafe Catuai.

Author(s)

Paulo Cesar Ossani

Marcelo Angelo Cirillo

Examples

```
data(DataFreq)
DataFreq
```

DataInd *Frequency data set.*

Description

Set of data categorized by coffees, on sensorial abilities in the consumption of special coffees.

Usage

```
data(DataInd)
```

Format

Data set of a research done with the purpose of evaluating the concordance between the responses of different groups of consumers with different sensorial abilities. The experiment relates the sensorial analysis of special coffees defined by (A) Yellow Bourbon, cultivated at altitudes greater than 1200 m; (D) idem to (A) differing only in the preparation of the samples; (B) Acaia cultivated at an altitude of less than 1,100 m; (C) identical to (B) but differentiating the sample preparation. Here the data are categorized by coffees. The example given demonstrates the results found in OSSANI et al. (2017).

References

OSSANI, P. C.; CIRILLO, M. A.; BOREM, F. M.; RIBEIRO, D. E.; CORTEZ, R. M.. Quality of specialty coffees: a sensory evaluation by consumers using the MFACT technique. *Revista Ciencia Agronomica (UFC. Online)*, v. 48, p. 92-100, 2017.

OSSANI, P. C. *Qualidade de cafes especiais e nao especiais por meio da analise de multiplos fatores para tabelas de contingencias.* 2015. 107 p. Dissertacao (Mestrado em Estatistica e Experimentacao Agropecuaria) - Universidade Federal de Lavras, Lavras, 2015.

Examples

```
data(DataInd) # categorized data set

data <- DataInd[,2:ncol(DataInd)]

rownames(data) <- as.character(t(DataInd[1:nrow(DataInd),1]))

group.names = c("Group 1", "Group 2", "Group 3", "Group 4")

mf <- MFA(data, c(16,16,16,16), c(rep("f",4)), group.names)

print("Principal components variances:"); round(mf$mtxA,2)

print("Matrix of the Partial Inertia / Score of the Variables:"); round(mf$mtxEV,2)

tit <- c("Scree-plot","Individuals","Individuals / Types coffees","Inercias Groups")
```

```
Plot.MFA(mf, titles = tit, xlabel = NA, ylabel = NA,
         posleg = 2, boxleg = FALSE, color = TRUE,
        namarr = FALSE, linlab = NA, casc = FALSE) # plotting several graphs on the screen
```

DataMix *Mixed data set.*

Description

Simulated set of mixed data on consumption of coffee.

Usage

```
data(DataMix)
```

Format

Data set with 10 rows and 7 columns. Being 10 observations described by 7 variables: Cooperatives/Tasters, Average grades given to analyzed coffees, Years of work as a taster, Taster with technical training, Taster exclusively dedicated, Average frequency of the coffees Classified as special, Average frequency of the coffees as commercial.

Author(s)

Paulo Cesar Ossani

Marcelo Angelo Cirillo

Examples

```
data(DataMix)
DataMix
```

DataQuali *Qualitative data set*

Description

Set simulated of qualitative data on consumption of coffee.

Usage

```
data(DataQuali)
```

Format

Data set simulated with 12 rows and 6 columns. Being 12 observations described by 6 variables: Sex, Age, Smoker, Marital status, Sportsman, Study.

Author(s)

Paulo Cesar Ossani

Marcelo Angelo Cirillo

Examples

```
data(DataQuali)
DataQuali
```

DataQuan *Quantitative data set*

Description

Set simulated of quantitative data on grades given to some sensory characteristics of coffees.

Usage

```
data(DataQuan)
```

Format

Data set with 6 rows and 11 columns. Being 6 observations described by 11 variables: Coffee, Chocolate, Caramelised, Ripe, Sweet, Delicate, Nutty, Caramelised, Chocolate, Spicy, Caramelised.

Author(s)

Paulo Cesar Ossani

Marcelo Angelo Cirillo

Examples

```
data(DataQuan)
DataQuan
```

FA *Factor Analysis (FA).*

Description

Performs factorial analysis (FA) in a data set.

Usage

```
FA(data, method = "PC", type = 2, nfactor = 1, rotation = "None",
   scoresobs = "Bartlett", converg = 1e-5, iteracao = 1000,
   testfit = TRUE)
```

Arguments

data	Data to be analyzed.
method	Method of analysis: "PC" - Principal Components (default), "PF" - Principal Factor, "ML" - Maximum Likelihood.
type	1 for analysis using the covariance matrix, 2 for analysis using the correlation matrix (default).
rotation	Type of rotation: "None" (default), "Varimax" and "Promax".
nfactor	Number of factors (default = 1).
scoresobs	Type of scores for the observations: "Bartlett" (default) or "Regression".
converg	Limit value for convergence to sum of the squares of the residuals for Maximum likelihood method (default = 1e-5).
iteracao	Maximum number of iterations for Maximum Likelihood method (default = 1000).
testfit	Tests the model fit to the method of Maximum Likelihood (default = TRUE).

Value

mtxMC	Matrix of correlation / covariance.
mtxAutvlr	Matrix of eigenvalues.
mtxAutvec	Matrix of eigenvectors.
mtxvar	Matrix of variances and proportions.
mtxcarga	Matrix of factor loadings.
mtxvaresp	Matrix of specific variances.
mtxcomuna	Matrix of commonalities.
mtxresidue	Matrix of residues.
vlrsqrs	Upper limit value for sum of squares of the residues.

vlrsqr	Sum of squares of the residues.
mtxresult	Matrix with all associated results.
mtxscores	Matrix with scores of the observations.
coefscores	Matrix with the scores of the coefficients of the factors.

Author(s)

Paulo Cesar Ossani

Marcelo Angelo Cirillo

References

MINGOTI, S. A. *Analise de dados atraves de metodos de estatistica multivariada:* uma abordagem aplicada. Belo Horizonte: UFMG, 2005. 297 p.

Kaiser, H. F.*The varimax criterion for analytic rotation in factor analysis.* Psychometrika 23, 187-200, 1958.

RENCHER, A. C. *Methods of multivariate analysis.* 2th. ed. New York: J.Wiley, 2002. 708 p.

FERREIRA, D. F. *Estatistica Multivariada.* 2a ed. revisada e ampliada. Lavras: Editora UFLA, 2011. 676 p.

See Also

Plot.FA

Examples

```
data(DataQuan) # data set

data <- DataQuan[,2:ncol(DataQuan)]

rownames(data) <- DataQuan[,1]

res <- FA(data, method = "PC", type = 2, nfactor = 3, rotation = "None",
          scoresobs = "Bartlett", converg = 1e-5, iteracao = 1000,
          testfit = TRUE)

print("Matrix with all associated results:"); round(res$mtxresult,3)

print("Sum of squares of the residues:"); round(res$vlrsqr,3)

print("Matrix of the factor loadings.:"); round(res$mtxcarga,3)

print("Matrix with scores of the observations:"); round(res$mtxscores,3)

print("Matrix with the scores of the coefficients of the factors:"); round(res$coefscores,3)
```

GrandTour *Animation technique Grand Tour.*

Description

Performs the exploration of the data through the technique of animation Grand Tour.

Usage

```
GrandTour(data, method = "Interpolation", title = NA, xlabel = NA,
          ylabel = NA, size = 1.1, grid = TRUE, color = TRUE, linlab = NA,
          class = NA, classcolor = NA, posleg = 2, boxleg = TRUE,
          axesvar = TRUE, axes = TRUE, numrot = 200, choicerot = NA,
          savptc = FALSE, width = 3236, height = 2000, res = 300)
```

Arguments

data	Numerical data set.
method	Method used for rotations: "Interpolation" - Interpolation method (default), "Torus" - Torus method, "Pseudo" - Pseudo Grand Tour method.
title	Titles of the graphics, if not set, assumes the default text.
xlabel	Names the X axis, if not set, assumes the default text.
ylabel	Names the Y axis, if not set, assumes the default text.
size	Size of the points in the graphs.
grid	Put grid on graphs (default = TRUE).
color	Colored graphics (default = TRUE).
linlab	Vector with the labels for the observations.
class	Vector with names of data classes.
classcolor	Vector with the colors of the classes.
posleg	0 with no caption, 1 for caption in the left upper corner, 2 for caption in the right upper corner (default), 3 for caption in the right lower corner, 4 for caption in the left lower corner.
boxleg	Puts the frame in the caption (default = TRUE).
axesvar	Puts axes of rotation of the variables (default = TRUE).
axes	Plots the X and Y axes (default = TRUE).
numrot	Number of rotations (default = 200). If method = "Interpolation", numrot represents the angle of rotation.

choicerot	Choose specific rotation and display on the screen, or save the image if savptc = TRUE.
savptc	Saves graphics images to files (default = FALSE).
width	Graphics images width when savptc = TRUE (defaul = 3236).
height	Graphics images height when savptc = TRUE (default = 2000).
res	Nominal resolution in ppi of the graphics images when savptc = TRUE (default = 300).

Value

Graphs with rotations.

proj.data	Projected data.
vector.opt	Vector projection.
method	method used on Grand Tour.

Author(s)

Paulo Cesar Ossani

Marcelo Angelo Cirillo

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Examples

```
data(iris) # database

res <- GrandTour(iris[,1:4], method = "Torus", title = NA, xlabel = NA, ylabel = NA,
                 color = TRUE, linlab = NA, class = NA, posleg = 2, boxleg = TRUE,
                 axesvar = TRUE, axes = FALSE, numrot = 10, choicerot = NA,
                 savptc = FALSE, width = 3236, height = 2000, res = 300)

print("Projected data:"); res$proj.data
print("Projection vectors:"); res$vector.opt
print("Grand Tour projection method:"); res$method


res <- GrandTour(iris[,1:4], method = "Interpolation", title = NA, xlabel = NA, ylabel = NA,
                 color = TRUE, linlab = NA, posleg = 2, boxleg = FALSE, axesvar = FALSE,
                 axes = FALSE, numrot = 10, choicerot = NA, class = iris[,5],
                 classcolor = c("goldenrod3","gray53","red"),savptc = FALSE,
                 width = 3236, height = 2000, res = 300)

print("Projected data:"); res$proj.data
print("Projection vectors:"); res$vector.opt
print("Grand Tour projection method:"); res$method
```

GSVD *Generalized Singular Value Decomposition (GSVD).*

Description

Given the matrix A of order nxm, the generalized singular value decomposition (GSVD) involves the use of two sets of positive square matrices of order nxn and mxm respectively. These two matrices express constraints imposed, respectively, on the lines and columns of A.

Usage

```
GSVD(data, plin = NULL, pcol = NULL)
```

Arguments

data	Matrix used for decomposition.
plin	Weight for rows.
pcol	Weight for columns

Details

If plin or pcol is not used, it will be calculated as the usual singular value decomposition.

Value

d	Eigenvalues, that is, line vector with singular values of the decomposition.
u	Eigenvectors referring rows.
v	Eigenvectors referring columns.

Author(s)

Paulo Cesar Ossani

Marcelo Angelo Cirillo

References

ABDI, H. Singular Value Decomposition (SVD) and Generalized Singular Value Decomposition (GSVD). In: SALKIND, N. J. (Ed.). *Encyclopedia of measurement and statistics.* Thousand Oaks: Sage, 2007. p. 907-912.

Examples

```
data <- matrix(c(1,2,3,4,5,6,7,8,9,10,11,12), nrow = 4, ncol = 3)

svd(data)  # Usual Singular Value Decomposition

GSVD(data) # GSVD with the same previous results

# GSVD with weights for rows and columns
GSVD(data, plin = c(0.1,0.5,2,1.5), pcol = c(1.3,2,0.8))
```

IM *Indicator matrix.*

Description

In the indicator matrix the elements are arranged in the form of *dummy* variables, in other words, 1 for a category chosen as a response variable and 0 for the other categories of the same variable.

Usage

```
IM(data, names = TRUE)
```

Arguments

data	Categorical data.
names	Include the names of the variables in the levels of the Indicator Matrix (default = TRUE).

Value

mtxIndc	Returns converted data in the indicator matrix.

Author(s)

Paulo Cesar Ossani

Marcelo Angelo Cirillo

References

RENCHER, A. C. *Methods of multivariate analysis.* 2th. ed. New York: J.Wiley, 2002. 708 p.

Examples

```
data <- matrix(c("S","S","N","N",1,2,3,4,"N","S","T","N"), nrow = 4, ncol = 3)

IM(data, names = FALSE)

data(DataQuali) # qualitative data set

IM(DataQuali, names = TRUE)
```

LocLab *Function for better position of the labels in the graphs.*

Description

Function for better position of the labels in the graphs.

Usage

```
LocLab(x, y = NULL, labels = seq(along = x), cex = 1,
       method = c("SANN", "GA"), allowSmallOverlap = FALSE,
       trace = FALSE, shadotext = FALSE,
       doPlot = TRUE, ...)
```

Arguments

x	Coordinate x
y	Coordinate y
labels	The labels
cex	cex
method	Not used
allowSmallOverlap	Boolean
trace	Boolean
shadotext	Boolean
doPlot	Boolean
...	Other arguments passed to or from other methods

Value

See the text of the function.

MDS *Multidimensional Scaling (MDS).*

Description

Performs Multidimensional Scaling (MDS) on a data set.

Usage

```
MDS(data, distance = "euclidean", title = NA, xlabel = NA,
    ylabel = NA, posleg = 2, boxleg = TRUE, axes = TRUE,
    size = 1.1, grid = TRUE, color = TRUE, linlab = NA,
    class = NA, classcolor = NA, savptc = FALSE, width = 3236,
    height = 2000, res = 300)
```

Arguments

data	Data to be analyzed.
distance	Metric of the distance: "euclidean" (default), "maximum", "manhattan", "canberra", "binary" or "minkowski".
title	Titles of the graphics, if not set, assumes the default text.
xlabel	Names the X axis, if not set, assumes the default text.
ylabel	Names the Y axis, if not set, assumes the default text.
posleg	0 with no caption, 1 for caption in the left upper corner, 2 for caption in the right upper corner (default), 3 for caption in the right lower corner, 4 for caption in the left lower corner.
boxleg	Puts the frame in the caption (default = TRUE).
axes	Plot the X and Y axes (default = TRUE).
size	Size of the points in the graphs.
grid	Put grid on graphs (default = TRUE).
color	Colored graphics (default = TRUE).
linlab	Vector with the labels for the observations.
class	Vector with names of data classes.
classcolor	Vector with the colors of the classes.
savptc	Saves graphics images to files (default = FALSE).
width	Graphics images width when savptc = TRUE (defaul = 3236).
height	Graphics images height when savptc = TRUE (default = 2000).
res	Nominal resolution in ppi of the graphics images when savptc = TRUE (default = 300).

Value

Multidimensional Scaling.

`mtxD` Matrix of the distances.

Author(s)

Paulo Cesar Ossani

Marcelo Angelo Cirillo

References

MINGOTI, S. A. *Analise de dados atraves de metodos de estatistica multivariada:* uma abordagem aplicada. Belo Horizonte: UFMG, 2005. 297 p.

RENCHER, A. C. *Methods of multivariate analysis.* 2th. ed. New York: J.Wiley, 2002. 708 p.

Examples

```
data(iris) # data set

data <- iris[,1:4]

cls <- iris[,5] # data class

md <- MDS(data = data, distance = "euclidean", title = NA, xlabel = NA,
          ylabel = NA, posleg = 2, boxleg = TRUE, axes = TRUE, color = TRUE,
          linlab = NA, class = cls, classcolor = c("goldenrod3","gray53","red"),
          savptc = FALSE, width = 3236, height = 2000, res = 300)

print("Matrix of the distances:"); md$mtxD
```

MFA *Multiple Factor Analysis (MFA).*

Description

Perform Multiple Factor Analysis (MFA) on groups of variables. The groups of variables can be quantitative, qualitative, frequency (MFACT) data, or mixed data.

Usage

```
MFA(data, groups, typegroups = rep("n",length(groups)), namegroups = NULL)
```

Arguments

data	Data to be analyzed.
groups	Number of columns for each group in order following the order of data in 'data'.
typegroups	Type of group: "n" for numerical data (default), "c" for categorical data, "f" for frequency data.
namegroups	Names for each group.

Value

vtrG	Vector with the sizes of each group.
vtrNG	Vector with the names of each group.
vtrplin	Vector with the values used to balance the lines of the Z matrix.
vtrpcol	Vector with the values used to balance the columns of the Z matrix.
mtxZ	Matrix concatenated and balanced.
mtxA	Matrix of the eigenvalues (variances) with the proportions and proportions accumulated.
mtxU	Matrix U of the singular decomposition of the matrix Z.
mtxV	Matrix V of the singular decomposition of the matrix Z.
mtxF	Matrix global factor scores where the lines are the observations and the columns the components.
mtxEFG	Matrix of the factor scores by group.
mtxCCP	Matrix of the correlation of the principal components with original variables.
mtxEV	Matrix of the partial inertias / scores of the variables

Author(s)

Paulo Cesar Ossani

Marcelo Angelo Cirillo

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See Also

Plot.MFA

Examples

```
data(DataMix) # mixed dataset

data <- DataMix[,2:ncol(DataMix)]

rownames(data) <- DataMix[1:nrow(DataMix),1]
```

```
group.names = c("Grade Cafes/Work", "Formation/Dedication", "Coffees")

mf <- MFA(data = data, c(2,2,2), typegroups = c("n","c","f"), group.names) # performs MFA

print("Principal Component Variances:"); round(mf$mtxA,2)

print("Matrix of the Partial Inertia / Score of the Variables:"); round(mf$mtxEV,2)
```

MVar *Multivariate Analysis.*

Description

Package for multivariate analysis, having functions that perform simple correspondence analysis (CA) and multiple correspondence analysis (MCA), principal components analysis (PCA), canonical correlation analysis (CCA), factorial analysis (FA), multidimensional scaling (MDS), linear (LDA) and quadratic discriminant analysis (QDA), hierarchical and non-hierarchical cluster analysis, simple and multiple linear regression, multiple factor analysis (MFA) for quantitative, qualitative, frequency (MFACT) and mixed data, biplot, scatter plot, projection pursuit (PP), grant tour method and other useful functions for the multivariate analysis.

Details

Package:	MVar
Type:	Package
Version:	2.1.9
Date:	2022-10-05
License:	GPL(>= 2)
LazyLoad:	yes

Author(s)

Paulo Cesar Ossani and Marcelo Angelo Cirillo.

Maintainer: Paulo Cesar Ossani <ossanipc@hotmail.com>

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YOUNG, F. W.; FALDOWSKI R. A.; McFARLANE M. M. *Multivariate statistical visualization, in Handbook of Statistics*, Vol 9, C. R. Rao (ed.), The Netherlands: Elsevier Science Publishers, 959-998, 1993.

`NormData` *Normalizes the data.*

Description

Function that normalizes the data globally, or by column.

Usage

```
NormData(data, type = 1)
```

Arguments

`data`	Data to be analyzed.
`type`	1 normalizes overall (default), 2 normalizes per column.

Value

`dataNorm`	Normalized data.

Author(s)

Paulo Cesar Ossani

Marcelo Angelo Cirillo

Examples

```
data(DataQuan) # set of quantitative data

data <- DataQuan[,2:8]

res  <- NormData(data, type = 1) # normalizes the data globally

res # Globally standardized data

sd(res)   # overall standard deviation

mean(res) # overall mean


res <- NormData(data, type = 2) # normalizes the data per column

res # standardized data per column

apply(res, 2, sd) # standard deviation per column

colMeans(res)     # column averages
```

`NormTest` *Test of normality of the data.*

Description

Check the normality of the data, based on the asymmetry coefficient test.

Usage

```
NormTest(data, sign = 0.05)
```

Arguments

`data`	Data to be analyzed.
`sign`	Test significance level (default 5%).

Value

`statistic`	Observed Chi-square value, that is, the test statistic.
`chisquare`	Chi-square value calculated.
`gl`	Degree of freedom.
`p.value`	p-value.

Author(s)

Paulo Cesar Ossani

Marcelo Angelo Cirillo

References

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FERREIRA, D. F. *Estatistica Multivariada.* 2a ed. revisada e ampliada. Lavras: Editora UFLA, 2011. 676 p.

Examples

```
data <- cbind(rnorm(100,2,3), rnorm(100,1,2))

NormTest(data)

plot(density(data))


data <- cbind(rexp(200,3), rexp(200,3))

NormTest(data, sign = 0.01)

plot(density(data))
```

PCA *Principal Components Analysis (PCA).*

Description

Performs principal component analysis (PCA) in a data set.

Usage

```
PCA(data, type = 1)
```

Arguments

data	Data to be analyzed.
type	1 for analysis using the covariance matrix (default), 2 for analysis using the correlation matrix.

Value

mtxC	Matrix of covariance or correlation according to "type".
mtxAutvlr	Matrix of eigenvalues (variances) with the proportions and proportions accumulated.
mtxAutvec	Matrix of eigenvectors - principal components.
mtxVCP	Matrix of covariance of the principal components with the original variables.
mtxCCP	Matrix of correlation of the principal components with the original variables.
mtxscores	Matrix with scores of the principal components.

Author(s)

Paulo Cesar Ossani

Marcelo Angelo Cirillo

References

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See Also

Plot.PCA

Examples

```
data(DataQuan) # set of quantitative data

data <- DataQuan[,2:8]

rownames(data) <- DataQuan[1:nrow(DataQuan),1]

pc <- PCA(data, 2) # performs the PCA

print("Covariance matrix / Correlation:"); round(pc$mtxC,2)

print("Principal Components:"); round(pc$mtxAutvec,2)

print("Principal Component Variances:"); round(pc$mtxAutvlr,2)

print("Covariance of the Principal Components:"); round(pc$mtxVCP,2)

print("Correlation of the Principal Components:"); round(pc$mtxCCP,2)
```

```
print("Scores of the Principal Components:"); round(pc$mtxscores,2)
```

`Plot.CA` *Graphs of the simple (CA) and multiple correspondence analysis (MCA).*

Description

Graphs of the simple (CA) and multiple correspondence analysis (MCA).

Usage

```
Plot.CA(CA, titles = NA, xlabel = NA, ylabel = NA,
        size = 1.1, grid = TRUE, color = TRUE, linlab = NA,
        savptc = FALSE, width = 3236, height = 2000,
        res = 300, casc = TRUE)
```

Arguments

`CA`	Data of the CA function.
`titles`	Titles of the graphics, if not set, assumes the default text..
`xlabel`	Names the X axis, if not set, assumes the default text.
`ylabel`	Names the Y axis, if not set, assumes the default text.
`size`	Size of the points in the graphs.
`grid`	Put grid on graphs (default = TRUE).
`color`	Colored graphics (default = TRUE).
`linlab`	Vector with the labels for the observations.
`savptc`	Saves graphics images to files (default = FALSE).
`width`	Graphics images width when savptc = TRUE (defaul = 3236).
`height`	Graphics images height when savptc = TRUE (default = 2000).
`res`	Nominal resolution in ppi of the graphics images when savptc = TRUE (default = 300).
`casc`	Cascade effect in the presentation of the graphics (default = TRUE).

Value

Returns several graphs.

Author(s)

Paulo Cesar Ossani

Marcelo Angelo Cirillo

See Also

CA

Examples

```
data(DataFreq) # frequency data set

data <- DataFreq[,2:ncol(DataFreq)]

rownames(data) <- DataFreq[1:nrow(DataFreq),1]

res <- CA(data, "f") # performs CA

tit <- c("Scree-plot","Observations", "Variables", "Observations / Variables")

Plot.CA(res, titles = tit, xlabel = NA, ylabel = NA,
        color = TRUE, linlab = rownames(data), savptc = FALSE,
        width = 3236, height = 2000, res = 300, casc = FALSE)


data(DataQuali) # qualitative data set

data <- DataQuali[,2:ncol(DataQuali)]

res <- CA(data, "c", "b") # performs CA

tit <- c("","","Graph of the variables")

Plot.CA(res, titles = tit, xlabel = NA, ylabel = NA,
        color = TRUE, linlab = NA, savptc = FALSE,
        width = 3236, height = 2000, res = 300,
        casc = FALSE)
```

Plot.CCA *Graphs of the Canonical Correlation Analysis (CCA).*

Description

Graphs of the Canonical Correlation Analysis (CCA).

Usage

```
Plot.CCA(CCA, titles = NA, xlabel = NA, ylabel = NA,
         size = 1.1, grid = TRUE, color = TRUE, savptc = FALSE,
         width = 3236, height = 2000, res = 300, casc = TRUE)
```

Arguments

CCA	Data of the CCA function.
titles	Titles of the graphics, if not set, assumes the default text.
xlabel	Names the X axis, if not set, assumes the default text.
ylabel	Names the Y axis, if not set, assumes the default text.
size	Size of the points in the graphs.
grid	Put grid on graphs (default = TRUE).
color	Colored graphics (default = TRUE).
savptc	Saves graphics images to files (default = FALSE).
width	Graphics images width when savptc = TRUE (defaul = 3236).
height	Graphics images height when savptc = TRUE (default = 2000).
res	Nominal resolution in ppi of the graphics images when savptc = TRUE (default = 300).
casc	Cascade effect in the presentation of the graphics (default = TRUE).

Value

Returns several graphs.

Author(s)

Paulo Cesar Ossani

Marcelo Angelo Cirillo

See Also

CCA

Examples

```
data(DataMix) # database

data <- DataMix[,2:ncol(DataMix)]

rownames(data) <- DataMix[,1]

X <- data[,1:2]

Y <- data[,5:6]

res <- CCA(X, Y, type = 2, test = "Bartlett", sign = 0.05) # performs CCA

tit <- c("Scree-plot","Correlations","Scores of the group X","Scores of the group Y")

Plot.CCA(res, titles = tit, xlabel = NA, ylabel = NA,
         color = TRUE, savptc = FALSE, width = 3236,
         height = 2000, res = 300, casc = TRUE)
```

`Plot.Cor` *Plot of correlations between variables.*

Description

It performs the correlations between the variables of a database and presents it in graph form.

Usage

```
Plot.Cor(data, title = NA, grid = TRUE, leg = TRUE, boxleg = FALSE,
         text = FALSE, arrow = TRUE, color = TRUE, namesvar = NA,
         savptc = FALSE, width = 3236, height = 2000, res = 300)
```

Arguments

`data`	Numeric data set.
`title`	Title for the plot, if not defined it assumes standard text.
`grid`	Puts grid on plot (default = TRUE).
`leg`	Put the legend on the plot (default = TRUE)
`boxleg`	Put frame in the legend (default = FALSE).
`text`	Puts correlation values in circles (default = FALSE).
`arrow`	Positive (up) and negative (down) correlation arrows (default = TRUE).
`color`	Colorful plot (default = TRUE).
`namesvar`	Vector with the variable names, if omitted it assumes the names in 'date'.
`savptc`	Saves graphics images to files (default = FALSE).
`width`	Graphics images width when savptc = TRUE (defaul = 3236).
`height`	Graphics images height when savptc = TRUE (default = 2000).
`res`	Nominal resolution in ppi of the graphics images when savptc = TRUE (default = 300).

Value

Plot with the correlations between the variables in 'date'.

Author(s)

Paulo Cesar Ossani

Examples

```
data(iris) # data set

Plot.Cor(data = iris[,1:4], title = NA, grid = TRUE, leg = TRUE, boxleg = FALSE,
         text = FALSE, arrow = TRUE, color = TRUE, namesvar = NA, savptc = FALSE,
         width = 3236, height = 2000, res = 300)

Plot.Cor(data = iris[,1:4], title = NA, grid = TRUE, leg = TRUE, boxleg = FALSE,
         text = TRUE, arrow = TRUE, color = TRUE, namesvar = c("A1","B2","C3","D4"),
         savptc = FALSE, width = 3236, height = 2000, res = 300)
```

Plot.FA *Graphs of the Factorial Analysis (FA).*

Description

Graphs of the Factorial Analysis (FA).

Usage

```
Plot.FA(FA, titles = NA, xlabel = NA, ylabel = NA, size = 1.1,
        grid = TRUE, color = TRUE, linlab = NA, axes = TRUE, class = NA,
        classcolor = NA, posleg = 2, boxleg = TRUE, savptc = FALSE,
        width = 3236, height = 2000, res = 300, casc = TRUE)
```

Arguments

FA	Data of the FA function.
titles	Titles of the graphics, if not set, assumes the default text.
xlabel	Names the X axis, if not set, assumes the default text.
ylabel	Names the Y axis, if not set, assumes the default text.
size	Size of the points in the graphs.
grid	Put grid on graphs (default = TRUE).
color	Colored graphics (default = TRUE).
linlab	Vector with the labels for the observations.
axes	Plots the X and Y axes (default = TRUE).
class	Vector with names of data classes.
classcolor	Vector with the colors of the classes.
posleg	0 with no caption, 1 for caption in the left upper corner, 2 for caption in the right upper corner (default), 3 for caption in the right lower corner, 4 for caption in the left lower corner.

boxleg	Puts the frame in the caption (default = TRUE).
savptc	Saves graphics images to files (default = FALSE).
width	Graphics images width when savptc = TRUE (defaul = 3236).
height	Graphics images height when savptc = TRUE (default = 2000).
res	Nominal resolution in ppi of the graphics images when savptc = TRUE (default = 300).
casc	Cascade effect in the presentation of the graphics (default = TRUE).

Value

Returns several graphs.

Author(s)

Paulo Cesar Ossani

Marcelo Angelo Cirillo

See Also

FA

Examples

```
data(iris) # conjunto de dados

data <- iris[,1:4]

cls <- iris[,5] # classe dos dados

res <- FA(data, method = "PC", type = 2, nfactor = 3)

tit <- c("Scree-plot","Scores of the Observations","Factorial Loadings","Biplot")

cls <- as.character(iris[,5])

Plot.FA(FA = res, titles = tit, xlabel = NA, ylabel = NA,
        color = TRUE, linlab = NA, savptc = FALSE, size = 1.1,
        posleg = 1, boxleg = FALSE, class = cls, axes = TRUE,
        classcolor = c("blue3","red","goldenrod3"),
        width = 3236, height = 2000, res = 300, casc = FALSE)
```

Plot.MFA *Graphics of the Multiple Factor Analysis (MFA).*

Description

Graphics of the Multiple Factor Analysis (MFA).

Usage

```
Plot.MFA(MFA, titles = NA, xlabel = NA, ylabel = NA,
         posleg = 2, boxleg = TRUE, size = 1.1, grid = TRUE,
         color = TRUE, groupscolor = NA, namarr = FALSE,
         linlab = NA, savptc = FALSE, width = 3236,
         height = 2000, res = 300, casc = TRUE)
```

Arguments

MFA	Data of the MFA function.
titles	Titles of the graphics, if not set, assumes the default text.
xlabel	Names the X axis, if not set, assumes the default text.
ylabel	Names the Y axis, if not set, assumes the default text.
posleg	1 for caption in the left upper corner, 2 for caption in the right upper corner (default), 3 for caption in the right lower corner, 4 for caption in the left lower corner.
boxleg	Puts frame in legend (default = TRUE).
size	Size of the points in the graphs.
grid	Put grid on graphs (default = TRUE).
color	Colored graphics (default = TRUE).
groupscolor	Vector with the colors of the groups.
namarr	Puts the points names in the cloud around the centroid in the graph corresponding to the global analysis of the Individuals and Variables (default = FALSE).
linlab	Vector with the labels for the observations, if not set, assumes the default text.
savptc	Saves graphics images to files (default = FALSE).
width	Graphics images width when savptc = TRUE (defaul = 3236).
height	Graphics images height when savptc = TRUE (default = 2000).
res	Nominal resolution in ppi of the graphics images when savptc = TRUE (default = 300).
casc	Cascade effect in the presentation of the graphics (default = TRUE).

Value

Returns several graphs.

Author(s)

Paulo Cesar Ossani

Marcelo Angelo Cirillo

See Also

MFA

Examples

```
data(DataMix) # set of mixed data

data <- DataMix[,2:ncol(DataMix)]

rownames(data) <- DataMix[1:nrow(DataMix),1]

group.names = c("Grade Cafes/Work", "Formation/Dedication", "Coffees")

mf <- MFA(data, c(2,2,2), typegroups = c("n","c","f"), group.names) # performs MFA

tit <- c("Scree-Plot","Observations","Observations/Variables",
         "Correlation Circle","Inertia of the Variable Groups")

Plot.MFA(MFA = mf, titles = tit, xlabel = NA, ylabel = NA,
         posleg = 2, boxleg = FALSE, color = TRUE,
         groupscolor = c("blue3","red","goldenrod3"),
         namarr = FALSE, linlab = NA, savptc = FALSE,
         width = 3236, height = 2000, res = 300,
         casc = TRUE) # plotting several graphs on the screen

Plot.MFA(MFA = mf, titles = tit, xlabel = NA, ylabel = NA,
         posleg = 2, boxleg = FALSE, color = TRUE,
         namarr = FALSE, linlab = rep("A?",10),
         savptc = FALSE, width = 3236, height = 2000,
         res = 300, casc = TRUE) # plotting several graphs on the screen
```

Plot.PCA *Graphs of the Principal Components Analysis (PCA).*

Description

Graphs of the Principal Components Analysis (PCA).

Usage

```
Plot.PCA(PC, titles = NA, xlabel = NA, ylabel = NA, size = 1.1,
         grid = TRUE, color = TRUE, linlab = NA, axes = TRUE, class = NA,
         classcolor = NA, posleg = 2, boxleg = TRUE, savptc = FALSE,
         width = 3236, height = 2000, res = 300, casc = TRUE)
```

Arguments

PC	Data of the PCA function.
titles	Titles of the graphics, if not set, assumes the default text.
xlabel	Names the X axis, if not set, assumes the default text.
ylabel	Names the Y axis, if not set, assumes the default text.
size	Size of the points in the graphs.
grid	Put grid on graphs (default = TRUE).
color	Colored graphics (default = TRUE).
linlab	Vector with the labels for the observations.
axes	Plots the X and Y axes (default = TRUE).
class	Vector with names of data classes.
classcolor	Vector with the colors of the classes.
posleg	0 with no caption, 1 for caption in the left upper corner, 2 for caption in the right upper corner (default), 3 for caption in the right lower corner, 4 for caption in the left lower corner.
boxleg	Puts the frame in the caption (default = TRUE).
savptc	Saves graphics images to files (default = FALSE).
width	Graphics images width when savptc = TRUE (defaul = 3236).
height	Graphics images height when savptc = TRUE (default = 2000).
res	Nominal resolution in ppi of the graphics images when savptc = TRUE (default = 300).
casc	Cascade effect in the presentation of the graphics (default = TRUE).

Value

Returns several graphs.

Author(s)

Paulo Cesar Ossani

Marcelo Angelo Cirillo

See Also

PCA

Examples

```
data(iris) # data set

data <- iris[,1:4]

cls <- iris[,5] # data class

pc <- PCA(data, 2)

tit <- c("Scree-plot","Observations","Correlations")

cls <- as.character(iris[,5])

Plot.PCA(PC = pc, titles = tit, xlabel = NA, ylabel = NA,
         color = TRUE, linlab = NA, savptc = FALSE, size = 1.1,
         posleg = 2, boxleg = FALSE, class = cls, axes = TRUE,
         classcolor = c("blue3","red","goldenrod3"),
         width = 3236, height = 2000, res = 300, casc = FALSE)
```

`Plot.PP` *Graphics of the Projection Pursuit (PP).*

Description

Graphics of the Projection Pursuit (PP).

Usage

```
Plot.PP(PP, titles = NA, xlabel = NA, ylabel = NA, posleg = 2, boxleg = TRUE,
        size = 1.1, grid = TRUE, color = TRUE, classcolor = NA, linlab = NA,
        axesvar = TRUE, axes = TRUE, savptc = FALSE, width = 3236, height = 2000,
        res = 300, casc = TRUE)
```

Arguments

`PP`	Data of the PP_Optimizer function.
`titles`	Titles of the graphics, if not set, assumes the default text.
`xlabel`	Names the X axis, if not set, assumes the default text.
`ylabel`	Names the Y axis, if not set, assumes the default text.
`posleg`	0 with no caption, 1 for caption in the left upper corner, 2 for caption in the right upper corner (default), 3 for caption in the right lower corner, 4 for caption in the left lower corner.
`boxleg`	Puts the frame in the caption (default = TRUE).

size	Size of the points in the graphs.
grid	Put grid on graphs (default = TRUE).
color	Colored graphics (default = TRUE).
classcolor	Vector with the colors of the classes.
linlab	Vector with the labels for the observations.
axesvar	Puts axes of rotation of the variables, only when dimproj > 1 (default = TRUE).
axes	Plots the X and Y axes (default = TRUE).
savptc	Saves graphics images to files (default = FALSE).
width	Graphics images width when savptc = TRUE (defaul = 3236).
height	Graphics images height when savptc = TRUE (default = 2000).
res	Nominal resolution in ppi of the graphics images when savptc = TRUE (default = 300).
casc	Cascade effect in the presentation of the graphics (default = TRUE).

Value

Graph of the evolution of the indices, and graphs whose data were reduced in two dimensions.

Author(s)

Paulo Cesar Ossani

Marcelo Angelo Cirillo

See Also

PP_Optimizer and PP_Index

Examples

```
data(iris) # dataset

# Example 1 - Without the classes in the data
data <- iris[,1:4]

findex <- "kurtosismax" # index function

dim <- 1 # dimension of data projection

sphere <- TRUE # spherical data

res <- PP_Optimizer(data = data, class = NA, findex = findex,
                    optmethod = "GTSA", dimproj = dim, sphere = sphere,
                    weight = TRUE, lambda = 0.1, r = 1, cooling = 0.9,
                    eps = 1e-3, maxiter = 500, half = 30)

Plot.PP(res, titles = NA, posleg = 1, boxleg = FALSE, color = TRUE,
        linlab = NA, axesvar = TRUE, axes = TRUE, savptc = FALSE,
```

```
        width = 3236, height = 2000, res = 300, casc = FALSE)


# Example 2 - With the classes in the data
class <- iris[,5] # data class

res <- PP_Optimizer(data = data, class = class, findex = findex,
                    optmethod = "GTSA", dimproj = dim, sphere = sphere,
                    weight = TRUE, lambda = 0.1, r = 1, cooling = 0.9,
                    eps = 1e-3, maxiter = 500, half = 30)

tit <- c(NA,"Graph example") # titles for the graphics

Plot.PP(res, titles = tit, posleg = 1, boxleg = FALSE, color = TRUE,
        classcolor = c("blue3","red","goldenrod3"), linlab = NA,
        axesvar = TRUE, axes = TRUE, savptc = FALSE, width = 3236,
        height = 2000, res = 300, casc = FALSE)


# Example 3 - Without the classes in the data, but informing
#             the classes in the plot function
res <- PP_Optimizer(data = data, class = NA, findex = "Moment",
                    optmethod = "GTSA", dimproj = 2, sphere = sphere,
                    weight = TRUE, lambda = 0.1, r = 1, cooling = 0.9,
                    eps = 1e-3, maxiter = 500, half = 30)

lin <- c(rep("a",50),rep("b",50),rep("c",50)) # data class

Plot.PP(res, titles = NA, posleg = 1, boxleg = FALSE, color = TRUE,
        linlab = lin, axesvar = TRUE, axes = TRUE, savptc = FALSE,
        width = 3236, height = 2000, res = 300, casc = FALSE)


# Example 4 - With the classes in the data, but not informed in plot function
class <- iris[,5] # data class

dim <- 2 # dimension of data projection

findex <- "lda" # index function

res <- PP_Optimizer(data = data, class = class, findex = findex,
                    optmethod = "GTSA", dimproj = dim, sphere = sphere,
                    weight = TRUE, lambda = 0.1, r = 1, cooling = 0.9,
                    eps = 1e-3, maxiter = 500, half = 30)

tit <- c("",NA) # titles for the graphics

Plot.PP(res, titles = tit, posleg = 1, boxleg = FALSE, color = TRUE,
        linlab = NA, axesvar = TRUE, axes = TRUE, savptc = FALSE,
        width = 3236, height = 2000, res = 300, casc = FALSE)
```

Plot.Regr *Graphs of the linear regression results.*

Description

Graphs of the linear regression results.

Usage

```
Plot.Regr(Reg, typegraf = "Scatterplot", title = NA, xlabel = NA,
          ylabel = NA, namevary = NA, namevarx = NA, size = 1.1,
          grid = TRUE, color = TRUE, intconf = TRUE, intprev = TRUE,
          savptc = FALSE, width = 3236, height = 2000, res = 300,
          casc = TRUE)
```

Arguments

Reg	Regression function data.
typegraf	Type of graphic: "Scatterplot" - Scatterplot 2 to 2, "Regression" - Graph of the linear regression, "QQPlot" - Graph of the normal probability of the residues, "Histogram" - Histogram of the residues, "Fits" - Graph of the adjusted values versus residuals, "Order" - Graph of the order of the observations versus the residuals.
title	Titles of the graphics, if not set, assumes the default text.
xlabel	Names the X axis, if not set, assumes the default text.
ylabel	Names the Y axis, if not set, assumes the default text.
namevary	Variable name Y, if not set, assumes the default text.
namevarx	Name of the variable X, or variables X, if not set, assumes the default text.
size	Size of the points in the graphs.
grid	Put grid on graphs (default = TRUE).
color	Colored graphics (default = TRUE).
intconf	Case typegraf = "Regression". Graphics with confidence interval (default = TRUE).
intprev	Case typegraf = "Regression". Graphics with predictive interval (default = TRUE).
savptc	Saves graphics images to files (default = FALSE).
width	Graphics images width when savptc = TRUE (defaul = 3236).
height	Graphics images height when savptc = TRUE (default = 2000).
res	Nominal resolution in ppi of the graphics images when savptc = TRUE (default = 300).
casc	Cascade effect in the presentation of the graphics (default = TRUE).

Value

Returns several graphs.

Author(s)

Paulo Cesar Ossani

See Also

Regr

Examples

```
data(DataMix)

Y <- DataMix[,2]

X <- DataMix[,7]

name.y <- "Medium grade"

name.x <- "Commercial coffees"

res <- Regr(Y, X, namevarx = name.x , intercepts = TRUE, sigf = 0.05)

tit <- c("Scatterplot")
Plot.Regr(res, typegraf = "Scatterplot", title = tit,
          namevary = name.y, namevarx = name.x, color = TRUE,
          savptc = FALSE, width = 3236, height = 2000, res = 300)

tit <- c("Scatterplot with the adjusted line")
Plot.Regr(res, typegraf = "Regression", title = tit,
          xlabel = name.x, ylabel = name.y, color = TRUE,
          intconf = TRUE, intprev = TRUE, savptc = FALSE,
          width = 3236, height = 2000, res = 300)

dev.new() # necessary to not overlap the following graphs to the previous graph

par(mfrow = c(2,2))

Plot.Regr(res, typegraf = "QQPlot", casc = FALSE)
Plot.Regr(res, typegraf = "Histogram", casc = FALSE)
Plot.Regr(res, typegraf = "Fits", casc = FALSE)
Plot.Regr(res, typegraf = "Order", casc = FALSE)
```

PP_Index *Function to find the Projection Pursuit indexes (PP).*

Description

Function used to find Projection Pursuit indexes (PP).

Usage

```
PP_Index(data, class = NA, vector.proj = NA,
         findex = "HOLES", dimproj = 2, weight = TRUE,
         lambda = 0.1, r = 1, ck = NA)
```

Arguments

data	Numeric dataset without class information.
class	Vector with names of data classes.
vector.proj	Vector projection.
findex	Projection index function to be used: "lda" - LDA index, "pda" - PDA index, "lr" - Lr index, "holes" - Holes index (default), "cm" - Central Mass index, "pca" - PCA index, "friedmantukey" - Friedman Tukey index, "entropy" - Entropy index, "legendre" - Legendre index, "laguerrefourier" - Laguerre Fourier index, "hermite" - Hermite index, "naturalhermite" - Natural Hermite index, "kurtosismax" - Maximum kurtosis index, "kurtosismin" - Minimum kurtosis index, "moment" - Moment index, "mf" - MF index, "chi" - Chi-square index.
dimproj	Dimension of data projection (default = 2).
weight	Used in index LDA, PDA and Lr to weight the calculations for the number of elements in each class (default = TRUE).
lambda	Used in the PDA index (default = 0.1).
r	Used in the Lr index (default = 1).
ck	Internal use of the CHI index function.

Value

num.class	Number of classes.
class.names	Class names.
findex	Projection index function used.
vector.proj	Projection vectors found.
index	Projection index found in the process.

Author(s)

Paulo Cesar Ossani

Marcelo Angelo Cirillo

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See Also

`PP_Optimizer` and `Plot.PP`

Examples

```
data(iris) # data set

data <- iris[,1:4]

# Example 1 - Without the classes in the data
ind <- PP_Index(data = data, class = NA, vector.proj = NA,
                findex = "moment", dimproj = 2, weight = TRUE,
                lambda = 0.1, r = 1)

print("Number of classes:"); ind$num.class
print("class Names:"); ind$class.names
print("Projection index function:"); ind$findex
print("Projection vectors:"); ind$vector.proj
print("Projection index:"); ind$index


# Example 2 - With the classes in the data
class <- iris[,5] # data class

findex <- "pda" # index function

sphere <- TRUE # spherical data

res <- PP_Optimizer(data = data, class = class, findex = findex,
                    optmethod = "SA", dimproj = 2, sphere = sphere,
                    weight = TRUE, lambda = 0.1, r = 1, cooling = 0.9,
                    eps = 1e-3, maxiter = 1000, half = 30)

# Comparing the result obtained
if (match(toupper(findex),c("LDA", "PDA", "LR"), nomatch = 0) > 0) {
  if (sphere) {
     data <- apply(predict(prcomp(data)), 2, scale) # spherical data
  }
} else data <- as.matrix(res$proj.data[,1:Dim])

ind <- PP_Index(data = data, class = class, vector.proj = res$vector.opt,
                findex = findex, dimproj = 2, weight = TRUE, lambda = 0.1,
                r = 1)

print("Number of classes:"); ind$num.class
print("class Names:"); ind$class.names
print("Projection index function:"); ind$findex
print("Projection vectors:"); ind$vector.proj
print("Projection index:"); ind$index
print("Optimized Projection index:"); res$index[length(res$index)]
```

PP_Optimizer *Optimization function of the Projection Pursuit index (PP).*

Description

Optimization function of the Projection Pursuit index (PP).

Usage

```
PP_Optimizer(data, class = NA, findex = "HOLES",
             dimproj = 2, sphere = TRUE, optmethod = "GTSA",
             weight = TRUE, lambda = 0.1, r = 1, cooling = 0.9,
             eps = 1e-3, maxiter = 3000, half = 30)
```

Arguments

data	Numeric dataset without class information.
class	Vector with names of data classes.
findex	Projection index function to be used: "lda" - LDA index, "pda" - PDA index, "lr" - Lr index, "holes" - Holes index (default), "cm" - Central Mass index, "pca" - PCA index, "friedmantukey" - Friedman Tukey index, "entropy" - Entropy index, "legendre" - Legendre index, "laguerrefourier" - Laguerre Fourier index, "hermite" - Hermite index, "naturalhermite" - Natural Hermite index, "kurtosismax" - Maximum kurtosis index, "kurtosismin" - Minimum kurtosis index, "moment" - Moment index, "mf" - MF index, "chi" - Chi-square index.
dimproj	Dimension of the data projection (default = 2).
sphere	Spherical data (default = TRUE).
optmethod	Optimization method GTSA - Grand Tour Simulated Annealing or SA - Simulated Annealing (default = "GTSA").
weight	Used in index LDA, PDA and Lr to weight the calculations for the number of elements in each class (default = TRUE).
lambda	Used in the PDA index (default = 0.1).
r	Used in the Lr index (default = 1).
cooling	Cooling rate (default = 0.9).
eps	Approximation accuracy for cooling (default = 1e-3).
maxiter	Maximum number of iterations of the algorithm (default = 3000).
half	Number of steps without incrementing the index, then decreasing the cooling value (default = 30).

Value

num.class	Number of classes.
class.names	Class names.
proj.data	Projected data.
vector.opt	Projection vectors found.
index	Vector with the projection indices found in the process, converging to the maximum, or the minimum.
findex	Projection index function used.

Author(s)

Paulo Cesar Ossani

Marcelo Angelo Cirillo

References

COOK, D., LEE, E. K., BUJA, A., WICKHAM, H.. Grand tours, projection pursuit guided tours and manual controls. In Chen, Chunhouh, Hardle, Wolfgang, Unwin, e Antony (Eds.), *Handbook of data Visualization*, Springer Handbooks of Computational Statistics, chapter III.2, p. 295-314. Springer, 2008.

LEE, E., COOK, D., KLINKE, S., LUMLEY, T.. Projection pursuit for exploratory supervised classification. *Journal of Computational and Graphical Statistics*, 14(4):831-846, 2005.

See Also

Plot.PP and PP_Index

Examples

```
data(iris) # data set

# Example 1 - Without the classes in the data
data <- iris[,1:4]

class <- NA # data class

findex <- "kurtosismax" # index function

dim <- 1 # dimension of data projection

sphere <- TRUE # spherical data

res <- PP_Optimizer(data = data, class = class, findex = findex,
                    optmethod = "GTSA", dimproj = dim, sphere = sphere,
                    weight = TRUE, lambda = 0.1, r = 1, cooling = 0.9,
                    eps = 1e-3, maxiter = 1000, half = 30)

print("Number of classes:"); res$num.class
```

```
print("class Names:"); res$class.names
print("Projection index function:"); res$findex
print("Projected data:"); res$proj.data
print("Projection vectors:"); res$vector.opt
print("Projection index:"); res$index


# Example 2 - With the classes in the data
class <- iris[,5] # classe dos dados

res <- PP_Optimizer(data = data, class = class, findex = findex,
                    optmethod = "GTSA", dimproj = dim, sphere = sphere,
                    weight = TRUE, lambda = 0.1, r = 1, cooling = 0.9,
                    eps = 1e-3, maxiter = 1000, half = 30)

print("Number of classes:"); res$num.class
print("class Names:"); res$class.names
print("Projection index function:"); res$findex
print("Projected data:"); res$proj.data
print("Projection vectors:"); res$vector.opt
print("Projection index:"); res$index
```

Regr *Linear regression.*

Description

Performs linear regression on a data set.

Usage

```
Regr(Y, X, namevarx = NA, intercepts = TRUE, sigf = 0.05)
```

Arguments

Y	Variable response.
X	Regression variables.
namevarx	Name of the variable, or variables X, if not set, assumes the default text.
intercepts	Consider the intercept in the regression (default = TRUE).
sigf	Level of significance of residue tests(default = 5%).

Value

Betas	Regression coefficients.
CovBetas	Covariance matrix of the regression coefficients.
ICc	Confidence interval of the regression coefficients.
hip.test	Hypothesis test of the regression coefficients.

ANOVA	Regression analysis of the variance.
R	Determination coefficient.
Rc	Corrected coefficient of determination.
Ra	Adjusted coefficient of determination.
QME	Variance of the residues.
ICQME	Confidence interval of the residue variance.
prev	Prediction of the regression fit.
IPp	Predictions interval
ICp	Interval of prediction confidence
error	Residuals of the regression fit.
error.test	It returns to 5% of significance the test of independence, normality and homogeneity of the variance of the residues.

Author(s)

Paulo Cesar Ossani

References

CHARNET, R.; at al.. *Analise de modelos de regressao lienar,* 2a ed. Campinas: Editora da Unicamp, 2008. 357 p.

RENCHER, A. C.; SCHAALJE, G. B. *Linear models in statisctic.* 2th. ed. New Jersey: John & Sons, 2008. 672 p.

RENCHER, A. C. *Methods of multivariate analysis.* 2th. ed. New York: J.Wiley, 2002. 708 p.

See Also

Plot.Regr

Examples

```
data(DataMix)

Y <- DataMix[,2]

X <- DataMix[,6:7]

name.x <- c("Special Coffees", "Commercial Coffees")

res <- Regr(Y, X, namevarx = name.x , intercepts = TRUE, sigf = 0.05)

print("Regression Coefficients:"); round(res$Betas,4)
print("Analysis of Variance:"); res$ANOVA
print("Hypothesis test of regression coefficients:"); round(res$hip.test,4)
print("Determination coefficient:"); round(res$R,4)
print("Corrected coefficient of determination:"); round(res$Rc,4)
print("Adjusted coefficient of determination:"); round(res$Ra,4)
print("Tests of the residues"); res$error.test
```

`Scatter` *Scatter plot.*

Description

Performs the scatter plot.

Usage

```
Scatter(data, ellipse = TRUE, ellipse.level = 0.95, rectangle = FALSE,
        title = NA, xlabel = NA, ylabel = NA,  posleg = 2, boxleg = TRUE,
        axes = TRUE, size = 1.1, grid = TRUE, color = TRUE, linlab = NA,
        class = NA, classcolor = NA, savptc = FALSE, width = 3236,
        height = 2000, res = 300)
```

Arguments

`data`	Data with x and y coordinates.
`ellipse`	Place an ellipse around the classes (default = TRUE).
`ellipse.level`	Significance level of the ellipse (defaul = 0.95).
`rectangle`	Place rectangle to differentiate classes (default = FALSE).
`title`	Titles of the graphics, if not set, assumes the default text.
`xlabel`	Names the X axis, if not set, assumes the default text.
`ylabel`	Names the Y axis, if not set, assumes the default text.
`posleg`	0 with no caption, 1 for caption in the left upper corner, 2 for caption in the right upper corner (default), 3 for caption in the right lower corner, 4 for caption in the left lower corner.
`boxleg`	Puts the frame in the caption (default = TRUE).
`axes`	Plots the X and Y axes (default = TRUE).
`size`	Size of the points in the graphs.
`grid`	Put grid on graphs (default = TRUE).
`color`	Colored graphics (default = TRUE).
`linlab`	Vector with the labels for the observations.
`class`	Vector with names of data classes.
`classcolor`	Vector with the colors of the classes.
`savptc`	Saves graphics images to files (default = FALSE).
`width`	Graphics images width when savptc = TRUE (defaul = 3236).
`height`	Graphics images height when savptc = TRUE (default = 2000).
`res`	Nominal resolution in ppi of the graphics images when savptc = TRUE (default = 300).

Value

Scatter plot.

Author(s)

Paulo Cesar Ossani

References

RENCHER, A. C. *Methods of multivariate analysis.* 2th. ed. New York: J.Wiley, 2002. 708 p.

ANTON, H.; RORRES, C. *Elementary linear algebra: applications version.* 10th ed. New Jersey: John Wiley & Sons, 2010. 768 p.

Examples

```
data(iris) # data set

data <- iris[,3:4]

cls <- iris[,5] # data class

Scatter(data, ellipse = TRUE, ellipse.level = 0.95, rectangle = FALSE,
        title = NA, xlabel = NA, ylabel = NA,  posleg = 1, boxleg = FALSE,
        axes = FALSE, size = 1.1, grid = TRUE, color = TRUE, linlab = NA,
        class = cls, classcolor = c("goldenrod3","blue","red"),
        savptc = FALSE, width = 3236, height = 2000, res = 300)

Scatter(data, ellipse = FALSE, ellipse.level = 0.95, rectangle = TRUE,
        title = NA, xlabel = NA, ylabel = NA,  posleg = 1, boxleg = TRUE,
        axes = FALSE, size = 1.1, grid = TRUE, color = TRUE, linlab = NA,
        class = cls, classcolor = c("goldenrod3","blue","red"),
        savptc = FALSE, width = 3236, height = 2000, res = 300)
```

Index